

# Mining Large Scale Datasets

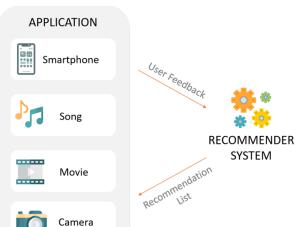
#### **Recommender Systems**

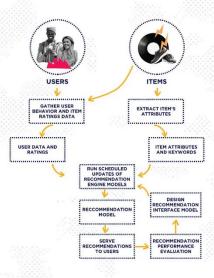
(Adapted from CS246@Starford.edu by Prof. Sérgio Matos; http://www.mmds.org)

#### Recommendations





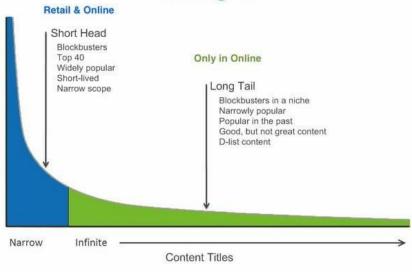




### Scarcity vs Abundance

- Shelf space in traditional stores is scarce (and expensive)
  - Also: TV schedule, movie theaters, newspaper pages, ...
- Web enables near-zero-cost dissemination of information about products
  - ~ Abundance
- ⇒ More choice necessitates better filters
  - Recommendation engines
  - Association rules:
     How Into Thin Air made Touching the Void a bestseller

### The Long Tail



### Types of recommendations

- Editorial and hand curated
  - List of favorites
  - Lists of "essential" items
- Simple aggregates
  - Top 10
  - Most Popular
  - Recent Uploads

#### ⇒ Tailored to individual users

Amazon, Netflix, ...

#### Formal model

- X = set of Customers
- **S** = set of Items
- Utility function  $u : X \times S \rightarrow R$ 
  - R = set of ratings
  - R is a totally ordered set
  - e.g., 0-5 stars, real number in [0,1]

# Utility matrix

	Avatar	LotR	Matrix	PotC
Alice	1		0.2	
Bob		0.5		0.3
Carol	0.2		1	
David				0.4

### Key problems

- (1) Gathering "known" ratings for matrix
  - How to collect the data in the utility matrix
- (2) Extrapolate unknown ratings from the known ones
  - Mainly interested in high unknown ratings
  - Interested in knowing what users like, not what they don't like
- (3) Evaluating extrapolation methods
  - How to measure success/performance of recommendation methods

### Gathering ratings

- Explicit
  - Ask people to rate items
  - Doesn't work well in practice most people won't be bothered; biased to those willing to rate
  - Crowdsourcing: Pay people to label items
- Implicit
  - Learn ratings from user actions
     E.g., purchase / watching implies high rating
  - What about low ratings?

### Extrapolating ratings

- Key problem: Utility matrix U is sparse
  - Most people have not rated most items
  - Cold start

New items have no ratings New users have no history

- Three approaches to recommender systems
  - Content-based
  - Collaborative
  - Latent factor based

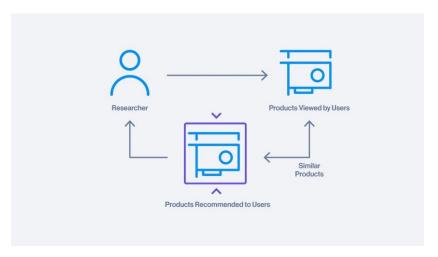
#### Content-based recommendation

#### Main idea

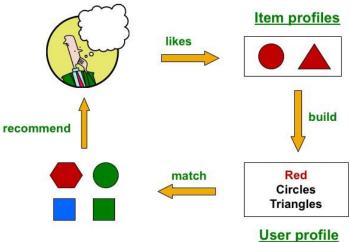
Recommend to customer x items similar to previous items rated highly by x

- Movie recommendations
   Recommend movies with same actor(s), director, genre, ...
- Websites, blogs, news
   Recommend other sites with "similar" content

#### Content-based recommendation



#### Overview



### Item profiles

- Create an item profile for each item
  - A set (vector) of features
  - Movies: author, title, actor, director, ...
  - Text: Set of "important" words in document
- How to pick important features?
  - Usual heuristic from text mining is TF-IDF (Term frequency \* Inverse Doc Frequency)
  - Doc profile = set of words with highest TF-IDF scores

### User profiles and prediction

- User profile possibilities
  - Weighted average of rated item profiles
  - Variation: weight by difference from average rating for item
- Prediction heuristic: Cosine similarity of user and item profiles
   Given user profile x and item profile i, estimate

$$u(\mathbf{x}, \mathbf{i}) = \cos(\mathbf{x}, \mathbf{i}) = \frac{\mathbf{x} \cdot \mathbf{i}}{\|\mathbf{x}\| \cdot \|\mathbf{i}\|}$$

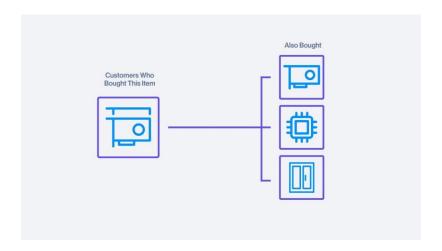
#### Content-based: Pros

- + No need for data on other users
- + Able to recommend to users with unique tastes
- + Able to recommend new and unpopular items
  - No first-rater problem
- + Able to provide explanations
  - Explain recommended items by listing content-features that caused items to be recommended

#### Content-based: Cons

- Finding the appropriate features is hard
  - E.g., images, movies, music
- Recommendations for new users
  - How to build a user profile?
- Overspecialization
  - Never recommends items outside user's content profile
  - People might have multiple interests
  - Unable to exploit quality judgments of other users

## Collaborative filtering



### Collaborative filtering

- Consider user x
- Find set N of other users whose ratings are "similar" to x's ratings
- Estimate x's ratings based on ratings of the N users



### Finding "similar" users: Similarity metric

	HP1	HP2	HP3	TW	SW1	SW2	SW3
$\overline{A}$	4			5	1		,
B	5	5	4				
C				2	4	5	
D		3					3

• Intuitively we want sim(A, B) > sim(A, C)

## Finding "similar" users: Similarity metric

	HP1	HP2	HP3	TW	SW1	SW2	SW3
$\overline{A}$	4			5	1		
B	5	5	4				
C				2	4	5	
D		3					3

Jaccard similarity

$$sim(A, B) = 1/5 < 2/4 = sim(A, C)$$

Problem: Ignores the values of ratings

Finding "similar" users: Similarity metric

	HP1	HP2	HP3	TW	SW1	SW2	SW3
$\overline{A}$	4			5	1		
B	5	5	4				
C				2	4	5	
D		3					3

• Cosine similarity 
$$sim(\mathbf{x}, \mathbf{y}) = cos(\mathbf{r}_{\mathbf{x}}, \mathbf{r}_{\mathbf{y}}) = \frac{\mathbf{r}_{\mathbf{x}} \cdot \mathbf{r}_{\mathbf{y}}}{\|\mathbf{r}_{\mathbf{x}}\| \cdot \|\mathbf{r}_{\mathbf{y}}\|}$$
  
 $sim(A, B) = 0.380 > 0.322 = sim(A, C)$ 

• Problem: Treats missing ratings as "negative" (disliked)  $r_A = 4, 0, 0, 5, 1, 0, 0, r_B = 5, 5, 4, 0, 0, 0, 0$ 

## Finding "similar" users: Similarity metric

			HP3	TW	SW1	SW2	SW3
$\overline{A}$	2/3			5/3	-7/3		
B	1/3	1/3	-2/3				
C		1/3		-5/3	1/3	4/3	
D		0			,		0

• Cosine similarity 
$$sim(\mathbf{x}, \mathbf{y}) = cos(\mathbf{r}_{\mathbf{x}}, \mathbf{r}_{\mathbf{y}}) = \frac{\mathbf{r}_{\mathbf{x}} \cdot \mathbf{r}_{\mathbf{y}}}{\|\mathbf{r}_{\mathbf{x}}\| \cdot \|\mathbf{r}_{\mathbf{y}}\|}$$
  
 $sim(A, B) = 0.380 > 0.322 = sim(A, C)$ 

- Problem: Treats missing ratings as "negative" (disliked)
- Solution: subtract the (row) mean
  - = Pearson correlation coefficient

## Finding "similar" users: Similarity metric

	HP1	HP2	HP3	TW	SW1	SW2	SW3
A	4			5	1		
$\boldsymbol{B}$	5	5	4				
C				2	4	5	
D		3					3

- Pearson correlation coefficient
  - $S_{xy}$  = items rated by both users x and y

$$sim(\mathbf{x}, \mathbf{y}) = \frac{\sum_{s \in S_{xy}} (r_{xs} - \bar{r_{\mathbf{x}}})(r_{ys} - \bar{r_{\mathbf{y}}})}{\sqrt{\sum_{s \in S_{xy}} (r_{xs} - \bar{r_{\mathbf{x}}})^2} \sqrt{\sum_{s \in S_{xy}} (r_{ys} - \bar{r_{\mathbf{y}}})^2}}$$

$$sim(A, B) = 0.092 > -0.559 = sim(A, C)$$

### **Predicting ratings**

From similarity metric to recommendations

- Let  $\mathbf{r}_{\mathbf{x}}$  be the vector of ratings for user  $\mathbf{x}$
- Let N be the set of k users most similar to x who have rated item i
- Prediction for item i of user x:

$$r_{xi} = \frac{1}{k} \sum_{y \in N} r_{yi}$$

or even better,

$$r_{xi} = \frac{\sum_{y \in N} s_{xy} \cdot r_{yi}}{\sum_{y \in N} s_{xy}}$$
 ,  $s_{xy} = sim(x, y)$ 

### Item-Item Collaborative Filtering

- Item-item vs User-user
- For item *i*, find other similar items
- Estimate rating for item i based on ratings for similar items
- Can use same similarity metrics and prediction functions as in user-user model

$$r_{xi} = \frac{\sum_{j \in N(i;x)} s_{ij} \cdot r_{xj}}{\sum_{j \in N(i;x)} s_{ij}}$$

 $s_{ij}$ : similarity of items i and j  $r_{xj}$ : rating of user x on item jN(i;x): set items rated by x that are similar to i

movies

users 10 11 12 

- unknown rating

- rating between 1 to 5

movies

users

	1	2	3	4	5	6	7	8	9	10	11	12
1	1		3		?	5			5		4	
2			5	4			4			2	1	3
3	2	4		1	2		3		4	3	5	
4		2	4		5			4			2	
5			4	3	4	2					2	5
6	1		3		3			2			4	

- estimate rating of movie 1 by user 5



#### **Neighbor selection:**

Identify movies similar to movie 1, rated by user 5

Here we use Pearson correlation as similarity: 1) Subtract mean rating  $m_i$  from each movie i

 $m_1 = (1+3+5+5+4)/5 = 3.6$ row 1: [-2.6, 0, -0.6, 0, 0, 1.4, 0, 0, 1.4, 0, 0.4, 0]

2) Compute cosine similarities between rows

	users													
		1	2	3	4	5	6	7	8	9	10	11	12	sim(1,m)
	1	1		3		?	5			5		4		1.00
	2			5	4			4			2	1	3	-0.18
movies	<u>3</u>	2	4		1	2		3		4	3	5		<u>0.41</u>
Ε	4		2	4		5			4			2		-0.10
	5			4	3	4	2					2	5	-0.31
	<u>6</u>	1		3		3			2			4		<u>0.59</u>

Compute similarity weights:

	1	2	3	4	5	6	7	8	9	10	11	12
1	1		3		2.6	5			5		4	
2			5	4			4			2	1	3
<u>3</u>	2	4		1	2		3		4	3	5	
4		2	4		5			4			2	
5			4	3	4	2					2	5
<u>6</u>	1		3		3			2			4	

Predict by taking weighted average:

$$r_{1.5}$$
 = (0.41\*2 + 0.59\*3) / (0.41+0.59) = 2.6

$$r_{ix} = \frac{\sum_{j \in N(i;x)} s_{ij} \cdot r_{jx}}{\sum s_{ij}}$$

movie

#### Item-item vs User-user

	Avatar	LotR	Matrix	PotC
Alice	1		0.2	
Bob		0.5		0.3
Carol	0.2		1	
David				0.4

- In theory, these are dual approaches with similar performance
- In practice, it has been observed that item-item often works better than user-user
- Why? Items are simpler, users have multiple tastes

## Pros/Cons of Collaborative Filtering

- + Works for any kind of item
  - No feature selection needed
  - Cold Start
    - Need enough users in the system to find a match
  - Sparsity
    - The user/ratings matrix is sparse
    - Hard to find users that have rated the same items
  - First rater
    - Cannot recommend an item that has not been previously rated
    - New items, esoteric items
  - Popularity bias
    - Cannot recommend items to someone with unique taste
    - Tends to recommend popular items

### Hybrid methods

Combine predictions from two or more different recommenders

- e.g. Global baseline + CF
- Perhaps using a linear model

Add content-based methods to collaborative filtering

- Item profiles for new item problem
- Demographics to deal with new user problem

#### Global Baseline Estimate

- Estimate Joe's rating for the movie *The Sixth Sense* 
  - Joe has not rated any movie similar to *The Sixth Sense*
- Global Baseline approach
  - Mean movie rating: 3.7 stars
  - The Sixth Sense is **0.5 stars above average**
  - Joe rates 0.2 stars below average
  - Baseline estimate: 3.7 + 0.5 0.2 = 4 stars

### Combining Global Baseline with CF

- Global Baseline estimate:
  - Joe will give *The Sixth Sense* **4 stars**
- Local neighborhood (CF):
  - Joe did not like related movie Signs
    - Rated it 1 star below his average
- Final estimate:
  - Joe will rate The Sixth Sense 4—1 = 3 stars

### CF: Common practice

- Define similarity s<sub>ij</sub> of items i and j
- Select k nearest neighbors N(i;x)
  - Items most similar to i, that were rated by x
- Estimate rating  $r_{xi}$  as the weighted average

$$r_{xj} = b_{xi} + \frac{\sum_{j \in N(i;x)} s_{ij} \cdot (r_{xj} - b_{xj})}{\sum_{j \in N(i;x)} s_{ij}}$$

$$b_{xi} = \mu + b_x + b_i$$
 baseline estimate for  $r_{xi}$ 

 $\mu$  = overall mean movie rating  $b_x$  = rating deviation of user x = (avg rating of user x) -  $\mu$   $b_i$  = rating deviation of movie i = (avg rating of movie i) -  $\mu$ 

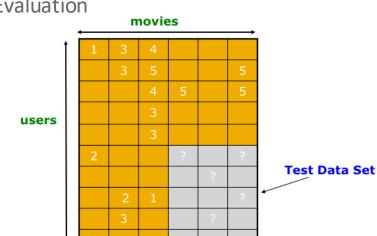
#### **Evaluation**

#### movies

<b></b>		ovie	5		<b></b>
1	3	4			
	3	5			5 5
		4	5		5
		3			
		3			
2			2		2
				5	
	2	1			1
	3			3	
1					

#### users

#### **Evaluation**



### **Evaluating predictions**

- Compare predictions with known ratings
  - Root-mean-square error (RMSE)

$$\sqrt{\frac{\sum_{si}(r_{si}-r_{si}^*)^2}{\sum_{si}1}}$$
 where  $r_{xi}$  is predicted;  $r_{xi}^*$  is the true rating

- Precision at top 10
- Rank correlation
   Spearman's correlation between system's and user's complete rankings
- Another approach: 0/1 model (dislike/like)
  - Coverage
    - # items/users for which the system can make predictions
  - Precision
  - Receiver operating characteristic (ROC)
     Tradeoff curve between false positives and false negatives

#### Problems with error measures

- Narrow focus on accuracy sometimes misses the point
  - Prediction diversity
  - Prediction context
  - Order of predictions
- In practice, we care only about predicting high ratings
  - RMSE might penalize a method that does well for high ratings and badly for others

#### Hands On

- The objective of this exercise is to consolidate your understanding of the algorithms and logic implemented in your solutions to Assignment 2.
- For each problem (A, B, and C), provide clear, structured pseudocode that outlines the major steps and reasoning behind your implementation.
- The instructions are available in the shared folder, under Assignment 2.
- You should write the pseudocode in pen and paper.
- Alloted time: 50 minutes.
- Submit a photo of the hand-written document by 11:50/18:50 on the link available on e-learning.

### Assignment 3- part A

- Write a 3-4 page summary on Locality Sensitivity Hashing and its use in collaborative filtering.
- Instructions are available on the shared folder, under Assignment 3
- Deadline for submission on e-learning: 18th of May 2025, 23h59.
- Part B of the assignment will be a practical one and will be introduced next class.