

# ReXNet: Diminishing Representational Bottleneck on Convolutional Neural Network

Dongyoon Han, Sangdoo Yun, Byeoungho Heo, YoungJoon Yoo

Clova AI Research, NAVER Corp.

# What is Representational Bottleneck?

- When we reduce the dimension of data, we lose some important representations.
- This leads our model to bad performance.
- Softmax layer also make representational bottleneck.

ConvNet Configuration					
A	A-LRN	B	C	D	E
11 weight layers	11 weight layers	13 weight layers	16 weight layers	16 weight layers	19 weight layers
input (224 × 224 RGB image)					
conv3-64	conv3-64 <b>LRN</b>	conv3-64	conv3-64	conv3-64	conv3-64
maxpool					
conv3-128	conv3-128	conv3-128	conv3-128	conv3-128	conv3-128
maxpool					
conv3-256	conv3-256	conv3-256	conv3-256	conv3-256	conv3-256
conv3-256	conv3-256	conv3-256	<b>conv1-256</b>	<b>conv3-256</b>	conv3-256
maxpool					
conv3-512	conv3-512	conv3-512	conv3-512	conv3-512	conv3-512
conv3-512	conv3-512	conv3-512	<b>conv1-512</b>	<b>conv3-512</b>	conv3-512
maxpool					
conv3-512	conv3-512	conv3-512	conv3-512	conv3-512	conv3-512
conv3-512	conv3-512	conv3-512	<b>conv1-512</b>	<b>conv3-512</b>	conv3-512
maxpool					
FC-4096					
FC-4096					
FC-1000					
soft-max					

# Rep. Bottleneck can occur in every layer

- The layers with limited encoding capability of generating discriminative features can be considered as the representational bottleneck.

# Contributions

- Investigation of representational bottleneck problem in a DNN.
- New design principles with improved network architectures.
- SOTA result on ImageNet dataset
- Prominent transfer learning result on COCO detection and other classifications.

# Preliminary: Feature Encoding

- Given an  $L$ -depth network with  $N$  features are encoded from  $d_0$ -dimensional input  $X_0 \in \mathbb{R}^{d_0 \times N}$  features are represented as  $X_L = \sigma(W_L(\dots f_1(W_1 X_0)))$  with the weight matrix  $W_i \in \mathbb{R}^{d_i \times d_{i-1}}$ .
- We call the layer with  $d_i > d_{i-1}$  an expend layer with  $d_i < d_{i-1}$  an condense layer.
- Each of  $f_i(\cdot)$  denotes  $i$ -th point-wise nonlinearity, such as a ReLU with a BN layer.
- $\sigma(\cdot)$  denotes Softmax Function.

# Preliminary: Feature Encoding

- Let  $W_i \hat{X}_{i-1}$  is convolution operation with weight  $W_i \in \mathbb{R}^{d_i \times k_i^2 d_{i-1}}$  and  $\hat{X}_{i-1} \in \mathbb{R}^{k_i^2 d_{i-1} \times whN}$ .
- Each  $i$ -th layer's output  $X_i$  can be written as:

$$X_i = \begin{cases} f_i(W_i \hat{X}_{i-1}) & 1 \leq i < L, \\ \sigma(W_L \hat{X}_{L-1}) & i = L. \end{cases}$$

# Softmax Bottleneck

- Output of cross-entropy loss is  $\log \sigma(W_L X_{L-1})$ , whose rank is bounded by the rank of  $W_L X_{L-1}$ , which is  $\min(d_L, d_{L-1})$ .
- As the input dimension  $d_{L-1}$  is smaller than the output dimension  $d_L$ , the encoded features can't fully represent the whole category due to rank deficiency.
- Then, what if we increase  $d_{L-1}$  closer to  $d_L$ ?

# Layer-wise rank expansion

- We conjecture the layers that expand the channel size (i.e., expand layers) such as downsampling blocks would have a rank deficiency and may have the representational bottleneck.
- To mitigate the problem, we expand the rank of weight matrix  $W_i$ .
- Given the  $i$ -th feature generated by a layer,  $X_i = f_i(W_i X_{i-1}) \in \mathbb{R}^{d_i \times whN}$ , rank of  $X_i$  is bounded to  $\min(d_i, d_{i-1})$ .

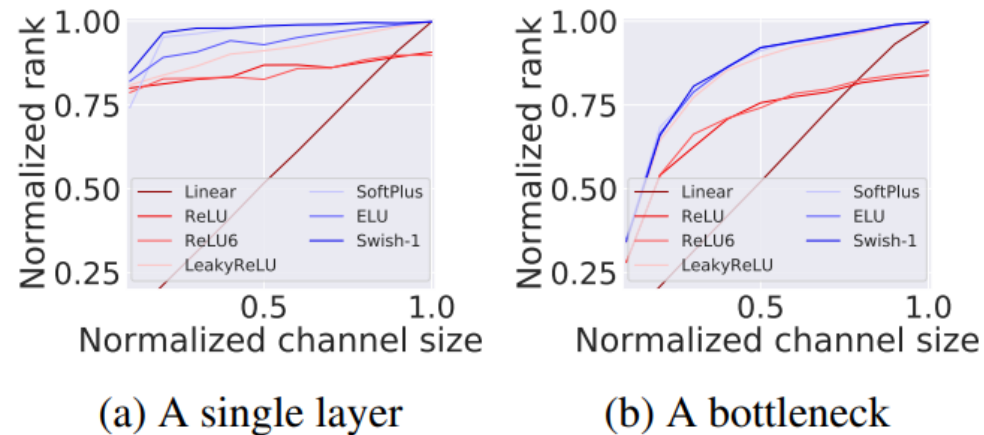


# Layer-wise rank expansion

- We represent  $f(X) = X \circ g(X)$ , where  $\circ$  denotes the pointwise multiplication with another pointwise function  $g$ .
- Following the inequality  $\text{rank}(f(X)) \leq \text{rank}(X) \cdot \text{rank}(g(X))$ , the rank of  $X_i$  is bounded as,  
$$\text{rank}(X_i) \leq \text{rank}(W_i X_{i-1}) \cdot \text{rank}(g_i(W_i X_{i-1})).$$
- For nonlinear function  $g$  with larger rank, we can use Swish-1 or ELU.
- When  $d_i$  is fixed, if we adjust the  $d_{i-1}$  close to  $d_i$ , we can get possibility of the unbounded rank up to the feature dimension.

# Layer-wise rank expansion

- From empirical studies, we observe properly selected nonlinear functions can largely expand the rank.
- And the normalized input channel size ( $d_{in}/d_{out}$ ) is closely related to the rank of the feature.



# New Principles to design good model

1. Enlarge the input channel size (dimension) of a layer.
2. Equip with a proper nonlinearity.
3. Design a network with many expand layers.

# Improve Network Architecture

- Representational bottleneck occur in expand layers like :
- Downsampling blocks or layers,
- First layer in a bottleneck module, inverted bottleneck blocks
- And Penultimate layers.

# Improve Network Architecture

- We can improve our model by:
- Expanding the input channel size of the conv layer.
- Replacing nonlinearity like ReLU, ReLU6.

# ReXNets

- Introduce new CNN model **Rank eXpansion Networks (ReXNets)**

Table 8: **Specification of ReXNet-1.0x.** Bottleneck1 and bottleneck6 denote the  $3 \times 3$  inverted bottleneck with the expansion ratio of 1 and 6, respectively. In each block, SE denotes whether Squeeze Excitation Module (SE-module) [14] is used. SW denotes Swish-1 [36] is used after the convolution, and SW/RE6 denotes Swish and ReLU6 is used after the first  $1 \times 1$  convolution and the  $3 \times 3$  depthwise convolution [13], respectively.

Input	Operator	# of channels	SE	Nonlinearity	Stride
$224^2 \times 3$	conv $3 \times 3$	32	-	SW	2
$112^2 \times 32$	bottleneck1	16	-	SW/RE6	1
$112^2 \times 16$	bottleneck6	27	-	SW/RE6	2
$56^2 \times 27$	bottleneck6	38	-	SW/RE6	1
$56^2 \times 38$	bottleneck6	50	✓	SW/RE6	2
$28^2 \times 50$	bottleneck6	61	✓	SW/RE6	1
$28^2 \times 61$	bottleneck6	72	✓	SW/RE6	2
$14^2 \times 72$	bottleneck6	84	✓	SW/RE6	1
$14^2 \times 84$	bottleneck6	95	✓	SW/RE6	1
$14^2 \times 95$	bottleneck6	106	✓	SW/RE6	1
$14^2 \times 106$	bottleneck6	117	✓	SW/RE6	1
$14^2 \times 117$	bottleneck6	128	✓	SW/RE6	1
$14^2 \times 128$	bottleneck6	140	✓	SW/RE6	2
$7^2 \times 140$	bottleneck6	151	✓	SW/RE6	1
$7^2 \times 151$	bottleneck6	162	✓	SW/RE6	1
$7^2 \times 162$	bottleneck6	174	✓	SW/RE6	1
$7^2 \times 174$	bottleneck6	185	✓	SW/RE6	1
$7^2 \times 185$	conv $1 \times 1$ , pool $7 \times 7$	1280	-	SW	1
$1^2 \times 1280$	fc	1000	-	-	1

# Conclusion

- Representational bottleneck is big problem in CNNs.
- Matrix Rank is closely related to the bottleneck problem.
- Expand layers are likely to suffer from the problem.
- So we propose a set of design principles to handle this.

# ReXNet: Diminishing Representational Bottleneck on Convolutional Neural Network

Paper: <https://arxiv.org/abs/2007.00992>

Official PyTorch Implementation: <https://github.com/clovaai/rexnet>

Thank you for watching!