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Pour obtenir le grade de

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Spécialité : Sciences de la Terre et de l'Univers et de l'Environnement

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préparée au sein du **Laboratoire Institut des Géosciences de l'Environnement**  
dans l'**École Doctorale Sciences de la Terre de l'Environnement et des Planètes**

## Modélisation biogéochimique des nutriments dans un estuaire tropical urbanisé et scénario de gestion de l'eutrophisation

## Modeling of nutrient dynamics in an urbanized tropical estuary and application to eutrophication risk management

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*For Vinh thúi*

# Abstract

This thesis examines the application of Positive Matrix Factorization (PMF) for source apportionment of atmospheric pollution. We develop advanced optimization techniques and validation frameworks that enhance the accuracy and reliability of PMF in identifying pollution sources across European urban environments.

Our research demonstrates that improved model configuration and validation protocols can significantly reduce uncertainties in source contribution estimates, providing policy makers with more reliable data for targeted interventions.

**Keywords:** keyword1, keyword2, keyword3, keyword4

# Résumé

Cette thèse examine l'application de la Factorisation Matricielle Positive (PMF) pour l'attribution des sources de pollution atmosphérique. Nous développons des techniques d'optimisation avancées et des cadres de validation qui améliorent la précision et la fiabilité de la PMF dans l'identification des sources de pollution dans les environnements urbains européens.

Notre recherche démontre que des protocoles améliorés de configuration et de validation du modèle peuvent réduire significativement les incertitudes dans les estimations de contribution des sources, fournissant aux décideurs politiques des données plus fiables pour des interventions ciblées.

**Mots-clés:** mot-clé1, mot-clé2, mot-clé3, mot-clé4

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# List of Abbreviations

Abbreviation	Definition
PMF	Positive Matrix Factorization
EPA	Environmental Protection Agency
PM	Particulate Matter
BS	Bootstrap
DISP	Displacement
ME-2	Multilinear Engine version 2
CMB	Chemical Mass Balance
PCA	Principal Component Analysis
EV	Explained Variation
LEZ	Low Emission Zone
BAT	Best Available Technology

# List of Symbols

Symbol	Name	Unit
$a$	distance	m
$P$	power	W (J s <sup>-1</sup> )
$\omega$	angular frequency	rad

# Introduction

## **i** Note

This chapter demonstrates all major features available in Quarto for thesis writing. Each section showcases different elements and their cross-referencing capabilities to ensure everything works correctly.

## Figures

Quarto supports multiple ways to include figures:

### Single Figure



FIGURE 1: Organization logo

You can reference this as Figure 1.

### Side-by-Side Figures

See Figure 2 and Figure 3 side by side.

### Figure with Custom Attributes

You can reference this as Figure 4.

### Subfigures

Reference the combined figure as Figure 5 or individual subfigures as Figure 5a and Figure 5b.

### Figure Generated from CSV Data

Reference this figure as Figure 6.

### Multiple Data Series Plot

Reference this figure as Figure 7.

*Figures*



FIGURE 2: Logo



FIGURE 3: Cover Page



FIGURE 4: Organization logo

## Figures



(A) Logo 1

(B) Logo 2

FIGURE 5: Combined figures demonstration

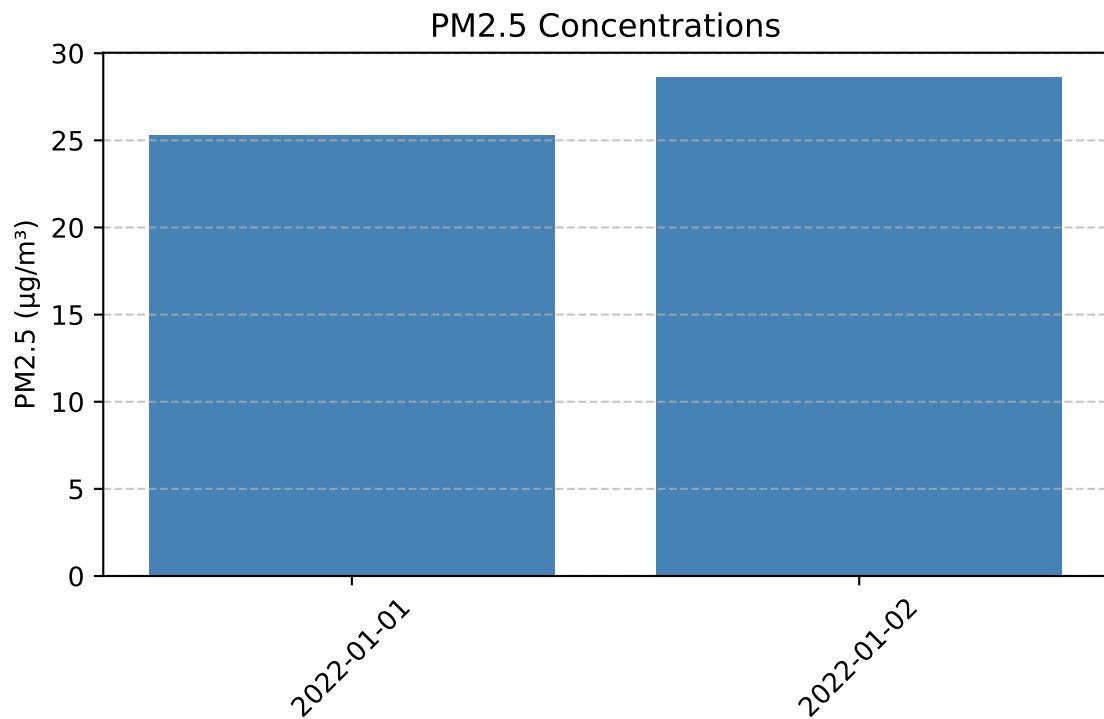


FIGURE 6: Plot generated from CSV data

## Tables

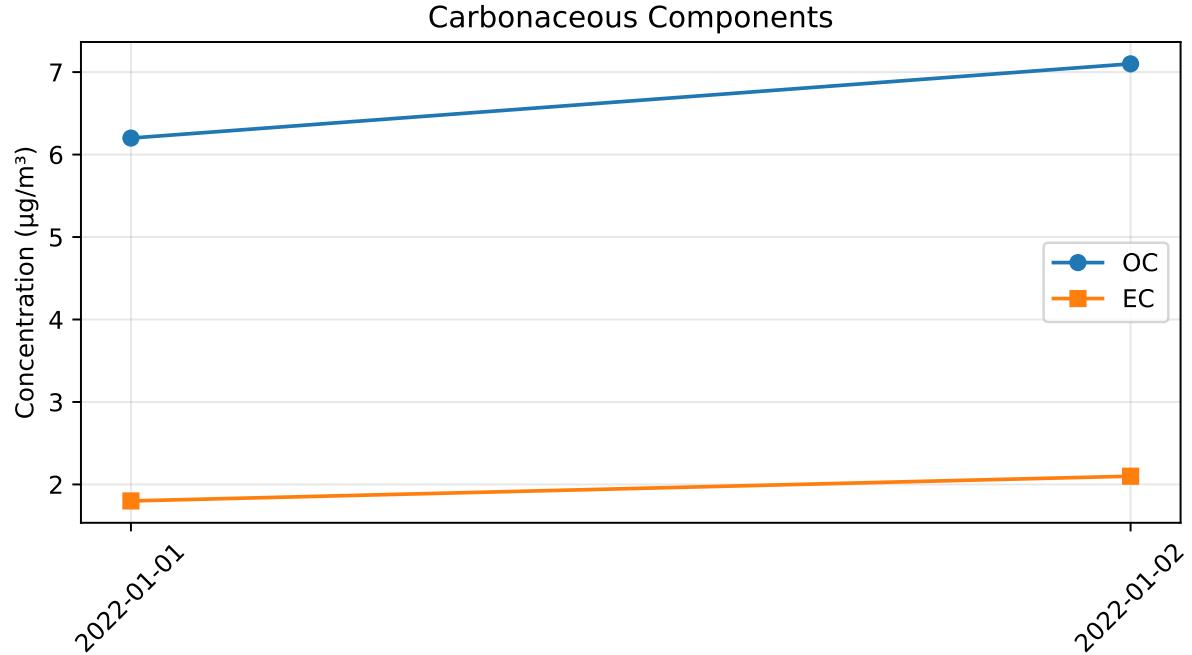


FIGURE 7: Multiple parameters from CSV data

## Tables

### Simple Table

TABLE 3: Basic Features

Feature	Description
Figures	Embedded images and graphics
Tables	Structured data presentation
Equations	Mathematical expressions

Reference as Table 3.

### Grid Table

TABLE 4: Grid Table Example

Column 1	Column 2
Row 1	Data
Row 2	Data

Reference as Table 4.

### Pipe Table with Alignment

TABLE 5: Aligned Table

Left	Center	Right
L1	C1	R1

## Tables

Left	Center	Right
L2	C2	R2

Reference as Table 5.

## Table from CSV Data

TABLE 6: Data imported from CSV file

Date	PM2.5	SO4	NO3
2022-01-01	25.3	4.2	3.1
2022-01-02	28.6	4.8	3.5

Reference this as Table 6.

## Simple Formatted Table

TABLE 7: Summary of key parameters

Parameter	Min	Max	Average
PM2.5	25.3	28.6	26.95
SO4	4.2	4.8	4.5
NO3	3.1	3.5	3.3
OC	6.2	7.1	6.65
EC	1.8	2.1	1.95

Reference as Table 7.

## Tables Containing Figures

### Single-Figure Table

TABLE 8: Single-Figure Table

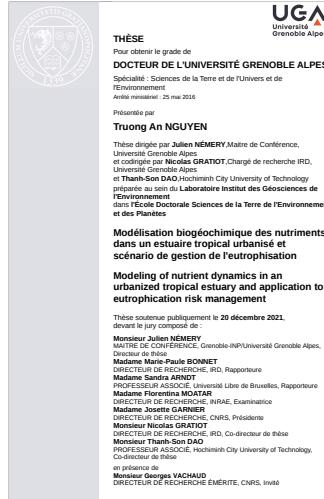
Figure	Description
	Organization logo example

Reference as Table 8.

### Multi-Figure Table

Tables

TABLE 9: Multi-Figure Table

Figure 1	Figure 2	Description
		Side-by-side figures example

Reference as Table 9.

Figure-Only Table

TABLE 10: Table with only a figure and no visible borders


--

Reference as Table 10.

Headerless Figure Table

Tables

TABLE 11: Table with hidden header row

---

Figure
The logo consists of the letters "UGA" in a large, bold, dark blue sans-serif font. To the right of "GA" is a small orange triangle pointing upwards. Below "UGA" is the text "Université" on one line and "Grenoble Alpes" on the next line, also in a dark blue sans-serif font.

---

Reference as Table 11.

**Clean Figure Table (No Borders, No Header)**

TABLE 12: Clean table with figure only

---

The logo consists of the letters "UGA" in a large, bold, dark blue sans-serif font. To the right of "GA" is a small orange triangle pointing upwards. Below "UGA" is the text "Université" on one line and "Grenoble Alpes" on the next line, also in a dark blue sans-serif font.
--

---

Reference as Table 12.

**Multiple Clean Figures Table**

Tables

TABLE 13: Multiple figures in a clean table



	<b>UGA</b> Université Grenoble Alpes
<b>THÈSE</b>	
Pour obtenir le grade de	
<b>DOCTEUR DE L'UNIVERSITÉ GRENOBLE ALPES</b>	
Spécialité : Sciences de la Terre et de l'Univers et de l'Environnement	
Arrêté ministériel : 25 mai 2016	
Présentée par	
<b>Truong An NGUYEN</b>	
Thèse dirigée par <b>Julien NÉMERY</b> , Maître de Conférence, Université Grenoble Alpes et codirigée par <b>Nicolas GRATIOT</b> , Chargé de recherche IRD, Université Grenoble Alpes et <b>Thanh-Son DAO</b> , Hochiminh City University of Technology préparée au sein du Laboratoire Institut des Géosciences de l'Environnement dans l'École Doctorale Sciences de la Terre de l'Environnement et des Planètes	
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en présence de <b>Monsieur Georges VACHAUD</b> DIRECTEUR DE RECHERCHE ÉMÉRITE, CNRS, Invité	

Reference as Table 13.

Ultra-Clean Figure Table

TABLE 14: Ultra-clean table with invisible header



Reference as Table 14.

*Equations*

## Equations

### Inline Equations

Inline math:  $E = mc^2$  or  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

### Display Equations

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \quad (1)$$

$$\nabla \times \mathbf{B} = \mu_0 \left( \mathbf{J} + \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right) \quad (2)$$

Reference Maxwell's equations as Equation 1 and Equation 2.

### Single Equation with Label

$$f(x) = \int_{-\infty}^{\infty} \hat{f}(\xi) e^{2\pi i \xi x} d\xi \quad (3)$$

Reference as Equation 3.

### Equation Arrays

$$\begin{array}{rcl} z & = & a \\ f(x, y, z) & = & x + y + z \end{array} \quad (4)$$

Reference as Equation 4.

### LaTeX Equation with Matrix

$$A = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{bmatrix} \quad (5)$$

Reference as Equation 5.

## Code Blocks

### Basic Python Code

---

#### Listing 0.1

---

25°C is equal to 77.0°F

---

Reference as Listing 0.1.

### Data Import Example

---

#### Listing 0.2

---

Number of rows: 2

Number of columns: 16

First few column names:

Date, PM2.5, Na, S04, N03

---

## Citations

Reference as Listing 0.2.

## Citations

Citations can be:

- Single: Paatero and Tapper (1994)
- Multiple: (Agency 2019; Norris et al. 2014)
- In-text: Paatero and Tapper (1994) states that...
- Parenthetical: (Paatero and Tapper 1994)

## Callouts

### Note Title

This is a note callout for important observations.

### Warning

This is a warning callout for potential issues.

### Important

This is an important callout for critical information.

### Tip

This is a tip callout for helpful advice.

## Cross-References

You can reference:

- Figures: Figure 1, Figure 2, Figure 5
- Tables: Table 3, Table 4, Table 6, Table 8, Table 9, Table 10, Table 11, Table 12, Table 13, Table 14
- Equations: Equation 3, Equation 1, Equation 5
- Code: Listing 0.1, Listing 0.2

## Additional Features

### Footnotes

Here's a footnote reference<sup>1</sup> and another one<sup>2</sup>.

### Definition Lists

**Term 1** Definition 1

**Term 2** Definition 2

### Blockquotes

This is a blockquote. It can span multiple lines.

---

<sup>1</sup>This is the footnote content.

<sup>2</sup>Footnotes can contain multiple paragraphs.

## Text Formatting

**Bold text**, *italic text*, ~~strikethrough~~, `inline code`

## Lists

Ordered list:

1. First item
2. Second item
3. Third item

Unordered list:

- Item one
- Item two
- Item three

## Theorems

**Theorem 0.1** (Pythagorean Theorem). *For a right-angled triangle with sides  $a$ ,  $b$  and hypotenuse  $c$ :*

$$a^2 + b^2 = c^2$$

Reference as Theorem 0.1.

# Chapter 1: Literature Review

Some Authors

## ! Chapter Summary

This chapter provides a comprehensive review of the existing literature pertinent to Positive Matrix Factorization (PMF) and its application in source apportionment of atmospheric pollutants. It delves into the mathematical underpinnings of PMF, comparing it with other receptor models like Chemical Mass Balance (CMB) and Principal Component Analysis (PCA). Key historical developments, seminal studies, common challenges, and advancements in PMF methodology are discussed, establishing the theoretical framework and identifying the research niche for this thesis.

This is the literature review chapter. It should appear with the title “Literature Review” in the navigation.

## 1.1 PMF Mathematical Foundation

The basic PMF model is defined by the following equation:

$$X_{ij} = \sum_{k=1}^p g_{ik} f_{kj} + e_{ij} \quad (1.1)$$

Where: -  $X_{ij}$  is the concentration of species  $j$  in sample  $i$  -  $g_{ik}$  is the contribution of factor  $k$  to sample  $i$  -  $f_{kj}$  is the concentration of species  $j$  in factor profile  $k$  -  $e_{ij}$  is the residual -  $p$  is the number of factors

## 1.2 Introduction to Source Apportionment Models

Table 1.1 summarizes the mathematical representations of various source apportionment models discussed in this thesis.

TABLE 1.1: Mathematical Representations of Source Apportionment Models

Model	Equation	Description	Key Constraints
PMF	$X_{ij} = \sum_{k=1}^p g_{ik} f_{kj} + e_{ij}$	Positive Matrix Factorization	$g_{ik} \geq 0, f_{kj} \geq 0$
CMB	$C_i = \sum_{j=1}^n a_{ij} S_j + e_i$	Chemical Mass Balance	Requires source profiles
PCA	$X = TP^T + E$	Principal Component Analysis	Orthogonal components
UNMIX	$C = AS$	Multivariate receptor model	Geometrically determined factors

## 1.3 Tables and Figures

### 1.3.1 Mathematical Equations in Tables

Table 1.2 presents key PMF models with their mathematical formulations and applications in source apportionment studies.

TABLE 1.2: PMF Model Variations with Their Mathematical Formulations

Model	Mathematical Formulation	Key Features	Application in PM Studies
Basic PMF	$X_{ij} = \sum_{k=1}^p g_{ik} f_{kj} + e_{ij}$	Non-negativity constraints	First applied by Paatero and Tapper (1994)
Weighted PMF	$Q = \sum_{i=1}^n \sum_{j=1}^m \left( \frac{e_{ij}}{\sigma_{ij}} \right)^2$	Uncertainty-weighted residuals	Extended by Hyndman et al. (2002)
ME-2 Engine	$Q_{\text{aux}} = Q + \alpha^2 \sum (f_{kj} - f_{kj}^*)^2$	Target factor profiles	Recommended by Norris et al. (2014)
Robust PMF	$Q = \sum_{i=1}^n \sum_{j=1}^m h(e_{ij}/\sigma_{ij})$	Outlier protection	Used in Agency (2019)

### 1.3.2 Data-Driven Tables from CSV Files

Table 1.3 shows London PM2.5 component data loaded directly from a CSV file.

TABLE 1.3: London PM2.5 Component Concentrations ( g/m<sup>3</sup>)

	SO4	NO3	NH4	OC	EC
count	3	3	3	3	3
mean	4.77	3.5	2.37	7.1	2.5
std	0.25	0.3	0.25	0.3	0.2
min	4.5	3.2	2.1	6.8	2.3
25%	4.65	3.35	2.25	6.95	2.4
50%	4.8	3.5	2.4	7.1	2.5
75%	4.9	3.65	2.5	7.25	2.6
max	5	3.8	2.6	7.4	2.7

### 1.3.3 Analysis Methods with Citations

Table 1.4 presents key analysis methods used in this study with relevant citations and their significance.

TABLE 1.4: Statistical Analysis Methods with Citations

Method	Mathematical Representation	Application	Reference
Correlation Analysis	$r_{xy} = \frac{\sum(x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum(x_i - \bar{x})^2 \sum(y_i - \bar{y})^2}}$	Component relationships	See Paatero and Tapper (1994)
Linear Regression	$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$	Trend analysis	As per Hyndman et al. (2002)
Principal Component Analysis	$\mathbf{X} = \mathbf{T}\mathbf{P}^T + \mathbf{E}$	Dimensionality reduction	Compared in Norris et al. (2014)
Cluster Analysis	$d(x, y) = \sqrt{\sum_{i=1}^n (x_i - y_i)^2}$	Source grouping	Applied by Agency (2019)

### 1.3.4 Mixed Content Table with Cross-References

Table 1.5 demonstrates how to include multiple content types in a single table, including references to figures, tables, and equations.

TABLE 1.5: Integration of Results with Cross-References

Factor	Contribution Range	Seasonal Pattern	Related Figure/Table	Statistical Significance
Traffic	15-35%	Highest in winter (Figure 4.2)	See Table 4.1	$p < 0.01 (\chi^2 = 15.3)$
Industrial	20-30%	Consistent year-round	Equation Equation 1.1	$p < 0.05 (t = 2.4)$
Biomass Burning	5-30%	Winter > Fall > Spring > Summer	Table 1.2	$p < 0.001 (F = 8.7)$
Secondary Formation	15-50%	See Figure 4.1	Compare to Agency (2019) findings	$r^2 = 0.76 (p < 0.01)$

### 1.3.5 Comparative Source Profiles

Table 1.6 compares source profiles identified in this study with those reported in previous research.

TABLE 1.6: Comparative Source Profiles (Bold = Dominant, *Italic* = Secondary)

Component	Traffic Profile	Industrial Profile	Biomass Profile	Secondary Profile
SO <sup>2</sup>	20%	35%	15%	<b>25%</b> (Norris et al. 2014)
NO	25%	15%	20%	<b>35%</b> (Agency 2019)
NH	10%	5%	25%	<b>55%</b> (Paatero and Tapper 1994)
OC	35%	15%	<b>40%</b> (Hyndman et al. 2002)	10%
EC	<b>45%</b>	10%	25%	5%

# Chapter 2: Optimization and Validation of PMF Models

Some authors

## ! Chapter Summary

This chapter focuses on the methodological core of the thesis: the optimization and validation of Positive Matrix Factorization (PMF) models. It presents a systematic framework for selecting optimal model parameters, such as the number of factors and the FPEAK rotational parameter, to achieve physically meaningful solutions. Furthermore, the chapter details a multi-faceted validation strategy, incorporating techniques like bootstrap analysis, displacement of factor elements (DISP), and combined BS-DISP analysis, to rigorously assess the stability, uncertainty, and robustness of the derived source profiles and contributions.

Under review at Science of the Total Environment

## 2.1 Abstract

This chapter presents a comprehensive framework for optimizing and validating PMF (Positive Matrix Factorization) models in European urban environments ([Paatero and Tapper 1994](#)). We develop a systematic approach for model parameter selection and results validation using multiple complementary techniques ([Hyndman et al. 2002](#); [Norris et al. 2014](#)).

## 2.2 Methods

### 2.2.1 Model Optimization Framework

The PMF optimization process ([Agency 2019](#)) involves iterative refinement of several key parameters:

1. Number of factors (p):

$$Q(p) = \sum_{i=1}^n \sum_{j=1}^m \left( \frac{x_{ij} - \sum_{k=1}^p g_{ik} f_{kj}}{\sigma_{ij}} \right)^2 \quad (2.1)$$

2. FPEAK parameter ( $\phi$ ):

$$Q(\phi) = Q_{base} + P(\phi) \quad (2.2)$$

where  $P(\phi)$  is the penalty term for non-zero FPEAK values ([Agency 2019](#)).

### 2.2.2 Validation Methods

We employed three complementary validation approaches as recommended by ([Norris et al. 2014](#)):

1. Bootstrap analysis
2. DISP (displacement) analysis
3. BS-DISP combined analysis

## 2.3 Results

### 2.3.1 Factor Number Selection

### 2.3.2 PMF Results Summary

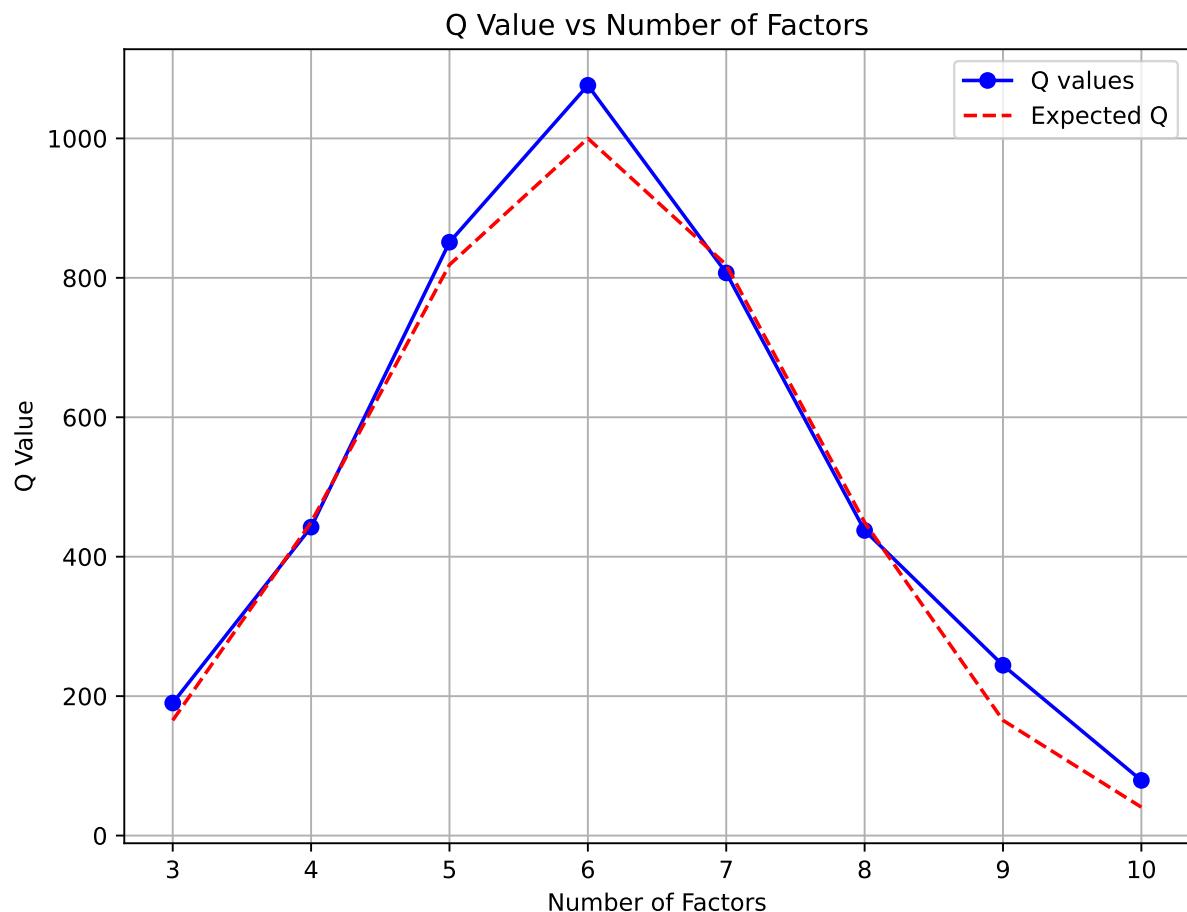


FIGURE 2.1: Q-value vs number of factors

TABLE 2.1: Summary of PMF results for different factor numbers

Factors	Q/Q_exp	R <sup>2</sup>	Sources Identified
3	1.5	0.75	Basic
4	1.3	0.82	Improved
5	1.2	0.87	Good
6	1	0.91	Optimal
7	0.92	0.92	Splitting
8	0.91	0.93	Splitting+

## 2.4 Advanced Model Optimization Techniques

### 2.4.1 Mathematical Formulations of Optimization Metrics

Table 2.2 presents the mathematical formulations of various optimization metrics used in PMF model development and their interpretation.

TABLE 2.2: Mathematical Formulations for PMF Model Optimization

Metric	Mathematical Formulation	Interpretation	Reference
Q/Q <sub>exp</sub>	$\frac{Q}{n \times m - p \times (n+m)}$	Should approach 1.0	Paatero and Tapper (1994)
Explained Variation (EV)	$EV_{jk} = \frac{\sum_{i=1}^n g_{ik} f_{kj}}{\sum_{i=1}^n x_{ij}}$	Factor importance for each species	Hyndman et al. (2002)
Residual Analysis	$r_{ij} = \frac{x_{ij} - \sum_{k=1}^p g_{ik} f_{kj}}{\sigma_{ij}}$	Should be normally distributed	Norris et al. (2014)
BS Mapping	$s = \frac{1}{n_{boot}} \sum_{n=1}^{n_{boot}} d_n^2$	Stability of factors	Agency (2019)
DISP Swap Count	Number of factor swaps at $d_{max}$	< 5% for stable solution	Norris et al. (2014)
BS-DISP Error	$\Delta Q/Q_{exp} < 0.5\%$	Indicates robust factors	Agency (2019)

### 2.4.2 Cross-Validation with External Datasets

Table 2.3 compares our PMF results with external validation datasets, building upon the findings from Section 1.3.

TABLE 2.3: Cross-Comparison Between PMF Results and External Validation Data

Source	PMF Contribution (%)	External Validation (%)	Correlation (r)	Reference	Comparison to Table 1.6
					Comparison to Table 1.6
Traffic	$35.2 \pm 4.5$	$33.8 \pm 5.2$	0.87	Traffic counts	Within 5% of values in Table 1.6
Industry	$22.7 \pm 3.8$	$24.5 \pm 6.1$	0.81	Emission inventory	Consistent with profiles in Table 1.2
Biomass	$18.5 \pm 6.2$	$20.1 \pm 5.8$	0.79	Levoglucosan	Similar to findings in Agency (2019)
Secondary	$23.6 \pm 5.3$	$21.6 \pm 4.9$	0.92	$\text{NH}_4/\text{SO}_4$ ratio	Matches equation Equation 1.1 predictions

### 2.4.3 Rotational Ambiguity Analysis

Table 2.4 shows the impact of different FPEAK values on the model results, as formulated in equation Equation 2.2.

TABLE 2.4: Impact of FPEAK Values on PMF Model Results

FPEAK Value	$\Delta Q/Q_{exp}$ (%)	Factor Identity Changes	G-Space Correlation Changes	Recommended by
-1.0	+8.5%	Major	Decreased correlations	Rarely used
-0.5	+2.2%	Moderate	Slight decreases	Hyndman et al. (2002) for specific cases
-0.2	+0.4%	Minor	Minimal changes	Norris et al. (2014) as lower bound
0.0	0.0%	<b>Base run</b>	<b>Reference point</b>	Paatero and Tapper (1994) as default
+0.2	+0.5%	Minor	Minimal changes	Norris et al. (2014) as upper bound
+0.5	+2.5%	Moderate	Slight increases	Sometimes used
+1.0	+9.2%	Major	Increased correlations	Rarely used

#### 2.4.4 Advanced Model Uncertainty Metrics

TABLE 2.5: Bootstrap Uncertainty Results for Source Contributions

Source	Base Contribution (%)	Bootstrap Mean (%)	Bootstrap 5th (%)	Bootstrap 95th (%)	BS Mapping (%)	DISP Error (%)
Traffic	35.2	34.8	31.5	38.2	95	0.2
Industry	22.7	23.1	20.2	25.9	92	0.3
Biomass	18.5	18.2	15.8	22.5	88	0.4
Secondary	23.6	23.9	21.1	26.8	97	0.1

#### 2.4.5 Integration with Results from Other Chapters

Table 2.6 presents an integrated view of our PMF model results, linking to findings from other chapters and using complex mathematical notation.

TABLE 2.6: Integrated Analysis of Source Contributions Across Chapters

Source	Mathematical Expression for Time Series	Spatial Distribution	Temporal Pattern	Policy Implications
Traffic	$g_{i1} = \beta_0 + \beta_1(\text{traffic count})_i + \varepsilon_i$	Urban cores (see Table 1.6)	Weekday peaks (see Figure 4.2)	LEZ expansion
Industry	$g_{i2} = \sum_{j=1}^m \gamma_j (\text{industrial activity})_{j,i} + \varepsilon_i$	Industrial zones	Consistent patterns	Emission standards
Biomass	$g_{i3} = \alpha \exp\left(-\frac{(T_i - T_0)^2}{2\sigma^2}\right) + \varepsilon_i$	Residential areas	Winter peaks	Regulation of wood burning
Secondary	$g_{i4} = \lambda \sin\left(\frac{2\pi t_i}{365}\right) + \gamma t_i + \varepsilon_i$	Regional	Summer peaks	Regional cooperation

#### 2.4.6 Model Comparison Matrix

Table 2.7 compares various receptor models for source apportionment, building on the equations in Table 1.1 from the introduction.

TABLE 2.7: Comparison of Receptor Models for Source Apportionment

Model Type	Mathematical Basis	Strengths	Limitations	Compared to PMF
PMF	$X = GF + E$ with $g_{ik} \geq 0, f_{kj} \geq 0$	Non-negativity constraints, uncertainty weighting	Rotational ambiguity	Base model
PCA/APCS	$X = TP^T + E$	Simple implementation	Cannot ensure non-negativity	Inferior for source apportionment
CMB	$C_i = \sum_{j=1}^n a_{ij} S_j + e_i$	Uses source profiles	Requires prior knowledge	More constrained than PMF
UNMIX	$C = AS$ with $A \geq 0, S \geq 0$	Geometrically determines edges	Fewer factors than PMF	Less statistical power
ME-2	$X = GF + E$ with partial constraints	Can include prior knowledge	Complex implementation	Enhanced version of PMF
Hybrid Models	PMF + dispersion models: $C_{i,j} = \sum_{k=1}^p D_{i,j,k} \cdot Q_k$	Combines receptor and dispersion	Data intensive	Extended PMF application



## Unveiling the optimal regression model for source apportionment of the oxidative potential of PM<sub>10</sub>

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**Abstract.** The capacity of particulate matter (PM) to generate reactive oxygen species (ROS) in vivo leading to oxidative stress is thought to be a main pathway in the health effects of PM inhalation. Exogenous ROS from PM can be assessed by acellular oxidative potential (OP) measurements as a proxy of the induction of oxidative stress in the lungs. Here, we investigate the importance of OP apportionment methods for OP distribution by PM<sub>10</sub> sources in different types of environments. PM<sub>10</sub> sources derived from receptor models (e.g., EPA positive matrix factorization (EPA PMF)) are coupled with regression models expressing the associations between PM<sub>10</sub> sources and PM<sub>10</sub> OP measured by ascorbic acid (OP<sub>AA</sub>) and dithiothreitol assay (OP<sub>DTT</sub>). These relationships are compared for eight regression techniques: ordinary least squares, weighted least squares, positive least squares, Ridge, Lasso, generalized linear model, random forest, and multilayer perceptron. The models are evaluated on 1 year of PM<sub>10</sub> samples and chemical analyses at each of six sites of different typologies in France to assess the possible impact of PM source variability on PM<sub>10</sub> OP apportionment. PM<sub>10</sub> source-specific OP<sub>DTT</sub> and OP<sub>AA</sub> and out-of-sample apportionment accuracy vary substantially by model, highlighting the importance of model selection according to the datasets. Recommendations for the selection of the most accurate model are provided, encompassing considerations such as multicollinearity and homoscedasticity.

### 1 Introduction

Ambient particulate matter (PM) is one of the key contributors to atmospheric pollution and is responsible for approximately 7 million premature deaths worldwide yearly (WHO, 2021). Many epidemiological studies have linked PM exposure to adverse health effects including (i) acute effects studies using time series and related studies to evaluate the immediate impact of PM exposure (Bell et al., 2004; Dominici, 2004; Pope and Dockery, 2006; Peng et al., 2009) and (ii) cohort studies aiming to evaluate the long-term effects of

chronic PM exposure (Pelucchi et al., 2009; Crouse et al., 2012, 2015; Beelen et al., 2014; Ayres et al., 2008; Yu et al., 2021). These studies mainly focused on the association with PM mass concentrations. However, various research shows that the impacts of PM also depend on other factors such as chemical composition, size distribution, particle morphology, and biological mechanisms (Brook et al., 2010). The capacity of PM to generate reactive oxygen species (ROS) in vivo has recently been introduced as a pivotal indicator of PM biological mechanism with direct implications for oxida-

tive stress and cellular damage (Li et al., 2008; Lodovici and Bigagli, 2011; Mudway et al., 2020; Nelin et al., 2012; Rao et al., 2018; Ayres et al., 2008; Akhtar et al., 2010; Leni et al., 2020). The quantification of the PM capacity to oxidize biological media is called “oxidative potential” (OP) (Bates et al., 2019; Daellenbach et al., 2020; Dominutti et al., 2023). Various acellular assays of OP have been introduced, differentiating ROS generation mechanisms of PM (Dominutti et al., 2023; Calas et al., 2018). Dithiothreitol (DTT) and ascorbic acid (AA) assays are two of the commonly used procedures in the literature (Liu and Ng, 2023).

The relationship between PM chemical components and OP activities may indicate which components are the most prone to generating ROS (Calas et al., 2019; Godri et al., 2011; Yang et al., 2014; Janssen et al., 2014; Crobeddu et al., 2017; Szigeti et al., 2015, 2016; Calas et al., 2018). However, this research pathway struggles with the co-variation between measured and unmeasured PM components (Calas et al., 2018; Weber et al., 2018). An alternative approach is to examine the association between OP and sources of PM obtained using receptor models such as chemical mass balance, positive matrix factorization (PMF), or principal component analysis. PMF is the most popular method for its ability to quantify PM source contributions without extensive prior information on specific sources at the site studied (Belis et al., 2013; Viana et al., 2008; Paatero and Tappert, 1994; Brown et al., 2015; Paatero and Hopke, 2009).

Regression analysis is the most common and effective way to estimate the redox activity of receptor-model-derived PM sources (Bates et al., 2015; Deng et al., 2022; Li et al., 2023; Liu et al., 2018; Shangguan et al., 2022; Verma et al., 2014; J. Wang et al., 2020; Yu et al., 2019). Generally, this is achieved by regression analyses to characterize the relationship between OP activities ( $\text{nmol min}^{-1} \text{m}^{-3}$ ) and PM source contributions ( $\mu\text{g m}^{-3}$ ). This approach provides the OP activities attributed to each microgram of each source ( $\text{nmol min}^{-1} \mu\text{g}^{-1}$ ), denoted as “intrinsic OP”, which can be used to calculate the contribution of each source for each observation day. Numerous regression models can be used for such OP source apportionment (SA), with multiple linear regression fitted by ordinary least squares (OLS) being the most common regression technique (Bates et al., 2015; Deng et al., 2022; Li et al., 2023; Liu et al., 2018; Shangguan et al., 2022; Verma et al., 2014; Y. Wang et al., 2020; Yu et al., 2019). Further, some studies exclude sources with negative intrinsic OP, assuming that negative OP activities are geochemically nonsensical (Bates et al., 2018; Weber et al., 2018). Additionally, weighted least squares can be used to introduce a weighting term, generally using the OP analysis uncertainties to take into account the measurement uncertainties of the OP assays (Borlaza et al., 2021; Daellenbach et al., 2020; Dominutti et al., 2023; Fadel et al., 2023; in't Veld et al., 2023; Weber et al., 2021). Finally, non-linear models, such as multilayer perceptron, have been used to try to capture possible non-linearities between OP activities and

PM sources (Borlaza et al., 2021; Elangasinghe et al., 2014; D. Wang et al., 2023). However, no study to date has compared the performance and applicability of these various regression models. Each model entails different assumptions which should be carefully considered when selecting a given model.

This study aims to evaluate the variability in  $\text{PM}_{10}$  OP SA techniques by comparing eight regression techniques: multiple linear regression fitted by OLS, weighted least squares (WLS), positive least squares (PLS), ridge regression (Ridge), least absolute shrinkage and selection operator (Lasso), generalized linear model (GLM), random forest (RF), and multilayer perceptron (MLP). These techniques are applied to apportion  $\text{PM}_{10}$   $\text{OP}_{\text{AA}}$  and  $\text{PM}_{10}$   $\text{OP}_{\text{DTT}}$  to  $\text{PM}_{10}$  sources at six sites in France. The  $\text{PM}_{10}$  SA outputs have been published by Weber et al. (2021), using a harmonized PMF methodology based on 1 year of sampling with similar chemical analyses for a large set of chemical tracers. The results of the  $\text{PM}_{10}$  OP SA models are compared with regard to the estimated intrinsic  $\text{PM}_{10}$  OP of each source, the out-of-sample accuracy of the apportionment, and the assumptions inherent in each model. The most appropriate model at each site is compared with OLS to quantify the difference between choosing a model based on data characteristics vs. using the most common approach. Finally, this study provides guidelines for selecting the most suitable model in the strategy for OP contribution regarding sources of  $\text{PM}_{10}$ . This holds particular significance in the context of the implementation of OP monitoring as a novel air quality metric as foreseen in research programs (such as RI-Urbans) and in the process of the revision of European Directive 2008/50/CE.

## 2 Methodology

### 2.1 General organization of the study

Figure 1 illustrates the general workflow of this study. Sections 2.2, 2.3, and 2.4 describe the methods used to analyze the temporal evolution of  $\text{PM}_{10}$  sources and  $\text{PM}_{10}$  OP, identify collinearity among  $\text{PM}_{10}$  sources, and examine homoscedasticity in the relationship between  $\text{PM}_{10}$  OP and  $\text{PM}_{10}$  sources. Section 2.5 describes the eight regression techniques (OLS, WLS, PLS, Ridge, Lasso, GLM, RF, and MLP), used for  $\text{PM}_{10}$  OP SA. Each technique is applied to each site separately using  $\text{PM}_{10}$   $\text{OP}_v$  ( $\text{nmol min}^{-1} \text{m}^{-3}$ ) as the dependent variable and  $\text{PM}_{10}$  sources ( $\mu\text{g m}^{-3}$ ) as independent variables. The coefficient of the regression, called the “intrinsic  $\text{PM}_{10}$  OP” of the source ( $\text{nmol min}^{-1} \mu\text{g}^{-1}$ ), represents the capacity of each  $\mu\text{g}$  of  $\text{PM}_{10}$  from the given source to generate oxidative stress; the higher the intrinsic  $\text{PM}_{10}$  OP of a source, the more redox-active. Each model is trained on a randomly selected (without replacement) 80 % subsample of the dataset and validated on the remaining 20 %. This process is repeated 500 times to estimate uncertainty, a method particularly needed for sources with strong

seasonality. For WLS, PLS, Ridge, and Lasso models,  $\text{PM}_{10}$  OP analytical errors were used as a weighting, implying that the  $\text{PM}_{10}$  OP with the high analysis uncertainties has less influence on the model. These eight regression techniques were applied to find the relationship between  $\text{PM}_{10}$  OP and  $\text{PM}_{10}$  sources; however, PLS, Ridge, and Lasso were performed twice, with and without weighting, and consequently there are 11 results of regression techniques that will be presented. Section 2.6 describes the statistical validation of the models using root mean square error (RMSE), mean absolute error (MAE), and R-squared ( $R^2$ ). The geochemical validation is based on the regression coefficient (the intrinsic  $\text{PM}_{10}$  OP) of each source. These are calculated separately for the training and testing data and averaged across the 500 sampling iterations.

## 2.2 Study sites and $\text{PM}_{10}$ sources

Six French sites are selected in this work for their different typologies: Roubaix and Nice (traffic sites within urban areas), Port-de-Bouc (industrial hotspot), Talence (urban background site), Grenoble and Chamonix (urban background sites in an alpine valley). At each site, sampling was conducted over at least 1 year to capture the complete annual evolution of  $\text{PM}_{10}$  and its components. These sites and sampling series have been used and described by Weber et al. (2019).

In brief, daily filter samples were collected on pre-heated Pallflex quartz fiber filters every third day through high-volume sampling (DA80, Digitel). These filters were analyzed to determine the PM chemical species and OP activities. Further details regarding the chemical species and  $\text{PM}_{10}$  OP analysis methodology can be found in Weber et al. (2019, 2021). Briefly, elemental carbon (EC) and organic carbon (OC) were analyzed using the EUSAAR2 thermo-optical protocol with a Sunset Laboratory analyzer. Major ionic components ( $\text{Cl}^-$ ,  $\text{NO}_3^-$ ,  $\text{SO}_4^{2-}$ ,  $\text{NH}_4^+$ ,  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Mg}^{2+}$ ,  $\text{Ca}^{2+}$ ) and methanesulfonic acid (MSA) were measured by ion chromatography (IC). Anhydro sugars and saccharides (including levoglucosan, mannosan, arabitol, sorbitol, and mannitol) were analyzed by high-performance liquid chromatography with pulsed amperometric detection (HPLC-PAD). Major and trace elements (Al, Ca, Fe, K, As, Ba, Cd, Co, Cu, La, Mn, Mo, Ni, Pb, Rb, Sb, Sr, V, and Zn) were determined by inductively coupled plasma atomic emission spectroscopy or mass spectrometry (ICP-AES or ICP-MS). Furthermore, colocated  $\text{PM}_{10}$  measurements were conducted automatically at each site using the Tapered Element Oscillating Microbalance equipped with a Filter Dynamics Measurement System (TEOM-FDMS).

We used the  $\text{PM}_{10}$  sources identified by Weber et al. (2019), who performed a separate PMF for each site using a harmonized approach for all sites (the same chemical species and measurement methods, the same procedure to estimate uncertainties, and the same constraints on the prelim-

inary solutions). Table 1 provides a data description, including the sampling duration, the number of samples collected, and the  $\text{PM}_{10}$  sources identified at each site, while Fig. 2 presents the location of the sites in France together with the respective proportion of each  $\text{PM}_{10}$  source at each site.

## 2.3 OP analysis

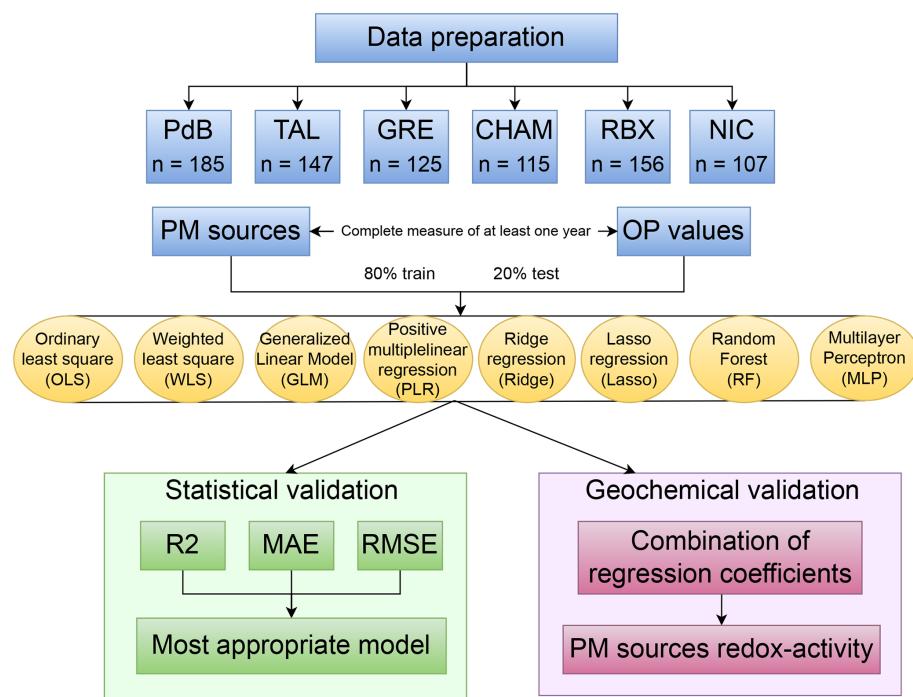
$\text{PM}_{10}$  OP assays were performed on  $\text{PM}_{10}$  extracted from the filters using simulated lung fluid, as detailed in Calas et al. (2017, 2018). The AA assay involved ascorbic acid, a natural antioxidant in the lungs inhibiting lipid and protein oxidation in the lining fluid, using the method presented by Kelly and Mudway (2003) and further described by Calas et al. (2018). Conversely, the DTT assay used dithiothreitol (DTT) as a chemical surrogate for cellular reducing agents, specifically nicotinamide adenine dinucleotide and nicotinamide adenine dinucleotide phosphate oxidase, thereby replicating *in vivo* interactions between  $\text{PM}_{10}$  and biological oxidants (Cho et al., 2005; Calas et al., 2018). Both assays measured the consumption of AA or DTT during the assay, i.e., the rate of the transfer of electrons from AA or DTT to oxygen. The assays were conducted with 96-well plates of UV-transparent quality (CELLSTAR, Greiner Bio-One), and absorption measurements were acquired using a TECAN spectrophotometer (Infinite M200 Pro) at the wavelengths of 265 nm for the AA assay and 412 nm for the DTT assay (Calas et al., 2017, 2018, 2019). Each sample extraction was subjected to four analyses; the  $\text{PM}_{10}$  OP in this study represents the mean and the analysis uncertainty is the standard deviation of these four  $\text{PM}_{10}$  OP analyses. After analysis, the  $\text{PM}_{10}$  OP activities of each sample were blank-subtracted using laboratory and field blanks, and normalized using the air sampling volumes and the mass concentration. The resulting OP<sub>v</sub> represents the  $\text{PM}_{10}$  OP due to  $\text{PM}_{10}$  per cubic meter of air ( $\text{nmol min}^{-1} \text{m}^{-3}$ ). To simplify the denotation of  $\text{PM}_{10}$  OP, OP is used to represent  $\text{PM}_{10}$  OP throughout this article.

## 2.4 Collinearity and heteroscedasticity tests

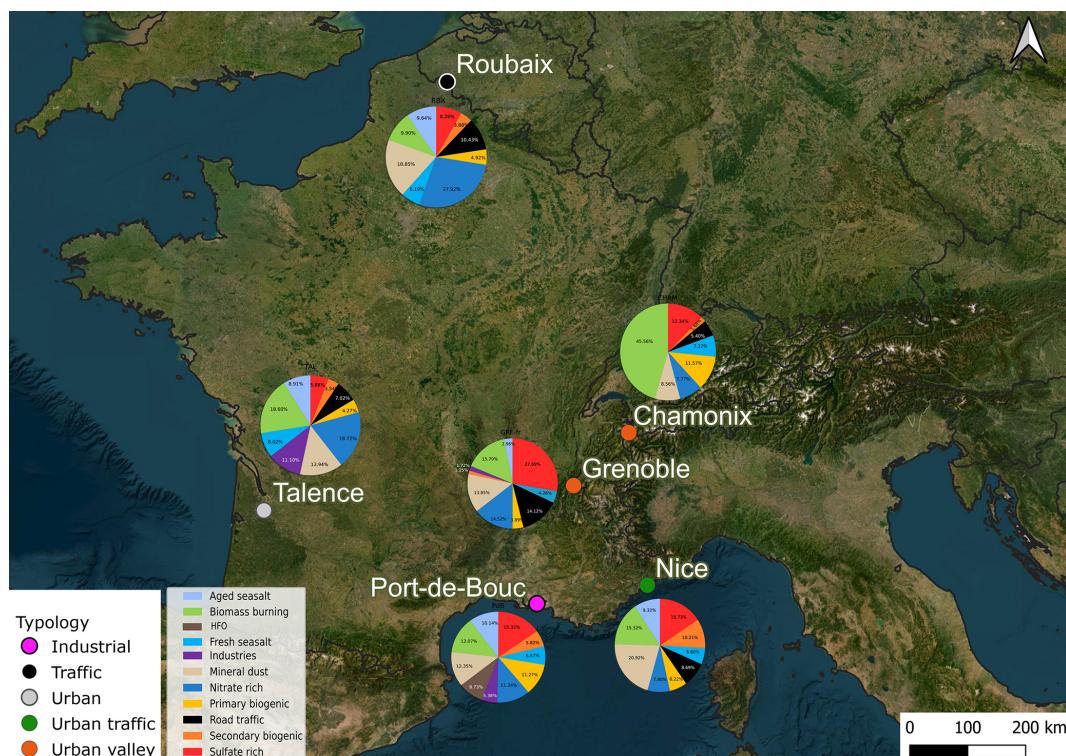
The result of a regression model strongly depends on the characteristics of the dataset because each model makes assumptions about the data. Two critical assumptions in OLS regression analysis are that (1) there is little collinearity between independent variables (the  $\text{PM}_{10}$  sources in this study) and (2) the variance of the regression residuals is constant (called “homoscedasticity”). These assumptions should be tested in different ways.

### 2.4.1 Collinearity

Collinearity occurs when one or more of the independent variables is close to a linear combination of the other independent variables. When collinearity is present, small



**Figure 1.** Workflow comparison of the methodology for PM<sub>10</sub> OP source apportionment.



**Figure 2.** The location of the sites selected for this study. The small colored dots represent the typology of the sites. The pie charts are the PM<sub>10</sub> source apportionment for each site with the colors identifying the PM<sub>10</sub> sources. Background photography from ESRI satellite imagery.

**Table 1.** Data description.

	PdB	TAL	GRE-fr	CHAM	RBX	NIC
Name	Port-de-Bouc	Talence	Grenoble	Chamonix	Roubaix	Nice
No. of samples	185	147	125	115	156	107
Sampling dates	June 2014 to June 2016	February 2012 to April 2013	February 2017 to March 2018	November 2013 to October 2014	January 2013 to May 2014	July 2014 to May 2015
No. of sources	10	10	10	8	9	9

changes in the data can cause large changes in estimated coefficients, and the estimated standard errors of the coefficients are large. The variance inflation factor (VIF) is an indicator of the collinearity between independent variables (Craney and Surles, 2002; O'Brien, 2007; Rosenblad, 2011). The VIF of a specific source is calculated as

$$\text{VIF}_i = \frac{1}{1 - R_i^2}, i = 1, \dots, p - 1, \quad (1)$$

where  $p$  is the number of  $\text{PM}_{10}$  sources and  $R^2$  is the coefficient of determination of a multiple linear regression model between the  $i$ th source and the other sources. The VIF values of a  $\text{PM}_{10}$  source present a range between 1 and  $\infty$ . The higher the VIF values, the greater the collinearity between this  $\text{PM}_{10}$  source and the other sources. A VIF value between 5 and 10 is commonly interpreted as moderate collinearity, while values greater than 10 indicate high collinearity (Craney and Surles, 2002).

#### 2.4.2 Heteroscedasticity

Heteroscedasticity occurs when the variance of regression residuals is not constant but varies for different values of the dependent variable. In this case, the estimated standard errors of the regression coefficients are not reliable. The Goldfeld–Quandt test was developed by Goldfeld and Quandt (1965) to evaluate residual variance in a regression model. To implement the Goldfeld–Quandt test, an OLS regression was performed between OP and  $\text{PM}_{10}$  sources to identify the residual of OP prediction. Next, the  $\text{PM}_{10}$  sources and corresponding residual are divided into three segments: the upper segment is the group with higher  $\text{PM}_{10}$  source concentration, the lower segment is the group with lower  $\text{PM}_{10}$  source concentration, and the middle segment, constituting 10 % of the moderate  $\text{PM}_{10}$  concentration, is excluded. A subsequent regression analysis is then conducted on the two remaining subgroups to determine the ratio of residual sums of squares. Finally, an  $F$  test is conducted on this ratio to assess whether the variances are the same, with a  $p$  value below 0.05 interpreted as evidence of heteroscedasticity.

The variance inflation factor (VIF) and the Goldfeld–Quandt test were performed in Python 3.9, using the statsmodels 0.14.0 package (Seabold and Perktold, 2010).

### 2.5 Regression models

The fundamental principle of regression models in this study is to use the  $\text{PM}_{10}$  sources to predict OP activities by identifying the parameters (coefficients and residuals) that minimize an error term (Hastie, 2009). A simple regression model can be represented by Eq. (2), which defines the estimated function of the regression model, and by Eq. (3), which estimates the residuals:

$$\hat{y} = f(X) + e, \quad (2)$$

$$e = y - \hat{y}, \quad (3)$$

where  $\hat{y}$  is the estimated OP ( $\text{nmol min}^{-1} \text{m}^{-3}$ ),  $X$  is the  $\text{PM}_{10}$  source contribution ( $\mu\text{g m}^{-3}$ ),  $y$  is the observed OP ( $\text{nmol min}^{-1} \text{m}^{-3}$ ), and  $e$  denotes the residuals ( $\text{nmol min}^{-1} \text{m}^{-3}$ ). Each model has certain assumptions and a minimization term, as presented in the next section.

#### 2.5.1 Ordinary least squares (OLS)

OLS is a linear regression technique that minimizes the residual sum of squares. This model is based on several assumptions: (1) linearity – the relationship between OP and  $\text{PM}_{10}$  sources is linear; (2) independence – the  $\text{PM}_{10}$  sources must be independent, with no collinearity; (3) homoscedasticity – the variance of residuals is constant across all values of  $\text{PM}_{10}$  sources; and (4) normality – the residuals are normally distributed. In the OLS model, the estimated equation and objective to minimize are defined as follows:

$$\hat{y} = \beta_0 + \sum_1^p \beta_i \cdot x_i, \quad (4)$$

$$\text{Minimize } \sum_{i=1}^m (y_i - \hat{y}_i)^2 \quad (5)$$

where  $\beta_0$  denotes the intercept ( $\text{nmol min}^{-1} \text{m}^{-3}$ ),  $\beta_i$  represents the regression coefficient (intrinsic OP,

$\text{nmol min}^{-1} \mu\text{g}^{-1}$ ) of source  $i$ ,  $x_i$  is the concentration of source  $i$  ( $\mu\text{g m}^{-3}$ ),  $p$  is the number of  $\text{PM}_{10}$  sources, and  $m$  is the number of observations.

### 2.5.2 Weighted least square (WLS)

The assumptions and the minimization term in WLS closely align with those in OLS. The only difference is that WLS accounts for heteroscedasticity by introducing a weighting term for individual OP observations whose variance is assumed to be related to the variance of the residuals. The estimation equation in WLS is the same as that of OLS, but the objective to minimize is expressed as

$$\begin{aligned} & \text{Minimize } \sum_{i=1}^m (y_i - \hat{y}_i)^2 \cdot w_i, \\ & w_i = \frac{1}{\text{SD}_i^2}, \end{aligned} \quad (6)$$

where  $w_i$  is the weight assigned to each observation and  $\text{SD}_i$  is the OP analysis variance of each observation.

### 2.5.3 Positive least squares (PLS)

The assumptions for PLS primarily include linearity, independence, and normality. PLS can be applied with weighting if there is heteroscedasticity in the data. PLS extends OLS with the constraint that the regression coefficients must be non-negative. The estimation equation and the error term, PLS, are similar to OLS (without weighting) and WLS (applying weighting). To ensure the positivity of coefficients, a specific condition must be met.

$$\beta_i \geq 0, \forall i \text{ in PM sources} \quad (7)$$

### 2.5.4 Ridge

Shrinkage methods such as Ridge regression try to produce a more interpretable model or reduce error in the presence of collinearity by selecting a subset of the independent variables. Ridge regression is introduced by Hoerl and Kennard (1970), and it incorporates a penalty term that shrinks the coefficients towards 0. Ridge regression minimizes the residual sum of squares plus a penalty term proportional to the sum of squares of the coefficients (L2 regularization) as shown in Eqs. (8) and (9). Consequently, Ridge regression reduces the influence of a  $\text{PM}_{10}$  source that exhibits minimal impact on OP prediction without excluding it from the model.

$$\text{Minimize } \sum_{i=1}^m (y_i - \hat{y}_i)^2 + \lambda \cdot \sum_{j=1}^p \beta_j^2 \quad (8)$$

$$\text{Minimize } \frac{1}{2m} \sum_{i=1}^m w_i (y_i - \hat{y}_i)^2 + \lambda \cdot \sum_{j=1}^p \beta_j^2 \quad (9)$$

Here,  $\lambda$  is the parameter representing the amount of shrinkage; the larger  $\lambda$ , the greater the shrinkage. The hyperparam-

eter tuning was implemented with different values of  $\lambda$  (5, 1, 0.5, 0.1, 0.01, 0.005, 0.001, 0.0005, and 0.0001). The best  $\lambda$  for every site varied from 0.005 to 0.01, and in this study, 0.01 was selected. Ridge can be applied with weighting to account for heteroscedasticity.

### 2.5.5 Least absolute shrinkage and selection operator (Lasso)

Lasso (Tibshirani, 1996) is a shrinkage method that uses a penalty term proportional to the sum of the absolute regression coefficients (L1 regularization). This penalty term shrinks the coefficients of a source with a low impact on OP prediction to 0, effectively removing it from the model. This results in a sparse model that may be easier to interpret and may reduce error on out-of-sample data. However, Lasso is more sensitive to outliers than Ridge regression and is less stable when data are collinear. Lasso can be applied with weighting to account for heteroscedasticity.

$$\text{Minimize } \sum_{i=1}^m (y_i - \hat{y}_i)^2 + \lambda \cdot \sum_{j=1}^p |\beta_j| \quad (10)$$

$$\text{Minimize } \frac{1}{2m} \sum_{i=1}^m w_i (y_i - \hat{y}_i)^2 + \lambda \cdot \sum_{j=1}^p |\beta_j| \quad (11)$$

Similar to Ridge,  $\lambda$  is the parameter representing the amount of shrinkage;  $\lambda$  is selected as 0.01 in this study by running the hyperparameter tuning using the same values as for Ridge.

### 2.5.6 Generalized linear model (GLM)

Generalized linear models, as introduced by McCullagh (1989), provide a framework for regression analysis that can contain non-normal error distributions and capture non-linear relationships between OP activities and  $\text{PM}_{10}$  sources. GLMs allow for error variance that is a function of the predicted value, hence accounting for heteroscedasticity. Key assumptions underlying GLM include (1) independence, (2) the non-normal distribution of OP, and (3) that the relationship between the  $\text{PM}_{10}$  sources and the transformed OP (logarithm in this study) is linear. The mathematical expression for GLM can be represented as follows:

$$\log(\hat{y}) = \beta_0 + \sum_0^p \beta_i \cdot x_i, \quad (12)$$

where  $\beta_0$  denotes the intercept,  $\beta_i$  represents the regression coefficient of source  $i$ , and  $x_i$  is the concentration of source  $i$ .

### 2.5.7 Random forest (RF)

RF, an ensemble learning method introduced by Breiman (2001), combines multiple decision trees to make predictions. In the reference implementation, each tree is grown

on a bootstrap sample of the data, and a random subset of the available features is evaluated at each node to choose the best split. The predictions of all trees are averaged to give the RF final prediction. RF is customizable via hyperparameters such as the number of trees, the size of the bootstrap sample, and the number of features to evaluate at each node. For hyperparameter tuning, 5-fold cross-validation was used on the training data. The training dataset was separated into five parts: four parts were used for training and the remaining part was used for validation. This process was repeated five times, and the hyperparameter value producing the lowest mean RMSE across the five parts was selected. The hyperparameter tuning is shown in Sect. S1.1 in the Supplement.

RF does not assume a specific equation to express the relationship between OP activities and  $\text{PM}_{10}$  sources, with the result that intrinsic OP could not be computed in this regression model. Nevertheless, RF can estimate the relative importance of each  $\text{PM}_{10}$  source in OP prediction. This study estimated the permutation importance of each  $\text{PM}_{10}$  source as the mean increase in the mean squared error of predicted OP when the values of the  $\text{PM}_{10}$  source were permuted.

### 2.5.8 Multilayer perception (MLP)

MLP is an artificial neural network that consists of multiple layers of interconnected nodes or neurons organized in a feedforward structure (Akhtar et al., 2018; Chianese et al., 2018; Bourlard and Wellekens, 1989). These layers include an input layer ( $\text{PM}_{10}$  sources), one layer or several hidden layers, and an output layer ( $\text{OP}_{\text{AA}}$  or  $\text{OP}_{\text{DTT}}$  activities). In MLP, the neurons in the hidden layers are linked to the previous neurons by the connection weight, where every neuron is independent and has a different weight. The output of each neuron depends on its inputs and an activation function, which, if non-linear, allows the model to capture non-linear relationships. The implementation of MLP includes three steps: (1) forward pass to training model – the input is passed to the model, multiplied with an initial weight, bias is added at every layer, and the output of the model is then calculated; (2) error calculation – after applying step 1, the output of the model and the observed data are used to calculate the error; (3) backward pass – the error is propagated back through the network, and the weights are then adjusted to minimize overall error. These three steps are repeated until the error is minimized.

The choice of hyperparameters to ensure the MLP model robustness is processed by hyperparameter tuning using 5-fold cross-validation, as shown in Sect. S1.2. Thanks to hyperparameter tuning, the two hidden layers and a logistic sigmoid activation function were selected in this study to capture the non-linear relationships between OP activities and  $\text{PM}_{10}$  sources.

All regression models were performed using the Python package statsmodels 0.14.0 (Seabold and Perktold, 2010) and scikit-learn 1.3.1 (Pedregosa et al., 2011).

### 2.5.9 Performance of the models

The performance metrics  $R^2$ -square ( $R^2$ ), mean absolute error (MAE), and root mean square error (RMSE) were used to assess the goodness of fit of the models, as described by Kuhn and Johnson (2013).  $R^2$  quantifies the ability of the model to explain the variance in the data.  $R^2=1$  indicates a perfect fit. RMSE represents the aggregation of the individual differences between predicted OP and measured OP, while MAE assesses the average magnitude of errors between them. Lower RMSE and MAE values indicate a better fit, with a perfectly fitting model yielding an RMSE or MAE of 0. Equations (13), (14), and (15), respectively, define  $R^2$ , MAE, RMSE. These indicators are computed for the training and testing data of each sampling iteration and averaged across the 500 sampling iterations.

$$R^2 = 1 - \frac{\text{Sum of Squared Residuals}}{\text{Total Sum of Squares}} = 1 - \frac{\sum_{i=0}^m (y_i - \hat{y}_i)^2}{\sum_{i=0}^m (y_i - \bar{y})^2} \quad (13)$$

$$\text{MAE} = \frac{\sum_{i=0}^m |y_i - \hat{y}_i|}{m} \quad (14)$$

$$\text{RMSE} = \sqrt{\frac{\sum_{i=0}^m (y_i - \hat{y}_i)^2}{m}} \quad (15)$$

## 3 Result and discussion

Assessments of collinearity and homoscedasticity are addressed in Sect. 3.1. Model performance, including key performance metrics and identification of the optimal model, is detailed in Sect. 3.2. Section 3.3 compares the intrinsic OP estimated by the different models. Section 3.4 compares the intrinsic OP between the combined best-fit and reference models. Lastly, Sect. 3.5 proposes recommendations for selecting an appropriate model.

### 3.1 Dataset characteristics

The contributions of identified sources ( $\mu\text{g m}^{-3}$ ) and the  $\text{OP}_{\text{V}}$  activities ( $\text{nmol min}^{-1} \text{m}^{-3}$ ) in each site are presented in Fig. 3, illustrating variations in annual average OP activities and  $\text{PM}_{10}$  source contributions by site. Most sites, including traffic and industrial sites, show higher  $\text{OP}_{\text{DTT}}$  activities than  $\text{OP}_{\text{AA}}$ . Conversely, for the alpine valley sites, CHAM presents higher  $\text{OP}_{\text{AA}}$  than  $\text{OP}_{\text{DTT}}$ , while GRE-fr experiences similar levels of  $\text{OP}_{\text{AA}}$  and  $\text{OP}_{\text{DTT}}$ . Additionally, the average OP activities in every site are not proportional to the average PM concentration. For instance, CHAM and NIC

had lower  $\text{PM}_{10}$  concentrations but higher OP activities than other sites, while TAL showed high  $\text{PM}_{10}$  concentrations but relatively lower OP activities.

The variations observed in the levels of  $\text{PM}_{10}$  and OP across six sites can be attributed to distinctions in the identified sources and their respective contributions. These disparities are contingent upon the unique typologies of each site, which are discussed in Weber et al. (2021). Further, we can observe a significant seasonality in the OP activities (Table S1 in the Supplement). The strong seasonality of OP in alpine valley sites has been addressed in previous studies (Borlaza et al., 2021; Dominutti et al., 2023; Weber et al., 2018, 2021), with thermal inversions during winter increasing pollutant concentrations and OP activities compared with summer. Conversely, OP activities in cold and warm periods in other sites are not significantly different.

The  $\text{PM}_{10}$  sources and their distribution vary among sites (Fig. 3) because of the difference in typology and local activities. For instance, in the industrial site (PdB), two specific sources are identified: shipping emissions (HFO), with an annual mean contribution of  $1.39 \mu\text{g m}^{-3}$ , and industrial sources at  $0.86 \mu\text{g m}^{-3}$ . The urban background site TAL also appears to be influenced by industrial sources ( $2.34 \mu\text{g m}^{-3}$ ), which might, however, be partly due to biases induced by the application of the harmonized receptor model protocol (Weber et al., 2019). Note that the application of a site-specific PMF procedure for this site leads to a much lower contribution of this source category but relatively similar contributions of other sources (Favez, 2017). GRE-fr, an urban background site in an alpine valley, presents significant long-range transport sources, with secondary sulfate contributing  $3.90 \mu\text{g m}^{-3}$  followed by biomass burning at  $2.21 \mu\text{g m}^{-3}$ . As expected, biomass burning is an abundant source in CHAM, accounting for  $7.28 \mu\text{g m}^{-3}$  of the PM contribution, while the traffic sites RBX and NIC displayed high contributions of traffic sources (at  $2.43$  and  $1.45 \mu\text{g m}^{-3}$ , respectively).

The presence of multicollinearity and homoscedasticity was tested to assess the data characteristics of every site. The only site with evidence of collinearity was NIC, where the VIF of the traffic source was equal to 5.0. For all other sites, VIF values are below 5, indicating limited collinearity among sources. This is expected, as the PMF analysis is constrained to avoid collinearity between sources. VIF values for each site can be found in Table S2.

The presence of heteroscedasticity is commonly found when the dependent variable (or OP in this study) exhibits a large difference between the minimum and maximum values or when the error variance varies proportionally with an independent variable ( $\text{PM}_{10}$  sources). The heteroscedasticity was assessed by applying the Goldfeld–Quandt test. Table 2 presents the  $p$  values of the Goldfeld–Quandt test, indicating homoscedasticity of OP prediction when  $p > 0.05$ . This test reveals that heteroscedasticity was detected in CHAM, in GRE-fr, in NIC for  $\text{OP}_{\text{AA}}$ , and in CHAM and TAL for  $\text{OP}_{\text{DTT}}$  (Table 2). We observed a large difference between the cold

**Table 2.** The  $p$  value of the Goldfeld–Quandt heteroscedasticity test.

	PdB	TAL	GRE-fr	CHAM	RBX	NIC
AA	0.15	0.78	$\ll 0.001$	$\ll 0.001$	0.44	0.002
DTT	0.59	$\ll 0.001$	0.189	$\ll 0.001$	0.56	0.91

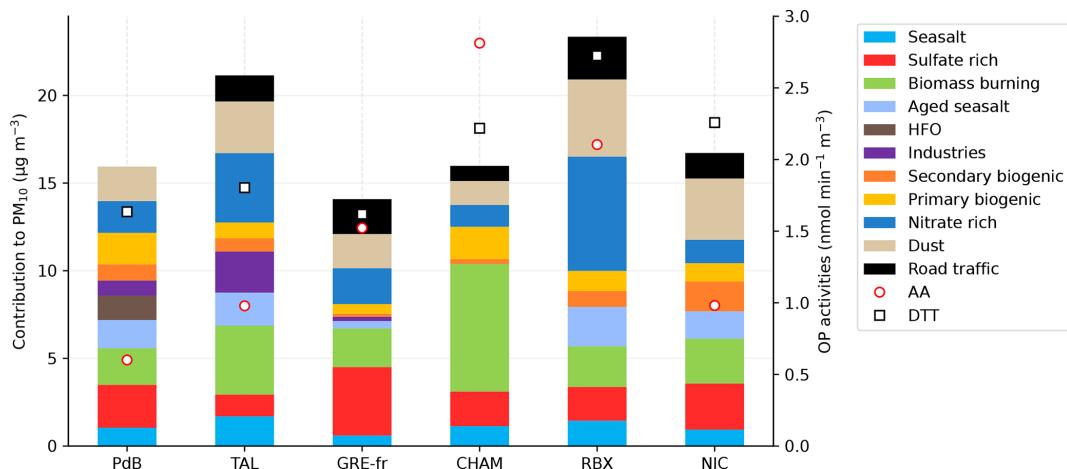
and warm periods for both  $\text{OP}_{\text{AA}}$  and  $\text{OP}_{\text{DTT}}$  in CHAM, similar to what was seen for  $\text{OP}_{\text{AA}}$  in GRE-fr (Table S1), which can be the reason for the presence of heteroscedasticity. For NIC and TAL, there is an insignificant difference between the cold and warm periods, which indicates the presence of heteroscedasticity may be because of the relationship between the  $\text{PM}_{10}$  sources and error variance. When heteroscedasticity is detected, unweighted regression for OP prediction according to the source may not accurately reflect the uncertainty in the intrinsic OP of each source. The scatterplots representing the relationship between the regression analysis residuals and the fitted values (for observed OP) are available in Figs. S1 and S2 in the Supplement.

### 3.2 Performance of regression models

The 11 regression models, with or without the weighting for some of them, were tested by comparing their performance metrics between the measured and reconstructed OPs. For each run ( $n = 500$  iterations), the  $R^2$ , RMSE, and MAE were computed for the testing and training dataset, resulting in 500 values for each performance metric. Figure 4 presents the mean  $R^2$  values of the training datasets as well as the mean and the standard deviation of the testing datasets of the  $\text{OP}_{\text{AA}}$  models across the 500 sampling iterations, and Fig. 5 presents the mean RMSE and MAE. The same result pattern was found for  $\text{OP}_{\text{DTT}}$ , as presented in Tables S3, S4, S5. The WLS, wPLS, wRidge, and wLasso models incorporated weighting, while the OLS, PLS, Ridge, Lasso, GLM, RF, and MLP models were unweighted.

OP predictions across all sites are statistically validated, with testing  $R^2$  values in RBX, NIC, PdB, TAL, CHAM, and GRE-fr observed to be 0.66, 0.76, 0.76, 0.78, 0.87, and 0.90, respectively. The lowest mean test set RMSE values are 0.70, 0.28, 0.21, 0.37, 0.70, and  $0.31 \text{ nmol min}^{-1} \text{ m}^{-3}$ , respectively, for the same sites. The lowest mean test set MAE values are 0.49, 0.23, 0.14, 0.25, 0.45, and  $0.21 \text{ nmol min}^{-1} \text{ m}^{-3}$ , respectively. Notably, the GLM model exhibits the lowest  $R^2$  values and the highest RMSE for all sites (Tables S3–S5). These results strongly suggest that the relationship between  $\text{OP}_{\text{AA}}$  and  $\text{PM}_{10}$  sources is not log-linear.

Differences in MAE, RMSE, and  $R^2$  between the training and testing database for RF and MLP are significant across the sites. Notably, RF displays a large difference in  $R^2$ , with a gap of up to 0.6 in RBX ( $R^2$  training: 0.92;  $R^2$  testing: 0.27). Similar gaps were found in RMSE and MAE. RF con-



**Figure 3.** The contribution of sources to  $\text{PM}_{10}$  and the OP activities in six sites. The left y axis and bar show the contribution of PM sources in  $\mu\text{g m}^{-3}$ . The right y axis, circles, and squares show the mean  $\text{OP}_v$  activities in  $\text{nmol min}^{-1} \text{m}^{-3}$ , with the red circle indicating  $\text{OP}_{\text{AA}}$  and the black square indicating  $\text{OP}_{\text{DTT}}$ .

sistently performed best on the training set, characterized by the highest  $R^2$  and the lowest MAE and RMSE values, but had lower test set  $R^2$  values than the other models (except GLM). Conversely, MLP exhibited training  $R^2$  values comparable to other models but lower test  $R^2$  values. These findings suggest overfitting: the flexible algorithms identify relationships in the training data that do not generalize to the testing data. This observation may be attributed to the limitations of data coverage, possibly failing to fully represent the underlying relationships, leading to poor performance in the testing datasets (Matsuki et al., 2016; Benkendorf and Hawkins, 2020; Stockwell and Peterson, 2002; Wisz et al., 2008; Hernandez et al., 2006; Hawkins, 2004; Raudys and Jain, 1991). Pearce and Ferrier (2000) recommended that the minimum number of samples for robust performance should be over 250 for GLM model, while Raudys and Jain (1991) showed that the minimum number of samples is based on the complexity of the model and the number of predictors. Additionally, Harrell (2016) suggested that the number of predictors (PM sources) should be below the number of samples divided by 15, a threshold not reached in this analysis. For example, in NIC, the minimum number of samples should be 135 for the training set ( $9 \text{ PM sources} \times 15$ ), while in total, we have only 107 samples. Therefore, we can also recommend that, for optimal performance of RF and MLP, the number of samples and PM sources should satisfy these thresholds.

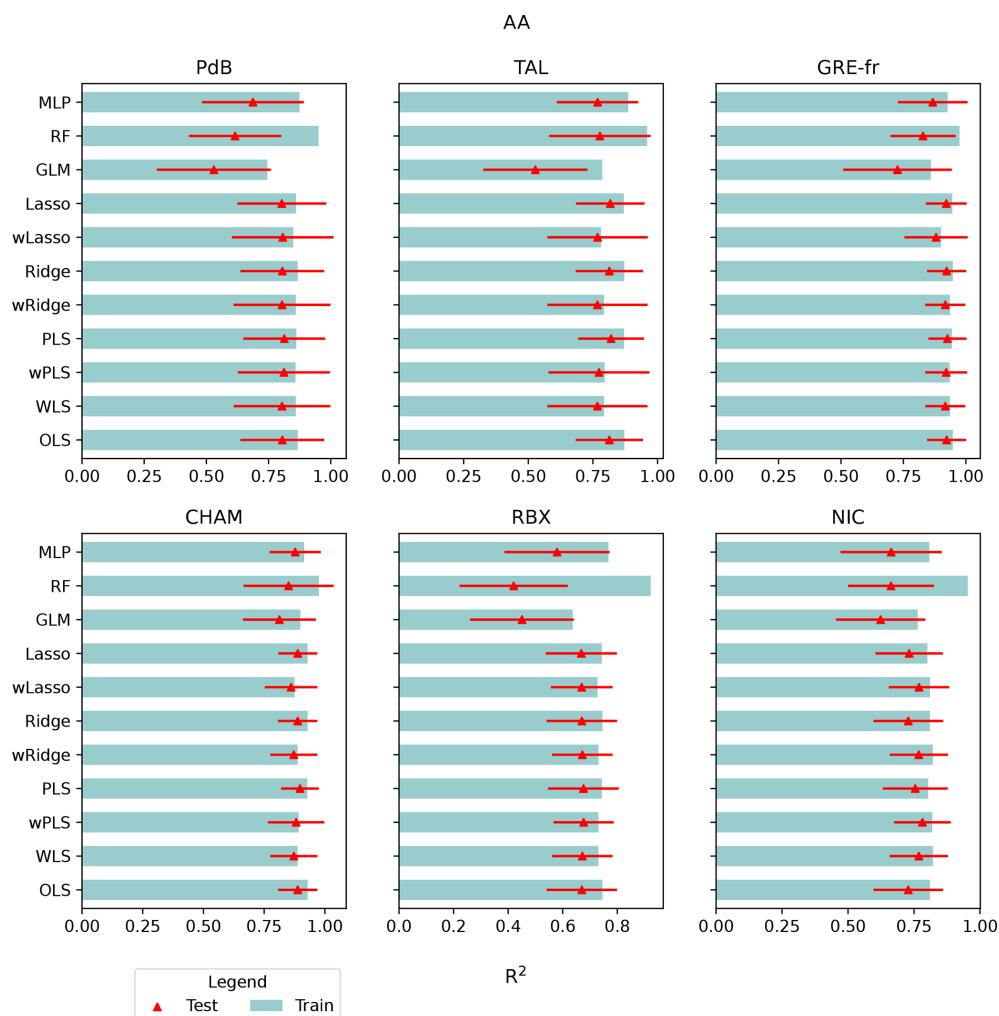
The WLS, OLS, wPLs, wRidge, and wLasso models show more robust performances with fewer differences between the training and testing data. At most sites, there is very little difference between the  $R^2$ , RMSE, and MAE of OLS and Ridge, with or without weighting, and often between PLS and Lasso as well. This consistency is observed even in the collinearity case of NIC, where  $\text{VIF}=5$ . The difference between these models is a maximum of 0.06 in  $R^2$ , 0.01 in

MAE, and 0.1 in RMSE, indicating that these models work well for OP prediction. Nevertheless, it is worth noting that every model exhibits different assumptions that have to be respected. The assumption violations may lead to unreliable regression coefficients (intrinsic OP) even though the prediction is good (Williams et al., 2013; Cohen et al., 2002).

The best model for each site was selected based on both data characteristics (collinearity and heteroscedasticity) and testing data performance. For sites with collinearity, Ridge and Lasso were considered the most appropriate. For sites with heteroscedasticity, models with weights were considered the most appropriate. For sites with neither collinearity nor heteroscedasticity, OLS and PLS were considered the most appropriate. Tables 3 and 4 present the best  $\text{OP}_{\text{AA}}$  and  $\text{OP}_{\text{DTT}}$  prediction models for each site. It follows that the best model is not necessarily the same one for both series of OP for a given site. As a rule, the model that exhibits the best performance metrics (the best model by error in Table 3 for  $\text{OP}_{\text{AA}}$  and Table 4 for  $\text{OP}_{\text{DTT}}$ ) is suited to be the best model chosen by data characteristics; therefore, choosing a model according to data characteristics help to obtain more reliable OP predictions.

### 3.3 Effect of the choice of a model on intrinsic OP

It is particularly important to try to define the best way of calculating the more accurate intrinsic OP of PM sources and the contribution of sources to OP, since these values are fundamental inputs in all the works of large-scale modeling of OP with chemical transport models (CTM) (Daellenbach et al., 2020; Vida et al., 2024). Figures 6 and 7 show the variations in intrinsic OP for all the models, focusing on the results of NIC as an example. The evaluation of the five other sites is presented in Figs. S3–S7 for  $\text{OP}_{\text{AA}}$  and Figs. S8–S12 for  $\text{OP}_{\text{DTT}}$ . The differences in equations, error term minimiza-



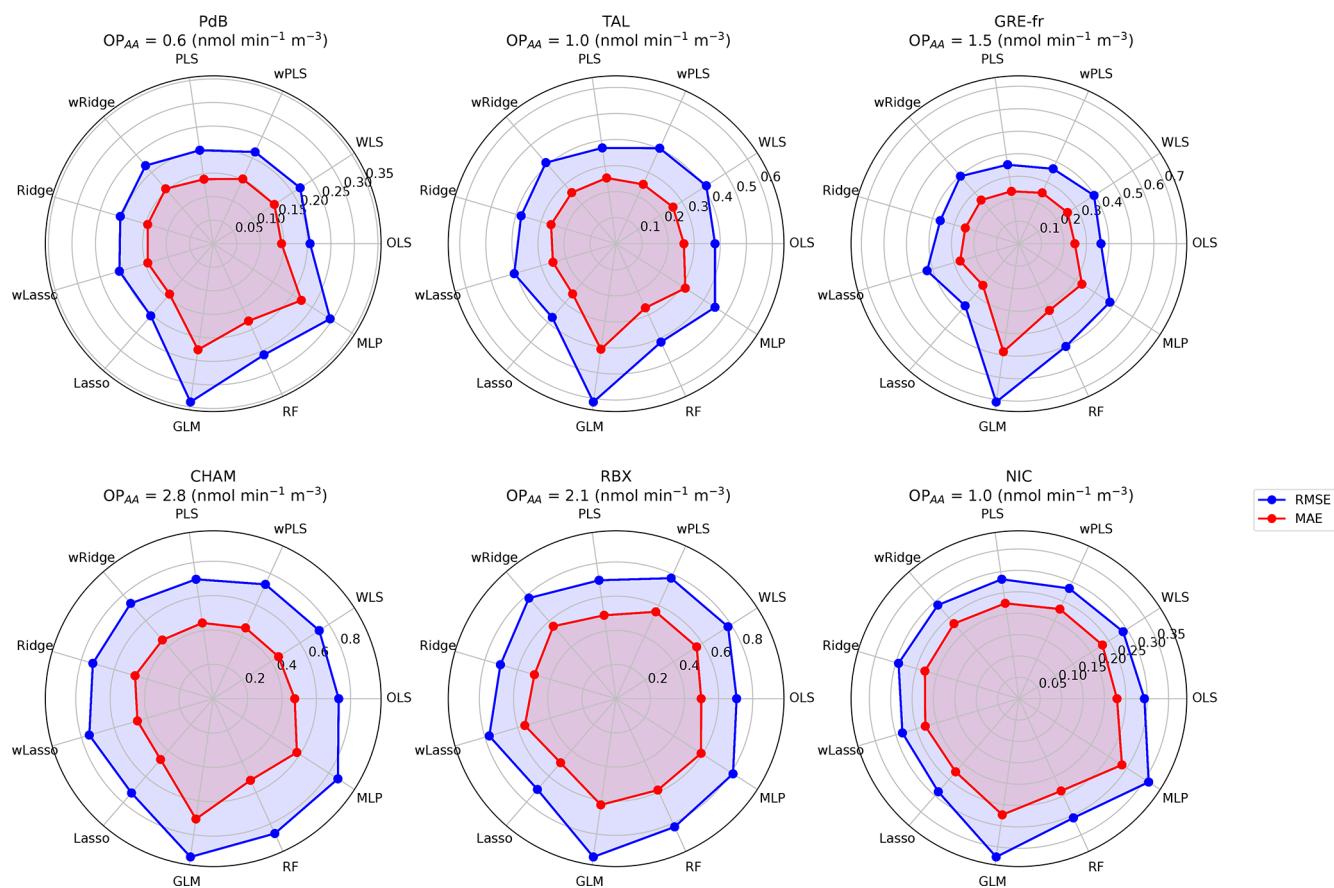
**Figure 4.** The  $R^2$  values of 11 OPAA models in six sites. The mean  $R^2$  of the training data is shown by the blue bars, the mean  $R^2$  of the testing data is shown by the red triangles, and the standard deviation of the  $R^2$  of the testing data is shown by the red bars. The y axis represents the models, and the x axis denotes the  $R^2$  values.

**Table 3.** Criteria for selection of the best model for OPAA.

	PdB	TAL	GRE-fr	CHAM	RBX	NIC
Collinearity	No	No	No	No	No	Yes
Heteroscedasticity	No	No	Yes	Yes	No	Yes
Best model by characteristic	OLS/PLS	OLS/PLS	WLS/wPLS	WLS/wPLS	OLS/ PLS	wRidge/wLasso
Best model by error	PLS	PLS	wPLS	wPLS	OLS	wRidge

tions, and assumptions can explain the differences in intrinsic OP per  $\mu\text{g}$  of source among the eight regression models. While the  $R^2$ , RMSE, and MAE values are similar among models (except for GLM, RF, and MLP), the intrinsic OP values significantly differ between the models with and without weighting and between the linear and non-linear regression

models. The average intrinsic OP of 500 iterations is discussed in this section, since these values are generally used to calculate the contribution of the  $\text{PM}_{10}$  source to OP in prior studies (Borlaza et al., 2021; Dominutti et al., 2023; Weber et al., 2018). The mean and standard deviation of intrinsic



**Figure 5.** The MAE and RMSE of 11 OP<sub>AA</sub> models in every site for the testing data. Blue and red lines represent the RMSE and the MAE, respectively. The values in the figure are the mean of the RMSE and MAE of 500 iterations.

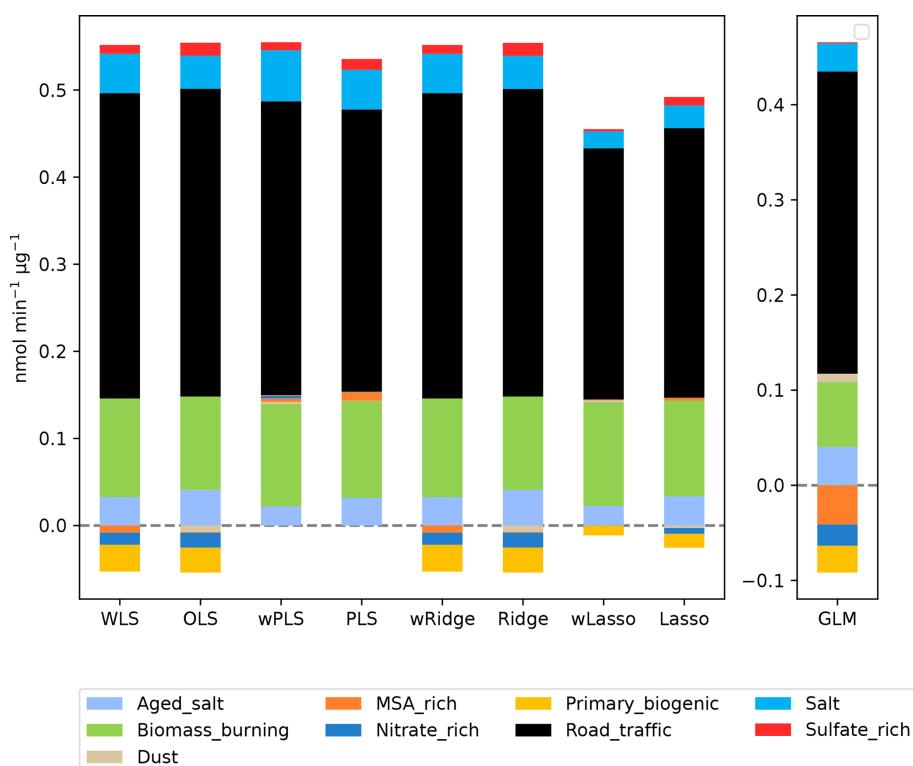
**Table 4.** Criteria for selection of the best model for OP<sub>DTT</sub>.

	PdB	TAL	GRE-fr	CHAM	RBX	NIC
Collinearity	No	No	No	No	No	Yes
Heteroscedasticity	No	Yes	No	Yes	No	No
Best model by characteristic	OLS/PLS	WLS/wPLS	OLS/PLS	WLS/wPLS	OLS/PLS	Ridge/Lasso
Best model by error	OLS	wPLS	PLS	wPLS	PLS	Ridge

OP<sub>AA</sub> and OP<sub>DTT</sub> for the six sites are shown in Tables S6 and S7, respectively.

The intrinsic OP<sub>AA</sub> of PM<sub>10</sub> sources at NIC is the same between WLS and wRidge and between the OLS and Ridge, revealing that the moderate collinearity of the road traffic source did not affect the estimated intrinsic OP<sub>AA</sub>. PLS sets the intrinsic OP<sub>AA</sub> of some sources to 0, therefore producing slightly different results. Lasso regression sets the intrinsic OP<sub>AA</sub> of some sources to 0 and shrinks the estimates for all other sources toward 0. GLM produces intrinsic OP<sub>AA</sub> values that represent a multiplicative change on the log scale,

and thus they are not directly comparable to the other models. However, the direction and importance of the sources are similar to the other models. Whatever the model, road traffic appears as the source with the highest intrinsic OP<sub>AA</sub>, followed by biomass burning, aged salt, salt, and sulfate-rich sources, in NIC. Traffic and biomass burning sources have been similarly recognized as significant contributors to OP<sub>AA</sub> in prior studies (Borlaza et al., 2021; Dominutti et al., 2023; Stevanović et al., 2023). The intrinsic OP of the dominant sources is stable, indicating that all these models could give the same information about the intrinsic OP of the



**Figure 6.** Intrinsic OP<sub>AA</sub> values of the different PM<sub>10</sub> sources at Nice obtained with the different models.

main sources. Conversely, the differences are larger between models for the sources with small to very small intrinsic OP (MSA-rich, primary biogenic, nitrate-rich, and dust sources), whose intrinsic OP varies from positive to negative among models.

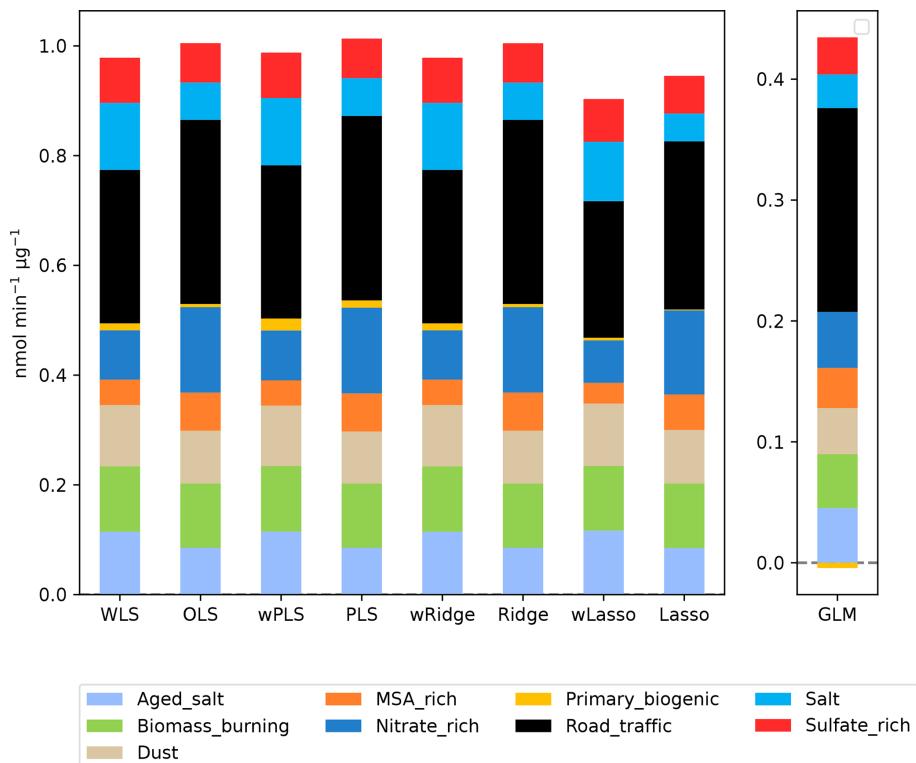
The OP<sub>DTT</sub> intrinsic values in NIC (Fig. 7) display minimal variation among the WLS and wPLS. This consistency is linked to the absence of negative intrinsic values. On the other hand, even though there is the presence of moderate collinearity, wRidge still has the same result as WLS and wPLS. In line with the OP<sub>AA</sub> results, the wLasso and GLM models exhibit distinct responses compared with the other models. The intrinsic OP<sub>DTT</sub> of all sources varies depending on the presence or absence of weighting. While the WLS models tend to amplify the influence of some sources (aged sea salt, primary biogenic, sea salt, and sulfate-rich sources), the OLS reduces the intrinsic OP<sub>DTT</sub> of these sources. Conversely, MSA-rich, nitrate, and road traffic sources undergo less influence in WLS but more influence in OLS. Different from OP<sub>AA</sub>, OP<sub>DTT</sub> prediction shows more variation among models, highlighting the effect of choosing a model on evaluating the intrinsic OP<sub>DTT</sub> of PM<sub>10</sub> sources.

The comparison of intrinsic OP among regression models in NIC demonstrated that OP<sub>DTT</sub> and OP<sub>AA</sub> intrinsic values exhibit variation across different models with and without weighting, illustrating that the choice of the model significantly influences the values obtained for intrinsic OP of

PM<sub>10</sub> sources (a similar pattern is observed for all other sites and shown in Figs. S3–S7 for OP<sub>AA</sub> and Figs. S8–S12 for OP<sub>DTT</sub>). Because of the difference in intrinsic OP across models, a comparison between the best-performing and most commonly used models (OLS) is presented in the following section to elucidate the advantage of choosing a model based on data characteristics (Sect. 3.4).

### 3.4 Comparisons between the best site-specific model and OLS

In this section, the intrinsic OP of the best model is selected for each site as discussed in Sect. 3.2, and the intrinsic values of each source are compared with the ones returned by the OLS model. The OLS model is used as a representative of usual practices that do not consider the database characteristics (Williams et al., 2013). The average intrinsic OP value of each PM<sub>10</sub> source is calculated from all 500 bootstrapping iterations for all sites where that particular source is identified. Intrinsic OP values obtained in this way from the best model (the best model presented in Table 3 for OP<sub>AA</sub> and Table 4 for OP<sub>DTT</sub>) encompassing all six sites are called “the intrinsic OP of the best model”, and the intrinsic OP values derived from the OLS from all six sites are called the “intrinsic OP of the reference model”.



**Figure 7.** Variations in the intrinsic OPDTT of the different PM<sub>10</sub> sources at Nice obtained with the different models.

A meaningful comparison of the two series of intrinsic values requires two conditions. First, intrinsic OP should be consistent across all sites. While recognizing that intrinsic OP values depend on diverse factors, we assumed the sites share fairly uniform PM<sub>10</sub> chemical source profiles in France. This is demonstrated by evaluating the Pearson distance and standardized identity distance similarity indicators of the source chemical profiles (Belis et al., 2015; Weber et al., 2019), and Fig. S13 indicates consistent profiles of sources for the six sites. Consequently, we could expect to observe minimal divergence in intrinsic OP values among these sites. Second, we postulate that negative intrinsic OP values are possible since previous studies have reported that total PM<sub>10</sub> intrinsic OP can be modulated due to the synergistic/antagonistic effects involving, for example, soluble copper, quinones, and bacteria (Borlaza et al., 2021; Pietrogrande et al., 2022; Samake et al., 2017; S. Wang et al., 2018; Xiong et al., 2017). Samake et al. (2017) demonstrated that the presence of bacterial cells in aerosol decreases the redox activity of Cu and 1,4-naphthoquinone, with a maximum decrease of 60 % compared with the oxidative reactivity considered individually. Pietrogrande et al. (2022) indicated that the mixture of Cu, Fe, 9,10-phenanthrene quinone, and 1,2-naphthoquinone reduces the rate consumption of AA and DTT by up to 50 % depending on the quantity of each chemical. Wang et al. (2018) reported that the mixing of Cu, naphthalene secondary organic aerosol (SOA), and phenanthrene

SOA only achieved half of the DTT rate consumption compared with the separately considered consumption. Xiong et al. (2017) showed the presence of antagonists in the interaction of Fe and quinones; nevertheless, it was much lower than those in the other studies (under 10 %). These references reported that the antagonistic effects of a mixture can significantly reduce the consumption rate of OP<sub>DTT</sub> and OP<sub>AA</sub>, and this impact varies widely from 10 % to 60 % depending on the type of chemical species and the quantity of each species in the mixture. Consequently, we consider here that the intrinsic OP value of an individual site for a given source could be negative only within a range of at most 60 % of the mean combined intrinsic OP value of this source across all sites. Negative intrinsic OP exceeding this criterion may result from the mathematical construction of the model. The comparison between the intrinsic OP<sub>AA</sub> of the best model and the reference model is presented in Sect. 3.4.1 and that of OP<sub>DTT</sub> is shown in Sect. 3.4.2.

### 3.4.1 OP<sub>AA</sub> activities

The results of the comparison of OP<sub>AA</sub> intrinsic values (Fig. 8 and Table S8) show that the anthropogenic sources have the highest intrinsic OP values in both the best model and the reference model. Among these sources, road traffic appears as the most prominent potent fraction, followed by biomass burning, HFO, and industrial sources. These results

are aligned with prior research (Calas et al., 2019; Daellenbach et al., 2020; Dominutti et al., 2023; Fadel et al., 2023; Fang et al., 2016; in't Veld et al., 2023; Weber et al., 2018; Zhang et al., 2020) which has highlighted the sensitivity of OP<sub>AA</sub> to concentrations of metals, black carbon, and organic carbon. The differences between the best model and the reference model were insignificant for these sources, demonstrating that the best model and the reference model consistently captured similar patterns for the most critical sources of OP activities.

However, the interquartile ranges (IQR) of the intrinsic OP values are consistently narrower for the best model across all sources, accounting for less divergence in intrinsic OP values across sites. Moreover, the median intrinsic OP values obtained from the best model closely approximated the mean values, indicating the absence of extreme intrinsic OP values. For instance, in the case of road traffic, the mean and median values were 0.24 and 0.23 nmol min<sup>-1</sup> µg<sup>-1</sup>, respectively. Conversely, the reference model exhibited a large difference between the mean and median values, implying lower consistency across sites and sampling iterations. The same result was observed in biomass burning source, in which the median and mean intrinsic OP in the best model had fewer discrepancies. Further, the biomass burning intrinsic OP in GRE-fr of the best model is more consistent with those in other sites (best: 0.30 nmol min<sup>-1</sup> µg<sup>-1</sup>; reference: 0.35 nmol min<sup>-1</sup> µg<sup>-1</sup>).

When considering sources with low intrinsic OP, the variability can be larger between the two methods. As an example, for the sulfate-rich sources, the median intrinsic OP values were positive (0.002 nmol min<sup>-1</sup> µg<sup>-1</sup>), while the mean intrinsic OP values were negative ( $-0.008 \text{ nmol min}^{-1} \mu\text{g}^{-1}$ ). The mean intrinsic OP in the best model exhibited fewer negative values in individual sites than in the reference model (for aged salt, salt, primary biogenic, MSA-rich, sulfate-rich, and nitrate-rich sources). In addition, the best model showed the least disparate intrinsic OP among individual sites, for instance, the aged salt sources in GRE-fr and the primary biogenic and salt sources in CHAM. Furthermore, the best model displayed an intrinsic OP meaningful in terms of geochemical validation, which was shown in the salt, primary biogenic, and sulfate-rich sources. For instance, in the reference model, the average intrinsic OP of the primary biogenic source in NIC ( $-0.03 \text{ nmol min}^{-1} \mu\text{g}^{-1}$ ), the intrinsic OP of salt in GRE-ft ( $-0.07 \text{ nmol min}^{-1} \mu\text{g}^{-1}$ ), and the sulfate-rich source in CHAM ( $-0.05 \text{ nmol min}^{-1} \mu\text{g}^{-1}$ ) represented a 100 % reduction compared with the mean intrinsic OP of all sites. Moreover, negative intrinsic OP was observed in NIC (primary biogenic), and some extreme values were observed in GRE-fr (aged salt, salt) and CHAM (salt, primary biogenic, MSA-rich; where heteroscedasticity was presented) in the OLS model, which underscores that the model assumptions on data characteristics proving false could impact the accu-

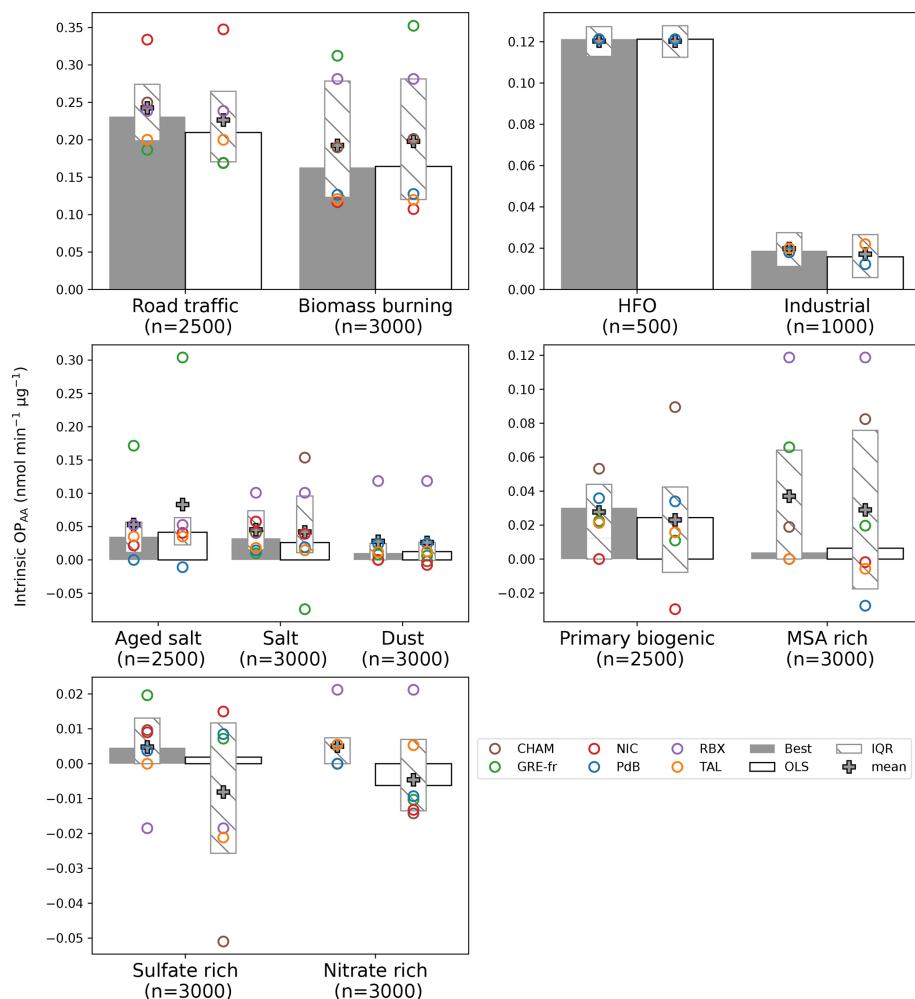
racy of OP prediction. Consequently, these results highlight the advantage of considering the data in the model selection.

The detailed comparison of intrinsic OP<sub>AA</sub> between the best model and the reference model is categorized into four groups and discussed in detail in Sect. S9. These groups include (1) anthropogenic sources without nitrate and sulfate (road traffic, biomass burning, HFO, and industrial sources); (2) natural inorganic sources (aged sea salt, sea salt, dust); (3) biogenic sources (primary biogenic and MSA-rich sources); and (4) nitrate and sulfate-rich sources.

### 3.4.2 OP<sub>DTT</sub> activities

Similar to OP<sub>AA</sub>, for OP<sub>DTT</sub> the IQR of the best model is narrower for most of the sources than the IQR of the reference model (OLS). Except for road traffic, industrial, and MSA-rich sources, the IQR is slightly higher in the best model (Fig. 9 and Table S9). In the two models, the mean intrinsic OP is essentially unchanged, where traffic is the most critical source ( $0.27 \pm 0.10$ ) followed by HFO ( $0.18 \pm 0.01$ ), biomass burning ( $0.12 \pm 0.03$ ), dust ( $0.12 \pm 0.07$ ), primary biogenic (best:  $0.10 \pm 0.06$ ; reference:  $0.12 \pm 0.08$ ) and MSA-rich sources (best:  $0.11 \pm 0.09$ ; reference:  $0.09 \pm 0.09$ ). The minimum difference between the two models in the dominant sources again confirms the conclusion in the OP<sub>AA</sub> comparison, demonstrating the similar pattern of the best model and the reference model in the most crucial sources of OP. For both the best and the reference models, OP<sub>DTT</sub> activities showed sensitivity to more sources compared with OP<sub>AA</sub>, as discussed in previous studies (Borlaza et al., 2021; Calas et al., 2019; Dominutti et al., 2023; Fadel et al., 2023).

While the best model and reference model give the same mean intrinsic OP<sub>DTT</sub> for all sites, the mean OP<sub>DTT</sub> at each individual site can vary substantially between the two models. The best model exhibited the positive intrinsic OP for all sources, while the reference model displayed negative intrinsic OP in RBX (MSA-rich and sulfate-rich sources). Especially in the case of sulfate-rich sources in RBX, the negative intrinsic OP in the reference model passed the threshold of the negative value, which presented a 110 % reduction compared to the mean intrinsic OP of all sites. This is also found in the OP<sub>AA</sub> comparison, which confirmed that the best model generates a geochemical meaningful intrinsic OP. In addition, the best model exhibited consistent intrinsic OP across sites, especially for the dust, salt, primary biogenic, and sulfate-rich sources in TAL (heteroscedasticity is presented in this site), where intrinsic OP in TAL in the best model is more similar to the other sites. For instance, the reference model showed that the intrinsic OP in TAL is  $0.20 \text{ nmol min}^{-1} \mu\text{g}^{-1}$ , far from the mean of all sites ( $0.07 \text{ nmol min}^{-1} \mu\text{g}^{-1}$ ). We observed the same for the intrinsic OP of the nitrate-rich source in CHAM (where the heteroscedasticity is detected), which displayed a less dissimilar OP in CHAM compared with the other site in the best



**Figure 8.** Intrinsic OP<sub>AA</sub> estimated by the best model and the reference method in the six sites. The y axis represents the intrinsic OP values in nmol min<sup>-1</sup> µg<sup>-1</sup>, and the x axis represents the sources. The gray bars are the median intrinsic OP values of the best models in the six sites ( $n = 500$  bootstrapping  $\times$  number of sites where the given source is detected) for each source. The white bars are the same median intrinsic OP values for the reference (OLS) model. The gray plus symbol represents the mean of intrinsic OP values. The hatched bars are the interquartile ranges of the intrinsic OP values. The dots represent the mean intrinsic OP of all sites, including gray – Chamonix, green – Grenoble, red – Nice, blue – Port-de-Bouc, purple – Roubaix, and orange – Talence.

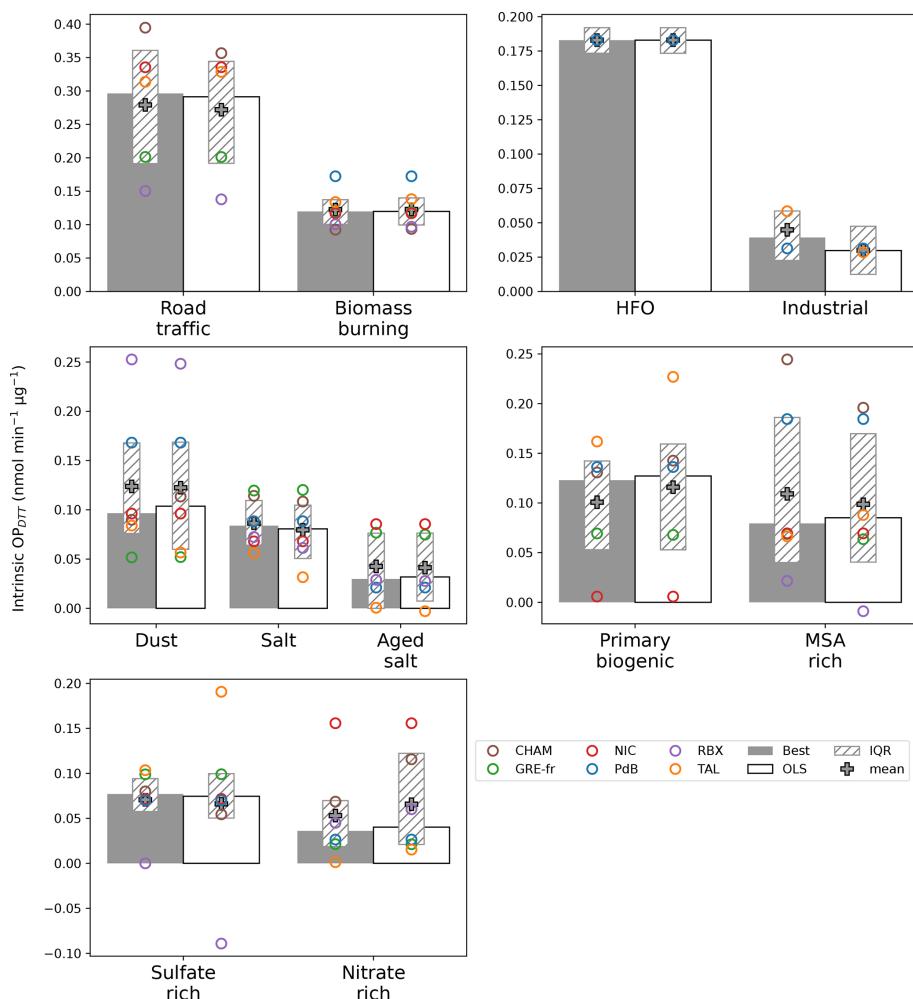
model. This again validates the conclusion in the OP<sub>AA</sub> comparison, demonstrating that respecting the model assumption is essential for obtaining a robust OP SA result.

The comparison of intrinsic OP between the best model and the reference model highlights the importance of considering the database characteristics when selecting a model for OP SA. For all the datasets studied here, using the best model for each site delivered more robust results, with reduced uncertainty and reduced differences in intrinsic OP across sites, and it provided a more geochemically meaningful intrinsic OP. The recommendation for selecting a model based on the characteristics of the database is presented in Sect. 3.5.

### 3.5 Guidelines for the selection of a regression model for OP SA

Our results have highlighted the benefits of choosing a model that matches the characteristics of the data to improve the robustness of the OP SA method. For this reason, this section develops a workflow to help make model selection decisions. Before selecting a regression for OP SA, the first question is whether the PM<sub>10</sub> sources are collinear and the second is whether the residual variance of the regression between OP and PM<sub>10</sub> mass is constant. These two questions represent the characteristics of PM<sub>10</sub> sources and OP activities, which vary according to the study site.

For data exhibiting collinearity between sources and generating a residual variance that varies according to the value of the PM<sub>10</sub> sources, weighted regularization regression can



**Figure 9.** Intrinsic OP<sub>DTT</sub> estimated by the best model and the reference model in the six sites. The y axis represents the intrinsic OP values in nmol min<sup>-1</sup> µg<sup>-1</sup>, and the x axis represents the sources. The gray bars are the median intrinsic OP values of the best models in the six sites ( $n = 500$  bootstrapping  $\times$  number of sites where the given source is detected) for each source. The white bars are the same median intrinsic OP values for the reference (OLS) model. The gray plus symbol represents the mean of intrinsic OP values. The hatched bars are the interquartile ranges of the intrinsic OP values. The dots represent the mean intrinsic OP of all sites, including gray – Chamonix, green – Grenoble, red – Nice, blue – Port-de-Bouc, purple – Roubaix, and orange – Talence.

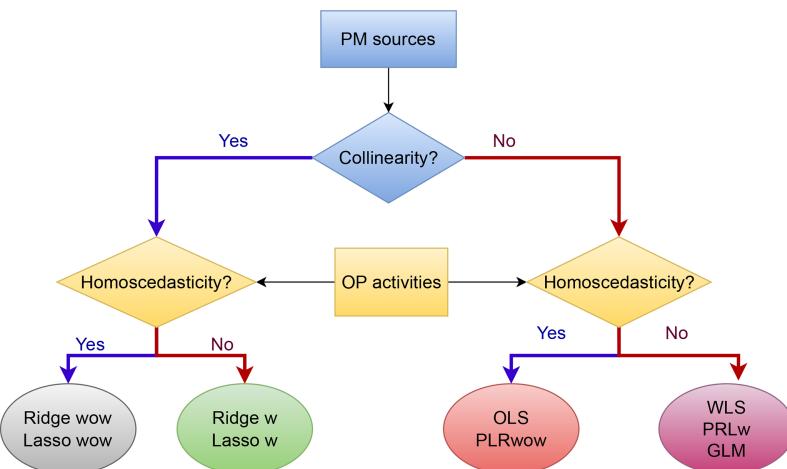
help to reduce collinearity and to match the model assumption about the residual. On the other hand, unweighted Ridge and Lasso are introduced for data showing collinearity and homoscedasticity. Additionally, data with no collinearity are suitable for OLS and unweighted PLS in the case of homoscedasticity, while WLS and weighted PLS are used for data with heteroscedasticity.

If the number of predictors (PM<sub>10</sub> sources) is below the number of samples divided by 15, RF and MLP can also be employed to capture possible non-linear relationships between the OP and PM<sub>10</sub> sources. However, cross-validation must be used to ensure that there is no overfitting. In addition, these models do not estimate intrinsic OP (nmol min<sup>-1</sup> µg<sup>-1</sup>) but only the importance of each PM<sub>10</sub> source to the OP prediction. This is a major drawback, since

the intrinsic OP of sources is a prerequisite for the modeling effort of OP with CTM. However, RF and MLP could be useful for OP prediction in the case of larger datasets generated by online instruments.

For each data characteristic there is more than one model that is suitable. Out-of-sample performance metrics should be employed to identify the most accurate of these models.

Finally, these techniques of OP apportionment could not be performed well with uncertain PMF-derived sources. The PMF results sometimes do not adequately represent PM mass concentration for several reasons, such as the lack of a trace species to identify a source, an insufficient sample size, the source contribution being too small to be identified (under 1 %), or collinearity issues. Important information could be missed because of these problems in PMF implementation,



**Figure 10.** Workflow in model selection considering the data characteristics.

which is explained by the model's low accuracy. Our study did not encounter this problem, since the PMF is harmonized and performed according to European recommendations which could perform the regression technique well and make it possible to obtain a very satisfactory successive OP modeled in comparison with observations after regression techniques ( $R^2$  from 0.7 to 0.9). However, this problem could potentially happen, and for these cases, we could recommend either subtracting the total source contribution from the PM mass concentration to get the part that PMF cannot simulate. The information in this part may contain vital sources. Alternatively, it is possible to re-execute the PMF to validate the result and ensure the robustness of the chemical profile and the contribution of sources.

Limitations and perspectives of the study:

- This study compares eight regression models but is not exhaustive; further research could add more regression techniques to evaluate result variations across models. The potential techniques that could be applied for OP SA are gradient boosting techniques for resolving regression models or supervised machine learning techniques which enable the investigation of linear and non-linear regression relationships. However, the consistently strong performance of ordinary linear regression across six locations in France suggests that there may be little to gain from applying more complex models in areas with similar  $\text{PM}_{10}$  sources.
- PMF coupled with a regression model remains a popular approach for OP SA. Notably, the uncertainties in PMF are typically addressed in chemical profiles but not in contributions. Incorporating uncertainty from variations in contributions into models could enhance their robustness compared with relying only on absolute PMF results.

- Observations ranged between 100 and 200 samples at each site, which may be insufficient to obtain a fair performance of GLM, decision tree, and neural network models, even though this number of samples is sufficient to address SA through the PMF model for offline analyses. Therefore, this study outlines well the limitations of GLM, RF, and MLP for offline datasets. Future investigations should be performed in an extended dataset, such as long-term or real-time measurement data, to investigate the performance of machine learning algorithms.
- This study only focused on the two most popular OP assays of  $\text{PM}_{10}$  (OP<sub>DTT</sub> and OP<sub>AA</sub>). However, there are various OP assays available, such as OP<sub>DCFH</sub>, OP<sub>OH</sub>, OP<sub>FOX</sub>, OP<sub>GSH</sub> and OP<sub>ESR</sub>, and different sizes of PM ( $\text{PM}_1$ ,  $\text{PM}_{2.5}$ ,  $\text{PM}_5$ ). Further research should include more OP assays, which can be helpful in evaluating the performance of various regression models for different OP and different PM sizes.
- This study used the analytical uncertainty as the weighting for the weighted model. However, the weighting can be selected based on different ways, as reported by Montgomery et al. (2012): (1) prior information from the theoretical model, (2) using the residual extracted from the OLS model, (3) selecting the weighting based on the uncertainty of the instrument if the dependent variable is measured by a different method, and (4) selecting the weighting based on the error of these observations if the dependent variable is the average of different observations.

#### 4 Conclusion

The results of the OP SA marked an important milestone as they were revealed for the first time through the use of eight

regression models, including OLS, WLS, PLS, GLM, Ridge, Lasso, RF, and MLP. This in-depth analysis was carried out on a complete set of data collected from six sites with different characteristics. The approach of selecting a suitable model for each site based on specific data characteristics resulted in a more consistent intrinsic OP across sites, in stark contrast to the variation observed when using the basic OLS model. The revelations of the study have provided concrete recommendations for the judicious selection of an appropriate regression model based on the unique characteristics of the dataset. These guidelines should help to improve the accuracy of OP assessments and contribute to the refinement of air quality assessment methods. In addition, the implications of this research extend to the implementation of OP monitoring as a new measure of air quality, particularly on European supersites. As this initiative aligns with the ongoing revision process of European Directive 2008/50/CE, the findings of the study assume a pivotal role in shaping the methodologies underpinning air quality assessments on a broader regulatory level.

**Code availability.** The code is available at <https://doi.org/10.5281/zenodo.11071884> (Ngoc Thuy, 2024).

**Data availability.** The datasets could be made available upon request by contacting the corresponding author.

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**Author contributions.** VDNT performed the data analysis for the OP source apportionment setup. GU and JLJ carried out the mentoring, supervision, and validation of the methodology and results. IH, PAD, and VDNT worked on the result visualization. OF, JLJ, and GU acquired funding for the original PM sampling and analysis. VDNT wrote the original draft. All authors reviewed and edited the manuscript.

**Competing interests.** The contact author has declared that none of the authors has any competing interests.

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# Chapter 3: Integration of PMF Results with Policy Development

Some authors

## ! Chapter Summary

This chapter bridges the gap between scientific research and practical application by exploring the integration of PMF source apportionment results into air quality policy development. Through illustrative case studies from various European urban environments, it demonstrates how robust PMF findings can inform targeted and effective pollution control strategies. The chapter also proposes a structured framework for translating complex scientific outputs into actionable policy recommendations, considering aspects such as cost-benefit analysis, stakeholder engagement, and realistic implementation timelines for proposed interventions.

Under review at Environmental Science & Policy

## 3.1 Abstract

This chapter examines how PMF source apportionment results can be effectively integrated into air quality policy development. We present case studies from multiple European cities and develop a framework for translating scientific findings into actionable policy recommendations.

## 3.2 Methods

### 3.2.1 Policy Impact Framework

TABLE 3.1: Framework for evaluating source-specific interventions

Source	Contribution (%)	Control Options	Implementation Cost	Health Impact	Stakeholder Support
Traffic	35	LEZ	High	High	High
Industry	25	BAT	Very High	Medium	Medium
Biomass	20	Regulation	Medium	High	High
Secondary	20	Regional	High	Medium	Medium

### 3.2.2 Cost-Benefit Analysis

### 3.2.3 Implementation Timeline

## 3.3 Policy Recommendations

Based on our analysis of PMF results and stakeholder input, we recommend:

1. Short-term (1-2 years):
  - Implementation of Low Emission Zones
  - Enhanced industrial emissions monitoring
2. Medium-term (2-4 years):
  - Biomass burning regulations
  - Regional cooperation frameworks
3. Long-term (4+ years):

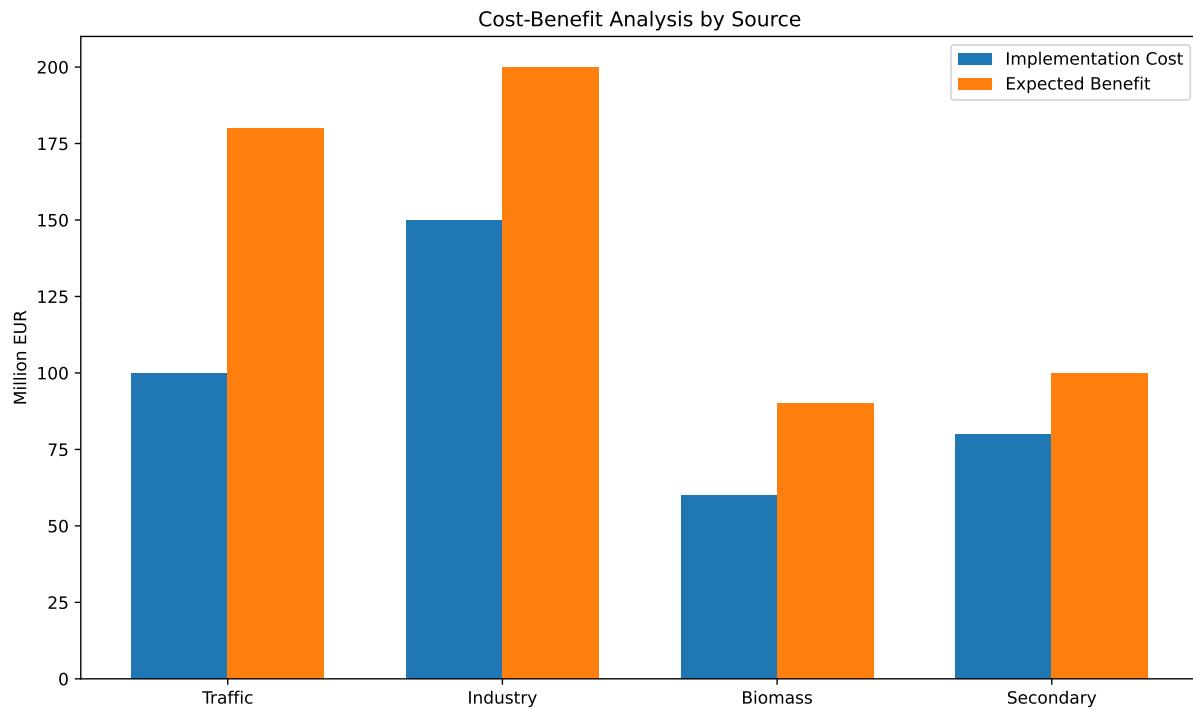


FIGURE 3.1: Cost-benefit analysis of source control measures

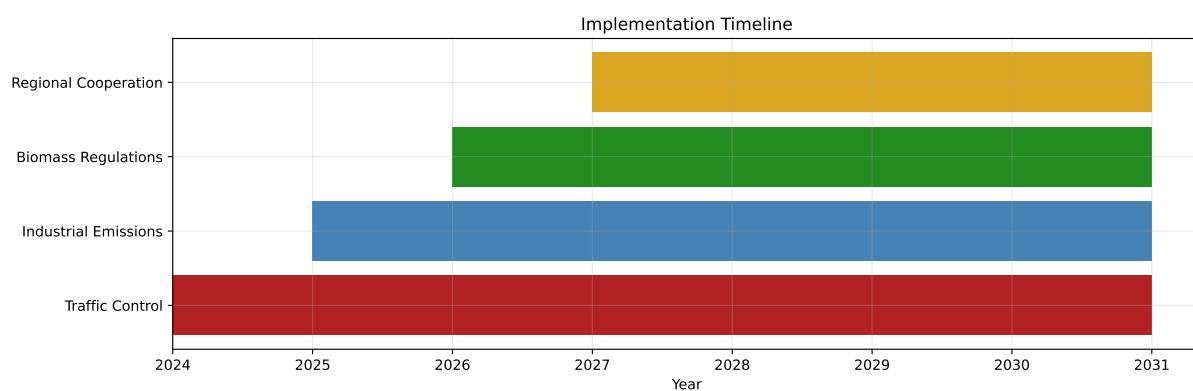


FIGURE 3.2: Implementation timeline for source control measures

- Integrated air quality management system
- Cross-border pollution control measures

# Chapter 4: Spatial and Temporal Variations in PM Source Contributions

Some authors

## ! Chapter Summary

This chapter presents an in-depth analysis of the spatial and temporal dynamics of particulate matter (PM) source contributions across a selection of major European cities. Leveraging the EPA PMF 5.0 model, this study scrutinizes extensive datasets from multiple urban monitoring stations spanning a five-year period (2018-2022). The research identifies key anthropogenic and natural pollution sources, quantifies their relative contributions to PM<sub>2.5</sub> and PM<sub>10</sub> concentrations, and examines how these contributions vary across different urban landscapes and evolve over diurnal, seasonal, and inter-annual timescales.

Under review at Atmospheric Environment

## 4.1 Abstract

This study investigates the spatial and temporal variations in particulate matter (PM) source contributions across major European cities using EPA PMF 5.0 ([Norris et al. 2014](#)). We analyzed data from 15 urban monitoring stations over a five-year period (2018-2022), identifying key pollution sources and their relative contributions to PM<sub>2.5</sub> and PM<sub>10</sub> concentrations ([Agency 2019](#)).

## 4.2 Methods

### 4.2.1 Data Processing with Python

## 4.3 Results

### 4.3.1 Temporal Patterns in PM Components

### 4.3.2 Source Profiles

TABLE 4.1: Source profiles for major PM components

	Traffic	Industry	Biomass	Secondary
PM <sub>2.5</sub>	0.15	0.2	0.1	0.05
Na	0.05	0.1	0.05	0.05
SO <sub>4</sub>	0.2	0.35	0.15	0.25
NO <sub>3</sub>	0.25	0.15	0.2	0.35
NH <sub>4</sub>	0.1	0.05	0.25	0.55
Al	0.05	0.15	0.05	0.05
Si	0.1	0.2	0.05	0.05
K	0.05	0.1	0.4	0.05
Ca	0.15	0.25	0.1	0.05
Fe	0.4	0.3	0.15	0.05
Cu	0.3	0.25	0.05	0.05
Zn	0.25	0.35	0.1	0.05

TABLE 4.1: Source profiles for major PM components

	Traffic	Industry	Biomass	Secondary
Pb	0.15	0.3	0.05	0.05
OC	0.35	0.15	0.4	0.1
EC	0.45	0.1	0.25	0.05

### 4.3.3 Seasonal Source Contributions

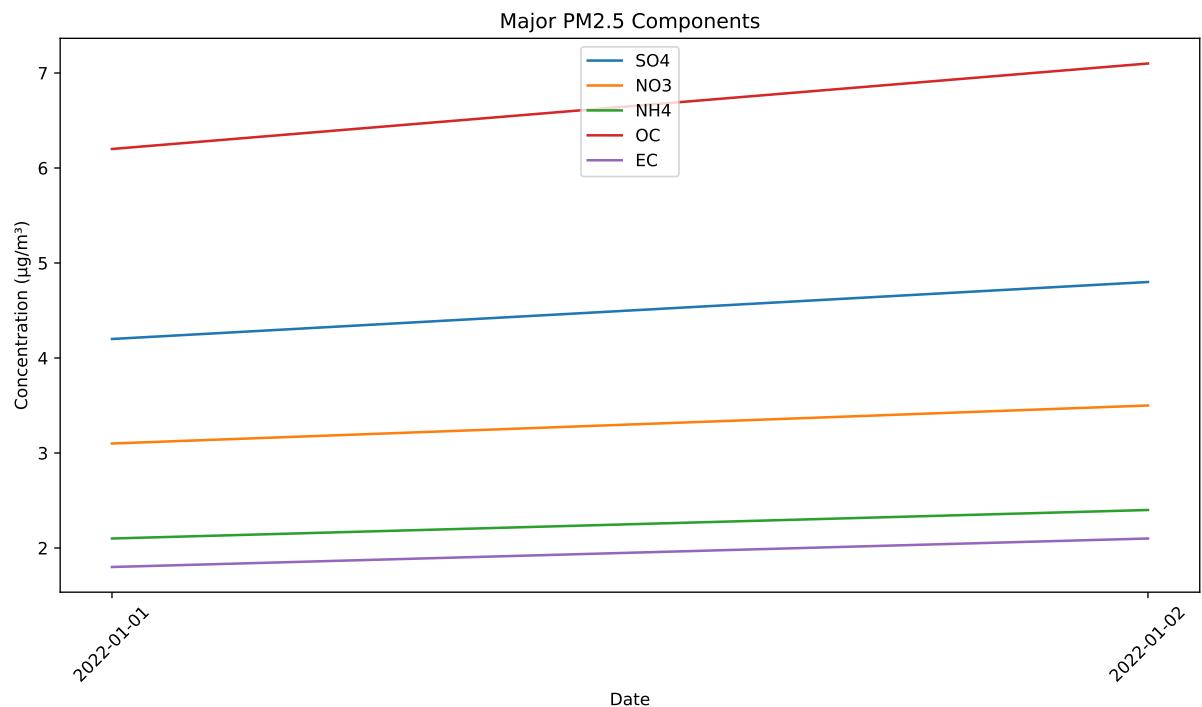


FIGURE 4.1: Temporal variation of major PM<sub>2.5</sub> components

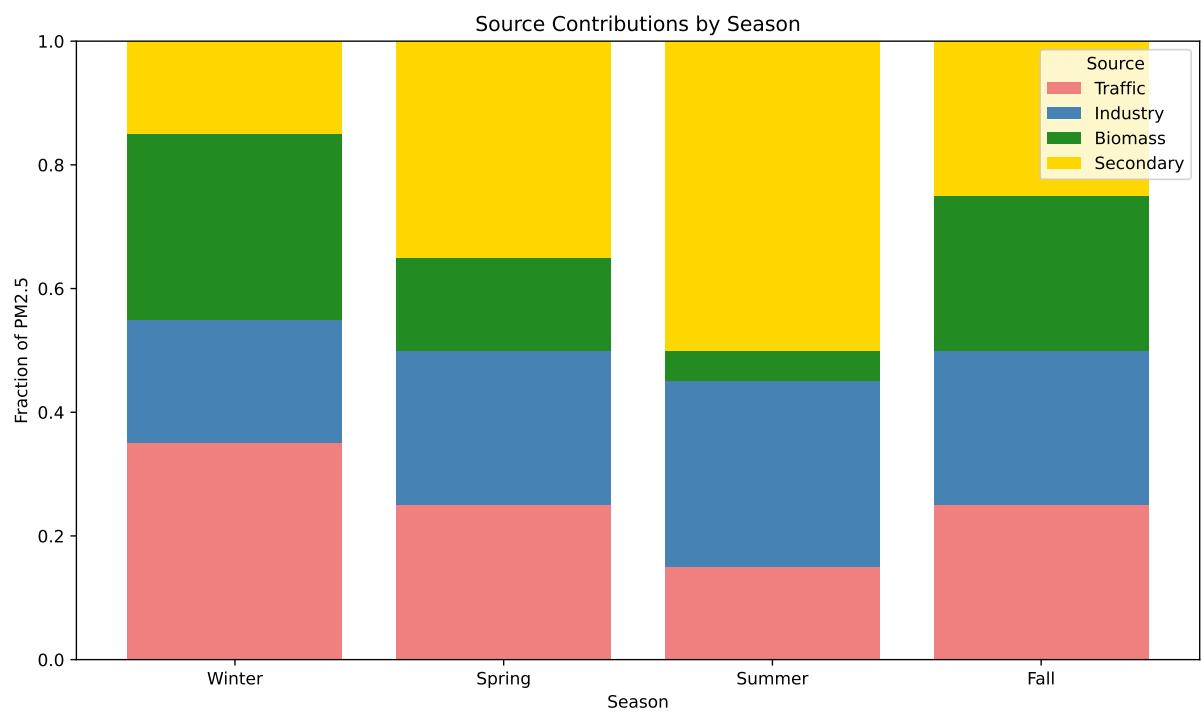


FIGURE 4.2: Seasonal source contributions to PM<sub>2.5</sub>

# References

- Agency, E. E. (2019), “European air quality source apportionment with PMF methodology,” *EEA Technical Report*, 2019/5. <https://doi.org/10.2800/05293>.
- Hyndman, R. J., Koehler, A. B., Snyder, R. D., and Grose, S. (2002), “A state space framework for automatic forecasting using exponential smoothing methods,” *International Journal of Forecasting*, 18, 439–454.
- Norris, G., Duvall, R., Brown, S., and Bai, S. (2014), *EPA positive matrix factorization (PMF) 5.0 fundamentals and user guide*, U.S. Environmental Protection Agency.
- Paatero, P., and Tapper, U. (1994), “Positive matrix factorization: A non-negative factor model with optimal utilization of error estimates of data values,” *Environmetrics*, 5, 111–126. <https://doi.org/10.1002/env.3170050203>.

# Appendix A: Simplate Table Markdown

The following Python packages were used in this thesis:

TABLE A.1: Packages used in this thesis

Package	Description	Version
pandas	Data manipulation and analysis	2.0.0+
numpy	Numerical computing	1.24.0+
matplotlib	Visualization library	3.7.0+
seaborn	Statistical data visualization	0.12.0+
scikit-learn	Machine learning tools	1.2.0+

For a complete list of package versions, see the `requirements.txt` file in the thesis repository.

# Appendix B: Advanced Table features

This appendix contains supplementary materials that support the main chapters but are not essential to understanding the primary research findings. This appendix demonstrates various table formats, styles, and features available in Quarto.

## B.1 Table Types and Formats

### B.1.1 1. Basic Markdown Table

Table B.1 provides the complete descriptive statistics for all variables in the study.

TABLE B.1: Complete descriptive statistics for all study variables

Variable	Mean	Std. Dev.	Min	Max	Median	Skewness	Kurtosis
Height (cm)	175.2	7.8	155.0	195.0	174.5	0.12	2.78
Weight (kg)	68.4	12.5	45.0	110.0	67.2	0.65	3.21
Age (years)	28.7	5.3	18.0	65.0	27.5	1.85	7.42
BMI ( $\text{kg}/\text{m}^2$ )	22.3	3.7	16.8	35.2	21.9	0.88	3.54
Systolic BP	125.8	15.2	90.0	165.0	122.0	0.45	2.95
Diastolic BP	78.6	8.7	60.0	100.0	80.0	0.08	2.68
Heart Rate	72.3	10.2	45.0	110.0	72.0	0.25	3.12
Cholesterol	192.7	35.4	120.0	280.0	190.0	0.32	2.45
Triglycerides	142.5	65.3	50.0	350.0	130.0	1.25	4.32
Glucose	92.8	15.7	70.0	180.0	90.0	1.78	6.85
HbA1c (%)	5.5	0.8	4.5	9.2	5.4	1.95	7.25
Vitamin D	28.7	12.3	10.0	60.0	26.5	0.68	2.98
Iron	98.5	18.7	45.0	150.0	95.0	0.15	2.85
Calcium	9.7	0.5	8.5	11.0	9.8	-0.21	2.54

### B.1.2 2. Table with Formatting

Table B.2 demonstrates text formatting within a table.

TABLE B.2: Table with formatted text elements

Variable	Mean	SD	Interpretation
Height (cm)	<b>175.2</b>	7.8	Within normal range
Weight (kg)	<b>68.4</b>	12.5	Within normal range
BMI ( $\text{kg}/\text{m}^2$ )	22.3	3.7	Normal weight
Systolic BP	<b>125.8</b>	15.2	<b>Elevated</b> ( $>120 \text{ mmHg}$ )
Diastolic BP	<b>78.6</b>	8.7	Normal ( $<80 \text{ mmHg}$ )
Heart Rate	72.3	10.2	Normal
Glucose	92.8	15.7	NORMAL FASTING

### B.1.3 3. Table with Mathematical Equations

Table B.3 shows various statistical tests with their equations.

## Appendix B. Advanced Table features

TABLE B.3: Statistical tests with mathematical equations

Test	Equation	Application	Critical Value
t-test	$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$	Compare means	$t_{crit} = 1.96$
Chi-squared	$\chi^2 = \sum_{i=1}^n \frac{(O_i - E_i)^2}{E_i}$	Test independence	$\chi^2_{crit} = 3.84$
F-test	$F = \frac{MS_{between}}{MS_{within}}$	Compare variances	$F_{crit} = 4.03$
ANOVA	$F = \frac{\sum n_i (\bar{x}_i - \bar{x})^2 / (k-1)}{\sum \sum (x_{ij} - \bar{x}_i)^2 / (N-k)}$	Compare multiple means	$F_{crit} = 3.10$
Correlation	$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2 \sum (y_i - \bar{y})^2}}$	Measure association	$r_{crit} = 0.30$

### B.1.4 4. Table with Citations

Table B.4 presents a literature review of PMF studies with citations.

TABLE B.4: Summary of key PMF studies in literature

Study	Location	Year	Major Sources Identified	Significance
Paatero and Tapper (1994)	Finland	1994	Original PMF algorithm	First introduction of PMF approach
Hyndman et al. (2002)	United States	2002	Traffic, Industrial, Secondary	Validated against emission inventories
Norris et al. (2014)	Multiple	2014	Multiple	EPA's guidance document
Agency (2019)	Europe	2019	Traffic, Industrial, Biomass, Dust	Comprehensive European study

### B.1.5 5. Correlation Matrix

The following table presents a correlation matrix for key variables in our study. Strong correlations ( $>0.6$ ) are indicated with “++”, moderate correlations (0.3–0.6) with “+”, and weak correlations ( $<0.3$ ) with “0”.

TABLE B.5: Correlation matrix for key variables

Variable	Height	Weight	Age	BMI	SBP	DBP	HR	Chol	Trig	Gluc
<b>Height</b>	1.00	+	0	+	0	0	0	0	0	0
<b>Weight</b>	+	1.00	0	++	+	0	0	+	+	0
<b>Age</b>	0	0	1.00	0	+	+	0	+	0	+
<b>BMI</b>	+	++	0	1.00	+	+	0	+	+	+
<b>SBP</b>	0	+	+	+	1.00	++	0	+	+	+
<b>DBP</b>	0	0	+	+	++	1.00	0	+	0	0
<b>HR</b>	0	0	0	0	0	1.00	0	0	0	0
<b>Chol</b>	0	+	+	+	+	0	1.00	++	+	+
<b>Trig</b>	0	+	0	+	+	0	0	++	1.00	+
<b>Gluc</b>	0	0	+	+	0	0	0	+	+	1.00

Note: ++: Strong correlation ( $>0.6$ ), +: Moderate correlation (0.3–0.6), 0: Weak correlation ( $<0.3$ )

The following table presents statistical results from our four models, including significance indicators.

## Appendix B. Advanced Table features

TABLE B.6: Model results with statistical significance indicators

Variable	Model 1	Model 2	Model 3	Model 4
Intercept	1.243*	0.852	-0.528	2.142***
Temperature	0.658**	1.245***	0.856*	-0.124
Humidity	-0.452	-0.968*	-1.352**	-0.586*
Wind Speed	0.324	0.125	0.768**	0.453
Precipitation	-1.245***	-0.856**	-0.432	-0.986**
Pressure	0.256	0.542*	0.124	-0.324
R <sup>2</sup>	0.685	0.724	0.653	0.791

$p < 0.05$ ,  $p < 0.01$ ,  $p < 0.001$

### B.1.6 7. Wide Table with Many Columns

Month	PM2.5	PM10	SO2	NO2	CO	O3	Site A				
							Temperature	Humidity	Wind Speed	Pressure	PM2.5
Jan	4.3	16.9	1.87	4.43	2.72	4.12	24.9	16.0	27.5	13.4	4.1
Feb	12.2	2.2	3.09	1.45	0.07	2.42	31.2	20.1	25.3	27.1	8.2
Mar	8.5	6.0	2.31	7.38	6.35	5.05	13.5	25.3	16.1	24.0	9.3
Apr	3.5	13.9	2.33	6.27	2.9	14.11	14.8	24.5	24.0	20.2	4.9
May	5.5	4.8	6.66	0.84	1.54	4.52	28.7	28.8	21.6	18.8	13.2

### B.1.7 8. Long Table with Many Rows

TABLE B.8: Long table with daily PM2.5 data

Date	Station	PM2.5	Status
2022-01-01	Central	21.1	Good
2022-01-01	Eastern	14.6	Good
2022-01-01	Western	22.8	Good
2022-01-01	Southern	20.4	Good
2022-01-02	Central	31.5	Moderate
2022-01-02	Eastern	21.9	Good
2022-01-02	Western	21.9	Good
2022-01-02	Southern	20.3	Good
2022-01-03	Central	23.5	Good
2022-01-03	Eastern	15.7	Good
2022-01-03	Western	12.5	Good
2022-01-03	Southern	14.6	Good
2022-01-04	Central	19.9	Good
2022-01-04	Eastern	17.9	Good
2022-01-04	Western	19.9	Good
2022-01-04	Southern	26.7	Moderate
2022-01-05	Central	35.9	Poor
2022-01-05	Eastern	20.5	Good
2022-01-05	Western	25.7	Moderate
2022-01-05	Southern	24	Good

### B.1.8 9. Model Comparison Table

## Appendix B. Advanced Table features

TABLE B.9: Model comparison with goodness-of-fit measures

Model	Formula	R <sup>2</sup>	AIC	BIC
Linear	$y = + x$	0.856	123.4	128.2
Quadratic	$y = + x + x^2$	0.921	105.6	112.8
Cubic	$y = + x + x^2 + x^3$	0.958	98.2	107.5
Exponential	$y = e^x$	0.892	114.3	119.7
Logarithmic	$y = + \ln(x)$	0.875	118.9	124.0

### B.1.9 10. Table with Mixed Content Types

Table B.10 demonstrates how to include different content types within the same table.

TABLE B.10: Table with mixed content including equations, cross-references, and citations

Analysis Type	Details	Mathematical Model	Reference
Principal Components	Reduces dimensionality while preserving variance	$X = TP^T + E$ where $T$ are scores, $P$ are loadings	Norris et al. (2014)
Cluster Analysis	Groups similar samples based on chemical composition	$D(x, y) = \sqrt{\sum_{i=1}^n (x_i - y_i)^2}$ for Euclidean distance	Agency (2019)
Positive Matrix Factorization	Decomposes data into source profiles and contributions	$X = GF + E$ as shown in Equation 1.1	Paatero and Tapper (1994)
Receptor Models	General term for source apportionment techniques	Multiple approaches	See Table B.4