## Chi-squared - robust version

$$\chi_{dof}^2 = \frac{1}{N-1} \sum_{i=1}^N \left( \frac{x_i - \overline{x}}{\sigma_i} \right)^2$$

We expect  $\chi^2_{\text{dof}}$  to be 1 to within a few  $\sqrt{2/(N-1)}$ 

If not, then we have a problem: either error distribution is not Gaussian, or the values of  $\sigma_i$  are unreliable, or the underlying quantity x does not have a fixed value  $\mu$ .

Therefore, if the error distribution is suspected to have slow-falling tails, such as the Cauchy distribution, or outliers are present, use  $\sigma_G$  to estimate the width of  $z_i$  and thus robust  $\chi^2_{dof}$ , instead of the formula above.