

i) Consider the grammar

$$S \rightarrow aAd \mid bBd \mid aBe \mid bAe$$

$$A \rightarrow C$$

$$B \rightarrow C$$

i) Create the LR(1) canonical sets of items

ii) Construct the CLR(1) parsing table for the grammar.

iii) Construct the LALR(1) parsing table for the grammar. Is this grammar LALR(1)? Justify.

Ans → ~~closed~~ Augmented Grammar →

$$S' \rightarrow S$$

$$S \rightarrow aAd$$

$$S \rightarrow bBd$$

$$S \rightarrow aBe$$

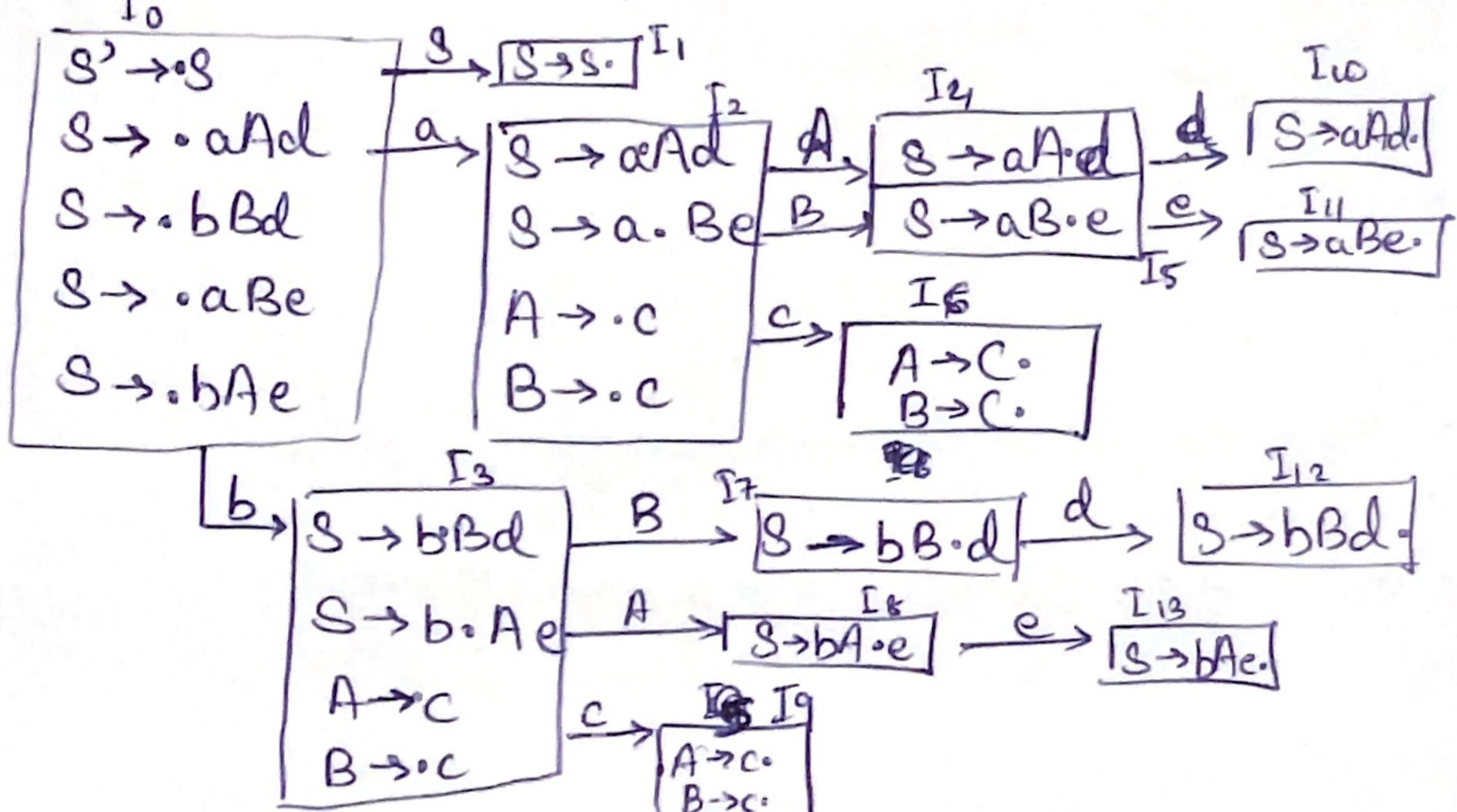
$$S \rightarrow bAe$$

$$A \rightarrow C$$

$$B \rightarrow C$$

LR(1)

i) Canonical sets of items →



ii) CLR(1) Parsing Table →

	Action						GoTo		
	a	b	c	d	e	\$	S	A	B
I ₀	s ₂	s ₃							
I ₁							accept		
I ₂		s ₆					4	5	
I ₃		s ₉					8	7	
I ₄			s ₁₀						
I ₅				s ₁₁					
I ₆				r ₆	r ₇				
I ₇				s ₁₂					
I ₈					s ₁₃				
I ₉				r ₇	r ₆				
I ₁₀						r ₂			
I ₁₁						r ₄			
I ₁₂						r ₃			
I ₁₃						r ₅			

iii) LALR(1) Parsing table →

	Action						GoTo		
	a	b	c	d	e	\$	A	B	
I ₀	s ₂	s ₃							1
I ₁						accept			
I ₂			s ₆				4	5	
I ₃			s ₆				8	7	
I ₄			s ₉						
I ₅				s ₁₀					
I ₆					r _{6/r7}	r _{6/r7}			
I ₇					s ₁₁				
I ₈						s ₁₂			
I ₉							r ₂		
I ₁₀							r ₄		
I ₁₁							r ₃		
I ₁₂							r ₅		

So, the grammar is not LALR(1) as there are reduce-reduce conflict in state 6.

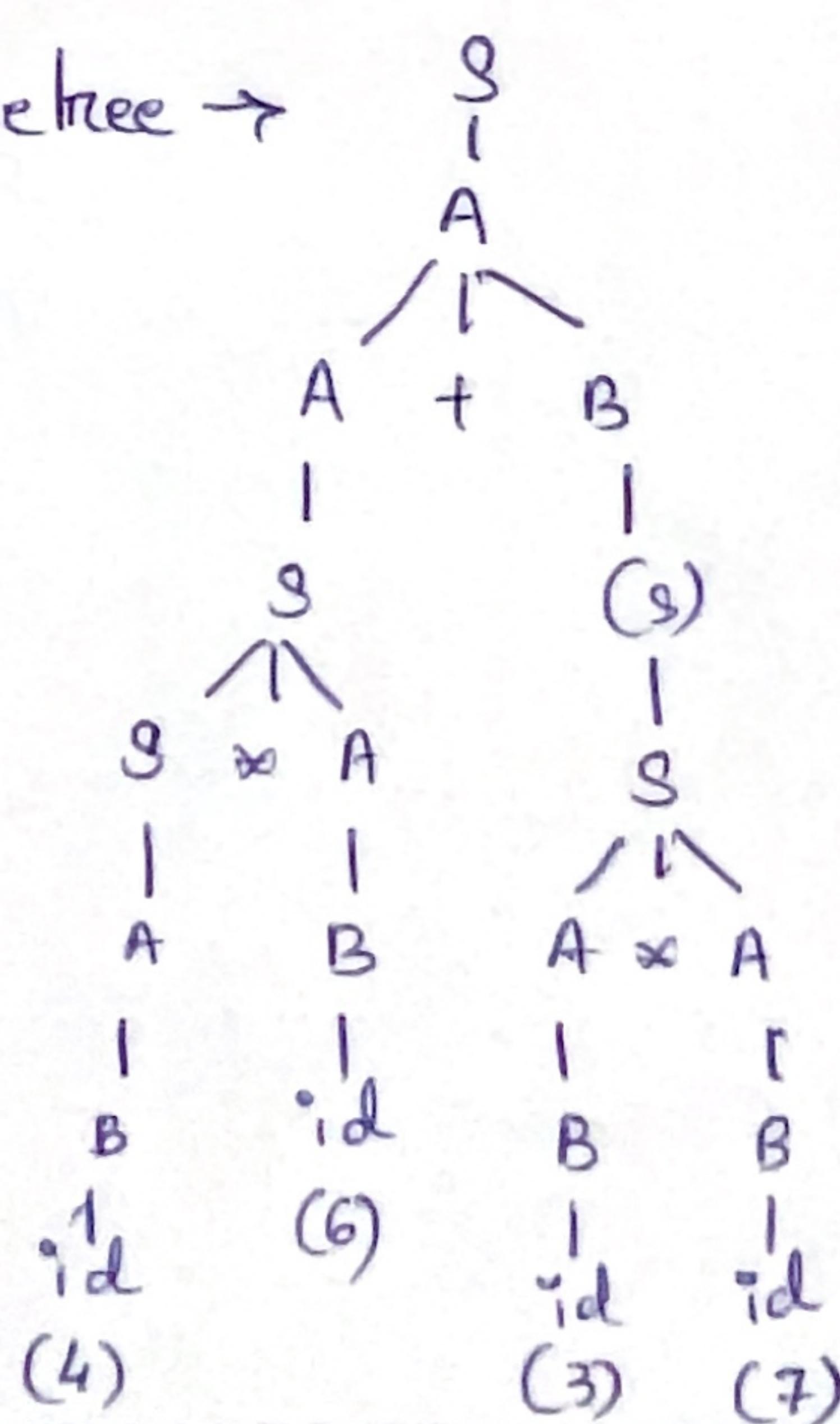
2) Consider the following grammar and their syntax Directed Translation (SDT) rules.

Productions	Semantic Rules
S → S * A	{S.val = S.val * A.val ?}
S → A	{S.val = A.val ?}
A → A + B	{A.val = A.val - B.val ?}
B → (S)	{B.val = ?}
A → B	{A.val = B.val ?}
B → id	{B.val = id.level ?}

Construct the annotated parse tree and evaluate the value of the expression 4 * 6 + 3 * 7.

Ans → S → A
 → A + B
 → (S) + B
 → (S * A) + B
 → (A + A) + B
 → (B * A) + B
 → (id * A) + B
 → (id * B) + B
 → (id * id) + B
 → (id * id) + (S)

Annotated Parse tree →



$\rightarrow (\text{id} * \text{id}) + (\text{S} * \text{A})$
 $\rightarrow (\text{id} * \text{id}) + (\text{A} * \text{A})$
 $\rightarrow (\text{id} * \text{id}) + (\text{B} * \text{A})$
 $\rightarrow (\text{id} * \text{id}) + (\text{id} * \text{A})$
 $\rightarrow (\text{id} * \text{id}) + (\text{id} * \text{B})$
 $\rightarrow (\text{id} * \text{id}) + (\text{id} * \text{id})$

Parse tree with annotations →

• Leaves (Terminals id) →

- $\text{id}(4) : B \rightarrow \text{id}, B.\text{val} = \text{id}. \text{lexval} = 4$
- $\text{id}(6) : B \rightarrow \text{id}, B.\text{val} = \text{id}. \text{lexval} = 6$
- $\text{id}(3) : B \rightarrow \text{id}, B.\text{val} = \text{id}. \text{lexval} = 3$
- $\text{id}(7) : B \rightarrow \text{id}, B.\text{val} = \text{id}. \text{lexval} = 7$

• Right subtree : $B \rightarrow (\text{S})$ for $3 * 7$:

• Subtree for (S) (inside (S)):

• Left $\text{S} \rightarrow \text{A} \rightarrow \text{B}$, $B \rightarrow \text{id}(3) : B.\text{val} = 3$

• Right $\text{B} \rightarrow \text{id}(7) : B.\text{val} = 7$

• $\text{S} \rightarrow \text{S} * \text{A} : \text{S}.\text{val} = \text{S}.\text{val} * \text{A}.\text{val} = 3 * 7 = 21$

• $B \rightarrow (\text{S}) : B.\text{val} = 2$ (fixed value for parenthesised expression)

• Left subtree : $\text{S} \rightarrow \text{S} * \text{A}$ for $4 * 6$:

• Left $\text{S} \rightarrow \text{A} \rightarrow \text{B} \rightarrow \text{id}(4) : B.\text{val} = 4$

• Right $\text{A} \rightarrow \text{B} \rightarrow \text{id}(6) : B.\text{val} = 6$

• $\text{S}.\text{val} = \text{S}.\text{val} * \text{A}.\text{val} = 4 * 6 = 24$

• Top $\text{A} \rightarrow \text{A} + \text{B}$:

• Left $\text{A} \rightarrow \text{B} \rightarrow \text{id}(4) : A.\text{val} = 4$

• Right $\text{B} \rightarrow \text{id}(6) : B.\text{val} = 6$

• $A.\text{val} = A.\text{val} - B.\text{val} = 4 - 6 = 22$

• Root $\text{S} \rightarrow \text{A}$

• $\text{S}.\text{val} = A.\text{val} = 22$.

∴ Value of expression as per SDT is 22.

Annotated Parse tree

$\text{S}[\text{val} = 22]$

 |

$\text{A}[\text{val} = 22]$

 / \

$\text{A}[\text{val} = 24] + \text{B}[\text{val} = 2]$

 |

$\text{S}[\text{val} = 24]$

 |

$(\text{S}[\text{val} = 21])$

 / \ / \

$\text{G}[\text{val} = 4] * \text{A}[\text{val} = 6] \text{ A}[\text{val} = 3] * \text{A}[\text{val} = 7]$

 |

$\text{A}[\text{val} = 4]$

 |

$\text{B}[\text{val} = 6] \text{ B}[\text{val} = 3] \text{ B}[\text{val} = 7]$

 |

$\text{id}[6]$

 |

$\text{id}[3]$

 |

$\text{id}[7]$

3) A shift reduce parser carries out the actions specified within braces immediately after reducing with the corresponding rule of grammar.

$$S \rightarrow aaW \quad \{ \text{print } '1' \}$$

$$S \rightarrow b \quad \{ \text{print } '2' \}$$

$$W \rightarrow Sc \quad \{ \text{print } '3' \}$$

Construct the annotated parse tree and find the translation of $aaaabcc$ using the syntax directed translation scheme described by the above rules.

$$\text{Ans} \rightarrow S \rightarrow aaW$$

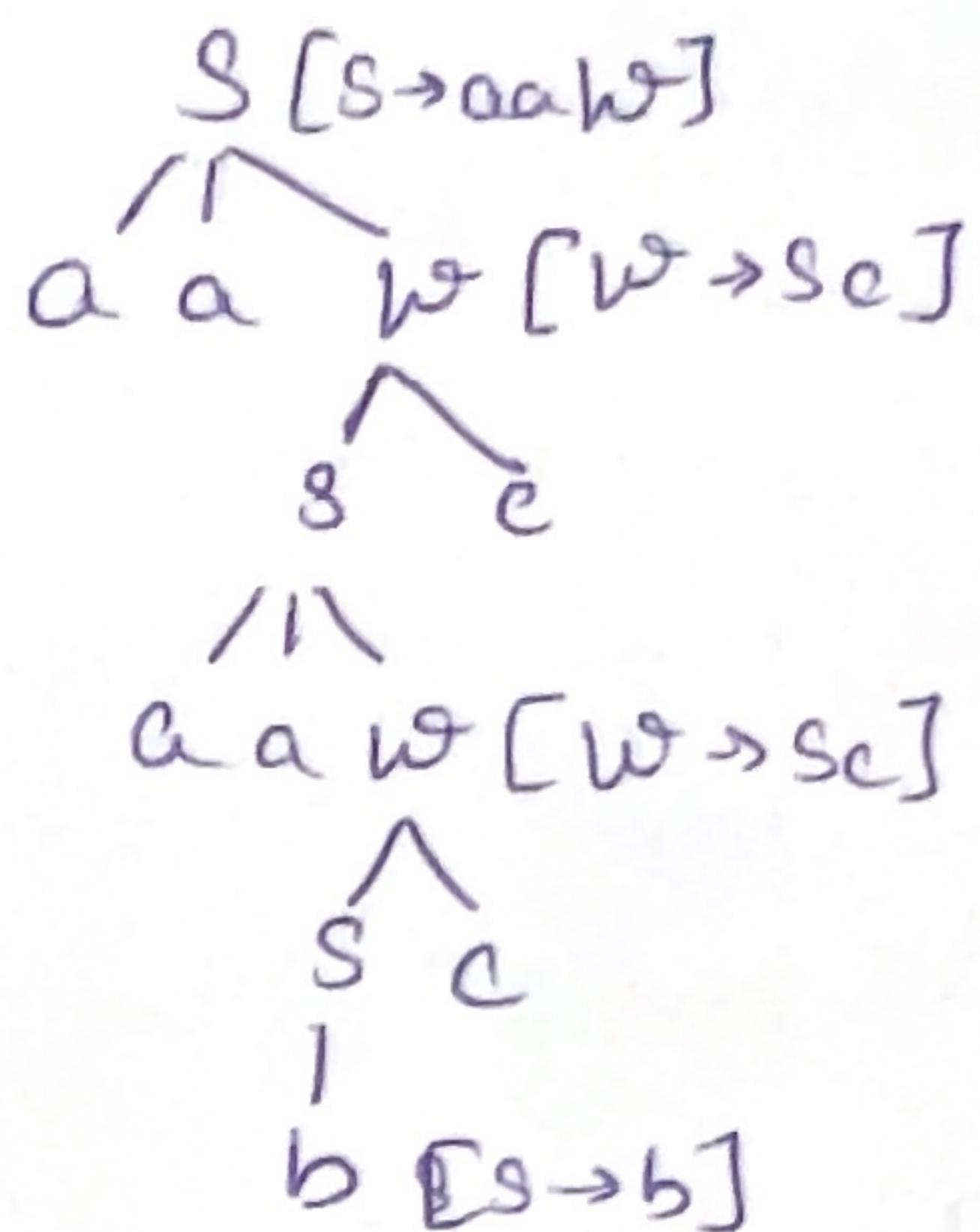
$$\rightarrow aaSc$$

$$\rightarrow aaaWc$$

$$\rightarrow aaaSc$$

$$\rightarrow aaaabcc$$

Annotated Parse tree →



Simulate Shift reduce parsing →

- Input: $aaaabcc$
- Stack: Initially empty
- Actions:
 1. shift a : Stack = a
 2. shift a : Stack = aa
 3. shift a : Stack = aaa
 4. shift a : Stack = $aaaa$
 5. shift b : Stack = $aaaab$
 6. reduce $S \rightarrow b$: Pop b , push \emptyset , print 2
• Stack = $aaaaS$

7. shift c : Stack ~~$aaaa$~~ $aaaac$ $\{ \text{print } 2 \}$ Sc

8. Reduce $W \rightarrow Sc$: Pop Sc , push W , print 3
• Stack = $aaaaw$

9. Reduce $S \rightarrow aaW$: Pop aaW , push S , print 1
• Stack = aaW

10. Shift c : Stack = $aaSc$

11. Reduce $W \rightarrow Sc$: Pop Sc , push W , print 3.
• Stack $\rightarrow aaW$

12. Reduce $S \rightarrow aaW$: Pop aaW , push S , print 1
• Stack $\rightarrow S$

13. Accept.

∴ Output sequence $\rightarrow 2 3 1 3 1$

4) Consider the expression $a + a * (b - c) + (b - c) * d$. Generate the three-address code TAC for the given expression.

Ans → Expression → $a + a * (b - c) + (b - c) * d$

Three - Address Code (TAC) → Let's ^{compute} $t_1 = b - c$

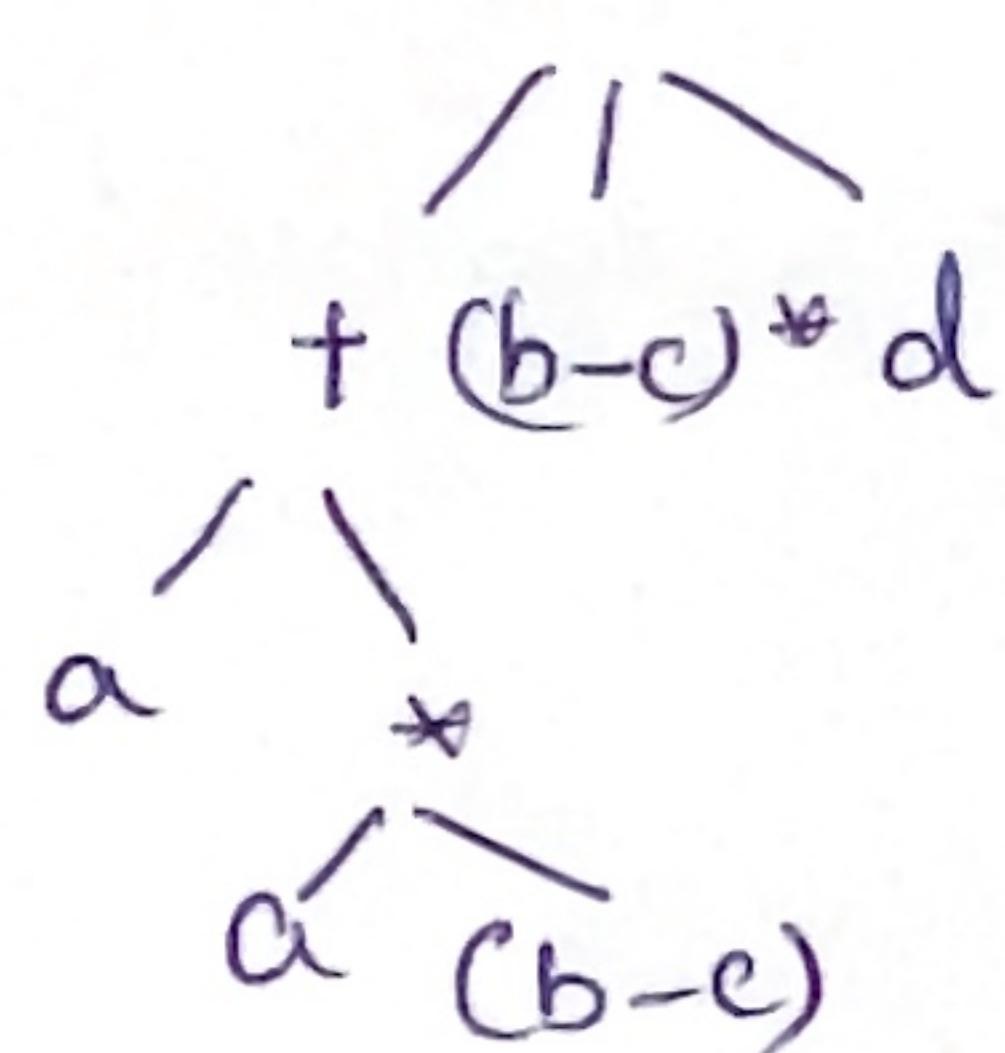
$$t_2 = a * (b - c) = a * t_1$$

$$t_3 = a + a * (b - c) = a + t_2$$

$$t_4 = \cancel{a + a * (b - c)} + (b - c) * d = t_1 * d$$

$$t_5 = t_3 + t_4$$

Parse tree →



5) Represent the three - address code that is generated in Q4, using the following intermediate code formats:

- i) Quadruples
- ii) Triples
- iii) Indirect Triples

Ans → i) Quadruples →

TAC to Quadruples →

- $t_1 = b - c \rightarrow (\text{sub}, b, c, t_1)$
- $t_2 = a * t_1 \rightarrow (\text{mul}, a, t_1, t_2)$
- $t_3 = a + t_2 \rightarrow (\text{add}, a, t_2, t_3)$
- $t_4 = t_1 * d \rightarrow (\text{mul}, t_1, d, t_4)$
- $t_5 = t_3 + t_4 \rightarrow (\text{add}, t_3, t_4, t_5)$

Table →

Index	Op	Arg1	Arg 2	Result
0	sub	b	c	t1
1	mul	a	t1	t2
2	add	a	t2	t3
3	mul	t1	d	t4
4	add	t3	t4	t5

ii) Triples →

- $t_1 = b - c \rightarrow (\text{sub}, b, c)$ at index 0 (result is index 0)
- $t_2 = a * t_1 \rightarrow (\text{mul}, a, 0)$ at index 1 (uses t1 as index 0)
- $t_3 = a + t_2 \rightarrow (\text{add}, a, 1)$ at index 2 (uses t2 as index 1)
- $t_4 = t_1 * d \rightarrow (\text{mul}, 0, d)$ at index 3 (uses t1 as index 0)
- $t_5 = t_3 + t_4 \rightarrow (\text{add}, 2, 3)$ at index 4 (uses t3 as index 2, t4 as index 3)

Triples Table →

<u>Index</u>	<u>Op</u>	<u>Arg 1</u>	<u>Arg 2</u>
0	sub	b	c
1	mul	a	0
2	add	a	1
3	mul	0	d
4	add	2	3

iii) Indirect Triples → Indirect triples ~~store~~ store the same triples as above but use a separate instruction pointer list to reference them.

Instruction pointer list → Since no reordering is specified, the pointer list is sequential →

<u>Index</u>	<u>Instruction</u>
0	0
1	1
2	2
3	3
4	4