

BIG O

-> BIG O in layman language

a tool to analyze the performance of your code or algorithm

let's take a step back to understand from where big O notation is coming

-> Asymptotic analysis

- defining the mathematical boundation of any algorithm to define its run-time performance.
- helps in concluding the best case, average case, and worst case scenario of an algorithm.
- bound to input which means if there is no input, algo will work in constant time.

-> need of doing this analysis?

- define performance of a system.
- take example of an assembly line for a soft drink bottle.
 - Say first step is to clean the bottle

BIG O

- second is to fill bottle
- third is to seal it
- fourth is to print the logo
- let's say each of the step takes 1 second per bottle except filling which takes 5 sec.
- the overall performance of the system will be 5 sec.
- similarly for software systems knowing the performance of different blocks or different algorithms helps identify the overall performance of the software system

-> Asymptotic Notations

- Big oh Notation (O)
- Omega Notation (Ω)
- Theta Notation (Θ)

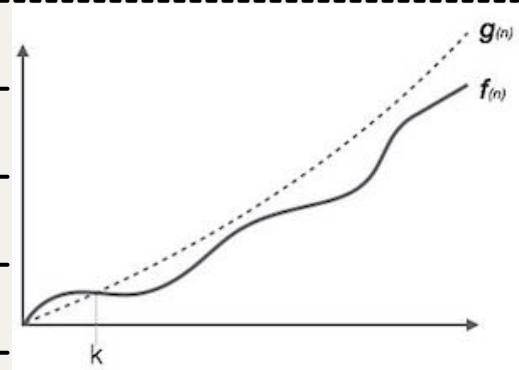
Big oh is mostly used and considered. So let's begin :)

BIG O

-> Dive in Big O notation

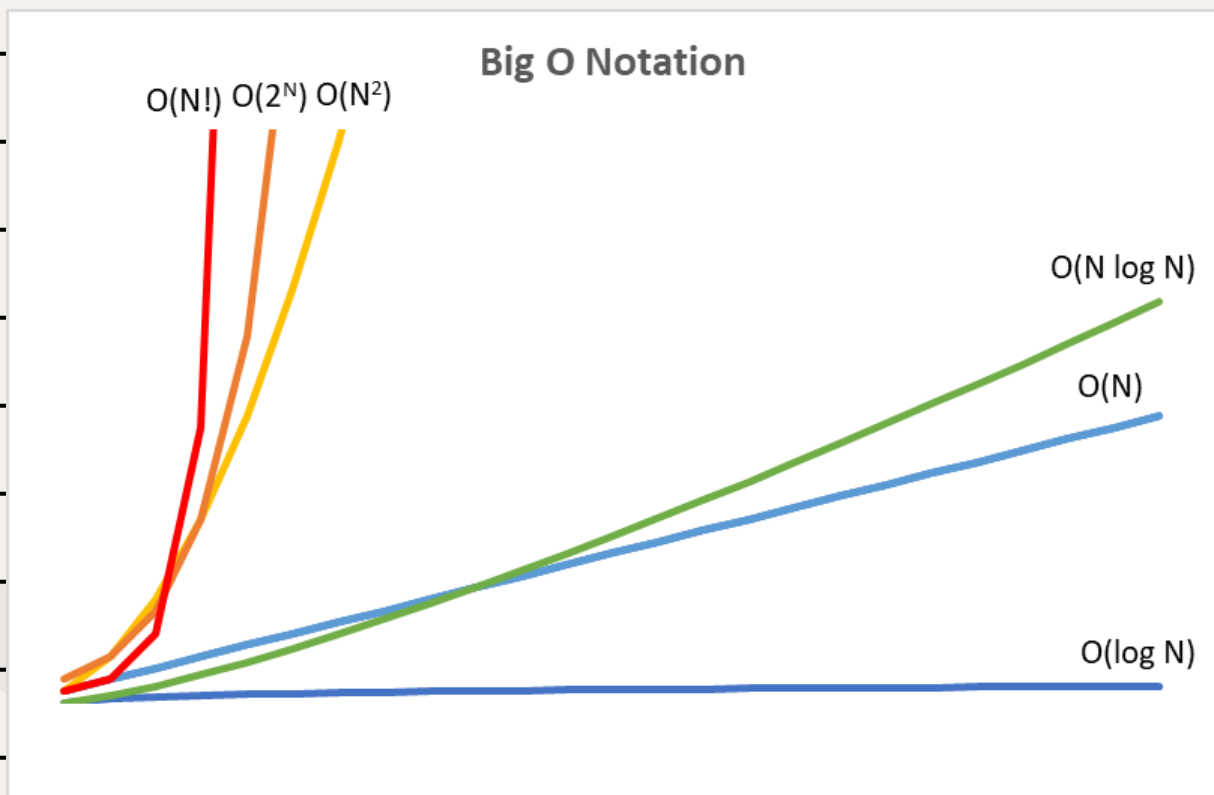
- express the upper boundary of an algorithm running time.

- say $f(n)$ and $g(n)$ are functions for positive integers



- then, $f(n) = O(g(n))$
- $f(n) \leq cg(n)$ for all $n \geq n_0$

$f(n)$ is big oh of $g(n)$



BIG O

-> Finding the Big O complexity

- analyze input
- figure out the different operations in the algorithms
- figure out the operations with the higher complexities. These operations define the Big O complexity of your code of your code

| | | |
|--------------|---------------|-------------------|
| Complexity ↑ | $O(N!)$ | Factorial |
| | $O(2^N)$ | Exponential |
| | $O(N^3)$ | Cubic |
| | $O(N^2)$ | Quadratic |
| | $O(N \log N)$ | $N \times \log N$ |
| | $O(N)$ | Linear |
| | $O(\log N)$ | Logarithmic |
| | $O(1)$ | Constant |

BIG O

-> Algos and their time complexity

- Logarithmic algorithm – $O(\log n)$ – Binary Search.
- Linear algorithm – $O(n)$ – Linear Search.
- Superlinear algorithm – $O(n \log n)$ – Heap Sort, Merge Sort.
- Polynomial algorithm – $O(n^c)$ – Bubble Sort, Selection Sort, Insertion Sort
- Exponential algorithm – $O(c^n)$ – Tower of Hanoi.
- Factorial algorithm – $O(n!)$ – Traveling Salesman, and other backtracking problems.

-> Space complexity

- identifying memory footprint or space complexity is as important as time complexity
- analyze the input and identify how much space it occupies

BIG O

- look at pieces of the program responsible for memory usage. For example, recursive implementation as it reserves memory for recursion stack

-> Quick references

| Data Structure | Time Complexity | | | | | | | | Space Complexity |
|---------------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|---------------------|
| | Average | | | | Worst | | | | Worst |
| | Access | Search | Insertion | Deletion | Access | Search | Insertion | Deletion | |
| <u>Array</u> | $\theta(1)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ |
| <u>Stack</u> | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ |
| <u>Queue</u> | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ |
| <u>Singly-Linked List</u> | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ |
| <u>Doubly-Linked List</u> | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ | $\theta(n)$ | $\theta(1)$ | $\theta(1)$ | $\theta(n)$ |
| <u>Skip List</u> | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n \log(n))$ |
| <u>Hash Table</u> | N/A | $\theta(1)$ | $\theta(1)$ | $\theta(1)$ | N/A | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ |
| <u>Binary Search Tree</u> | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ |
| <u>Cartesian Tree</u> | N/A | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | N/A | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ |
| <u>B-Tree</u> | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(n)$ |
| <u>Red-Black Tree</u> | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(n)$ |
| <u>Splay Tree</u> | N/A | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | N/A | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(n)$ |
| <u>AVL Tree</u> | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(n)$ |
| <u>KD Tree</u> | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(\log(n))$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ | $\theta(n)$ |

credits: <https://www.bigocheatsheet.com/>

BIG O

-> Quick references

Array Sorting Algorithms

| Algorithm | Time Complexity | | | Space Complexity |
|-----------------------|---------------------|------------------------|-------------------|------------------|
| | Best | Average | Worst | Worst |
| <u>Quicksort</u> | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $O(n^2)$ | $O(\log(n))$ |
| <u>Mergesort</u> | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $O(n \log(n))$ | $O(n)$ |
| <u>Timsort</u> | $\Omega(n)$ | $\Theta(n \log(n))$ | $O(n \log(n))$ | $O(n)$ |
| <u>Heapsort</u> | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $O(n \log(n))$ | $O(1)$ |
| <u>Bubble Sort</u> | $\Omega(n)$ | $\Theta(n^2)$ | $O(n^2)$ | $O(1)$ |
| <u>Insertion Sort</u> | $\Omega(n)$ | $\Theta(n^2)$ | $O(n^2)$ | $O(1)$ |
| <u>Selection Sort</u> | $\Omega(n^2)$ | $\Theta(n^2)$ | $O(n^2)$ | $O(1)$ |
| <u>Tree Sort</u> | $\Omega(n \log(n))$ | $\Theta(n \log(n))$ | $O(n^2)$ | $O(n)$ |
| <u>Shell Sort</u> | $\Omega(n \log(n))$ | $\Theta(n(\log(n))^2)$ | $O(n(\log(n))^2)$ | $O(1)$ |
| <u>Bucket Sort</u> | $\Omega(n+k)$ | $\Theta(n+k)$ | $O(n^2)$ | $O(n)$ |
| <u>Radix Sort</u> | $\Omega(nk)$ | $\Theta(nk)$ | $O(nk)$ | $O(n+k)$ |
| <u>Counting Sort</u> | $\Omega(n+k)$ | $\Theta(n+k)$ | $O(n+k)$ | $O(k)$ |
| <u>Cubesort</u> | $\Omega(n)$ | $\Theta(n \log(n))$ | $O(n \log(n))$ | $O(n)$ |

credits: <https://www.bigocheatsheet.com/>

hope you found
it useful

do like, share, comment
and save!

follow Ankit Pangasa for
more such useful content!



BIG O

- look at pieces of the program responsible for memory usage. For example, recursive implementation as it reserves memory for recursion stack

-> Quick references

| Data Structure | Time Complexity | | | | | | | | Space Complexity |
|---------------------------|-----------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|------------------|
| | Average | | | | Worst | | | | Worst |
| | Access | Search | Insertion | Deletion | Access | Search | Insertion | Deletion | |
| <u>Array</u> | $O(1)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| <u>Stack</u> | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| <u>Queue</u> | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| <u>Singly-Linked List</u> | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| <u>Doubly-Linked List</u> | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ | $O(n)$ | $O(1)$ | $O(1)$ | $O(n)$ |
| <u>Skip List</u> | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n \log(n))$ |
| <u>Hash Table</u> | N/A | $O(1)$ | $O(1)$ | $O(1)$ | N/A | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| <u>Binary Search Tree</u> | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| <u>Cartesian Tree</u> | N/A | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | N/A | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |
| <u>B-Tree</u> | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| <u>Red-Black Tree</u> | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| <u>Splay Tree</u> | N/A | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | N/A | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| <u>AVL Tree</u> | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ |
| <u>KD Tree</u> | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(\log(n))$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ | $O(n)$ |

credits: <https://www.bigocheatsheet.com/>