

Solution 1:

Given,

Fabric sheet = 5000sqft

Total time consumed = 40 hours*60 minutes = 2400 minutes

Number of laborers = 35

So, Total number of laborers and consumed time = 2400 minutes*35 laborers = 84000 minutes that equals to 1400 hours

Decision Variable:

Here, the decision variables are Collegiate (C) and Mini (M)

Objective Function:

Maximation Dmax = $32C + 24M$

Constraints: $C \leq 1000$, $M \leq 1200$

Mathematical Formulation:

$3C + 2M \leq 5000$ (Fabric sheet)

$(3/4)C + (2/3)M \leq 1400$ (Time) where $C, M \geq 0$

Each Collegiate requires 45 minutes of labor that is $3/4$ hours.

Each Mini requires 40 minutes of labor that is $2/3$ hours.

Solution 2:**a) Decision variables:**

Let P1, Q1 & R1 are the variables assigned to Plant 1.

Let P2, Q2 & R2 are the variables assigned to Plant 1.

Let P3, Q3 & R3 are the variables assigned to Plant 1.

b) Linear programming model:

Objective function Lmax = $420P1 + 420P2 + 420P3 + 360Q1 + 360Q2 + 360Q3 + 300R1 + 300R2 + 300R3$

c) Time Constraints:

Plants Capacity:

$$P1+Q1+R1 \leq 750 \text{ (plant 1 spare capacity)}$$

$$P2+Q2+R2 \leq 900 \text{ (plant 2 spare capacity)}$$

$$P3+Q3+R3 \leq 450 \text{ (plant 3 spare capacity)}$$

Sales Forecast:

$$P1+Q1+R1 \leq 900 \text{ (sales forecast of Large)}$$

$$P2+Q2+R2 \leq 1200 \text{ (sales forecast of Medium)}$$

$$P3+Q3+R3 \leq 750 \text{ (sales forecast of Small)}$$

Maximum space availability:

$$20P1+15Q1+12R1 \leq 13000 \text{ (storage space in plant 1)}$$

$$20P2+15Q2+12R2 \leq 12000 \text{ (storage space in plant 2)}$$

$$20P3+15Q3+12R3 \leq 5000 \text{ (storage space in plant 3)}$$

$$P_{\max}, Q_{\max}, R_{\max} \geq 0$$

As per the given analysis each plant must have same percentage of its production units

$$P1+Q1+R1/750 = P2+Q2+R2/900 = P3+Q3+R3/450$$

$$450(P1+Q1+R1) - 750(P3+Q3+R3) = 0$$

$$900(P1+Q1+R1) - 750(P2+Q2+R2) = 0$$

$$450(P2+Q2+R2) - 900(P3+Q3+R3) = 0$$

Non-Negativity

$$\text{Where } P1, P2, P3, Q1, Q2, Q3, R1, R2, R3 \geq 0$$