

**AM5510 : BIOMEDICAL SIGNALS & SYSTEMS**  
**Programming Assignment #2 : ACTION POTENTIAL SIMULATION**

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**MATLAB CODE**

```
% Initializing Constants
Erest = -68; % mV
EK = -74.7; % mV
ENa = 54.2; % mV

C = 1; % 10^-6F/cm2

GK = 12; % m/cm2
GNa = 30; % m/cm2

Vm0 = Erest;
dt = 0.01; % ms
tmax = 10; % ms

t = 0:dt:tmax;
n = zeros(size(t));
m = zeros(size(t));
h = zeros(size(t));
Vm = zeros(size(t));
gK = zeros(size(t));
gNa = zeros(size(t));

% Initializing Io_values and tPW_values
Io_values = [5, 25, 75]; % uA
tPW_values = [0.2, 0.8]; % ms

% Simulation loop
for Io = Io_values
    for tPW = tPW_values

        % Initializing values at t=0
        Vm(1) = Vm0;
        n(1) = 0.3;
        m(1) = 0.065;
        h(1) = 0.6;

        % Stimulus current
        Is = zeros(size(t));
        Is(t > 0 & t < tPW) = Io;

        % Simulation
        for i = 2:length(t)
            % Step 1: Calculating rate constants
            v = Vm(i - 1) - Erest;
            alpha_n = (0.01 * (10 - v)) / (exp((10 - v) / 10) - 1);
            beta_n = 0.125 * exp(-v / 80);
            alpha_m = (0.1 * (25 - v)) / (exp((25 - v) / 10) - 1);
            beta_m = 4 * exp(-v / 18);
            alpha_h = 0.07 * exp(-v / 20);
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beta_h = 1 / (exp((30 - v) / 10) + 1);

% Step 2: Calculate changes in n, m, and h
delta_n = dt * (alpha_n * (1 - n(i - 1)) - beta_n * n(i - 1));
delta_m = dt * (alpha_m * (1 - m(i - 1)) - beta_m * m(i - 1));
delta_h = dt * (alpha_h * (1 - h(i - 1)) - beta_h * h(i - 1));

% Update n, m, and h
n(i) = n(i - 1) + delta_n;
m(i) = m(i - 1) + delta_m;
h(i) = h(i - 1) + delta_h;

% Step 3: Calculating ionic conductance and currents
gK(i) = GK * n(i)^4;
gNa(i) = GNa * m(i)^3 * h(i);

% Step 4: Calculating total current
IK = gK(i) * (Vm(i - 1) - EK);
INa = gNa(i) * (Vm(i - 1) - ENa);
IC = Is(i) - (IK + INa);

% Step 5: Calculating membrane voltage
delta_VM = (IC / C) * dt;
Vm(i) = Vm(i - 1) + delta_VM;

end

% Plotting results
figure;
subplot(3, 1, 1);
plot(t, Vm);
title(['Membrane Voltage (Io = ', num2str(Io), ', tPW = ', num2str(tPW), ' ms)']);
xlabel('Time (ms)');
ylabel('Vm (mV)');

subplot(3, 1, 2);
plot(t, gK);
title('Potassium Conductance (gK)');
xlabel('Time (ms)');
ylabel('gK (mS/cm^2)');

subplot(3, 1, 3);
plot(t, gNa);
title('Sodium Conductance (gNa)');
xlabel('Time (ms)');
ylabel('gNa (mS/cm^2)');
end
end

```

OUTPUT WHEN  $dt = 0.01ms$

**Step 1 - Rate Constants ( $t = 0.01$  ms):**

$\alpha_n = 0.038838$

$\beta_n = 0.13584$

$\alpha_m = 0.13945$

$\beta_m = 5.7893$

$\alpha_h = 0.097636$

$\beta_h = 0.024953$

**Step 2 - Changes in  $n$ ,  $m$ , and  $h$  at  $t = 10$  ms**

$\Delta n = -0.0002912$

$\Delta m = 3.2441e-07$

$\Delta h = 0.00039634$

**Step 3 - Ionic Conductance at  $t = 10$  ms**

$g_K = 0.27408$

$g_{Na} = 0.00018472$

**Step 4 - total current at  $t = 10$  ms**

$I_K = 0.012334$

$I_{Na} = -0.023802$

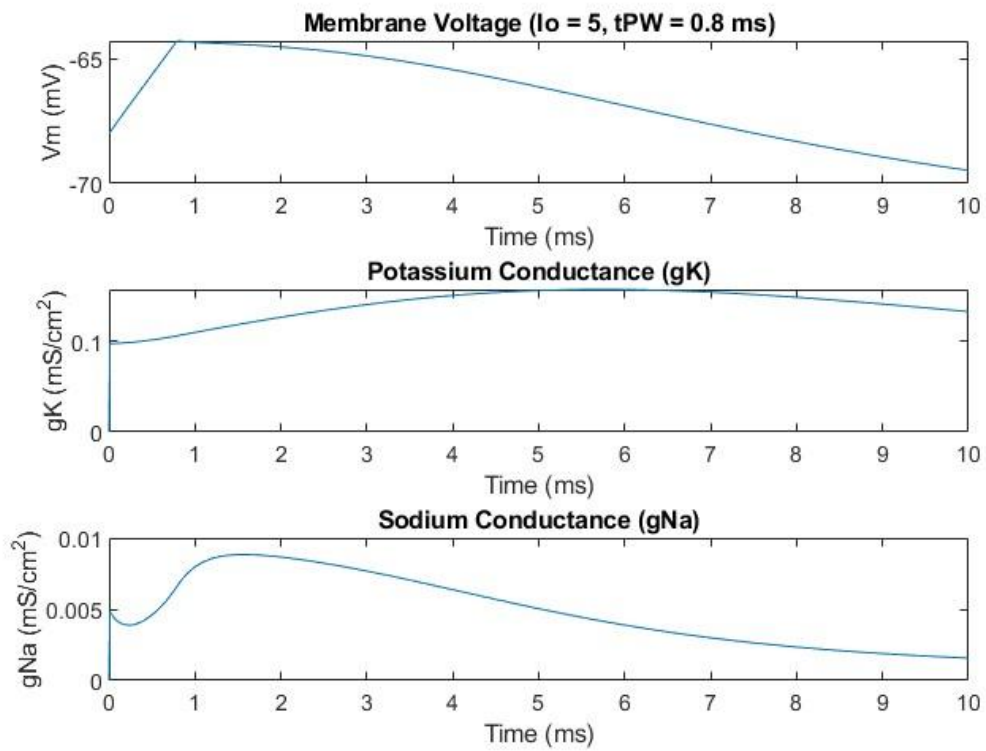
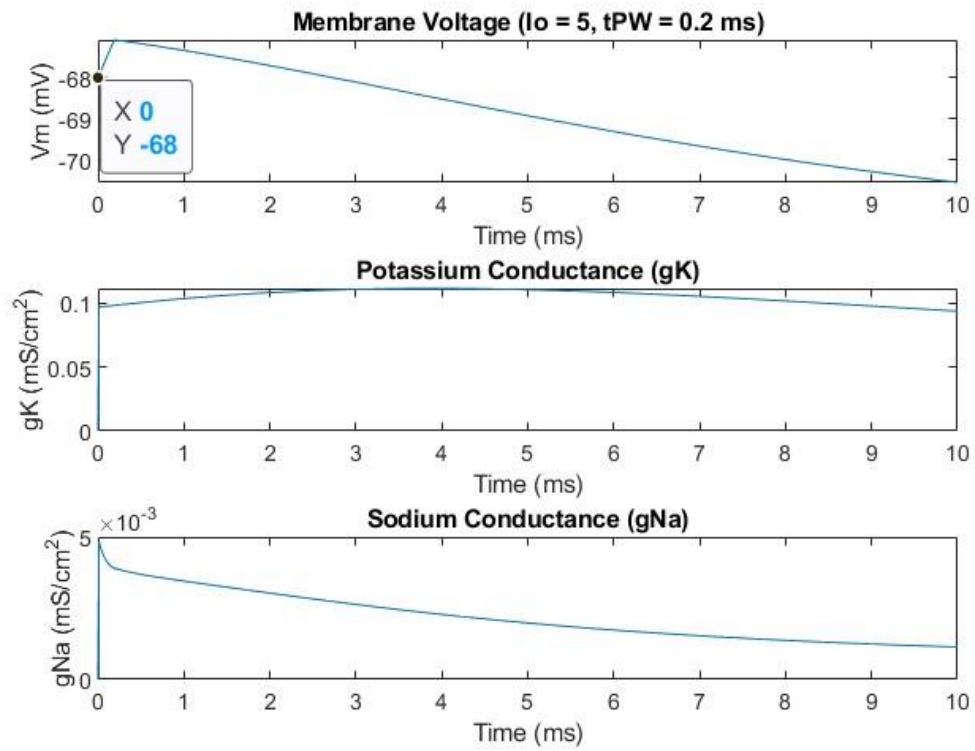
$I_C = 0.011469$

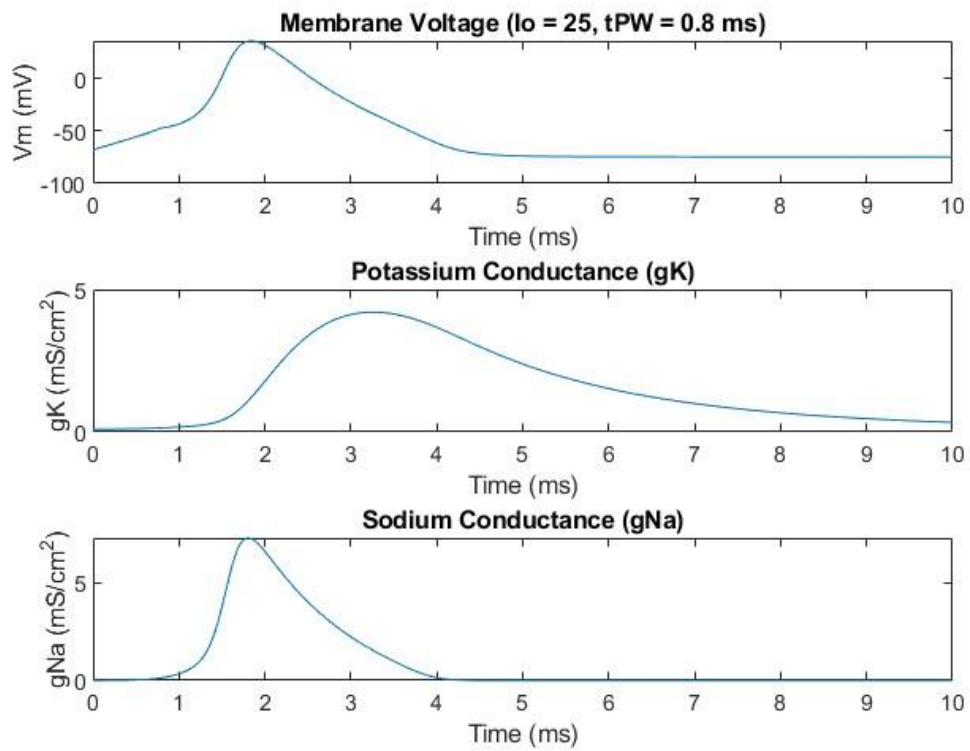
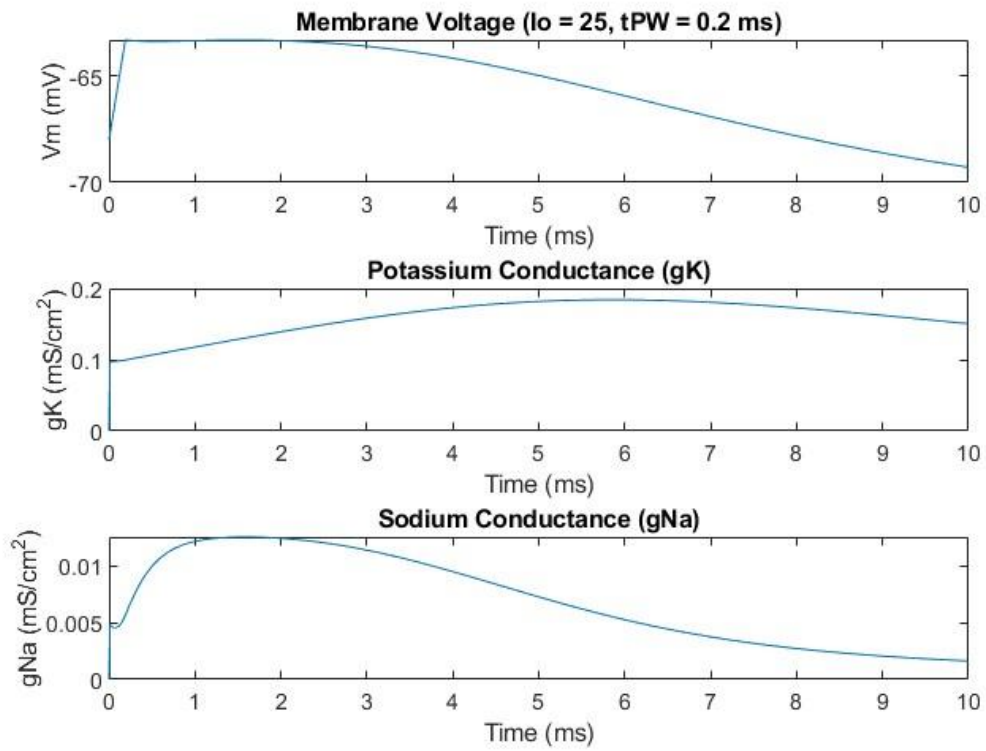
**Step 5 - membrane voltage at  $t = 10$  ms**

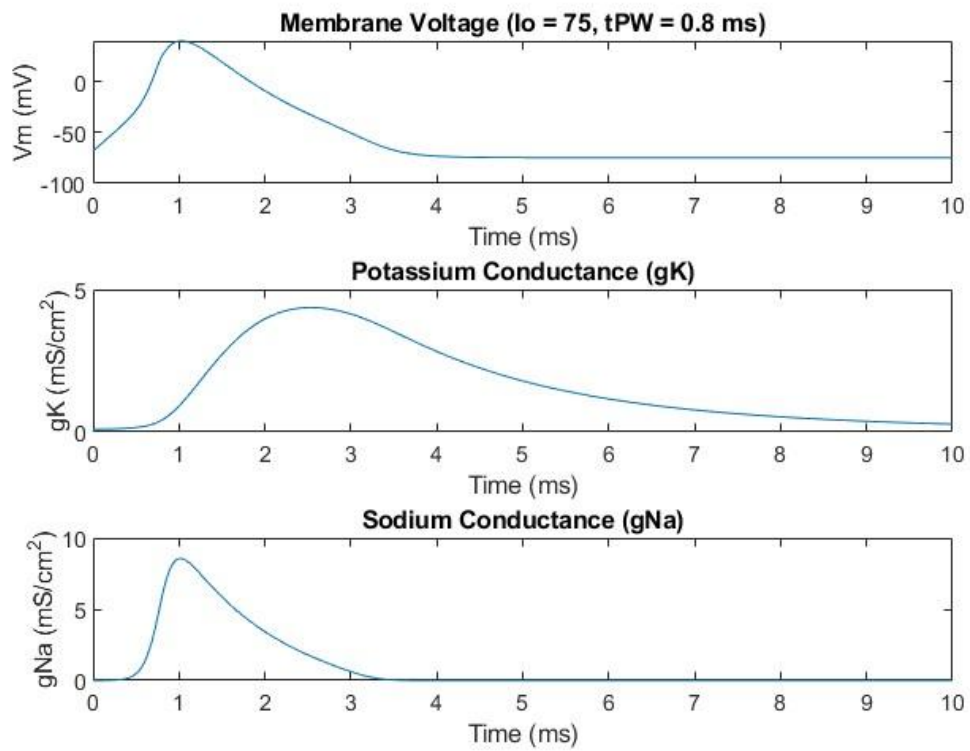
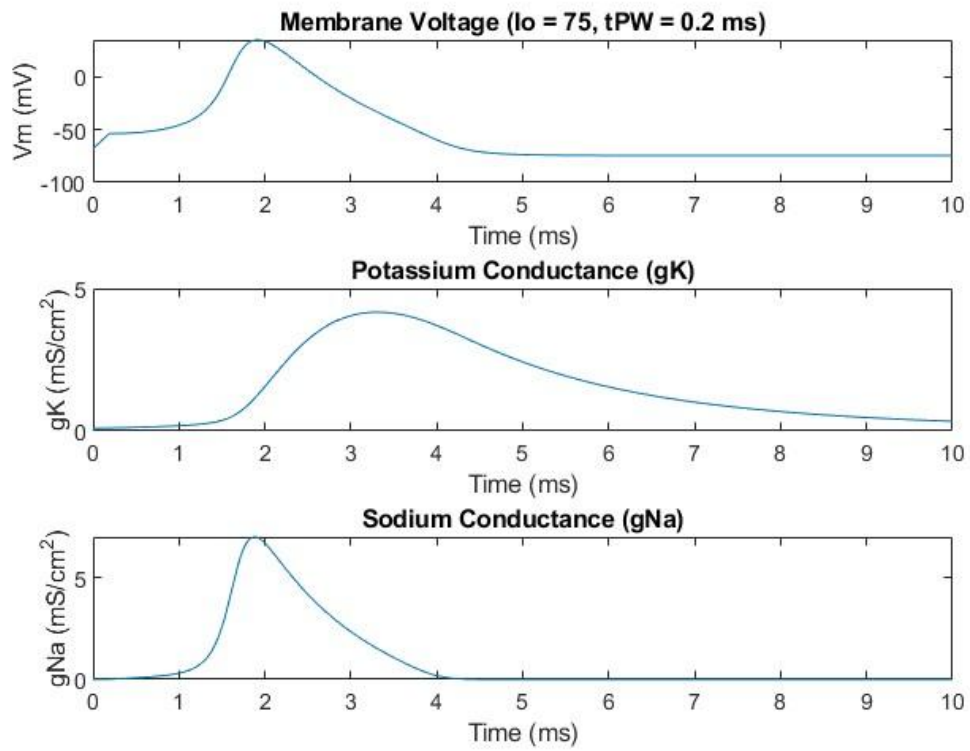
$\Delta V_M = 0.00011469$

$V_M(i) = -74.6549$

$I_o$  is in  $\mu A$  and  $t_{PW}$  is in ms.







OUTPUT WHEN  $dt = 0.1\text{ms}$

**Step 1 - Rate Constants ( $t = 0.1\text{ ms}$ ):**

$\text{Alpha}_n = 0.03884$

$\text{Beta}_n = 0.13584$

$\text{Alpha}_m = 0.13946$

$\text{Beta}_m = 5.789$

$\text{Alpha}_h = 0.097631$

$\text{beta}_h = 0.024955$

**Step 2 - Changes in  $n$ ,  $m$ , and  $h$  at  $t = 10\text{ ms}$**

$\Delta n = -0.0028264$

$\Delta m = 3.6314\text{e-}06$

$\Delta h = 0.0038707$

**Step 3 - Ionic Conductance at  $t = 10\text{ ms}$**

$g_K = 0.25372$

$g_{Na} = 0.00018915$

**Step 4 - total current at  $t = 10\text{ ms}$**

$I_K = 0.011663$

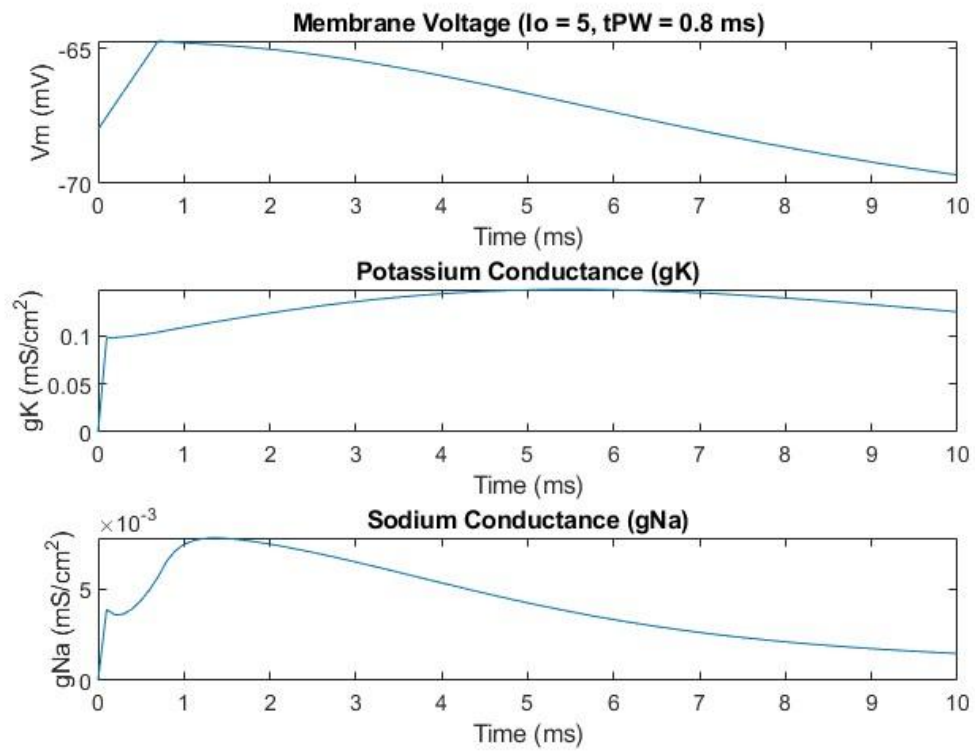
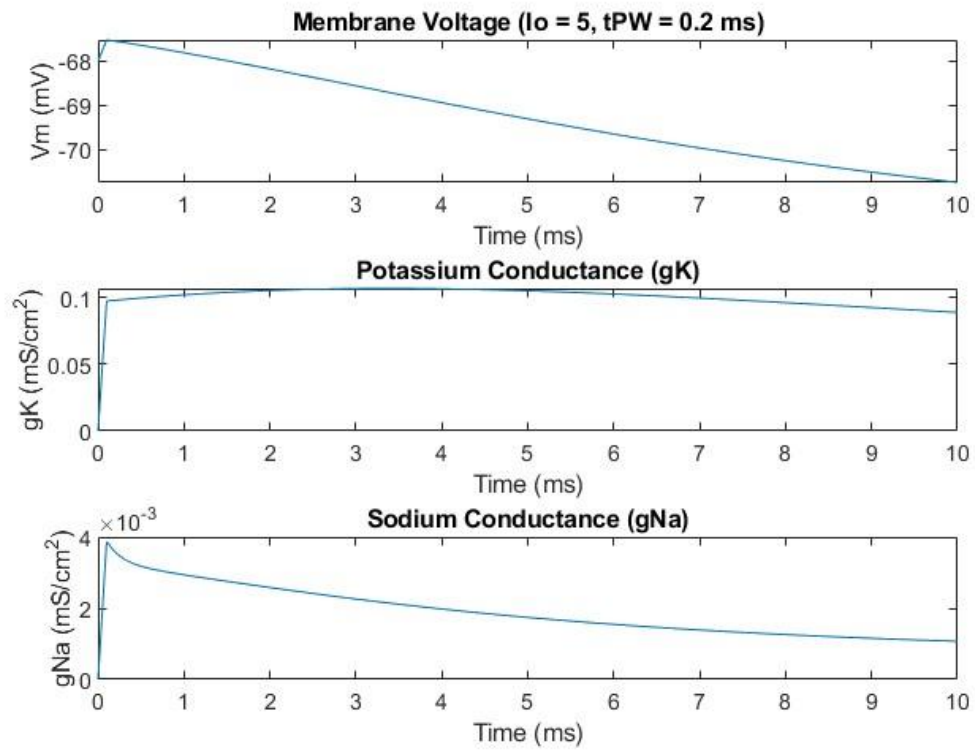
$I_{Na} = -0.024372$

$I_C = 0.012709$

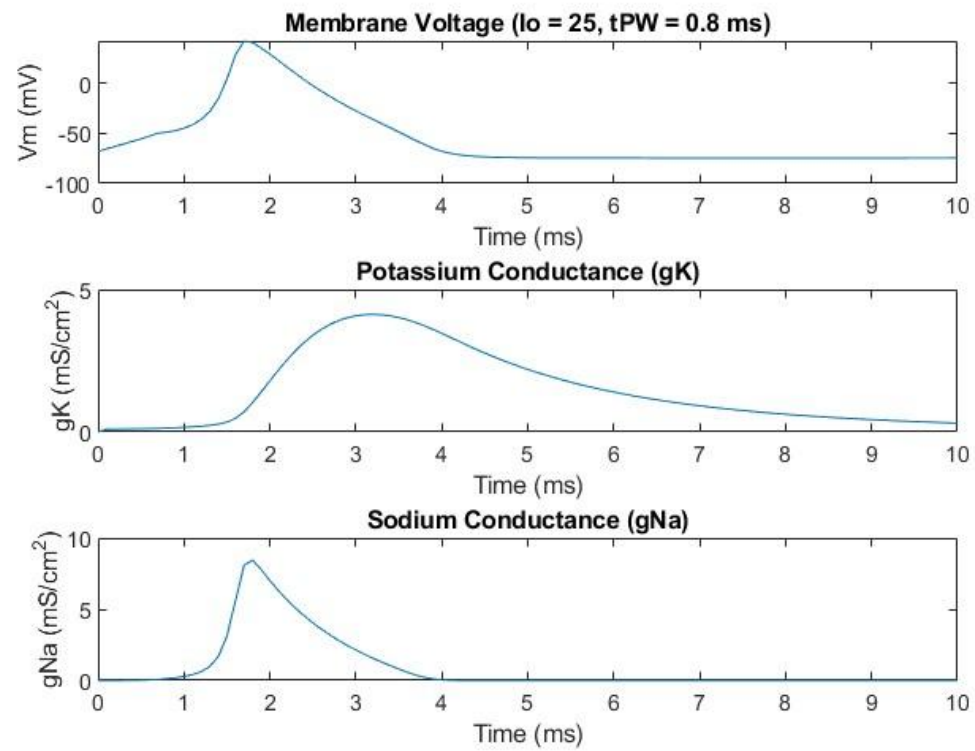
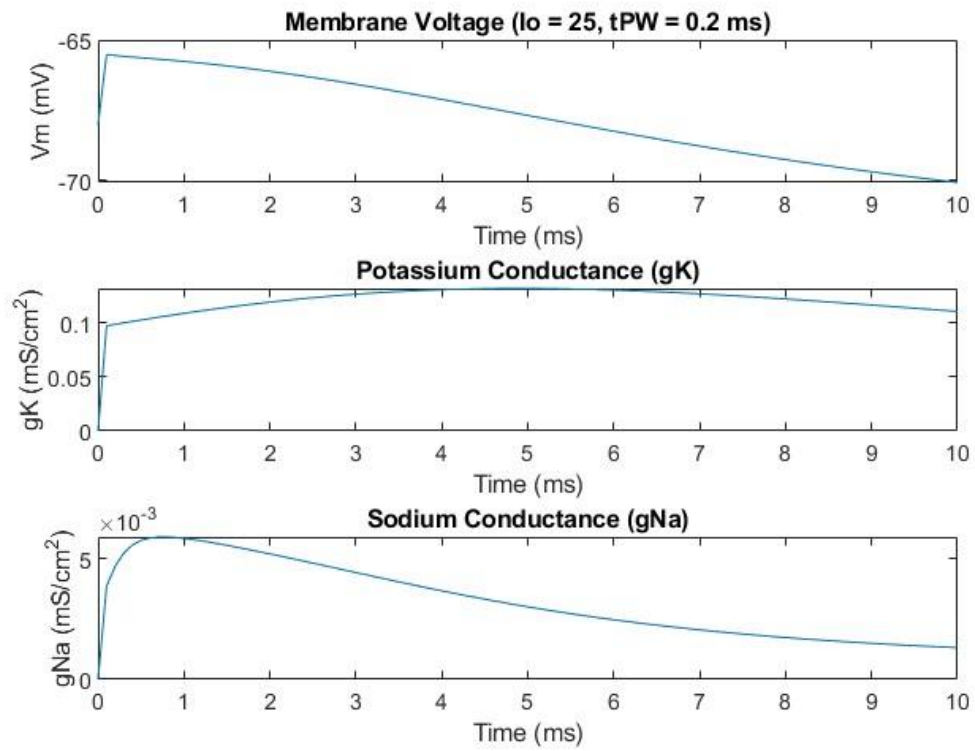
**Step 5 - membrane voltage at  $t = 10\text{ ms}$**

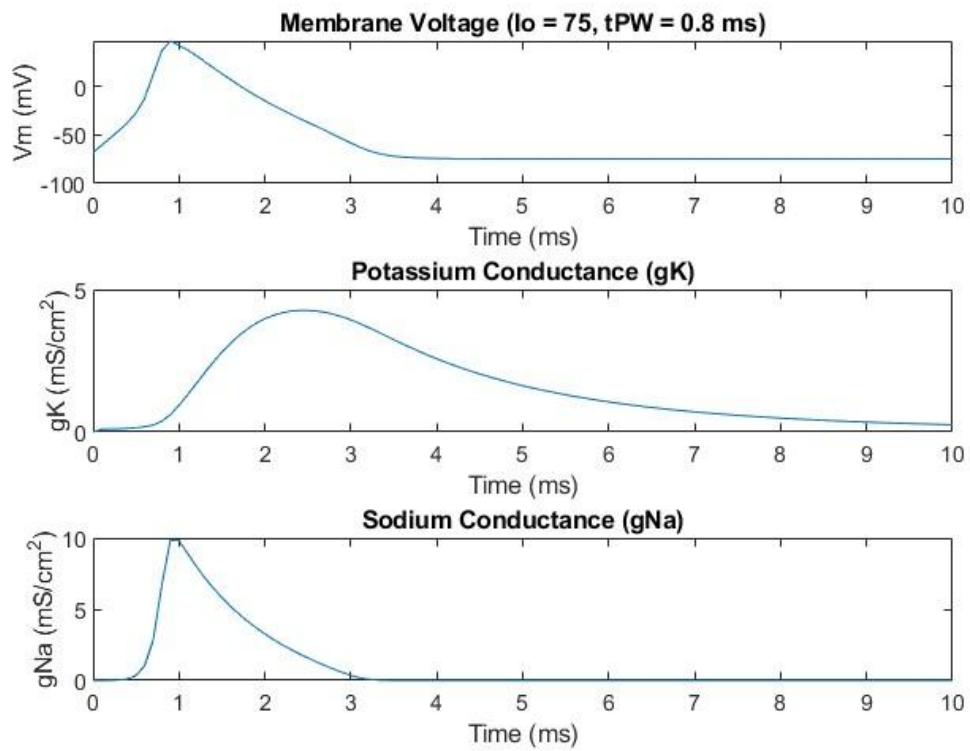
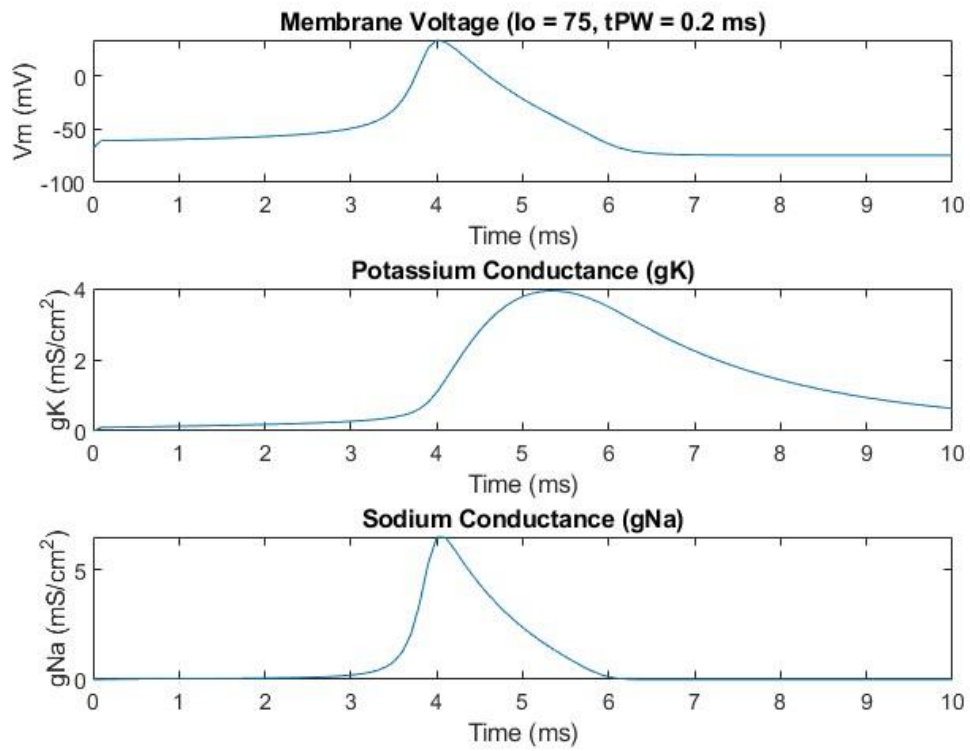
$\Delta V_M = 0.0012709$

$V_M(i) = -74.6528$









## **OBSERVATION**

- The selection of the time step ( $\Delta t$ ) in the simulation plays a crucial role in balancing simulation accuracy and computational efficiency.
- A smaller time step enhances accuracy but demands greater computational resources, whereas a larger time step sacrifices some accuracy to expedite simulations.
- The decision regarding  $\Delta t$  should align with the simulation's particular objectives and the computational capabilities at hand