

# 11.9.3.6

EE23BTECH11022 - G DILIP REDDY

## Question:

For what values of  $x$ , the numbers  $-\frac{2}{7}, x, -\frac{7}{2}$  are in G.P ?

## Solution:

Let  $r$  be the common ratio

$$\Rightarrow \frac{x}{(-\frac{2}{7})} = \frac{(-\frac{7}{2})}{x} = r$$

$$x^2 = \left(-\frac{2}{7}\right) \cdot \left(-\frac{7}{2}\right)$$

$$x^2 = 1$$

$$x = 1, -1$$

$$r = \frac{x}{(-\frac{2}{7})}$$

$$\Rightarrow r = \frac{7}{2} \text{ or } -\frac{7}{2}$$

The signal corresponding to this is

$$x_1(n) = \left(-\frac{7}{2}\right)^{n-1} u(n) \quad (8)$$

$$x_2(n) = -\left(\frac{7}{2}\right)^{n-1} u(n) \quad (9)$$

Applying z-Transform :

$$x(n) \xleftrightarrow{z} X(z)$$

$$\text{ROC} : z \in \left(-\infty, -\frac{7}{2}\right) \cup \left(\frac{7}{2}, \infty\right)$$

$$\Rightarrow X_1(z) = \left(\frac{1}{7}\right) \left(\frac{4z}{7+2z}\right) \quad (10)$$

$$\Rightarrow X_2(z) = \left(\frac{1}{7}\right) \left(\frac{4z}{7-2z}\right) \quad (11)$$

Variable	Description	Value
$x(0)$	First term of the GP	$-\left(\frac{2}{7}\right)$
$x(2)$	Third term of the GP	$-\left(\frac{7}{2}\right)$
$r$	Common ratio of the GP	
$x(n)$	General term	

TABLE 1: Variables Used

(1)

(2)

(3)

(4)

(5)

(6)

(7)

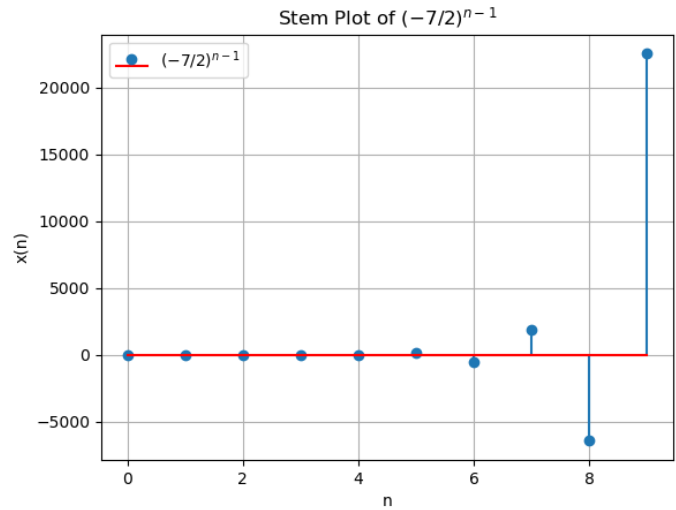


Fig. 1: Stem Plot of  $x_1(n)$

(8)

(9)

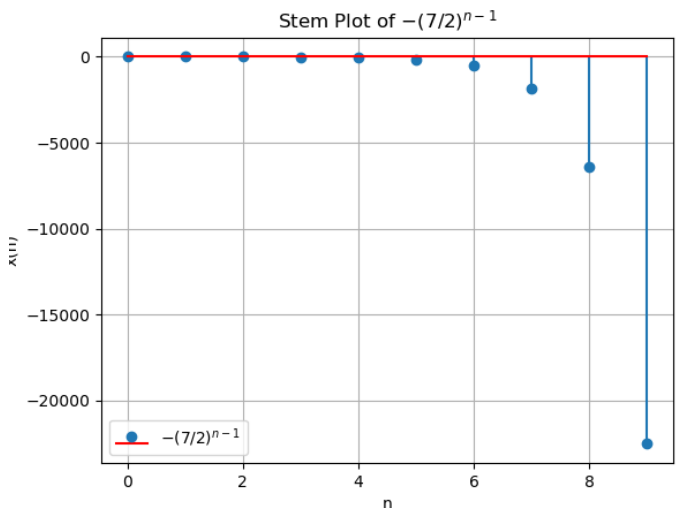


Fig. 2: Stem Plot of  $x_2(n)$