Table 1: SSL Comparison: MNIST: Average (standard deviation) classification accuracy over 100 trials.

# Labels per class	1	2	3	4	5
High order Laplace LearningN $= 10$ m $= 0.1$	35.7 (5.6)	38.9 (4.5)	41.3 (3.7)	42.7 (2.9)	43
High order laplace learningN $=20$ m $=0.1$	41.7(5.5)	47.8(5.3)	51.0 (3.8)	53.2(3.1)	54
High order laplace learning $N=30$ m $=0.1$	39.8(5.1)	46.5(5.0)	50.0(3.8)	52.6(3.0)	53
High order Laplace LearningN $=40$ m $=0.1$	37.8(4.7)	44.9(4.6)	48.6(3.6)	51.5(3.1)	52
High order laplace learning $N=50$ m $=0.1$	36.8(4.7)	44.1 (4.5)	48.0(3.6)	51.0(3.2)	52
High order laplace learningN $= 10$ m $= 0.2$	35.7(5.6)	38.8 (4.5)	41.2(3.7)	42.5(2.9)	43
High order laplace learningN $=20$ m $=0.2$	41.8 (5.5)	47.8(5.3)	51.0(3.8)	53.1 (3.1)	54
High order Laplace LearningN $=30$ m $=0.2$	40.1 (5.1)	46.8 (5.0)	50.2(3.8)	52.8(3.0)	54
High order Laplace LearningN $=40$ m $=0.2$	38.2 (4.8)	45.3(4.7)	49.0(3.6)	51.8(3.0)	53
High order Laplace learningN $= 50$ m $= 0.2$	37.3(4.8)	44.6 (4.5)	48.5 (3.6)	51.5 (3.2)	53
High order Laplace LearningN $= 10$ m $= 0.3000000000$	, ,	38.7 (4.5)	41.1 (3.7)	42.4 (2.9)	42
High order Laplace LearningN $= 20$ m $= 0.3000000000$	` ,	47.7(5.3)	51.0 (3.9)	53.1 (3.1)	54
High order Laplace LearningN $= 30$ M $= 0.3000000000$		47.0 (5.0)	50.4(3.8)	52.9(3.0)	54
High order Laplace learning $N=40$ m $=0.3000000000$	* *	45.7(4.7)	49.4 (3.6)	52.1 (3.0)	53
High order Laplace LearningN $= 50$ M $= 0.3000000000$	1 1	45.1 (4.6)	49.0 (3.5)	51.9 (3.2)	53
High order Laplace LearningN = $10$ M = $0.4$	35.5 (5.5)	38.5 (4.5)	40.9 (3.7)	42.2 (2.9)	42
High order Laplace learning $N=20$ $M=0.4$	41.8 (5.5)	47.6 (5.3)	50.9 (3.9)	52.9 (3.1)	54
High order Laplace learning $N=30$ M = $0.4$	40.6 (5.2)	47.1 (5.0)	50.5 (3.8)	53.0 (3.0)	54
High order Laplace learning $N = 40 \text{m} = 0.4$	39.0 (4.9)	46.0 (4.7)	49.6 (3.6)	52.3 (3.0)	53
HIGH ORDER LAPLACE LEARNINGN = 50M = 0.4	38.3 (5.0)	45.5 (4.6)	49.4 (3.5)	52.2 (3.1)	53
HIGH ORDER LAPLACE LEARNINGN = 10M = 0.5	35.4 (5.5)	38.3 (4.6)	40.7 (3.7)	42.0 (2.9)	42
High order Laplace learning $N=20$ M = $0.5$	41.7 (5.5)	47.5 (5.4)	50.8 (3.9)	52.8 (3.1)	54
High order Laplace LearningN = 30M = 0.5	40.8 (5.2)	47.2 (5.1)	50.6 (3.8)	53.0 (3.0)	54
HIGH ORDER LAPLACE LEARNINGN = 40M = 0.5	39.3 (5.0)	46.2 (4.7)	49.8 (3.6)	52.4 (3.0)	53
High order Laplace learning $N = 50 M = 0.5$ High order Laplace learning $N = 10 M = 0.6$	38.7 (5.1)	45.8 (4.7)	49.6 (3.5)	52.4 (3.1)	53 42
High order Laplace learning $N = 10M = 0.0$ High order Laplace learning $N = 20M = 0.6$	35.3 (5.6) 41.7 (5.6)	38.1 (4.6) 47.3 (5.5)	40.5 (3.7) $50.6 (3.9)$	41.7 (2.9) $52.6 (3.1)$	53
High order Laplace learning $N=20M=0.0$ High order Laplace learning $N=30M=0.6$	40.9 (5.3)	47.3 (5.3) $47.2 (5.1)$	50.5 (3.8)	52.0 (3.1) $52.9 (3.0)$	54
High order Laplace learning $N=30M=0.0$ High order Laplace Learning $N=40M=0.6$	39.6 (5.1)	46.4 (4.8)	49.9 (3.7)	52.5 (3.0) $52.5 (3.0)$	53
High order Laplace learning $N = 40M = 0.6$	39.1 (5.1)	46.0 (4.7)	49.8 (3.7)	52.6 (3.0) $52.6 (3.0)$	53
High order Laplace learning $N = 0.00$ High order Laplace learning $N = 10$ M = $0.7000000000$	( )	37.9 (4.6)	40.3 (3.7)	41.5 (3.0)	41
High order Laplace learning $N=20 M=0.700000000000000000000000000000000000$		47.0 (5.5)	50.4 (4.0)	52.3 (3.1)	53
High order Laplace learning $N=30 \text{M}=0.700000000000000000000000000000000000$		47.1 (5.2)	50.5 (3.8)	52.8 (3.0)	54
High order Laplace learning $N=40 M=0.700000000000000000000000000000000000$	* *	46.4 (4.8)	49.9 (3.7)	52.5 (3.0)	53
High order Laplace learning $N=50 M=0.700000000000000000000000000000000000$	. ,	46.2 (4.8)	49.9 (3.5)	52.6 (3.0)	53
High order Laplace LearningN $= 10$ m $= 0.8$	35.0 (5.5)	37.7(4.5)	40.1 (3.8)	41.2 (3.0)	41
High order Laplace LearningN $= 20$ m $= 0.8$	41.4 (5.7)	46.8(5.5)	50.1 (3.9)	52.0 (3.1)	53
High order Laplace LearningN $=30$ m $=0.8$	41.0 (5.3)		$50.3\ (3.8)$	$52.6\ (3.0)$	53
High order Laplace LearningN $=40$ m $=0.8$	40.0 (5.2)	46.4 (4.9)	49.8 (3.7)	52.4(2.9)	53
High order Laplace LearningN $= 50$ m $= 0.8$	39.7(5.2)	46.3(4.8)	$50.0\ (3.5)$	$52.6\ (3.0)$	53
High order Laplace LearningN $= 10$ m $= 0.9$	34.9(5.5)	37.4(4.5)	39.9(3.8)	40.9 (3.1)	41
High order Laplace LearningN $=20$ m $=0.9$	41.3 (5.7)	46.5(5.6)	49.8 (3.9)	51.6 (3.1)	53
High order Laplace LearningN $=30$ m $=0.9$	41.1 (5.4)	46.9(5.3)	50.1(3.8)	52.4(3.0)	53
High order Laplace LearningN $=40$ m $=0.9$	40.1 (5.3)	46.3(4.9)	49.7(3.7)	52.2(3.0)	53
High order Laplace learningN $=50$ m $=0.9$	39.9(5.3)	46.3(4.9)	49.9(3.6)	52.4 (3.0)	53
High order Laplace learningN $=10$ m $=1.0$	34.7(5.5)	37.1 (4.5)	39.6 (3.8)	40.6(3.1)	40
High order laplace learningN $=20$ m $=1.0$	41.1 (5.8)	$46.1\ (5.6)$	49.4 (3.9)	51.3 (3.2)	52
High order Laplace learningN $=30$ m $=1.0$	41.0(5.4)	46.6 (5.3)	49.8(3.7)	52.1 (3.1)	53
High order Laplace learning $N=40$ m $=1.0$	40.2(5.3)	46.2 (5.0)	49.5 (3.7)	51.9(3.0)	53
High order Laplace learning $N=50$ m $=1.0$	40.0 (5.4)	46.2 (4.9)	49.7 (3.6)	52.2 (3.0)	53
High order Laplace LearningN $= 10$ m $= 1.1$	34.5 (5.5)	36.8 (4.5)	39.3 (3.9)	40.2 (3.1)	40
High order Laplace learning $N=20$ m = 1.1	40.9 (5.8)	45.7 (5.6)	49.0 (3.9)	50.8 (3.2)	52
High order Laplace learning $N=30$ $M=1.1$	41.0 (5.5)	46.3 (5.4)	49.5 (3.7)	51.7 (3.1)	52
High order Laplace learning $N=40$ m = 1.1	40.3 (5.4)	46.0 (5.0)	49.3 (3.7)	51.6 (3.0)	52
High order Laplace learning $N=50$ m = $1.1$	40.1 (5.4)	46.1 (5.0)	49.5 (3.6)	51.9 (3.1)	53
High order Laplace LearningN $= 10$ M $= 1.2000000000$	, ,	36.5 (4.4)	39.0 (3.9)	39.8 (3.2)	40
High order Laplace LearningN = $20$ m = $1.2000000000$		45.3 (5.6)	48.6 (3.9)	50.3 (3.3)	51
High order Laplace learningN = $30$ M = $1.2000000000$		46.0 (5.4)	49.1 (3.7)	51.2 (3.2)	52
High order Laplace LearningN = $40$ M = $1.2000000000$		45.7 (5.1)	49.0 (3.7)	51.2 (3.1)	52
High order laplace learning $N=50$ m $=1.2000000000$	000002   40.2 (5.4)	45.8(5.1)	49.2(3.6)	51.5(3.1)	5