COMP 9517 Computer Vision

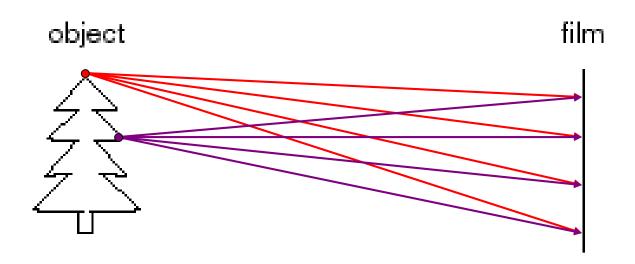
Image Formation

Geometry of Image Formation

Mapping between image and world coordinates

- Pinhole camera model
- Projective geometry
 - Vanishing points and lines
- Projection matrix

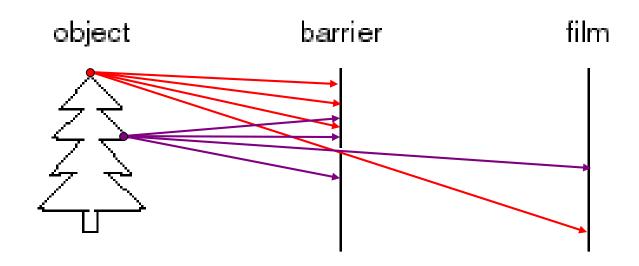
Image formation



Let us design a camera

- Idea 1: put a piece of film in front of an object
- Do we get a reasonable image?

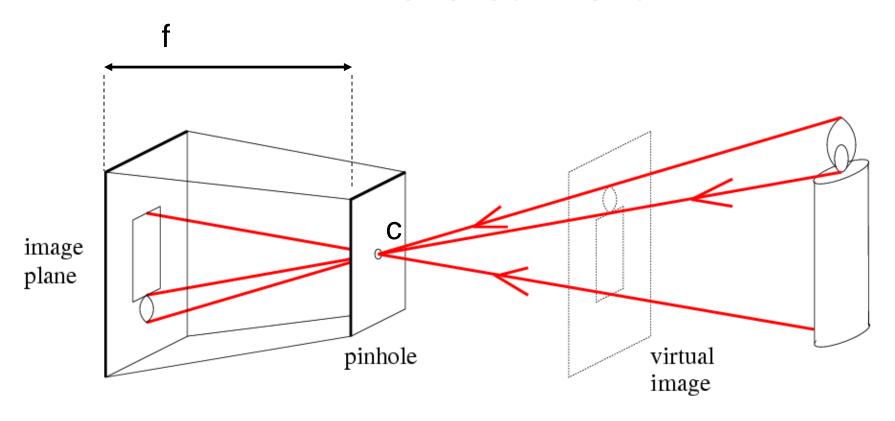
Pinhole camera



Idea 2: add a barrier to block off most of the rays

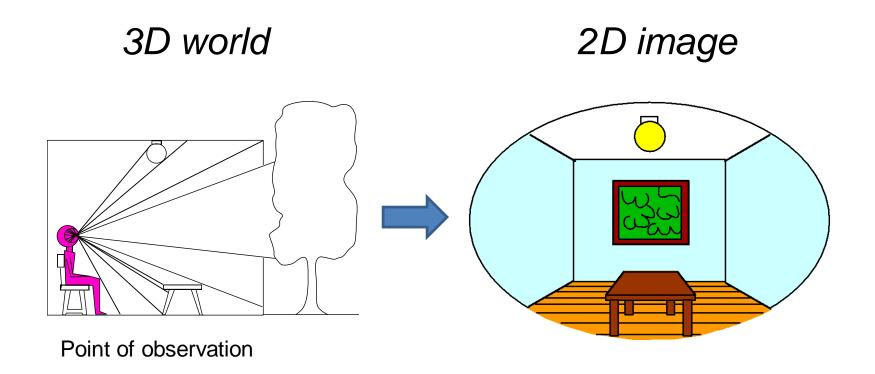
- This reduces blurring
- The opening known as the aperture

Pinhole camera



f = focal length
c = centre of the camera

Dimensionality Reduction Machine (3D to 2D)



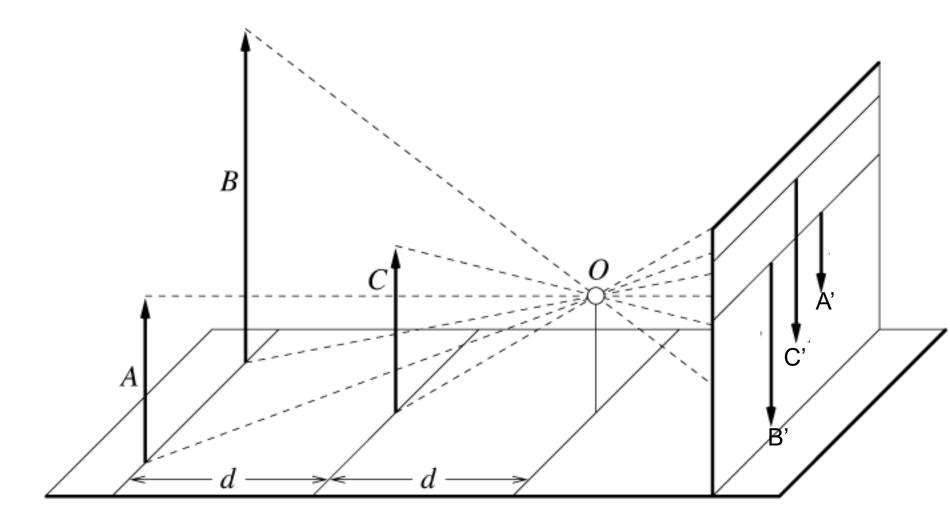
Projection can be tricky...



Projection can be tricky...



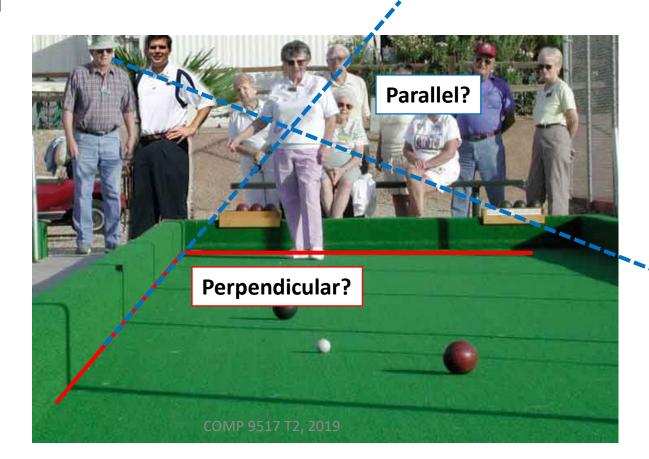
Length and area are not preserved



Projective Geometry

What is lost?

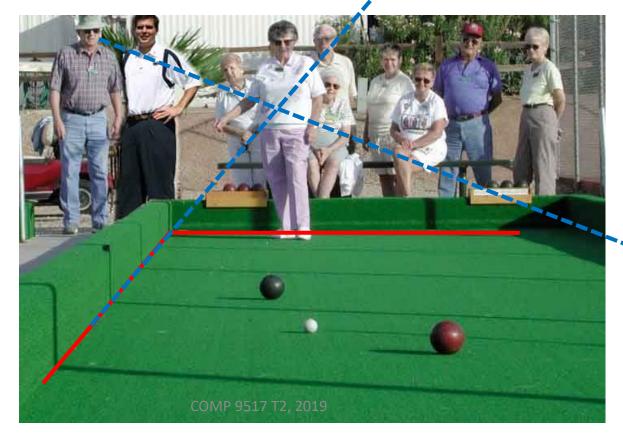
- Length
- Angles



Projective Geometry

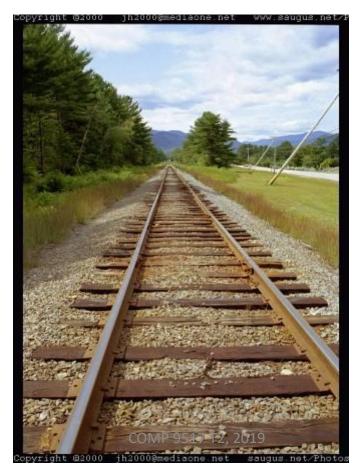
What is preserved?

Straight lines are still straight,

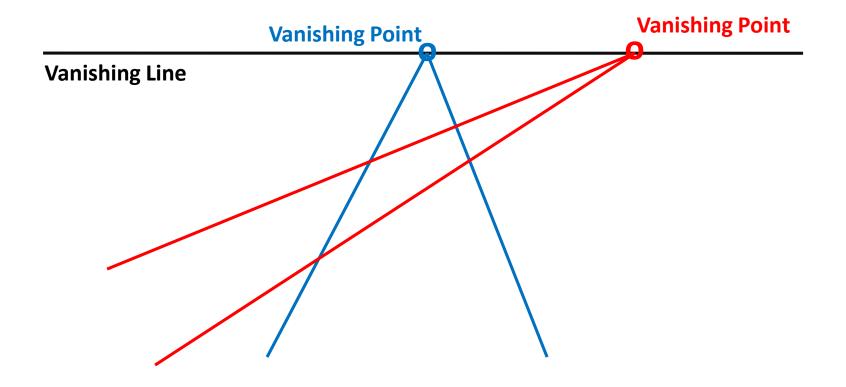


Vanishing points and lines

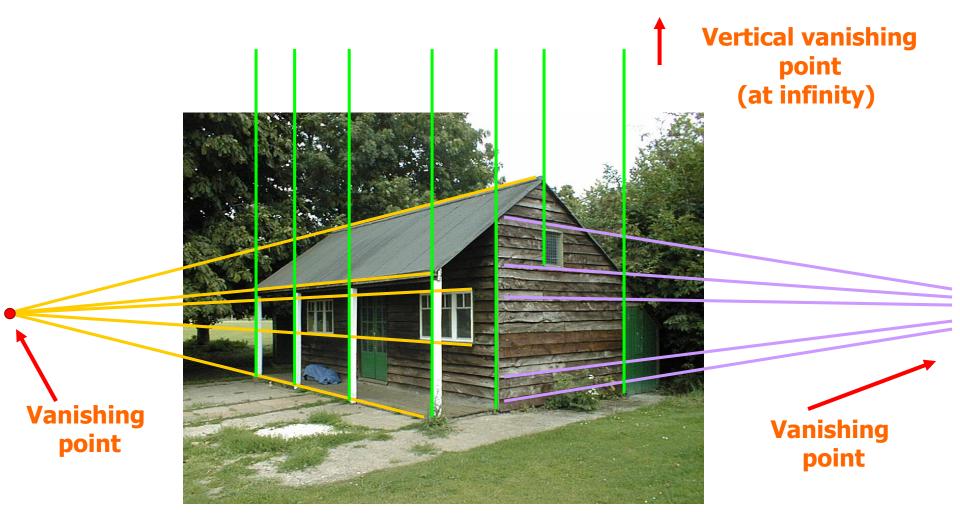
Parallel lines in the world intersect in the image at a "vanishing point"



Vanishing points and lines

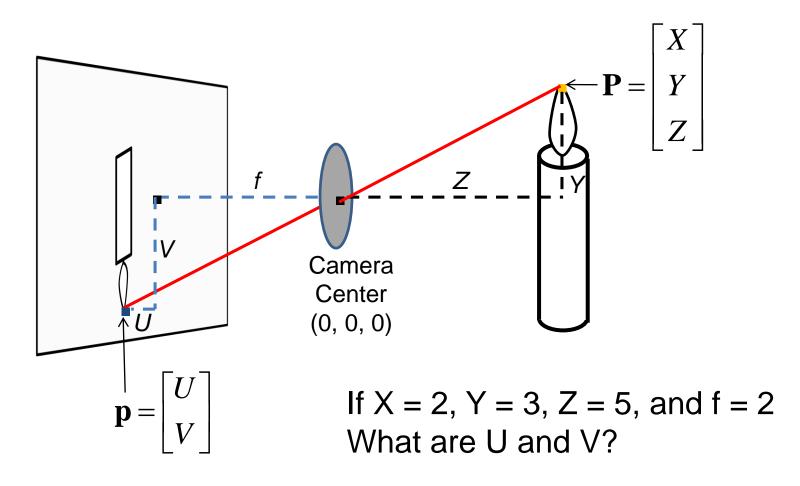


Vanishing points and lines

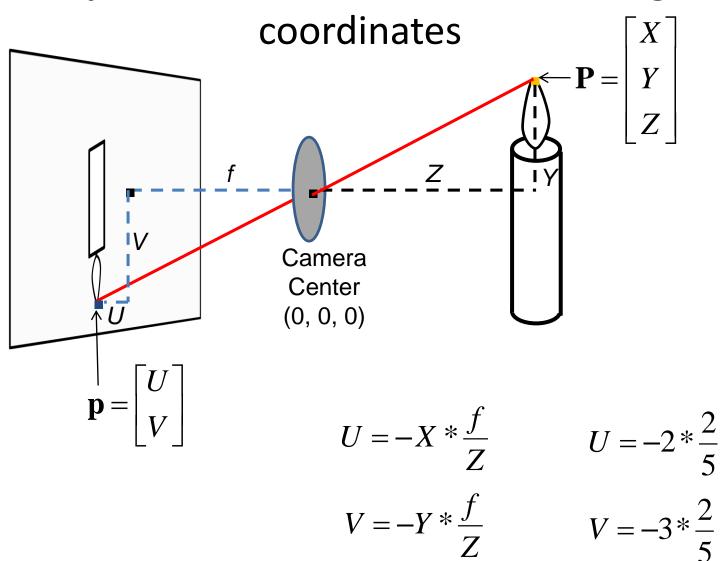


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Projection: world coordinates → image coordinates



Projection: world coordinates → image



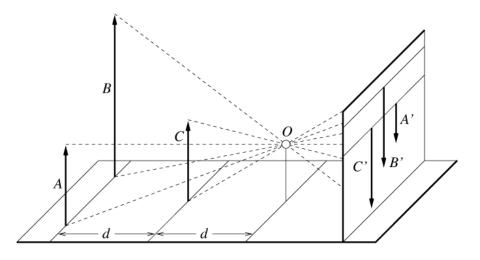
Perspective Projection

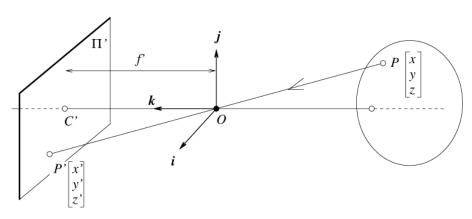
- Apparent size of object depends on its distance: far objects appear smaller
- By similar triangles

$$(x', y', z') \rightarrow (f\frac{x}{z}, f\frac{y}{z}, -f)$$

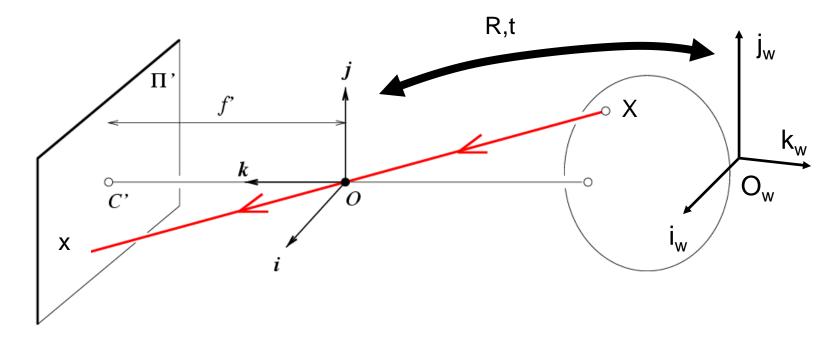
Ignore the third coordinate, and get

$$(x', y') \rightarrow (f\frac{x}{z}, f\frac{y}{z})$$





Projection matrix



$$x = K[R \ t]X$$

x: Image Coordinates: (u,v,1)

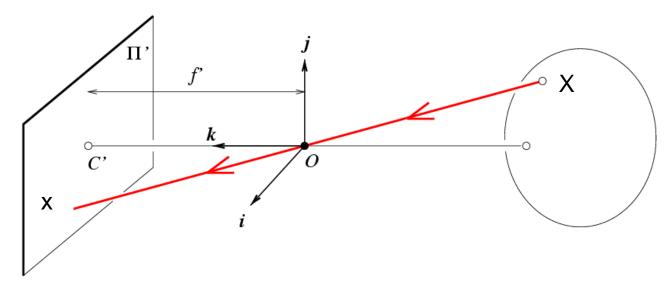
K: Intrinsic Matrix (3x3)

R: Rotation (3x3)

t: Translation (3x1)

X: World Coordinates: (X,Y,Z,1)

Pinhole Camera Model



- Unit aspect ratio
- Optical center at (0,0)
- No skew

Intrinsic Assumptions Extrinsic Assumptions

K

- No rotation
- Camera at (0,0,0)

$$\mathbf{X} = \mathbf{K} \begin{bmatrix} \mathbf{I} & \mathbf{0} \end{bmatrix} \mathbf{X} \implies w \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} \overline{f} & \overline{0} & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

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Homogeneous coordinates

• Line equation: ax + by + c = 0

$$line_i = \begin{vmatrix} a_i \\ b_i \\ c_i \end{vmatrix}$$

• Append 1 to pixel coordinate to get homogeneous coordinate u_i

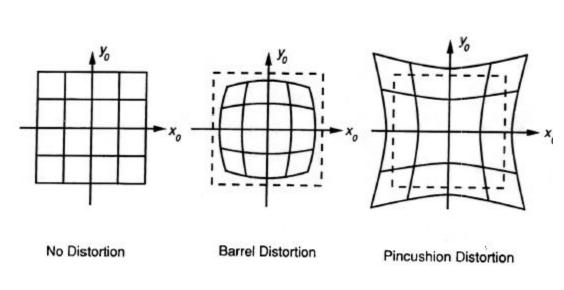
$$p_i = v_i$$

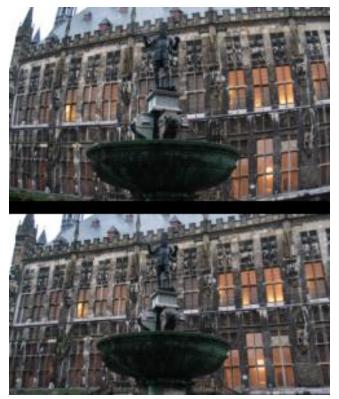
Line given by cross product of two points

$$line_{ij} = p_i \times p_j$$

• Intersection of two lines given by cross product of the lines $q_{ii} = line_i \times line_i$

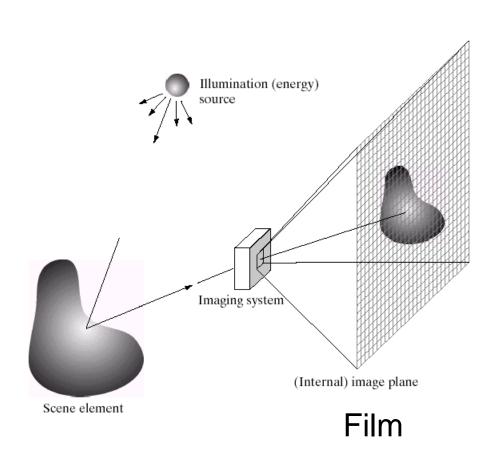
Beyond Pinholes: Radial Distortion

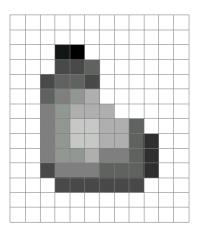




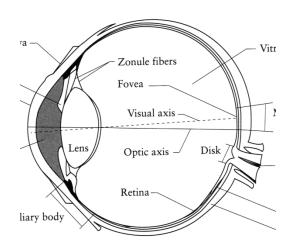
Corrected Barrel Distortion

Image Formation





Digital Camera

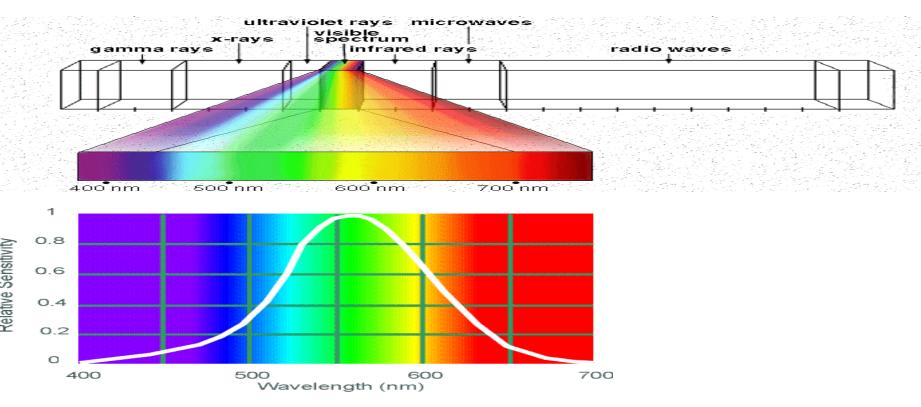


The Eye

Why do we care about human vision?

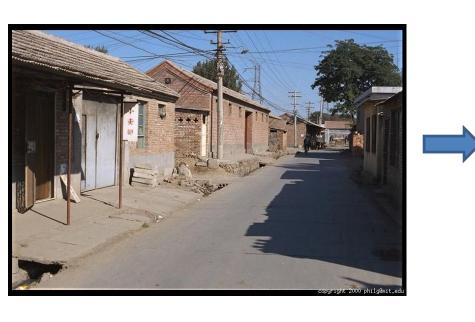
- Cameras necessarily imitate the frequency response of the human eye, so we should know that much.
- Computer vision probably would not get as much attention if biological vision (especially human vision) had not proved that it was possible to make important judgements from 2D images.

Electromagnetic Spectrum



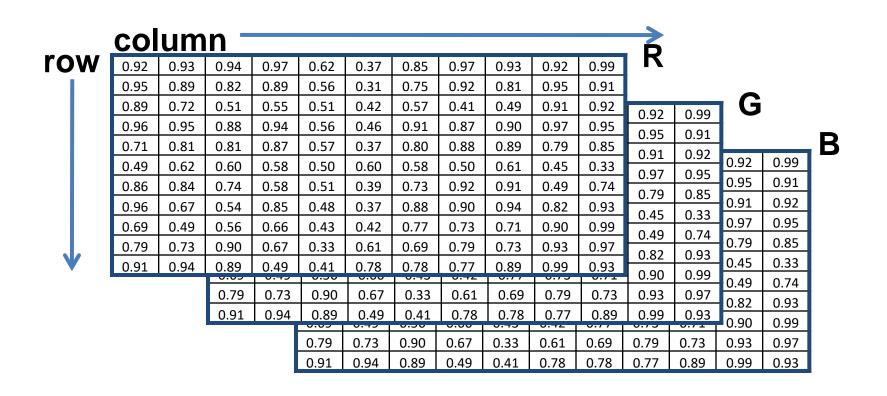
Human Luminance Sensitivity Function

Colour Image





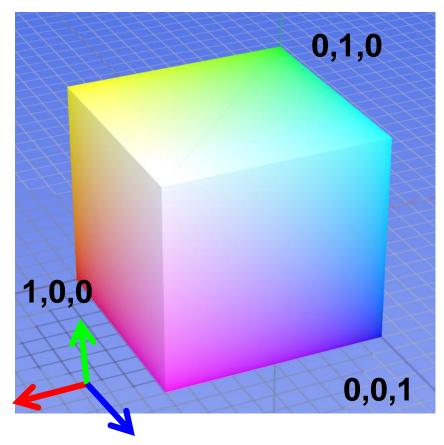
Images represented as a matrix



Colour spaces: RGB

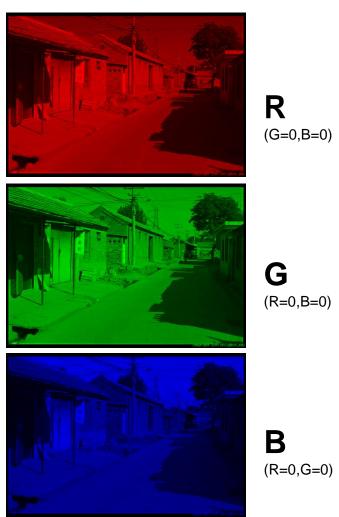
Default colour space





Some drawbacks

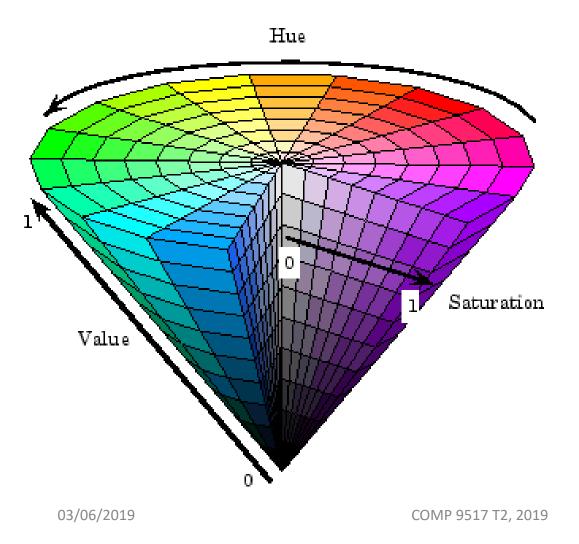
- Strongly correlated channels
- Non-perceptual

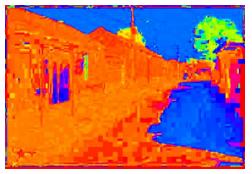


Colour spaces: HSV



Intuitive colour space









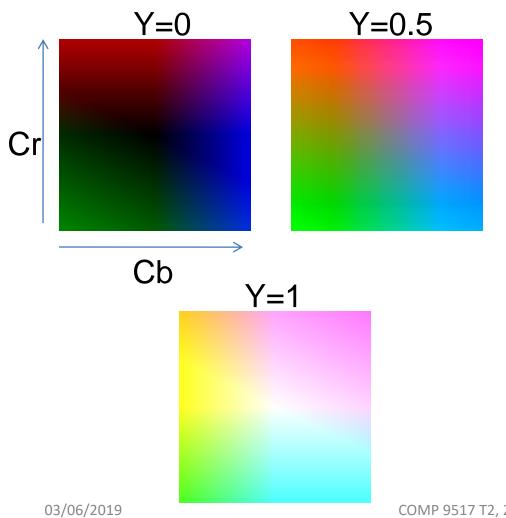
S (H=1,V=1)



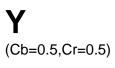
V (H=1,S=0)

Colour spaces: YCbCr

Fast to compute, good for compression, used by TV









Cb (Y=0.5, Cr=0.5)



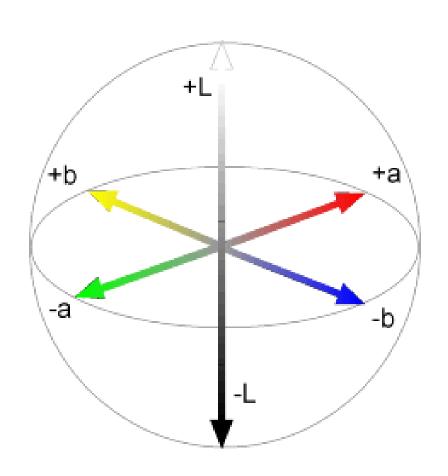
(Y=0.5,Cb=05)

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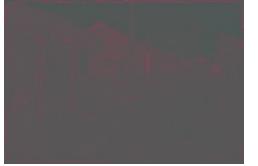
Colour spaces: L*a*b* "Perceptually uniform"* colour space







(a=0,b=0)



a (L=65,b=0)



b (L=65,a=0)

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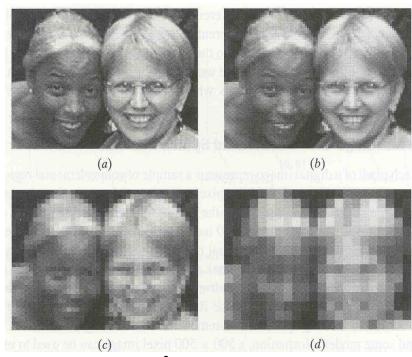
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Digitisation and Sampling

- Digitisation: converts analog image to digital image
- Sampling digitises the coordinates x and y:
 - spatial discretisation of picture function F (x,y)
 - use a grid of sampling points, normally rectangular: image sampled at points $x = j \Delta x$, $y = k \Delta y$, j = 1...M, k = 1...N.
 - $-\Delta x$, Δy called the **sampling intervals**.

Spatial Resolution

- Spatial Resolution: number of pixels per unit of length
- Resolution decreases by one half- see right
- Human faces can be recognized at 64 x 64 pixels per face



- Appropriate resolution is essential:
 - too little resolution, poor recognition
 - too much resolution, slow and wastes memory

Quantisation

- Quantisation digitises the intensity or amplitude values, ie F (x, y)
 - called intensity or gray level quantisation
 - Gray-level resolution:
 - usually has 16, 32, 64,, 128, 256 levels
 - number of levels should be high enough for human perception of shading details - human visual system requires about 100 levels for a realistic image.

For Reading

- Szeliski, Chapter 2
- Shapiro and Stockman, Chapter 2

Acknowledgement

- Slides from Derek Hoiem, Alexei Efros, Steve Seitz, and David Forsyth
- Image sources credited where possible
- Some material, including images and tables, were drawn from the referenced textbooks and associated online resources.