

Q1) What do you mean by Artificial Neural Network (ANN) and write down some applications of Artificial Neural Network?

Ans → An Artificial Neural Network (ANN) is a computational model inspired by the way biological neural networks in the human brain process information. It is a part of machine learning.

An ANN consists of multiple layers →

i) Input layer → Accepts the input data.

ii) Hidden layer → Layers between the input output that process the data through various transformation.

iii) Output layer → Produces the final result, such as a prediction or classification.

The applications of Artificial Neural Network (ANN) →

i) Image Recognition → Identifying objects in images.

ii) Natural Language Processing (NLP) → Used in speech recognition, language translation and ~~chat~~ chatbots.

iii) Autonomous Vehicles → Self-driving cars use ANNs for object recognition and decision-making.

Q2) Give some idea about the advantages and limitations of Artificial Neural Network.

Ans → Advantages of Artificial Neural Network (ANN) →

- i) Learning from data → Can learn patterns from large datasets without explicit programming.
- ii) Flexibility → Suitable for diverse tasks like classification, regression, and pattern recognition.
- iii) Fault tolerance → Can handle noisy or incomplete data.

Limitations of Artificial Neural Network →

- i) Data hungry → Requires large amount of high-quality data.
- ii) Computationally Expensive → Needs significant computational power and time.
- iii) Low of interpretability → Hard to understand how decisions are made.

Q3) What is Deep learning? Differentiate between Machine Learning and Deep learning.

Ans → Deep learning is a subset of machine learning that uses multi-layered neural networks to automatically learn features from large datasets, excelling in tasks like image recognition and language translation. It requires significant data & computational power.

Machine Learning

- i) ML is a subset of AI where algorithms learn from data and improve over time.

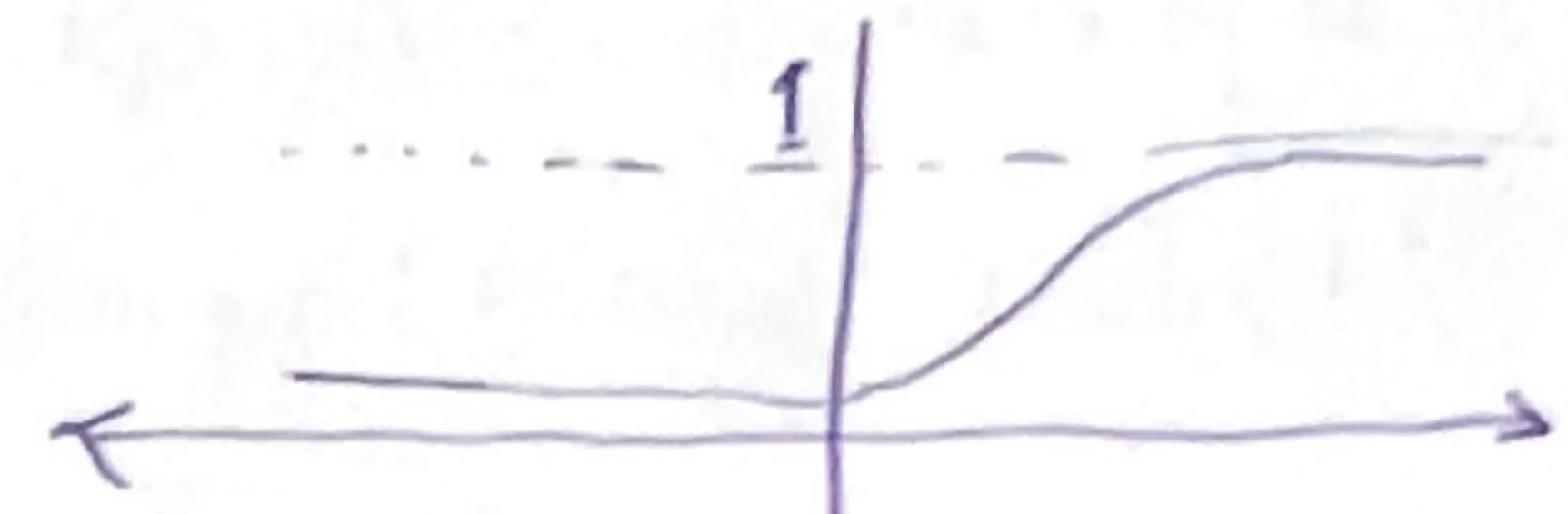
Deep Learning

- i) DL is a subset of ML that use neural networks with multiple layers to learn from large datasets.

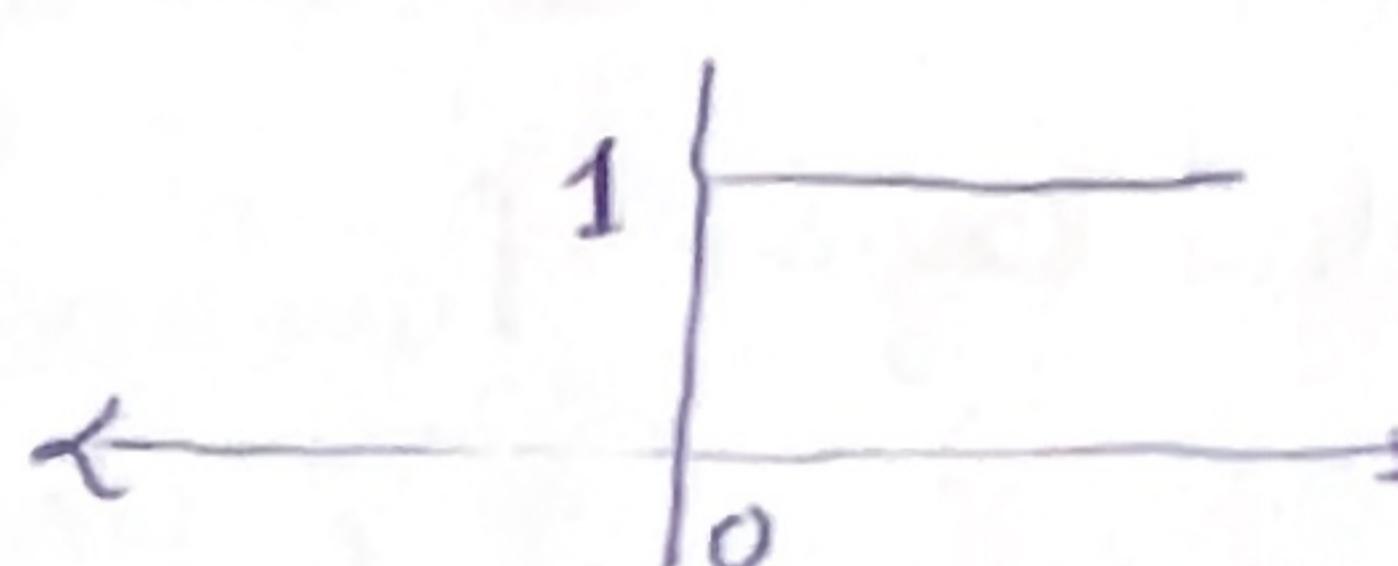
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|--|---|
| ii) Works well with smaller datasets.
iii) Requires manual feature extraction and selection.
iv) Less computationally intensive. | ii) Requires large datasets to perform effectively.
iii) Automatically learns features from raw data.
iv) Requires significant computational resources often with GPUs or TPUs. |
|--|---|

Q) 4) Describe four different types of activation functions.

Ans → i) Logistic Function $\rightarrow f(z) = \frac{1}{1+e^{-z}}$, $f(z) : R \rightarrow (0, 1)$



ii) Step function $\rightarrow f(z) = \begin{cases} 0, & \text{if } z < 0 \\ 1, & \text{if } z \geq 0 \end{cases}$



iii) Rectified linear unit function or ReLU(z) \rightarrow

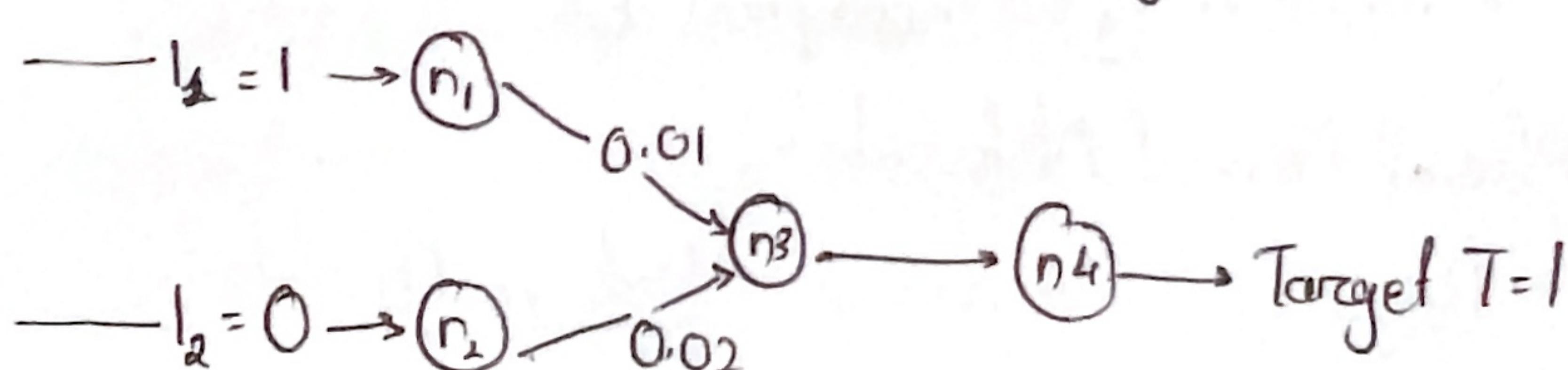
$$f(z) = \begin{cases} 0, & \text{if } z < 0 \\ z, & \text{if } z \geq 0 \end{cases} \quad \text{Range } (0, +\infty)$$



iv) Hyperbolic tangent function \rightarrow

$$\tanh(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$

5) Consider a simple neural network as shown in Figure. The inputs and initial weights are also shown in Figure. Target of the given neural network is $T=1$. Use back propagation to train the network. The activation function is sigmoid function. Using the learning rate = 0.3.



a) Perform the forward pass and calculate the predicted output.

b) Find out the error at the output layer.

c) Perform the backward pass and update the weights.

Ans → a) $I_1 = 1, I_2 = 0, w_1 = 0.01, w_2 = 0.02, w_3 = 0.03, T = 1$

$$\text{Net input of } n_3 = 1 \times 0.01 + 0 \times 0.02 = 0.01$$

$$\text{Output of } n_3 = \frac{1}{1+e^{-0.01}} = 0.5025$$

$$\text{Net input of } n_4 = 0.5025 \times 0.03 = 0.015$$

$$\text{Output of } n_4 = \frac{1}{1+e^{-0.015}} = 0.5038$$

b) Error = $\frac{1}{2} (1 - 0.5038)^2 = 0.1231$

c) Learning rate (η) = 0.3

$$w_3 \text{ new} = \frac{\delta E_{\text{total}}}{\delta w_3} = \frac{\delta E_{\text{total}}}{\delta \text{out}_{n_4}} \times \frac{\delta \text{out}_{n_4}}{\delta \text{net}_{n_4}} = \frac{\delta \text{net}_{n_4}}{\delta w_3}$$

$$\frac{\delta E_{\text{total}}}{\delta \text{out}_{n_4}} = (\text{out}_{n_4} - \text{Target}_{n_4}) = 0.5038 - 1 = -0.4962$$

$$\frac{\delta \text{out}_{n_4}}{\delta \text{net}_{n_4}} = \text{out}_{n_4} (1 - \text{out}_{n_4}) = 0.5038 (1 - 0.5038) = 0.2494 \\ \approx 0.25$$

$$\frac{\delta \text{net}_{n_4}}{\delta w_3} = \text{out}_{n_3} = 0.5025$$

$$w_3 \text{ new} = w_3 - (\eta \times \frac{\delta E_{\text{total}}}{\delta w_3}) = 0.03 - (0.3 \times -0.4962 \times 0.25 \times 0.5025) \\ = 0.03 + 0.0187 \\ = 0.0487.$$

w_1 new

$$\Delta w = \eta \times \delta n_3 \times 1$$

$$\delta(n_3) = \text{out}_{n_3} \times (1 - \text{out}_{n_3}) = 0.2499 \approx 0.25$$

$$I = \text{Input } I_1 = 1$$

$$\delta n_3 = 0.124 \times 0.3 \times 0.2499 = 0.00093$$

$$\Delta w = 0.3 \times 0.00093 \times 1 = 0.00028$$

$$w_1 \text{ new} = 0.01 + 0.00028 = 0.01028$$

w_2 new

$$I_2 = 0$$

$$\Delta w = \eta = \delta n_3 \times I_2 = 0$$

So, no change. $w_2 = \text{new}$.

Q6) What are the applications of SVD in machine learning and artificial intelligence?

Ans \rightarrow Singular value decomposition (SVD) is a popular image transformation technique. It has lot of applications in dimensionality reduction, image restoration, image compression and object recognition. SVD transforms a given matrix A to be factorized into matrices U, Σ , V^T .

$$A = U \Sigma V^T$$

U = Normalised Eigen Value matrix of AA^T .

V^T = Transpose of Normalised Eigen value matrix of A^TA .

Q7) Using singular value decomposition, find the matrices U, V and Σ for the matrix $A = \begin{bmatrix} 3 & 2 & 2 \\ 2 & 3 & -2 \end{bmatrix}$

Ans → Using SVD, we known that $A = U\Sigma V^T$.

For U, AA^T

$$AA^T = \begin{bmatrix} 3 & 2 & 2 \\ 2 & 3 & -2 \end{bmatrix} \begin{bmatrix} 3 & 2 \\ 2 & 3 \\ 2 & -2 \end{bmatrix} = \begin{bmatrix} 17 & 8 \\ 8 & 17 \end{bmatrix}$$

$$\lambda_1 = 25, \lambda_2 = 9$$

$$(x - \lambda I) \begin{pmatrix} p_1 \\ p_2 \end{pmatrix} = 0$$

For $\lambda_1 = 25$

$$\begin{bmatrix} 17 & 8 \\ 8 & 17 \end{bmatrix} - \begin{bmatrix} 25 & 0 \\ 0 & 25 \end{bmatrix} \begin{pmatrix} p_1 \\ p_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \Rightarrow \begin{bmatrix} -8 & 8 \\ 8 & -8 \end{bmatrix} \begin{pmatrix} p_1 \\ p_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$-8p_1 + 8p_2 = 0$$

$$\Rightarrow 8p_1 = 8p_2$$

$$\Rightarrow p_1 = p_2$$

Eigen vector for $\lambda_1 = 25 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$

$$\text{Normalize} = \begin{pmatrix} 1/\sqrt{2} \\ 1/\sqrt{2} \end{pmatrix}$$

For $(\lambda_2 = 9)$

$$\begin{bmatrix} 17 & 8 \\ 8 & 17 \end{bmatrix} \begin{bmatrix} 9 & 0 \\ 0 & 9 \end{bmatrix} \begin{pmatrix} p_1 \\ p_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \Rightarrow \begin{bmatrix} 8 & 8 \\ 8 & 8 \end{bmatrix} \begin{pmatrix} p_1 \\ p_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$8p_1 + 8p_2 = 0$$

$$\lambda_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$\Rightarrow p_2 = -p_1$$

$$\text{Normalize eigen vector} = \begin{pmatrix} -1/\sqrt{2} \\ 1/\sqrt{2} \end{pmatrix}$$

$$U = \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} \end{bmatrix}$$

$$\Sigma \rightarrow \sigma_1 = \sqrt{\lambda_1} = \sqrt{25} = 5$$

$$\sigma_2 = \sqrt{\lambda_2} = \sqrt{9} = 3$$

$$\Sigma = \begin{bmatrix} 5 & 0 & 0 \\ 0 & 3 & 0 \end{bmatrix}$$

$$V = A^T A$$

Eigen values are $\lambda_1 = 25$, $\lambda_2 = 9$, $\lambda_3 = 0$

$$A^T A = \begin{bmatrix} 3 & 2 \\ 2 & 3 \\ 2 & -2 \end{bmatrix} \begin{bmatrix} 3 & 2 & 2 \\ 2 & 3 & -2 \end{bmatrix} = \begin{bmatrix} 13 & 12 & 2 \\ 12 & 13 & -2 \\ 2 & -2 & 8 \end{bmatrix}$$

$$\text{For } \lambda_1 = 25 \quad (x - \lambda_1 I) \begin{pmatrix} P_1 \\ P_2 \\ P_3 \end{pmatrix} = 0$$

$$\begin{bmatrix} -12 & 12 & 2 \\ 12 & -12 & -2 \\ 2 & -2 & -17 \end{bmatrix} \begin{pmatrix} P_1 \\ P_2 \\ P_3 \end{pmatrix} = 0$$

$$-12P_1 + 12P_2 + 2P_3 = 0$$

$$\Rightarrow 12P_1 - 12P_2 - 2P_3 = 0 \quad \text{--- (1)}$$

$$\Rightarrow 2P_1 - 2P_2 - 17P_3 = 0 \quad \text{--- (2)}$$

$$P_3 = 0$$

$$P_1 = P_2$$

$$x_1 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} \quad N(x_1) = \begin{pmatrix} 1/\sqrt{2} \\ 1/\sqrt{2} \\ 0 \end{pmatrix}$$

$$\text{For } \lambda_2 = 9$$

$$\begin{bmatrix} 4 & 3 & -7 \\ 3 & 4 & -11 \\ -7 & -11 & -1 \end{bmatrix} \begin{pmatrix} P_1 \\ P_2 \\ P_3 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$

$$4P_1 + 3P_2 - 7P_3 = 0 \quad \text{--- (1)} \quad 3P_1 + 4P_2 - 11P_3 = 0 \quad \text{--- (2)}$$

$$-7P_1 - 11P_2 - P_3 = 0$$

$$\Rightarrow P_3 = 7P_1 - 11P_2$$

$$\Rightarrow -7P_1 - 11P_2 - 65P_3 = 0$$

$$\Rightarrow -7P_1 = 65P_2$$

$$\Rightarrow P_2 = -\frac{65}{7}P_1 \quad P_1 = \frac{61}{7}P_3$$

$$x_2 = \begin{pmatrix} 61/7 \\ -65/7 \\ 1 \end{pmatrix} \quad N(x_2) = \begin{pmatrix} 61/89 \\ -65/89 \\ 0 \end{pmatrix}$$

$$\text{For } \lambda_3 = 0$$

$$\begin{bmatrix} 13 & 12 & 2 \\ 12 & 13 & -2 \\ 2 & -2 & 8 \end{bmatrix} \begin{pmatrix} P_1 \\ P_2 \\ P_3 \end{pmatrix} = 0$$

$$P_1 = P_2 \quad P_3 = 0$$

$$x_3 = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix} \quad N(x_3) = \begin{pmatrix} 1/\sqrt{2} \\ 1/\sqrt{2} \\ 0 \end{pmatrix}$$

$$V = \begin{bmatrix} 1/\sqrt{2} & 61/89 & 1/\sqrt{2} \\ 1/\sqrt{2} & -65/89 & 1/\sqrt{2} \\ 0 & 0 & 0 \end{bmatrix}$$

Q8) What is Principal Component Analysis and how does it work?

Ans → It works on the condition that while the data in a higher dimension space is mapped to data in a lower dimension space the variance of the data in the lower dimensional space should be maximum.

- It is a statistical procedure that uses an orthogonal transformation that consists of a set of co-related variable to set of un-correlated variable.
- It is an unsupervised learning algorithm used to examine the inter relation between the set of relations.
- The main goal of principal component analysis is to reduce the dimensity of data set.

Q9) Given data $x_1: \{2, 3, 4, 5, 6, 7\}$ and $x_2: \{1, 5, 3, 6, 7, 8\}$. Compute the principal component using PCA algorithm.

Ans → $\bar{x} = \frac{2+3+4+5+6+7}{6} = 4.5$, $\bar{y} = \frac{1+5+3+6+7+8}{6} = 1.66$

Hence, the co-variance matrix is.

$$S = \begin{bmatrix} \text{cov}(x, x) & \text{cov}(x, y) \\ \text{cov}(y, x) & \text{cov}(y, y) \end{bmatrix}$$

$$\begin{aligned} \text{cov}(x, x) &= \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 \\ &= \frac{1}{6-1} [(2-4.5)^2 + (3-4.5)^2 + (4-4.5)^2 + (5-4.5)^2 + (6-4.5)^2 + (7-4.5)^2] \\ &= \frac{1}{5} (2.25 + 0.25 + 0.25 + 0.25 + 2.25 + 6.25) \\ &= \frac{11.5}{5} = 2.3 \end{aligned}$$

$$\begin{aligned} \text{cov}(x, y) &= \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}) \\ &= \frac{1}{5} [(2-4.5)(1-1.66) + (3-4.5)(5-1.66) + (4-4.5)(3-1.66) + (5-4.5)(6-1.66) + (6-4.5)(7-1.66) + (7-4.5)(8-1.66)] \\ &= \frac{1}{5} [(-2.5)(-0.66) + (-0.5)(3.34) + (0.5)(1.34) + (0.5)(4.34) + (1.5)(5.34) + (2.5)(6.34)] \\ &= \frac{1}{5} (26.87) = 5.374. \end{aligned}$$

$$\text{cov}(y, x) = \frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})(x_i - \bar{x}) = 5.375$$

$$\text{cov}(y, y) = 20.18672$$

Hence, $S = \begin{bmatrix} 2.3 & 5.374 \\ 5.374 & 20.18672 \end{bmatrix}$

$|S - \lambda I| = 0$

$$\left| \begin{bmatrix} 2.3 - \lambda & 5.374 \\ 5.374 & 20.1867 \end{bmatrix} \right| = 0$$

$$\Rightarrow (2.3 - \lambda)(20.1867 - \lambda) - (5.374)^2 = 0$$

$$\Rightarrow \lambda^2 - 22.4867\lambda + 17.58 = 0$$

$$\therefore \lambda_1 = 21.76780, \lambda_2 = 0.8096$$

Q10) What is the significance of Eigen vector and Eigen values in PCA?

Ans → Eigen vectors define the new axes (Principal components) that maximise variance in the data. Eigen values measures the amount of variance along each eigen vector.

The largest eigen values and their corresponding eigen vectors capture the most important feature of the data, enabling dimensionality reduction and pattern recognition.

Q11) What is the purpose of pooling layer in CNN?

Ans → Pooling is a down-sampling operation that reduces the dimensionality of a feature map. It is applied to rectify feature map to get pooled feature map.

Q12) Describe the term padding in CNN and the purpose of using padding in image processing.

Ans → Padding in CNN refers to adding extra pixels around the edges of an image before applying convolution.

Purpose of padding in Image Processing →

i) ~~Preserve~~ Preserve Dimensions → Ensure the output size of the feature map remain the same as the input size, which is important for deeper networks.

ii) Avoid Information Loss → Without padding, edge pixels are used less frequently in convolutions, leading to the loss of edge information.

iii) Control Output size → Padding allows flexibility in determining the size of the output feature map.

iv) Improve Performance → Helps maintain spatial information at the edges of the input image.

13) a) Feature map (a) = $\begin{bmatrix} 33 & 47 \\ 18 & 44 \end{bmatrix}$

b) Padded Input $\rightarrow \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 4 & 7 & 1 & 5 \\ 0 & 2 & 5 & 8 & 0 & 6 \\ 0 & 3 & 6 & 9 & 2 & 7 \\ 0 & 0 & 1 & 2 & 3 & 8 \\ 0 & 1 & 0 & 3 & 4 & 9 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$

Convolution with stride →

Feature map (b) = $\begin{bmatrix} 10 & 25 & 20 \\ 15 & 27 & 38 \\ 2 & 13 & 24 \end{bmatrix}$

c) Pooled Feature map (c) = [19.25]

14) What is Natural Language Processing and how does it differ from Natural Language Understanding (NLU) and Natural Language Generation (NLG)?

Ans → Natural Language Processing (NLP) is a ~~subset~~ field of Artificial Intelligence that focuses on enabling computers to process, analyze and generate human language. It encompasses a wide range of tasks, such as text analysis, language translation, speech recognition and sentiment analysis.

NLP

- i) Processing language data
- ii) Text or speech
- iii) Structured data
- iv) Sentiment Analysis

NLU

- i) Understanding language
- ii) Text or speech
- iii) Contextual meaning
- iv) Intent recognition

NLG

- i) Generating language
- ii) Structured data or intent.
- iii) Human-readable language
- iv) Chatbot responses.

15) Given the following corpus of 3 documents.

i) "The apple is red and sweet."

ii) "The orange is orange and tangy."

iii) "The fruit basket contains apples, oranges and bananas."

a) Calculate the TF for the term "apple" and "sweet" for the document (i). Also, calculate IDF for the terms "orange" and "fruit".

b) Find term-document matrix for documents(i) and(ii).

Ans \rightarrow TF = $\frac{\text{No. of occurrences of term in documents}}{\text{Total no. of terms in documents}}$

$$\begin{aligned}\text{Total term in document} &= ["\text{the}", "\text{apple}", "\text{is}", "\text{red}", "\text{and}", "\text{sweet}"] \\ &= 6\end{aligned}$$

$$TF(\text{apple}) = \frac{1}{6} = 0.1667 = TF(\text{sweet})$$

$$IDF(\text{orange}) = \log \left(\frac{3}{2} \right) = \log (1.5) = 0.1761$$

$$IDF(\text{fruit}) = \log (3) = 0.4771$$

b) Unique terms = ["the", "apple", "is", "red", "and", "sweet", "orange", "tangy"]

We calculate TF values for each term for both documents.

<u>Term</u>	<u>Documents (i)</u>	<u>Documents (ii)</u>
the	$\frac{1}{6} = 0.1667$	$\frac{1}{6} = 0.1667$
apple	$\frac{1}{6} = 0.1667$	0
is	$\frac{1}{6} = 0.1667$	$\frac{1}{6} = 0.1667$
red	$\frac{1}{6} = 0.1667$	0
and	$\frac{1}{6} = 0.1667$	$\frac{1}{6} = 0.1667$
sweet	$\frac{1}{6} = 0.1667$	0
orange	0	$\frac{2}{6} = 0.3333$
tangy	0	$\frac{1}{6} = 0.1667$