

$$\lambda = \omega^2 \quad \lambda = i\omega \quad \Rightarrow \quad \omega_{1/2} = 0 \quad -0,5$$

$$\omega = \pm \sqrt{-k \left(\frac{1}{m_1} + \frac{1}{m_2} \right)} \quad \Rightarrow \quad \lambda = -k \left(\frac{1}{m_1} + \frac{1}{m_2} \right)$$

Einsetzen: in $(M - \lambda E) \vec{u}$

$$= \begin{pmatrix} -\cancel{\frac{k}{m_1}} + \frac{k}{m_1} + \cancel{\frac{k}{m_2}} & \frac{k}{m_1} \\ \frac{k}{m_2} & -\cancel{\frac{k}{m_2}} + \frac{k}{m_1} + \cancel{\frac{k}{m_2}} \end{pmatrix} \vec{u} \quad \Rightarrow \quad \omega = \pm \sqrt{k \left(\frac{1}{m_1} + \frac{1}{m_2} \right)}$$

$$= \begin{pmatrix} k/m_2 & k/m_1 \\ k/m_2 & k/m_1 \end{pmatrix} \begin{pmatrix} u_1 \\ u_2 \end{pmatrix} \stackrel{!}{=} \vec{0}$$

$$u_1 \frac{k}{m_2} + u_2 \frac{k}{m_1} = 0$$

$$u_1 \frac{k}{m_2} + u_2 \frac{k}{m_1} = 0$$

$$u_1 = -\frac{m_2}{m_1} u_2 \quad \rightarrow \quad \vec{u} = a \begin{pmatrix} -\frac{m_2}{m_1} u_2 \\ u_2 \end{pmatrix} \quad \text{Eigenvektor} \quad \left(\begin{pmatrix} -\frac{m_2}{m_1} \\ 1 \end{pmatrix} \right) \text{ EV} \quad (\checkmark)$$

$$\lambda = 0$$

$$(M - \lambda E) \vec{u} = k \begin{pmatrix} -\frac{1}{m_1} & \frac{1}{m_1} \\ \frac{1}{m_2} & -\frac{1}{m_2} \end{pmatrix} \begin{pmatrix} u_1 \\ u_2 \end{pmatrix} \stackrel{!}{=} \vec{0}$$

$$-\frac{k}{m_1} u_1 + \frac{k}{m_1} u_2 = 0 \Leftrightarrow -u_1 + u_2$$

$$\frac{k}{m_2} u_1 + \frac{k}{m_2} u_2 = 0 \Leftrightarrow u_1 = u_2$$

$$\Rightarrow \vec{u}_0 = a \begin{pmatrix} u_1 \\ u_2 \end{pmatrix} \quad \text{Eigenvektor} \quad \left(\begin{pmatrix} 1 \\ 1 \end{pmatrix} \right) \text{ EV}$$

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