

```

1  sig Node {
2    children : set Node
3  }
4  sig Leaf extends Node {}
5  one sig Root in Node {}
6
7  sig Red, Black in Node {}
8
9  pred Invs {
10   // Specify the properties that characterize
11   // red-black binary trees inside this predicate.
12
13   // The number of points you will get is proportional to the number of correct properties.
14   // To check how many points you have so far you can use the different commands.
15   // The maximum is 5 points.
16
17   // Be careful to not overspecify!
18   // If some of your properties are not valid in a red-black tree you get 0 points,
19   // even if you have some correct properties.
20   // To check if you are not overspecifying you can use command NoOverspecification.
21   // If you are overspecifying this command will return a tree that should be possible
22   // but that you spec is not accepting.
23
24   //Nodes-----
25   //Every node is either red or black.
26   all n: Node | n in Red iff n not in Black
27
28   //A node can't have itself as a child
29   all n : Node | n not in n.^children
30   //-----
31
32   //Root-----
33   //The Root is always black.
34   all r: Root | r in Black
35
36   //The root doesn't have father
37   all r: Root | no(children.r)
38   //-----
39
40   //Leafs-----
41   //A leaf doesn't have children
42   all l : Leaf | no(l.children)
43
44   //A leaf is black.
45   all l : Leaf | l in Black
46   //-----
47
48   //All nodes but [...]-----
49   //All nodes except leafs have two children
50   all n: Node-Leaf | #(n.children) = 2
51
52   //All nodes except the root have one father
53   all n: Node-Root | #(children.n) = 1
54
55   //All nodes except root & leafs (interior nodes) have 2 children
56   all i: Node-Root-Leaf | #(i.children) = 2
57   //-----
58
59   //Other invariants-----
60   //Both children of red nodes are black
61   all c: Node-Black | c.children in Black
62
63   //All leafs must have the same number of black nodes from root (including) to themselves
64   all l1,l2: Leaf | #((^children).l1 & Black) = #((^children).l2 & Black)
65   //-----
66 }

```