

Lab: Searching and Sorting Algorithms

Please submit your solutions (source code) of all below-described problems in [Judge](#).

1. Binary Search

Implement an algorithm that finds the index of an element in a sorted array of integers in logarithmic time.

Examples

Input	Output	Comments
1 2 3 4 5 1	0	Index of 1 is 0
-1 0 1 2 4 1	2	Index of 1 is 2

Hints

First, if you're not familiar with the concept, read about binary search in [Wikipedia](#).

In short, if we have a **sorted collection** of comparable elements, instead of doing a linear search (which takes linear time), we can eliminate half the elements at each step and finish in logarithmic time. Binary search is a **divide-and-conquer** algorithm; we start at the middle of the collection, if we haven't found the element there, there are three possibilities:

- The element we're looking for is smaller – then look to the left of the current element, we know all elements to the right are larger
- The element we're looking for is larger – look to the right of the current element
- The element is not present, traditionally, return -1 in that case

Start by defining a method:

```
def binary_search(numbers, target):  
    return -1
```

Inside the method, define two variables defining the bounds to be searched and a while loop:

```
def binary_search(numbers, target):  
    left = 0  
    right = len(numbers) - 1  
    while left <= right:  
        # TODO  
        pass  
    return -1
```

Inside the while loop, we need to find the midpoint:

```
mid_idx = (left + right) // 2
```

If the key is to the left of the midpoint, move the right bound. If the key is to the right of the midpoint, move the left bound:

```
mid_el = numbers[mid_idx]
if mid_el == target:
    return mid_idx
if mid_el < target:
    left = mid_idx + 1
else:
    right = mid_idx - 1
```

2. Selection Sort

Write an implementation of **Selection Sort**. You should read an array of integers and sort them.

Output

- You should print out the sorted list in the format described below.

Examples

Input	Output
5 4 3 2 1	1 2 3 4 5
13 93 37 74 61 65 5 55 17 96 52 70 17 7 89 65 16 38 42 15 86 21 93 10 31 28 36 14 65 7 68 86 97 34 27 32 86 44 51 75 29 64 0 36 33 54 20 40 60 56 51 51 25 77 75 46 47 57 18 12 27 28 29 21 22 37 74 78 34 15 71 75 20 19 76 48 98 36 76 49 83 21 44 12 85 68 24 9 80 41 66 1 54 31 55 33 88 35 32 43	0 1 5 7 7 9 10 12 12 13 14 15 15 16 17 17 18 19 20 20 21 21 21 22 24 25 27 27 28 28 29 29 31 31 32 32 33 33 34 34 35 36 36 36 37 37 38 40 41 42 43 44 44 46 47 48 49 51 51 51 52 54 54 55 55 56 57 60 61 64 65 65 65 66 68 68 70 71 74 74 75 75 75 76 76 77 78 80 83 85 86 86 86 88 89 93 93 96 97 98

3. Bubble Sort

Write an implementation of **Bubble Sort**. You should read an array of integers and sort them.

Output

- You should print out the sorted list in the format described below.

Examples

Input	Output
5 4 3 2 1	1 2 3 4 5

13 93 37 74 61 65 5 55 17 96 52 70 17 7 89 65 16 38 42 15 86 21 93 10 31 28 36 14 65 7 68 86 97 34 27 32 86 44 51 75 29 64 0 36 33 54 20 40 60 56 51 51 25 77 75 46 47 57 18 12 27 28 29 21 22 37 74 78 34 15 71 75 20 19 76 48 98 36 76 49 83 21 44 12 85 68 24 9 80 41 66 1 54 31 55 33 88 35 32 43	0 1 5 7 7 9 10 12 12 13 14 15 15 16 17 17 18 19 20 20 21 21 21 22 24 25 27 27 28 28 29 29 31 31 32 32 33 33 34 34 35 36 36 36 37 37 38 40 41 42 43 44 44 46 47 48 49 51 51 51 52 54 54 55 55 56 57 60 61 64 65 65 65 66 68 68 70 71 74 74 75 75 75 76 76 77 78 80 83 85 86 86 86 88 89 93 93 96 97 98
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4. Insertion Sort

Write an implementation of **Insertion Sort**. You should read an array of integers and sort them.

Output

- You should print out the sorted list in the format described below.

Examples

Input	Output
5 4 3 2 1	1 2 3 4 5
13 93 37 74 61 65 5 55 17 96 52 70 17 7 89 65 16 38 42 15 86 21 93 10 31 28 36 14 65 7 68 86 97 34 27 32 86 44 51 75 29 64 0 36 33 54 20 40 60 56 51 51 25 77 75 46 47 57 18 12 27 28 29 21 22 37 74 78 34 15 71 75 20 19 76 48 98 36 76 49 83 21 44 12 85 68 24 9 80 41 66 1 54 31 55 33 88 35 32 43	0 1 5 7 7 9 10 12 12 13 14 15 15 16 17 17 18 19 20 20 21 21 21 22 24 25 27 27 28 28 29 29 31 31 32 32 33 33 34 34 35 36 36 36 37 37 38 40 41 42 43 44 44 46 47 48 49 51 51 51 52 54 54 55 55 56 57 60 61 64 65 65 65 66 68 68 70 71 74 74 75 75 75 76 76 77 78 80 83 85 86 86 86 88 89 93 93 96 97 98

5. Quicksort

Sort an array of elements using the famous quicksort.

Examples

Input	Output
5 4 3 2 1	1 2 3 4 5

6. Merge Sort

Sort an array of elements using the famous merge sort.

Examples

Input	Output

5 4 3 2 1	1 2 3 4 5
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