# Team Notebook

# April 5, 2023

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## 1 BasicNumberTheory

```
11 gcd(11 a, 11 b)
   if (b > a)
       return gcd(b, a);
   if (b == 0)
       return a;
   return gcd(b, a % b);
ll expo(ll a, ll b, ll mod)
   11 res = 1;
   while (b > 0)
       if (b & 1)
          res = (res * a) \% mod:
       a = (a * a) \% mod;
       b = b >> 1:
   return res;
void extendgcd(ll a, ll b, ll *v)
   if (b == 0)
       v[0] = 1:
       v[1] = 0:
       v[2] = a;
       return:
   extendgcd(b, a % b, v);
   11 x = v[1]:
   v[1] = v[0] - v[1] * (a / b);
   v[0] = x:
   return:
} // pass an arry of size1 3
ll mminv(ll a, ll b)
{
   11 arr[3];
   extendgcd(a, b, arr):
   return arr[0];
} // for non prime b
11 mminvprime(11 a, 11 b) { return expo(a, b - 2, b); }
```

```
bool revsort(ll a, ll b) { return a > b: }
11 combination(ll n, ll r, ll m, ll *fact, ll *ifact)
    ll val1 = fact[n];
    11 \text{ val2} = \text{ifact[n - r]}:
    11 val3 = ifact[r];
    return (((val1 * val2) % m) * val3) % m;
void google(int t) { cout << "Case #" << t << ": "; }</pre>
vector<ll> sieve(int n)
    int *arr = new int[n + 1]();
    vector<11> vect:
    for (int i = 2; i <= n; i++)
       if (arr[i] == 0)
           vect.push_back(i);
           for (int j = 2 * i; j <= n; j += i)
               arr[i] = 1:
    return vect:
11 mod_add(ll a, ll b, ll m)
    a = a \% m;
    b = b \% m:
    return (((a + b) \% m) + m) \% m:
11 mod mul(11 a, 11 b, 11 m)
    a = a \% m;
    b = b \% m:
    return (((a * b) % m) + m) % m;
11 mod sub(11 a, 11 b, 11 m)
    a = a \% m:
    b = b \% m;
    return (((a - b) % m) + m) % m;
11 mod_div(ll a, ll b, ll m)
    a = a % m;
    b = b \% m;
  return (mod_mul(a, mminvprime(b, m), m) + m) % m;
} // only for prime m
ll phin(ll n)
    11 \text{ number} = n:
```

## 2 DataStructures

#### 2.1 BIT

```
struct BIT{
   ll N; vll bit;
   void init(ll n){
       N = n; bit.assign(n+1, 0);
   void add(int x, int k) {
       for (: x \le N: x += x & -x) bit[x] += k:
   int rsum(int 1. int r) {
       int res = 0:
       for (int x = 1 - 1; x; x -= x & -x) res -= bit[x];
       for (int x = r: x: x -= x & -x) res += bit[x]:
       return res;
   11 find(ll val){
       11 curr = 0 , prevsum = 0;
       for(int i = log2(N); i \ge 0; i \longrightarrow 0
           if(curr + (1 << i) < N && prevsum + bit[curr + (1</pre>
                 << i)] < val){
               prevsum += bit[curr + (1 << i)]:</pre>
              curr += (1 << i);
       }
       return curr + 1;
```

```
void prints(void){
    printv(bit);
}

};
```

#### 2.2 **DSU**

```
// 1 based indexing
struct DSU{
   vll p;
   11 n , connected;
   vll sz:
   void init(ll n){
       p.resize(n+1):
       iota(p.begin(), p.end(), 0);
       sz.assign(n+1, 1);
       connected = n:
   }
   11 get(11 x) {
      if(x == p[x]){
          return x;
      }
       return p[x]=get(p[x]);
   ll getsz(ll u)
 return sz[get(u)];
   bool unite(int x, int y) {
      x = get(x);
      v = get(v);
      if(x == y) return false;
       connected --:
      if(sz[x] > sz[y])
  swap(x, y);
 sz[v] += sz[x];
 sz[x] = 0;
 p[x] = p[y];
      return true;
```

```
}
};
```

## 2.3 DSUrollback

```
int n , q;
const int maxN = 3e5+1:
vll sol;
struct DSU{
   vector<pll> st[4*maxN];
   vll p;
   //path compression wont work during rollbacks, so rank
        compression
   vll rank:
   // e is basically storing the states, where .first is
        storing the present, and .second is storing the past
        to the moment where it was changed(cool)
   vector<pair<int&, int>> e;
   // op is basically storing by how much or how the value
        changed
   vll op;
   int ans = 0:
   void init(int n){
      p.resize(n+1); rank.assign(n+1, 1);
      for(int i = 0 ; i <= n ; i++) p[i] = i;</pre>
       ans = n:
   }
   int get(int u){
      if(u == p[u]){
          return u:
       return get(p[u]);
   void add(int u . int v){
      u = get(u); v = get(v);
      if(u == v){
          op.pb(0);
          return;
      if(rank[u] > rank[v]) swap(u , v);
      ans--;
      op.pb(-1);
      e.pb({p[u] , p[u]});
      p[u] = v;
```

```
e.pb({rank[v] , rank[v]});
   rank[v] += rank[u]:
// update the range of queries from the index it starts
     to the index it ends [1,r] and total range will be
void upd(int node , int l , int r , int lx, int rx, pll p
   if(1x >= r || rx <= 1){}
       return;
   if(1x >= 1 && rx <= r){
       st[node].pb(p);
   }else{
       int mid = (1x+rx)/2:
       upd(2*node+1 , 1 , r , lx , mid , p);
       upd(2*node+2 , 1 , r , mid , rx , p);
   }
void undo(){
   if(!op.back()){
       op.pop_back();
       return:
   }else{
       ans++:
       op.pop_back();
       for(int i = 0 : i < 2 : i ++){
           e.back().first = e.back().second;
           e.pop_back();
}
//dfs in the interval tree
void build(int node, int 1 , int r){
   for(auto it: st[node]){
       add(it.first , it.second);
   if(r-1 == 1){
       sol.pb(ans);
   }else{
       int mid = (1+r)/2;
       build(2*node+1 , 1 , mid);
       build(2*node+2 , mid ,r);
   for(auto it: st[node]){
       undo():
   }
```

```
}
;
```

#### 2.4 LineContainer

```
vector<pll> all_lines;
11d intersection(pll 11 , pll 12){
    return ((11d)11.second - 12.second)/(12.first-11.first);
bool can_delete(pll 11 , pll 12 , pll 13){
    return intersection(11 , 12) < intersection(12 , 13); //</pre>
    //return intersection(11 , 12) > intersection(12 , 13);
        // max
}
void add line(ll k . ll b){
    pll nl = \{k,b\};
    while(all_lines.size() >= 2 && can_delete(all_lines[
        all_lines.size()-2] , all_lines.back() , nl)){
       all_lines.pop_back();
    all_lines.pb(nl);
}
int n;
11 vall(int pos , 11 x){
    return all_lines[pos].first*x + all_lines[pos].second;
ll compute_min(ll x){
    11 1 = -1:
    11 r = all_lines.size()-1;
    while(r-1 > 1){
       11 \text{ mid} = (1+r)/2;
       // vall(mid , x) < vall(mid+1 , x) // max
       if(vall(mid , x) > vall(mid+1 , x)){ // min
           1 = mid:
       }else{
           r = mid:
    return vall(r , x);
```

## 2.5 LineContainerDynamic

```
// LineContainer hull;
// for min for(int i = 0 : i < n : i ++){</pre>
      dp[i] = -hull.query(s[i]);
//
    hull.add(-f[i] . -dp[i]):
// }
// for max , no change
struct Line {
mutable ll k, m, p;
bool operator<(const Line& o) const { return k < o.k; }</pre>
bool operator<(11 x) const { return p < x; }</pre>
struct LineContainer : multiset<Line, less<>>> {
// (for doubles, use inf = 1/.0, div(a,b) = a/b)
static const ll inf = LLONG_MAX;
ll div(ll a, ll b) { // floored division
 return a / b - ((a ^ b) < 0 && a % b): }
 bool isect(iterator x, iterator y) {
 if (y == end()) return x \rightarrow p = inf, 0;
 if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
 else x->p = div(y->m - x->m, x->k - y->k);
 return x->p >= y->p;
 void add(ll k. ll m) {
 auto z = insert(\{k, m, 0\}), y = z++, x = y;
 while (isect(y, z)) z = erase(z);
 if (x != begin() \&\& isect(--x, y)) isect(x, y = erase(y));
 while ((y = x) != begin() && (--x)->p >= y->p)
  isect(x, erase(y));
 11 query(11 x) {
 assert(!empty());
 auto 1 = *lower_bound(x);
 return 1.k * x + 1.m;
};
```

### 2.6 Mo's

//Decomposing queries in blocks of  $\operatorname{sqrt}(N)$  size and storing the results in a vector, while increasing 1 and r in such a way, that it is most optimal.

```
const int N = 2e5 + 5:
const int Q = 2e5 + 5:
const int M = 1e6 + 5;
const int SZ = sqrt(N) + 1:
struct var{
ll l , r , idx;
} qr[Q];
int n , q , a[N]; ll freq[M];
ll ans[Q]; ll cur = 0;
bool comp(var &d1, var &d2){
int b1 = d1.1 / SZ:
 int b2 = d2.1 / SZ;
 if(b1 != b2){
  return b1 < b2:
   return (b1 & 1) ? d1.r < d2.r : d1.r > d2.r:
inline void add(ll x){...}
inline void del(11 x){...}
void mo(){
 cin >> n >> q;
 for(int i = 1; i <= n ; i++)cin >> a[i];
 for(int i = 1; i <= q ; i++){</pre>
   cin >> qr[i].1 >> qr[i].r;
   ar[i].idx = i:
 sort(qr+1, qr+q+1 , comp);
 for(int i = 1; i <= q ; i ++){</pre>
   while(1 < gr[i].1) remove(a[1++]);</pre>
   while(1 > qr[i].1) add(a[--1]);
   while(r < qr[i].r) add(a[++r]);
   while(r > qr[i].r) remove(a[r--]);
   ans[gr[i].idx] = cur:
```

## 2.7 SegTree

```
// 0-based indexed segment tree , with last element of
    range of element included
#define var 11

// struct var{
    // var as per needed in question (var present in the node
    of the segment tree)
```

```
// 11 x:
// }:
struct seg_tree{
ll size:
vector<var> a;
vector<ll> lazy;
vector<bool> clazy;
//declare invariant for calc
var invariant = INF:
void init(ll n){
 size = 1:
 while(size < n) size*=2;</pre>
 a.assign(2*size , INF);
 lazy.assign(2*size ,0);
 clazy.assign(2*size , false);
var merge( var b , var c){
 //merge nodes of the seg_tree
 // minimum:var a = min(b , c);
 return a:
}
   // apply operation defines what we are doing in range
        update . for adding a+=operation(a.b): . assignment:
         a = operation(a,b);
void apply operation(11 &a . 11 b){
 //addition:a +=b;
 //assignment: a=b;
void propagate(ll node , ll lx , ll rx){
 apply_operation(a[node] , lazy[node]);
 if(lx != rx){
  if(lazy[node]){
   apply_operation(lazy[2*node+1] , lazy[node]);
   apply_operation(lazy[2*node+2] , lazy[node]);
   clazy[2*node+1] = true;
   clazv[2*node+2] = true;
 }
 lazv[node] = 0;
 clazv[node]=false:
void build( vll &arr , ll l , ll r , ll node){
 if(1 == r){
```

```
if(1 < (11)arr.size()){</pre>
  //set value:
  a[node] = arr[1];
 return;
11 \text{ mid} = (1+r)/2;
build(arr , l , mid , 2*node+1 );
build(arr , mid+1 , r , 2*node+2);
a[node] = merge( a[2*node+1], a[2*node+2]);
void modify(ll 1 , ll r , ll v , ll node , ll lx , ll rx){
if(clazv[node]){
 propagate(node , lx , rx);
if(1x > r \mid \mid 1 > rx) return;
if(1x >= 1 \&\& rx <= r){}
 //addition:lazv[node]+=v
 //assignment:lazy[node]=v;
 lazy[node]+=v;
 clazy[node] = true;
 propagate(node , lx , rx);
 return:
11 \text{ mid} = (1x + rx)/2:
modify(1, r, v, 2*node+1, lx, mid);
modify(1 , r ,v , 2*node+2 , mid+1 , rx);
a[node] = merge( a[2*node+1] , a[2*node+2]);
var get(ll i , ll node, ll lx , ll rx){
if(clazy[node]){
 propagate(node , lx , rx);
if(rx == lx){
 return a[node];
11 \text{ mid} = (1x+rx)/2:
ll res:
if(i <= mid){</pre>
 return get(i , 2*node+1 , lx , mid);
 return get(i , 2*node+2 , mid+1 , rx);
void set(ll l , ll r , ll v , ll node , ll pos ){
```

```
if(clazv[node]){
 propagate(node , l , r);
if(1 == r){
 //set value
 //addition:lazy[node]+=v
 //assignment:lazy[node]=v;
 clazy[node] = 1;
 lazv[node] += v;
 propagate(node . 1 . r):
 return:
 11 \text{ mid} = (1+r)/2:
 if( pos <= mid){</pre>
 set(1 , mid , v , 2*node+1 , pos);
 set(mid+1 , r , v , 2*node+2 , pos);
a[node] = merge(a[2*node+1], a[2*node+2]);
var calc(11 1 , 11 r , 11 lx , 11 rx , 11 node){
if(clazy[node]){
 propagate(node , lx , rx);
if(r < lx | | l > rx){
 return INF:
if( 1 <= lx && r >= rx){
 return a[node];
11 \text{ mid} = (1x+rx)/2:
var sum1 = calc(1, r, lx, mid, 2*node+1);
 var sum2 = calc(1, r, mid+1, rx, 2*node+2);
return merge(sum1 . sum2):
//O BASED INDEXED , QUERY, AND STUFF WILL BE FROM O to n-1,
      if q is 1 to n, then 1--, r--, REMEMBER U DUMB
void build( vll &arr ){
build(arr , 0 , size-1 , 0):
var calc(ll l , ll r){
var ans = calc(1, r, 0, size-1, 0);
return ans:
void set(ll i . ll v){
set(0 , size-1 , v, 0 , i);
```

```
}
void modify(ll l , ll r , ll v){
  modify(l , r ,v , 0 , 0 , size-1);
}

var get(ll i){
  return get(i , 0 , 0, size-1);
}

void prints(void){
  cout << size << endl;
  printv(a);
  printv(lazy);
  printv(clazy);
}
};</pre>
```

# 3 Graph

## 3.1 Djikstra

```
int bfs(int source){
  vector<int>vis(N,0);
  vector<int>dist(N,INF);
  set<pair<int,int>>st;
  st.insert({0.source}):
  dist[source]=0:
  while(!st.emptv()){
     pair<int,int>p = *st.begin();
     st.erase(st.begin());
     int dis = p.first;
     int curr_vec = p.second;
     if(vis[curr vec]==0){
      for(auto child:graph[curr_vec]){
          int tempdist = dis+child.second;
          if(tempdist<dist[child.first]){</pre>
              st.insert({tempdist,child.first});
              dist[child.first] = tempdist:
          }
      }
     }
```

```
vis[curr_vec]=1;
}
```

#### 3.2 lca

```
int n, 1;
vector<vector<int>> adj;
int timer;
vector<int> tin, tout;
vector<vector<int>> up;
void dfs(int v, int p)
   tin[v] = ++timer:
   up[v][0] = p;
   for (int i = 1; i <= 1; ++i)</pre>
       up[v][i] = up[up[v][i-1]][i-1];
   for (int u : adj[v]) {
      if (u != p)
          dfs(u, v);
   tout[v] = ++timer:
bool is ancestor(int u. int v)
   return tin[u] <= tin[v] && tout[u] >= tout[v];
int lca(int u. int v)
   if (is ancestor(u, v))
      return u:
   if (is_ancestor(v, u))
       return v;
   for (int i = 1: i >= 0: --i) {
      if (!is_ancestor(up[u][i], v))
          u = up[u][i];
   return up[u][0];
```

```
void preprocess(int root) {
    tin.resize(n);
    tout.resize(n);
    timer = 0;
    l = ceil(log2(n));
    up.assign(n, vector<int>(1 + 1));
    dfs(root, root);
}
```

## 3.3 primMST

```
ll n . m . tot wt . e:
vector<vector<pll>>graph , tree;
vll parent , dist;
void prim_mst(ll source ){
   set<pll>st;
   st.insert({0,source});
   dist[source] = 0;
   vector<bool>vis(n+1 , false);
   while(!st.empty()){
       auto x = *st.begin();
       st.erase(x);
       11 u = x.second:
       if(vis[u]){
           continue;
       11 v = parent[u]:
       11 w = x.first;
       tree[v].pb({w , u});
       tree[u].pb({w , v});
       e++;
       vis[u] = true:
       tot_wt += x.first;
       for(auto edge: graph[u]){
           if(!vis[edge.second] && edge.first < dist[edge.</pre>
               second]){
              st.erase({dist[edge.second] , edge.second});
              dist[edge.second] = edge.first;
              parent[edge.second] = u;
              st.insert({edge.first . edge.second}):
      }
```

```
// if e != n , then it is impossible to form the mst

void init(){
   graph.resize(n+1);
   parent.assign(n+1 ,0);
   dist.assign(n+1 , INF);
   tree.resize(n+1);
}
```

## 4 Maths

#### 4.1 FFT

```
typedef double ld:
typedef complex<ld> cd;
#define pvll pair<11,vll>
// const int SIZE = 1<<19:
//inv = 1 (ifft) inv = 0 (fft)
void fft(vector<cd> &a. bool inv){
   int N = (int) a.size():
   //bit permutation reversal \rightarrow (0,1,2,3,4,5,6,7) \rightarrow
         (\lceil \{0,4\}, \{2,6\} \rceil, \lceil \{1,5\}, \{3,7\} \rceil)
   for(int i = 1, j = 0; i < N; i++){
       int bit = N>>1:
       for(; j&bit; bit >>= 1)
           j ^= bit:
       j ^= bit;
       if(i < i)
           swap(a[i], a[i]):
   }
   // omega(n,k) = (2*k*pi*i)/n; n'th roots of unity
   for(int len = 2; len <= N; len <<= 1){</pre>
       ld theta = 2*PI / len * (inv ? -1 : 1):
       cd wlen(cos(theta), sin(theta));
       for(int i = 0: i < N: i += len){</pre>
           cd w(1):
           for(int j = 0; j < len / 2; j++){</pre>
               cd u = a[i+j], v = a[i+j+len/2] * w;
               a[i+i] = u + v;
               a[i+j+len/2] = u - v;
               w *= wlen:
           }
       }
```

```
if(inv)
       for(cd &z : a)
          z /= N:
//a = multiplv(a,b) means a = a * b
vll multiply(vll a , vll b){
   ll n=1: vll v:
   while(n<((ll)a.size())+((ll)b.size())) n <<=1;</pre>
   vector<cd> fa(n), fb(n):
   for(int i = 0 : i < n : i ++) fa[i] = fb[i] = cd(0):
   for(int i = 0 ; i <a.size() ; i ++) fa[i] = cd(a[i]);</pre>
   for(int i = 0 ; i <b.size() ; i ++) fb[i] = cd(b[i]);</pre>
   fft(fa.false):
   fft(fb,false);
   for(int i = 0 : i < n : i ++){</pre>
       fa[i]=(fa[i]*fb[i]);
   fft(fa.true):
   for (int i = 0; i < a.size() + b.size() - 1; ++i) {</pre>
       v.push_back((long long)(fa[i].real() + 0.5));
   return v;
//exponentiation can be done, by resizing the inital array
    after 5n.
//and doing fft transformation,
//then exponentiating the values of points and then inverse
```

#### 4.2 fftconvmod

```
const int mod = 998244353;
typedef double ld;
typedef complex<double> cd;
typedef vector<cdouble> vd;
void fft(vector<cd>& a) {
   int n = sz(a), L = 31 - __builtin_clz(n);
   static vector<complex<long double>> R(2, 1);
   static vector<cd> rt(2, 1); // (^ 10% faster if double)
   for (static int k = 2; k < n; k *= 2) {
     R.resize(n); rt.resize(n);
   auto x = polar(1.0L, acos(-1.0L) / k);
   rep(i,k,2*k) rt[i] = R[i] = i&1 ? R[i/2] * x : R[i/2];
   }
   vi rev(n);
   rep(i,0,n) rev[i] = (rev[i / 2] | (i & 1) << L) / 2;</pre>
```

```
rep(i,0,n) if (i < rev[i]) swap(a[i], a[rev[i]]);
for (int k = 1: k < n: k *= 2)
 for (int i = 0; i < n; i += 2 * k) rep(j,0,k) {
 // cd z = rt[j+k] * a[i+j+k]; // (25\% faster if hand-
       rolled) /// include-line
  auto x = (double *)&rt[i+k]. v = (double *)&a[i+i+k]: ///
        exclude-line
  cd z(x[0]*y[0] - x[1]*y[1], x[0]*y[1] + x[1]*y[0]);
       / exclude-line
  a[i + j + k] = a[i + j] - z;
  a[i + i] += z:
vd conv(const vd& a, const vd& b) {
if (a.empty() || b.empty()) return {};
vd res(sz(a) + sz(b) - 1);
int L = 32 - builtin clz(sz(res)), n = 1 \ll L:
vector<cd> in(n), out(n);
copv(all(a), begin(in));
rep(i.0.sz(b)) in[i].imag(b[i]):
fft(in);
for (cd& x : in) x *= x:
rep(i,0,n) out[i] = in[-i & (n-1)] - conj(in[i]);
rep(i,0,sz(res)) res[i] = imag(out[i]) / (4 * n);
return res:
const int M = mod:
vll convMod(const vll &a. const vll &b) {
if (a.empty() || b.empty()) return {};
vll res(a.size() + b.size() - 1);
int B=32- builtin clz(res.size()), n=1<<B, cut=int(sqrt(M))</pre>
vector<cd> L(n), R(n), outs(n), outl(n);
   for(int i = 0; i < (int)a.size(); i ++) L[i] = cd((int)
        a[i] / cut, (int)a[i] % cut);
for(int i = 0 ; i < (int)b.size() ; i ++) R[i] = cd((int)b[</pre>
     i] / cut, (int)b[i] % cut);
fft(I.) . fft(R):
for(int i = 0 ; i < n ; i ++) {</pre>
 int j = -i & (n - 1);
 outl[j] = (L[i] + conj(L[j])) * R[i] / (2.0 * n);
 outs[j] = (L[i] - conj(L[j])) * R[i] / (2.0 * n) / 1i;
fft(outl), fft(outs);
  for(int i = 0 ; i < (int)res.size() ; i ++){</pre>
 11 av = ll(real(outl[i])+.5), cv = ll(imag(outs[i])+.5);
 11 bv = 11(imag(out1[i])+.5) + 11(real(outs[i])+.5);
 res[i] = ((av \% M * cut + bv) \% M * cut + cv) \% M:
```

```
}
return res;
}

vll binpow(vll b,ll p){
  vll ans=vll(1,1);
  for(;p;p>>=1){
    if(p&1)ans=convMod(ans,b);
    b=convMod(b,b);
  }
  return ans;
}
```

#### 4.3 ixclu

```
ll ixclu (ll num, ll lim) {
    vector<ll> p:
    for (11 i=2; i*i<=num; ++i)</pre>
       if (num % i == 0) {
           p.push back (i):
           while (num % i == 0)
               num /= i;
       }
    if (num > 1)
       p.push_back (num);
    11 sum = 0;
    for (ll msk=1; msk<(1<<p.size()); ++msk) {</pre>
       11 mult = 1, bits = 0;
       for (11 i=0; i<(11)p.size(); ++i)</pre>
           if (msk & (1<<i)) {</pre>
               ++bits;
               mult *= p[i]:
           }
       11 cur = lim / mult:
       if (bits % 2 == 1)
           sum += cur;
        else
           sum -= cur;
    return lim-sum;
```

#### 4.4 Matrix

```
#define maxn 2
struct Mat{
   int mat[maxn][maxn];
   int row,col;
   Mat(int row=2.int col=2){
       row= row:col= col:
       mat[0][0]=1;mat[0][1]=0;
       mat[1][0]=0;mat[1][1]=1;
   }
   bool identity(){
       if (mat [0] [0] == 1&&mat [0] [1] == 0&&mat [1] [0] == 0&&mat
            [1][1]==1)return 1:
       else return 0:
   }
};
Mat mod_add(Mat a,Mat b,int p=MOD){
   Mat ans(a.row,b.col);
   memset(ans.mat,0,sizeof(ans.mat));
   for(int i=0;i<a.row;i++)</pre>
       for(int j=0; j<a.col; j++){</pre>
           ans.mat[i][i]=a.mat[i][i]+b.mat[i][i]:
           ans.mat[i][j]%=p;
   return ans:
Mat mod_mul(Mat a,Mat b,int p=MOD){
   Mat ans(a.row.b.col):
   memset(ans.mat.0.sizeof(ans.mat)):
   for(int i=0;i<ans.row;i++)</pre>
       for(int k=0:k<a.col:k++)</pre>
           if(a.mat[i][k])
               for(int j=0; j<ans.col; j++)</pre>
                   ans.mat[i][j]=(ans.mat[i][j]+1LL*a.mat[i][
                        k]*b.mat[k][j])%p;
   return ans;
Mat mod_pow(Mat a,int k,int p=MOD) {
   Mat ans(a.row,a.col);
   for(int i=0;i<a.row;i++)for(int j=0;j<a.col;j++)ans.mat[i</pre>
        ][i]=(i==i);
   while(k){
       if(k&1)ans=mod mul(ans,a,p):
       a=mod_mul(a,a,p);
       k>>=1:
   return ans;
```

```
Mat fib(int n){
    Mat ans(2,2);
    ans.mat[0][1]=1;
    ans.mat[1][0]=1;
    ans.mat[1][1]=0;
    return mod_pow(ans,n,MOD);
}
```

#### 4.5 mint

```
11 myRand(11 B) {
return (ull)rng() % B;
const 11 MOD = 998244353:
template<11 mod = MOD> struct mint { // 1000000007
    1000000009
11 x;
mint() : x(0)  {}
mint(ll x) {
 x %= mod:
 if (_x < 0)_x += mod;
 x = _x;
mint& operator += (const mint &a) {
 x += a.x;
 if (x \ge mod) x = mod:
 return *this:
mint& operator -= (const mint &a) {
 x += mod - a.x:
 if (x \ge mod) x -= mod;
 return *this:
mint& operator *= (const mint &a) {
 x = (ull)x * a.x % mod:
 return *this:
mint pow(ll pw) const {
 mint res = 1;
 mint cur = *this:
 while(pw) {
 if (pw & 1) res *= cur;
  cur *= cur:
  pw >>= 1;
```

```
}
return res:
mint inv() const {
assert(x != 0):
11 t = x:
ll res = 1;
while(t != 1) {
 11 z = mod / t:
 res = (ull)res * (mod - z) % mod;
 t = mod - t * z:
return res;
mint& operator /= (const mint &a) {
return *this *= a.inv();
mint operator + (const mint &a) const {
return mint(*this) += a:
mint operator - (const mint &a) const {
return mint(*this) -= a:
mint operator * (const mint &a) const {
return mint(*this) *= a;
mint operator / (const mint &a) const {
return mint(*this) /= a:
bool sqrt(mint &res) const {
if (mod == 2 || x == 0) {
 res = *this;
 return true;
if (pow((mod - 1) / 2) != 1) return false:
if (mod % 4 == 3) {
 res = pow((mod + 1) / 4);
 return true;
int pw = (mod - 1) / 2:
int K = 30;
while((1 << K) > pw) K--:
while(true) {
 mint t = myRand(mod);
 mint a = 0, b = 0, c = 1:
 for (int k = K; k >= 0; k--) {
  a = b * b:
  b = b * c * 2:
  c = c * c + a * *this:
```

```
if (((pw >> k) & 1) == 0) continue:
   b = b * t + c:
   c = c * t + a * *this:
  if (b == 0) continue;
  c -= 1:
  c *= mint() - b.inv():
  if (c * c == *this) {
  res = c:
   return true:
 assert(false):
bool operator == (const mint &a) const {
 return x == a.x;
bool operator != (const mint &a) const {
 return x != a.x;
bool operator < (const mint &a) const {</pre>
 return x < a.x:
template<11 mod = MOD> struct Factorials {
using Mint = mint<mod>:
vector<Mint> f, fi;
Factorials(): f(), fi() {}
Factorials(int n) {
 n += 10:
 f = vector<Mint>(n);
 fi = vector<Mint>(n):
 f[0] = 1:
 for (int i = 1; i < n; i++)</pre>
 f[i] = f[i - 1] * i;
 fi[n-1] = f[n-1].inv();
 for (int i = n - 1; i > 0; i--)
 fi[i - 1] = fi[i] * i:
Mint C(int n. int k) {
 if (k < 0 \mid | k > n) return 0;
 return f[n] * fi[k] * fi[n - k]:
template<11 mod = MOD> struct Powers {
using Mint = mint<mod>;
```

```
vector<Mint> p. pi:
Powers() : p(), pi() {}
Powers(int n. Mint x) {
 n += 10:
 if (x == 0) {
 p = vector<Mint>(n);
 p[0] = 1;
 } else {
 p = vector<Mint>(n);
  pi = vector<Mint>(n):
  p[0] = pi[0] = 1:
  Mint xi = x.inv();
  for (int i = 1; i < n; i++) {</pre>
  p[i] = p[i - 1] * x;
  pi[i] = pi[i - 1] * xi;
Mint pow(int n) {
 if (n >= 0)
 return p[n];
 else
 return pi[-n];
template<11 mod = MOD> struct Inverses {
using Mint = mint<mod>;
vector<Mint> ii:
Inverses() : ii() {}
Inverses(int n) {
 n += 10;
 ii = vector<Mint>(n);
 ii[1] = 1:
 for (int x = 2: x < n: x++)
 ii[x] = Mint() - ii[mod % x] * (mod / x);
Mint inv(Mint x) {
 assert(x != 0):
 11 t = x.x:
 ll res = 1:
 while(t >= (int)ii.size()) {
 11 z = mod / t:
 res = (ull)res * (mod - z) % mod;
 t = mod - t * z:
 return ii[t] * res:
```

```
}
};
using Mint = mint<>;
```

#### 4.6 nCr

```
struct nCr{
   11 maxx , md;
   vll fact, ifact;
   inline ll mul(ll a, ll b) { return a *1LL* b % md ;}
   ll power(ll a, ll n) {
       if(n == 0) return 1 :
       int p = power(a, n/2) \% md:
       p = mul(p, p);
       return n & 1 ? mul(p, a) : p ;
   int invMod(int a) {return power(a,md-2);}
   void pre() {
       fact[0] = 1:
       for(int i = 1:i< maxx:++i) fact[i] = mul(i, fact[i])</pre>
            -17) :
       ifact[maxx-1] = invMod(fact[maxx-1]);
       for(int i = maxx-1 : i>0 :--i) ifact[i-1] = mul(ifact
            [i], i);
   nCr(int mxN, int M) {
       maxx = _mxN + 1;
       md = _M ;
       fact.resize(maxx) :
       ifact.resize(maxx) ;
       pre():
   11 C(11 n, 11 r) {
       if (n < r || r < 0 || n < 0) return 0:
       return mul(fact[n], mul(ifact[r], ifact[n-r]));
}:
//maxx N we need
//const int N = 100:
// initialise nCr struct
// nCr comb(N , mod);
```

#### 4.7 NTT

```
const 11 mod = 998244353;
```

```
namespace getPrimitive{
   11 powmod (11 a, 11 b, 11 p) {
       ll res = 1:
       while (b)
           if (b & 1)
              res = 11 (res * 111 * a % p), --b:
              a = 11 (a * 111 * a % p), b >>= 1;
       return res:
    }
    // to generate primitive root
    11 generator (11 p) {
       vector<ll> fact:
       ll phi = p-1, n = phi;
       for (11 i=2; i*i<=n; ++i)</pre>
           if (n % i == 0) {
              fact.push_back (i);
              while (n \% i == 0)
                  n /= i:
       if (n > 1)
           fact.push_back (n);
       for (11 res=2; res<=p; ++res) {</pre>
           bool ok = true:
           for (size t i=0: i<fact.size() && ok: ++i)</pre>
              ok &= powmod (res. phi / fact[i], p) != 1:
           if (ok) return res;
       return -1;
};
namespace NTT {
    vll perm, wp[2];
    const 11 mod = 998244353, G = 3; ///G is the primitive
        root of M(can be calculated using generator)
    ll root, inv. N. invN:
    11 power(ll a, ll p) {
       ll ans = 1:
       while (p) {
           if (p & 1) ans = (1LL*ans*a)%mod:
           a = (1LL*a*a) \% mod;
           p >>= 1:
       return ans:
```

```
// (mod-1)%n == 0 . condition for NTT. otherwise use CRT
void precalculate(ll n) {
    assert( (n&(n-1)) == 0 && (mod-1)%n==0):
   N = n:
   invN = power(N, mod-2):
    perm = wp[0] = wp[1] = vector<11>(N);
    perm[0] = 0:
   for (11 k=1; k<N; k<<=1)
       for (11 i=0: i<k: i++) {</pre>
           perm[i] <<= 1:
           perm[i+k] = 1 + perm[i];
    root = power(G, (mod-1)/N);
    inv = power(root, mod-2);
    wp[0][0]=wp[1][0]=1;
    for (11 i=1: i<N: i++) {</pre>
       wp[0][i] = (wp[0][i-1]*1LL*root)%mod;
       wp[1][i] = (wp[1][i-1]*1LL*inv)%mod;
}
void ntt(vector<ll> &v, bool invert = false) {
    if (v.size() != perm.size()) precalculate(v.size());
   for (11 i=0: i<N: i++)</pre>
       if (i < perm[i])</pre>
           swap(v[i], v[perm[i]]);
    for (11 len = 2; len <= N; len *= 2) {
       for (11 i=0, d = N/len: i<N: i+=len) {</pre>
           for (11 j=0, idx=0; j<len/2; j++, idx += d) {</pre>
               11 x = v[i+i]:
               11 v = (wp[invert][idx]*1LL*v[i+i+len/2])%
               v[i+j] = (x+y) = mod ? x+y - mod : x+y);
               v[i+j+len/2] = (x-y>=0 ? x-y : x-y+mod);
       }
   }
    if (invert) {
       for (l1 &x : v) x = (x*1LL*invN) \text{/mod}:
vector<ll> multiply(vector<ll> a, vector<ll> b) {
    while (n < a.size() + b.size()) n <<=1:
```

```
a.resize(n):
       b.resize(n):
       ntt(a);
       ntt(b):
       for (ll i=0; i<n; i++) a[i] = (a[i] * 1LL * b[i])%mod
       ntt(a, true);
       return a;
    //if polynomial exponentiation needed, instead resize the
         size of polynomial to atleast 5n . then
        exponentiate the coefficients and then inverse
        transform
}:
vll binpow(vll b,ll p){
    vll ans=vll(1.1):
    while(p > 0){
       if(p&1){
           ans = NTT::multiply(ans,b);
       cout << b.size() << endl;</pre>
       b = NTT::multiply(b,b);
       cout << b.size() << " " << count(all(b) , 0) << endl;</pre>
       p = p >> 1;
    return ans;
```

## 5 StressTestChecker

```
@echo off
g++ -std=c++17 -o test.exe test.cpp
g++ -std=c++17 -o soln.exe soln.cpp
g++ -std=c++17 -o brute.exe brute.cpp
for /1 %%x in (1, 1, 1000) do (
    test > input.in
    soln < input.in > output.out
    brute < input.in > output2.out
    fc output.out output2.out > diagnostics || exit /b
    echo %%x
)
echo all tests passed
pause
```

# 6 Strings

#### 6.1 KMP

```
vll kmp ( string &s){
   11 n = s.size():
   vll pi(n , 0);
   for(int i = 1 ; i < n ; i ++){</pre>
      11 j = pi[i-1];
       while(j > 0 \&\& s[i] != s[j]){
           j = pi[j-1];
      if(s[i] == s[j]) j++;
       pi[i] = j;
   return pi;
vector<vll>aut:
void compute_automaton(string s){
   s += '#':
   vll pi = kmp(s);
   ll n = s.size();
   for(int i = 0 ; i < n ;i++ ){</pre>
       for(int j = 0; j < 26; j ++){
           if(i > 0 \&\& s[i]!='a'+j){
              aut[i][j] = aut[pi[i-1]][j];
              aut[i][j] = i + ('a'+j == s[i]);
   }
```

## 6.2 Manachar

```
struct manacher{
  vector<int>p;
  void run_manacher(string s){
    int n = s.length();
    p.assign(n,1);
    int l=1,r=1;
    for(int i=1;i<n;i++){
        p[i] = max(011,min(r-i,p[1+r-i]));
    }
}</pre>
```

```
while(i+p[i] < n and i-p[i] >= 0 and s[i+p[i]] == s[i-p
              p[i]++;
          }
          if((i+p[i])>r){
              l = i-p[i];
              r = i+p[i];
      }
   void build(string s){
       string t;
       for(auto i:s){
          t.push_back('#');
          t.push_back(i);
       t.push_back('#');
       run manacher(t):
   int get_longest(int index,bool odd){
       if(odd){
           return (p[(2*index)+1])-1;
       }else{
          return (p[2*(index+1)])-1;
   }
   bool check_palindrome(int 1,int r){
       int l1 = l,r1=r;
       1 = (2*1+1);
       r = (2*r+1):
       int index = (1+r)>>1;
       if(p[index]-1>=(r1-11+1)){
          return true:
       }else{
          return false;
       }
   }
}m:
```

#### 6.3 Trie

```
typedef struct trie{
   typedef struct node{
```

```
node* nxt[2]:
   int cnt = 0;
   node(){
       nxt[0] = nxt[1] = NULL;
       cnt = 0;
   }
}Node;
Node* head:
trie(){
   head = new Node();
void insert(int x){
   Node* curr = head:
   for(int i=30;i>=0;i--){
       int b = (x>>i)&1;
       if(curr->nxt[b] == NULL){
          curr->nxt[b] = new Node();
       curr = curr->nxt[b];
       curr->cnt ++;
   }
void remove(int x){
   Node* curr = head:
   for(int i=30:i>=0:i--){
       int b = (x>>i)&1;
       curr = curr->nxt[b]:
       curr->cnt --;
```

```
} } } } } }
```

## 7 template

```
#include <bits/stdc++.h>
using namespace std;
#define INF 1e18
#define endl "\n"
#define pb push_back
#define ppb pop_back
#define mp make_pair
#define PI atan(1)*4
#define set_bits __builtin_popcount110
#define all(x) (x).begin(), (x).end()
#define vi vector<int>
#define vll vector<11>
#define pll pair<11,11>
#define rvsort(a) sort(all(a),greater<int>())
#define read(a,n) for(int i = 0; i < n; i ++){ cin >> a[i
#define printv(a) for(auto it: a){cout << it << " ";} cout</pre>
     << endl:
#define ms(arr, v) memset(arr, v, sizeof(arr))
```

```
typedef long long 11;
typedef unsigned long long ull;
typedef long double 11d;
mt19937 rng(chrono::steady_clock::now().time_since_epoch().
11 uid(11 1, 11 r) {return uniform_int_distribution<11>(1, r
    )(rng);}
void solve(){
int main() {
ios::sync_with_stdio(0);
cin.tie(0);
cout.tie(0):
11 t = 1;
cin >> t;
for(int i = 1 ; i <= t ; i++){</pre>
//google(i);
 solve();
return 0;
```