TAREA 4 Auil Cabezas

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1 Tarea 4 - Mario Cabezas - Lucas Auil

2 Carga de bibliotecas

```
[1]: import numpy as np
     import pandas as pd
     import matplotlib.pyplot as plt
     import statsmodels.api as sm
     import statsmodels.formula.api as smf
     import sklearn
     import scipy
     from scipy.linalg import eigh, cholesky
     from scipy.stats import norm
     import linearmodels.panel as lmp
     from pylab import plot, show, axis, subplot, xlabel, ylabel, grid
     import semopy
     import seaborn as sns
     from factor_analyzer import FactorAnalyzer
     from sklearn.decomposition import PCA
     %matplotlib inline
```

3 Carga y limpieza de datos

Lo primero que realizamos es cargar la data a trabajar que en este caso es la base de datos llamada junaeb2, la cual viene en formato csv

```
[2]: Xr = pd.read_csv('../TAREA FINAL/junaeb2.csv')
Xr

[2]: sexo edad imce vive_padre vive_madre sk1 sk2 sk3 sk4 sk5 ... \
```

85 0.75 1 2 0 1 1 76 0.71 1 0 0 2 2 2 1 68 0.27 0 1 2 3 3 84 2.05 1 1 1 1 1 1 1 1 4 0 86 1.05 1 1 1 1 1 1 1

1

59994	0	78	1.63		1		1	1	3	1 2	2	
59995	1	79	2.57		1		1	1	1	2 2	1	•••
59996	0	78	2.12		1		1	1	1	1 1	1	•••
59997	1	78	-0.43		1		1	1	1	1 1	2	•••
59998	0	78	-0.55		0		1	2	2	1 1	1	•••
	sk9	sk10	sk11	sk12	sk13	act_f	isica	area	educm	educp	madre	_work
0	2	2	2	3	2		NaN	0	11.0	11		-1
1	1	1	1	1	1		5.0	0	8.0	8		1
2	2	3	2	1	3		NaN	1	13.0	13		1
3	1	1	1	1	1		2.0	1	16.0	12		-1
4	1	1	1	1	1		1.0	1	17.0	15		0
	•••				•••		•••		•••			
59994	2	2	2	1	1		2.0	1	13.0	13		-1
59995	1	3	2	1	4		3.0	1	18.0	19		0
59996	1	3	1	1	1		3.0	1	13.0	9		1
59997	1	2	1	1	2		2.0	1	17.0	15		1
59998	1	1	1	1	1		1.0	1	18.0	11		1

[59999 rows x 23 columns]

Analizando tanto los datos desplegados en python como la base de datos en Excel , nos dimos cuenta que en las variables act_fisica y educm existian datos vacios, por lo que procedimos a eliminar completamente dichas filas de nuestra data

```
[3]: Xr.dropna(inplace=True)
Xr.reset_index(drop=True, inplace=True)
Xr
```

[0]				·	.	3		-1-4	-1-0	-1-0	_1_1	-1-5		`
[3]:		sexo			vive	_padre	vive_madre	SKI	sk2	SK3	sk4	sk5	•••	\
0		0	76	0.71		0	1	. 1	1	1	1	1	•••	
1		1	84	2.05		1	1	. 1	1	1	1	1	•••	
2		0	86	1.05		1	1	. 1	1	1	1	1	•••	
3		0	74	1.39		1	1	. 1	2	1	1	1	•••	
4		1	91	2.75		1	1	. 1	1	1	2	2	•••	
•••					•••	•••			••					
57	352	0	78	1.63		1	1	. 1	3	1	2	2	•••	
57	353	1	79	2.57		1	1	. 1	1	2	2	1	•••	
57	354	0	78	2.12		1	1	. 1	1	1	1	1	•••	
57	355	1	78	-0.43		1	1	. 1	1	1	1	2		
57	356	0	78	-0.55		0	1	. 2	2	1	1	1	•••	
		sk9	sk10	sk11	sk12	sk13	act_fisica	area	educm	ı ed	lucp	madre	. WO	rk
0		1	1	1	1	1	5.0	0	8.0		8		_	1
1		1	1	1	1	1	2.0	1	16.0)	12			-1
2		1	1	1	1	1	1.0	1	17.0)	15			0
3		1	1	1	1	1	4.0	0	8.0)	8			-1

4	3	3	3	2	2	2.0	1	20.0	19	1
	•••		•••							
57352	2	2	2	1	1	2.0	1	13.0	13	-1
57353	1	3	2	1	4	3.0	1	18.0	19	0
57354	1	3	1	1	1	3.0	1	13.0	9	1
57355	1	2	1	1	2	2.0	1	17.0	15	1
57356	1	1	1	1	1	1.0	1	18.0	11	1

[57357 rows x 23 columns]

```
[4]: Xr.dtypes
```

```
[4]: sexo
                      int64
                      int64
     edad
     imce
                    float64
     vive_padre
                      int64
     vive_madre
                      int64
     sk1
                      int64
     sk2
                      int64
     sk3
                      int64
                      int64
     sk4
     sk5
                      int64
     sk6
                      int64
     sk7
                      int64
     sk8
                      int64
     sk9
                      int64
     sk10
                      int64
     sk11
                      int64
     sk12
                      int64
     sk13
                      int64
     act_fisica
                    float64
     area
                      int64
     educm
                    float64
     educp
                      int64
                      int64
     madre_work
     dtype: object
```

```
[5]: Xr["act_fisica"] = Xr["act_fisica"].astype("int64")
Xr["educm"] = Xr["educm"].astype("int64")
Xr.dtypes
```

```
[5]: sexo int64
   edad int64
   imce float64
   vive_padre int64
   vive_madre int64
   sk1 int64
```

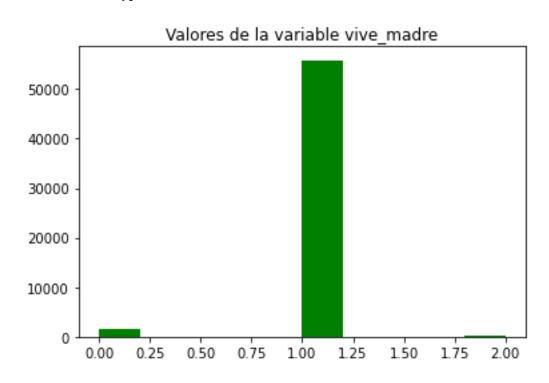
```
int64
sk2
sk3
                 int64
                 int64
sk4
sk5
                 int64
sk6
                 int64
sk7
                 int64
                 int64
sk8
sk9
                 int64
sk10
                 int64
sk11
                 int64
sk12
                 int64
sk13
                 int64
act_fisica
                 int64
                 int64
area
educm
                 int64
educp
                 int64
madre_work
                 int64
```

dtype: object

```
[6]: plt.hist(Xr['vive_madre'],color="green")
   plt.title("Valores de la variable vive_madre")
   Xr.vive_madre.value_counts()
```

[6]: 1 55832 0 1437 2 88

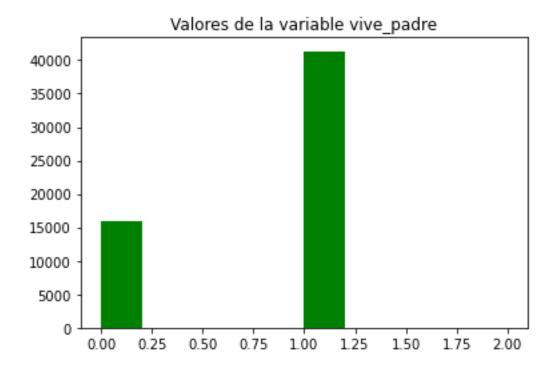
Name: vive_madre, dtype: int64



```
[7]: plt.hist(Xr['vive_padre'],color="green")
plt.title("Valores de la variable vive_padre")
Xr.vive_padre.value_counts()
```

[7]: 1 41337 0 15998 2 22

Name: vive_padre, dtype: int64



```
[8]: | Xr.drop(Xr[Xr['vive_madre']==2].index,inplace =True)
     Xr.drop(Xr[Xr['vive_padre']==2].index,inplace =True)
     Xr.reset_index(drop=True, inplace=True)
     Xr
[8]:
                             vive_padre vive_madre
                                                             sk2
                                                                  sk3
                                                                            sk5
                                                       sk1
                                                                       sk4
            sexo
                  edad
                        imce
     0
               0
                    76
                        0 71
                                                               1
```

O	U	10	0.11	O	_	_	_	_	_	_	•••
1	1	84	2.05	1	1	1	1	1	1	1	•••
2	0	86	1.05	1	1	1	1	1	1	1	•••
3	0	74	1.39	1	1	1	2	1	1	1	•••
4	1	91	2.75	1	1	1	1	1	2	2	•••
			•••			•••					
57242	0	78	1.63	1	1	1	3	1	2	2	

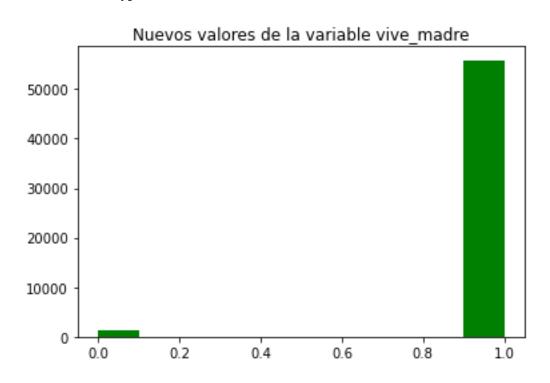
57243	1	79	2.57		1		1	1	1	2 2	2 1.	••
57244	0	78	2.12		1		1	1	1	1 1	. 1.	••
57245	1	78	-0.43		1		1	1	1	1 1	. 2.	••
57246	0	78	-0.55		0)	1	2	2	1 1	. 1.	••
	sk9	sk10	sk11	sk12	sk13	act_fis	sica	area	educm	educp	madre_	work
0	1	1	1	1	1		5	0	8	8		1
1	1	1	1	1	1		2	1	16	12		-1
2	1	1	1	1	1		1	1	17	15		0
3	1	1	1	1	1		4	0	8	8		-1
4	3	3	3	2	2		2	1	20	19		1
					•••		•••					
57242	2	2	2	1	1		2	1	13	13		-1
57243	1	3	2	1	4		3	1	18	19		0
57244	1	3	1	1	1		3	1	13	9		1
57245	1	2	1	1	2		2	1	17	15		1
57246	1	1	1	1	1		1	1	18	11		1

[57247 rows x 23 columns]

```
[9]: plt.hist(Xr['vive_madre'],color="green")
  plt.title("Nuevos valores de la variable vive_madre")
  Xr.vive_madre.value_counts()
```

[9]: 1 55828 0 1419

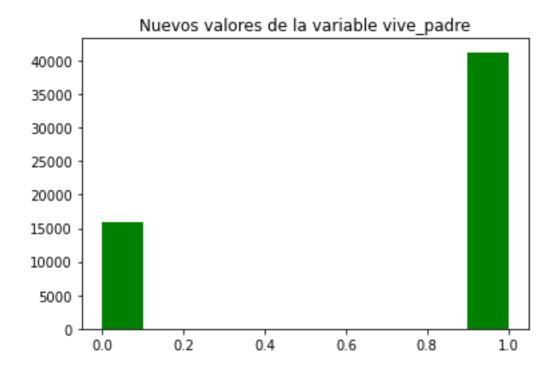
Name: vive_madre, dtype: int64



```
[10]: plt.hist(Xr['vive_padre'],color="green")
   plt.title("Nuevos valores de la variable vive_padre")
   Xr.vive_padre.value_counts()
```

[10]: 1 41280 0 15967

Name: vive_padre, dtype: int64

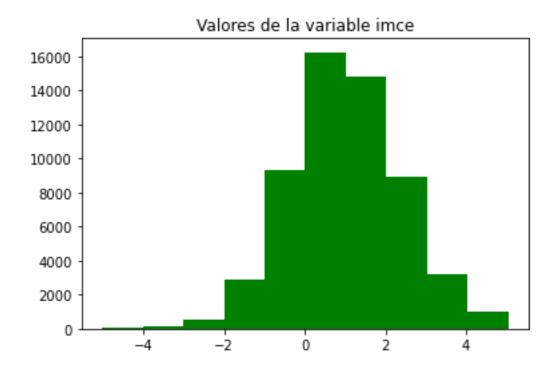


```
[11]: plt.hist(Xr['imce'],color="green")
    plt.title("Valores de la variable imce")
    Xr.imce.value_counts()
```

```
[11]: 0.74
                208
       1.07
                197
       0.87
                197
       0.73
                195
       0.39
                195
      -3.35
                  1
      -4.36
                  1
      -4.66
                  1
      -3.17
                  1
```

-4.88 1

Name: imce, Length: 928, dtype: int64



[12]:	<pre>Xr.drop(Xr[Xr['imce']<0].index,inplace =True)</pre>
	<pre>Xr.reset_index(drop=True, inplace=True)</pre>
	Xr

12]:		sexo	edad	imce	vive	padre	vive_madre	sk1	sk2	sk3	sk4	sk5	\	
	0	0	76	0.71		0	_ 1	1	1	1	1	1	•••	
	1	1	84	2.05		1	1	1	1	1	1	1	•••	
	2	0	86	1.05		1	1	1	1	1	1	1	•••	
	3	0	74	1.39		1	1	1	2	1	1	1	•••	
	4	1	91	2.75		1	1	1	1	1	2	2	•••	
					•••				•					
	44497	1	78	1.58		1	1	1	1	1	1	1	•••	
	44498	1	79	1.73		1	0	1	1	2	1	1	•••	
	44499	0	78	1.63		1	1	1	3	1	2	2	•••	
	44500	1	79	2.57		1	1	1	1	2	2	1	•••	
	44501	0	78	2.12		1	1	1	1	1	1	1		
		sk9	sk10	sk11	sk12	sk13	act_fisica	area	educi	n ed	lucp	madre	_work	
	0	1	1	1	1	1	5	0	8	3	8		1	
	1	1	1	1	1	1	2	1	16	3	12		-1	
	2	1	1	1	1	1	1	1	17	7	15		0	

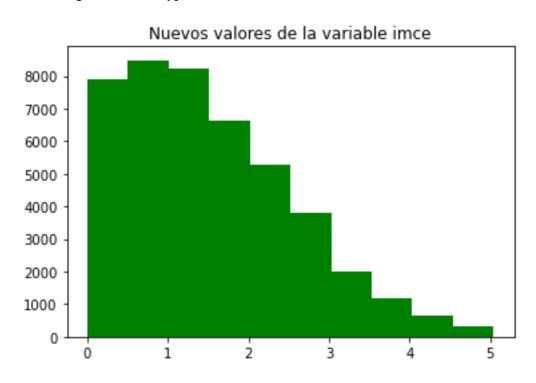
3	1	1	1	1	1		4	0	8	8	-1
4	3	3	3	2	2		2	1	20	19	1
	•••		•••			•••	•••		•••		
44497	1	4	3	3	5		1	0	13	12	-1
44498	1	1	2	1	2		2	1	17	17	1
44499	2	2	2	1	1		2	1	13	13	-1
44500	1	3	2	1	4		3	1	18	19	0
44501	1	3	1	1	1		3	1	13	9	1

[44502 rows x 23 columns]

```
[13]: plt.hist(Xr['imce'],color="green")
   plt.title("Nuevos valores de la variable imce")
   Xr.imce.value_counts()
```

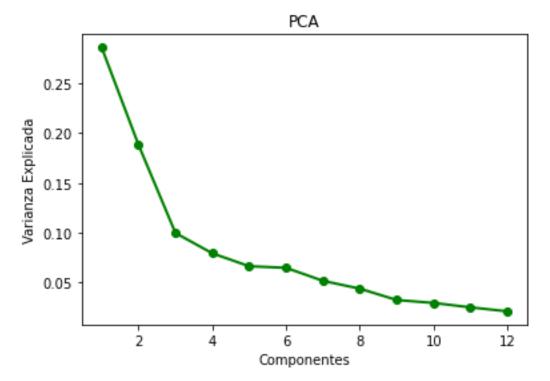
```
[13]: 0.74
               208
      1.07
               197
      0.87
               197
      0.39
               195
      0.73
               195
      5.02
                 3
      4.93
                 3
      4.82
                 2
      5.00
                 2
      4.89
```

Name: imce, Length: 505, dtype: int64



4 1 PCA

```
[14]: vector_sks = \( \) \( \text{Xr}[["sk1", "sk2", "sk3", "sk4", "sk5", "sk6", "sk7", "sk8", "sk9", "sk10", "sk11", "sk12" \) \( \text{pca} = PCA(n_components=12) \) \( \text{pca_features} = \text{pca_fit_transform(vector_sks)} \) \( \text{print(pca_explained_variance_ratio_)} \) \( [0.28606755 \ 0.18817514 \ 0.09973579 \ 0.07929705 \ 0.06632621 \ 0.06471883 \) \( 0.05164867 \ 0.0437851 \ 0.03238106 \ 0.0294521 \ 0.02499784 \ 0.02101661] \) \[ [15]: \( \text{PC_values} = \text{np.arange(pca.n_components_)} + 1 \) \\ \text{plt.plot(PC_values, pca.explained_variance_ratio_, 'o-', linewidth=2, \( \text{uplt.color='green'} \) \\ \text{plt.title('PCA')} \\ \text{plt.xlabel('Componentes')} \\ \text{plt.xlabel('Componentes')} \\ \text{plt.show()} \)
```



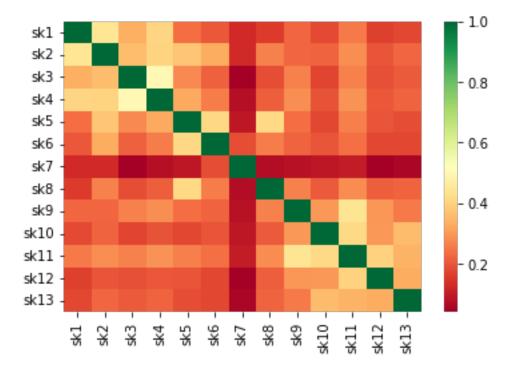
```
[16]: pca = PCA(n_components='mle')
   pca_features = pca.fit_transform(vector_sks)
   print(pca.explained_variance_ratio_)
```

```
[0.28606755 0.18817514 0.09973579 0.07929705 0.06632621 0.06471883 0.05164867 0.0437851 0.03238106 0.0294521 0.02499784 0.02101661]
```

Los valores propios de cada varaible son: $[0.28606755\ 0.18817514\ 0.09973579\ 0.07929705\ 0.06632621\ 0.06471883\ 0.05164867\ 0.0437851\ 0.03238106\ 0.0294521\ 0.02499784\ 0.02101661]$. Además, no fue posible disminuir las variables a un número óptimo, en función de la varianza de los datos, puesto que estas no tenían correlación entre sí.

```
[17]: sns.heatmap(vector_sks.corr(), cmap='RdYlGn')
```

[17]: <AxesSubplot:>



```
[18]: pca_vectors = pd.DataFrame(data = pca.components_)
pca_vectors.head()

[18]: 0 1 2 3 4 5 6 \
0 0.101837 0.228681 0.166704 0.180646 0.186154 0.249874 0.351651
1 0.007632 0.034134 0.066008 0.055333 0.040743 -0.028742 -0.923058
2 0.084242 0.266514 0.180453 0.191232 0.300941 0.341428 -0.115066
3 -0.004360 -0.033451 -0.039866 -0.031587 -0.046156 -0.002758 -0.032316
4 0.143585 0.268222 0.309358 0.295992 -0.021423 0.162823 -0.030117
```

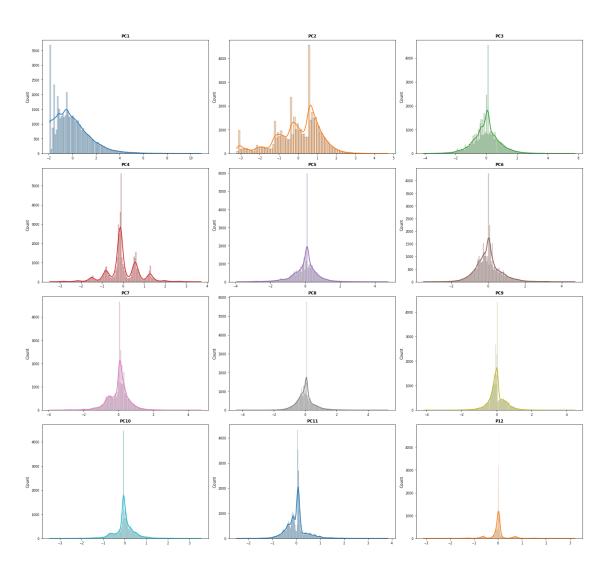
```
7
                        8
                                  9
                                                     11
                                            10
                                                               12
     0 0.291481
                 0.234854
                            0.406509
                                      0.282787
                                               0.293839
                                                         0.429516
     1 0.099394
                  0.086327
                            0.168557
                                      0.104073
                                               0.155922
                                                         0.236538
     2 0.477371
                  0.079394 -0.373427
                                      0.000937 -0.089114 -0.500784
     3 -0.095896
                  0.105624
                            0.707258
                                      0.138852
                                               0.022035 -0.672875
     4 -0.746663 0.111445 -0.196699 0.105288 0.259159 -0.096871
[19]: pca_df = pd.DataFrame(data=pca_features,columns=['PC1', 'PC2', |
       pca_df.describe().apply(lambda s: s.apply('{0:.3f}'.format))
[19]:
                  PC1
                             PC2
                                        PC3
                                                  PC4
                                                             PC5
                                                                        PC6 \
            44502.000
                       44502.000 44502.000
                                             44502.000
                                                       44502.000
                                                                  44502.000
     count
                                     -0.000
     mean
                0.000
                           0.000
                                                -0.000
                                                           -0.000
                                                                     -0.000
     std
                1.464
                           1.187
                                      0.864
                                                0.771
                                                           0.705
                                                                      0.696
     min
               -1.910
                          -3.208
                                     -4.086
                                                -3.485
                                                          -3.926
                                                                     -3.496
     25%
               -1.100
                          -0.714
                                     -0.465
                                                -0.255
                                                          -0.299
                                                                     -0.400
                                     -0.002
     50%
               -0.260
                           0.185
                                                -0.097
                                                           0.094
                                                                      0.018
     75%
                0.790
                           0.809
                                      0.454
                                                0.514
                                                           0.346
                                                                      0.283
               10.878
                           4.703
                                      5.779
                                                3.710
                                                           4.752
                                                                      4.718
     max
                  PC7
                             PC8
                                        PC9
                                                  PC10
                                                            PC11
                                                                        P12
     count
            44502.000
                       44502.000 44502.000
                                             44502.000
                                                       44502.000
                                                                  44502.000
                                     -0.000
                0.000
                           0.000
                                                0.000
                                                          -0.000
                                                                     -0.000
     mean
                0.622
                           0.573
                                      0.492
                                                0.470
                                                           0.433
                                                                      0.397
     std
     min
               -3.943
                          -4.363
                                     -4.163
                                                -3.469
                                                          -2.495
                                                                     -3.101
     25%
               -0.311
                          -0.289
                                     -0.212
                                                -0.116
                                                          -0.221
                                                                     -0.062
     50%
                0.065
                           0.026
                                     -0.016
                                                -0.038
                                                           0.051
                                                                      0.021
     75%
                0.315
                           0.191
                                      0.202
                                                0.189
                                                           0.113
                                                                      0.047
     max
                4.730
                           5.275
                                      4.471
                                                3.543
                                                           3.841
                                                                      3.208
```

En las siguientes gráficas se puede observar la distribución de cada componente

```
fig, axes = plt.subplots(nrows=4, ncols=3, figsize=(20, 20))
axes = axes.flat
columnas_numeric = pca_df.select_dtypes(include=['float64', 'int']).columns

for i, colum in enumerate(columnas_numeric):
    sns.histplot(
    data = pca_df,
    x = colum,
    stat = "count",
    kde = True,
    color = (list(plt.rcParams['axes.prop_cycle'])*2)[i]["color"],
```

Distribución variables numérica



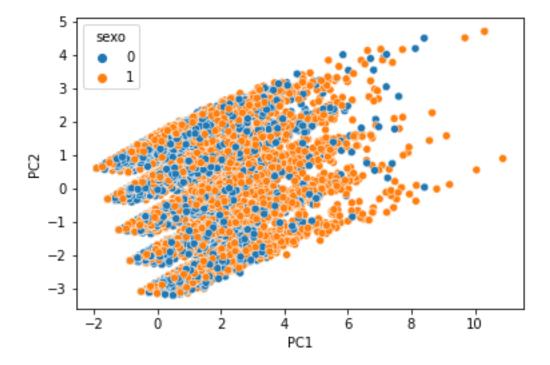
5 3

```
[35]: pca_df['sexo'] = 0
pca_df['sexo'] = np.where(Xr["sexo"] > 0, 1, pca_df['sexo'])
sns.scatterplot('PC1', 'PC2', data=pca_df, hue='sexo')
```

C:\Users\Hpp\anaconda3\lib\site-packages\seaborn_decorators.py:36:
FutureWarning: Pass the following variables as keyword args: x, y. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without an explicit keyword will result in an error or misinterpretation.

[35]: <AxesSubplot:xlabel='PC1', ylabel='PC2'>

warnings.warn(



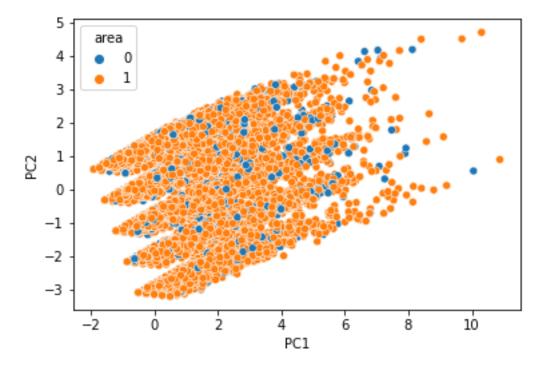
```
[36]: pca_df['area'] = 0
pca_df['area'] = np.where(Xr["area"] > 0, 1, pca_df['area'])
sns.scatterplot('PC1', 'PC2', data=pca_df, hue='area')
```

C:\Users\Hpp\anaconda3\lib\site-packages\seaborn_decorators.py:36:

FutureWarning: Pass the following variables as keyword args: x, y. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without an explicit keyword will result in an error or misinterpretation.

warnings.warn(

[36]: <AxesSubplot:xlabel='PC1', ylabel='PC2'>

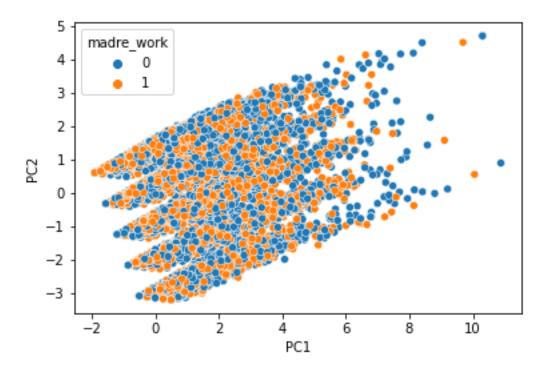


```
[37]: pca_df["madre_work"] = 0
pca_df["madre_work"] = np.where(Xr["madre_work"] > 0, 1, pca_df["madre_work"])
sns.scatterplot('PC1', 'PC2', data=pca_df, hue="madre_work")
```

C:\Users\Hpp\anaconda3\lib\site-packages\seaborn_decorators.py:36:
FutureWarning: Pass the following variables as keyword args: x, y. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without an explicit keyword will result in an error or misinterpretation.

warnings.warn(

[37]: <AxesSubplot:xlabel='PC1', ylabel='PC2'>

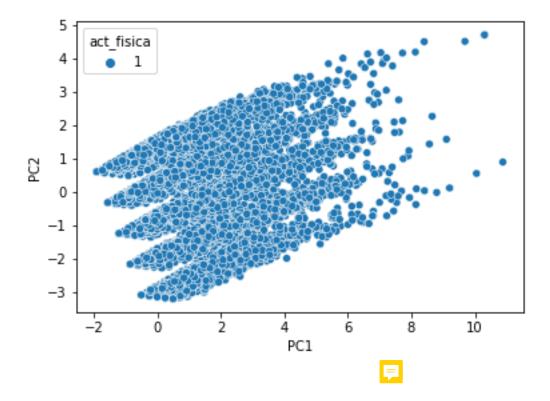


```
[38]: pca_df["act_fisica"] = 0
pca_df["act_fisica"] = np.where(Xr["act_fisica"] > 0, 1, pca_df["act_fisica"])
sns.scatterplot('PC1', 'PC2', data=pca_df, hue="act_fisica")
```

C:\Users\Hpp\anaconda3\lib\site-packages\seaborn_decorators.py:36:
FutureWarning: Pass the following variables as keyword args: x, y. From version 0.12, the only valid positional argument will be `data`, and passing other arguments without an explicit keyword will result in an error or misinterpretation.

warnings.warn(

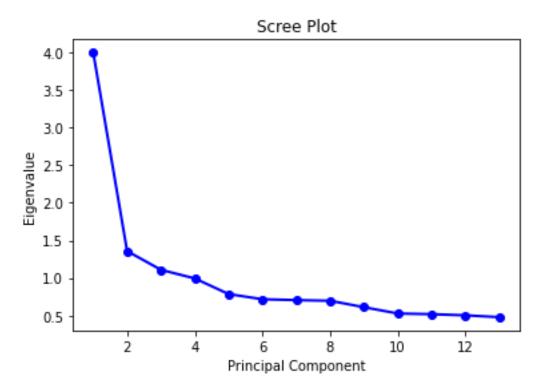
[38]: <AxesSubplot:xlabel='PC1', ylabel='PC2'>



se puede observar que no existen diferencias significativas entre grupos , ya que no se observa una clara separación entre grupos con respecto a ambos ejes del gráfico

6 4

```
[1.59537016e-02, 3.14375943e-02, 1.51335054e-01],
             [ 1.47858798e-01, -1.09890859e-01, 5.16256139e-01],
             [ 4.79056757e-01, 9.20273982e-02, 3.93230433e-02],
             [ 6.13861842e-01, -3.81052232e-02, -2.07578238e-02],
             [6.97308041e-01, 3.09136373e-02, -7.26688327e-04],
             [5.69219552e-01, -2.81948703e-02, -1.42155433e-03],
             [ 5.26432002e-01, 2.16588378e-02, -1.00089677e-02]])
[42]: fa.get_eigenvalues()
[42]: (array([3.99403324, 1.35709614, 1.10826633, 0.99384722, 0.78610007,
             0.71734716, 0.70564612, 0.69689018, 0.61153169, 0.52774476,
             0.51879723, 0.50343626, 0.47926359]),
       array([ 3.39429304, 0.75978216, 0.58015174, 0.2047792, 0.08742927,
              0.06254669, 0.03313104, 0.02348758, -0.02586072, -0.07677543,
             -0.09370486, -0.109146 , -0.17884126]))
[44]: values = np.arange(1,14)
      eigenvalues = pd.DataFrame(data=fa.get_eigenvalues())
      plt.plot(values, eigenvalues.loc[0], 'o-', linewidth=2, color='blue')
      plt.title('Scree Plot')
      plt.xlabel('Principal Component')
      plt.ylabel('Eigenvalue')
      plt.show()
```



```
[45]: fa.get_factor_variance()
[45]: (array([1.73806267, 1.57766252, 1.34554726]),
      array([0.13369713, 0.12135866, 0.10350364]),
       array([0.13369713, 0.25505578, 0.35855942]))
[48]: print(semopy.efa.explore_cfa_model(vector_sks, pval=0.05))
     eta1 = k11 + sk9 + sk10 + sk12
     eta2 = \sim sk7 + sk6
     eta3 =  k4 + sk2 + sk5 + sk11 + sk3 + sk9 + sk1 + sk6 + sk8 + sk12
     eta4 = ~sk11 + sk12 + sk13
[51]: efa_vectors = pd.DataFrame(data = fa.loadings_,

→index=["sk1","sk2","sk3","sk4","sk5","sk6","sk7","sk8","sk9","sk10","sk11","sk12","sk13"])
      efa vectors
[51]:
                  0
                             1
           sk1
      sk2 -0.030897 0.481835 0.244925
      sk3
           0.031844 0.638488 -0.046047
      sk4 -0.000152 0.738733 -0.029548
      sk5 -0.142107 -0.016406 0.846895
      sk6 -0.000270 0.041301 0.522560
      sk7
           0.015954 0.031438 0.151335
      sk8
           0.147859 -0.109891 0.516256
      sk9
           0.479057 0.092027 0.039323
      sk10 0.613862 -0.038105 -0.020758
      sk11 0.697308 0.030914 -0.000727
      sk12 0.569220 -0.028195 -0.001422
      sk13 0.526432 0.021659 -0.010009
       • En el grupo 0 quedará sk9,sk10,sk11,sk12,sk13 (intelectuales-curiosos);
       • En el grupo 1 quedará sk1,sk2,sk3,sk4 (cariñosos);
       • En el grupo 2 quedará sk5,sk6,sk7,sk8(sociables)
     7 5
[52]: Xf=vector_sks
      mod = """
      # measurement model
```

```
eta1 =~ sk9 + sk10 + sk11 + sk12 + sk13
eta2 =~ sk1 + sk2 + sk3 + sk4
eta3 =~ sk5 + sk6 + sk7 + sk8
    """

model = semopy.Model(mod)
out=model.fit(Xf)
print(out)
```

Name of objective: MLW Optimization method: SLSQP Optimization successful.

Optimization terminated successfully

Objective value: 0.164 Number of iterations: 40

Params: 1.393 1.256 1.144 1.351 1.924 1.625 1.781 1.042 0.572 1.143 0.478 0.239 1.429 0.440 0.203 0.156 0.277 0.594 0.700 0.090 0.201 0.160 0.360 0.141 0.087

0.048 0.157 0.057 0.047

```
[53]: model.inspect(mode='list', what="names", std_est=True)
```

```
[53]:
          lval
                op
                    rval
                          Estimate
                                     Est. Std Std. Err
                                                             z-value p-value
           sk9
                                     0.580567
      0
                    eta1
                           1.000000
      1
          sk10
                           1.393283
                                     0.561740
                                               0.016007
                                                           87.039845
                                                                          0.0
                    eta1
      2
                                                                          0.0
          sk11
                    eta1
                           1.256019
                                     0.722753
                                               0.012557
                                                          100.023741
      3
          sk12
                    eta1
                           1.144320
                                     0.543799
                                               0.013443
                                                           85.121476
                                                                          0.0
      4
          sk13
                    eta1
                           1.350601
                                     0.518536
                                               0.016411
                                                            82.29952
                                                                          0.0
      5
           sk1
                    eta2
                           1.000000
                                     0.586883
      6
           sk2
                    eta2
                          1.923701
                                     0.650616
                                               0.019852
                                                           96.902529
                                                                          0.0
      7
           sk3
                    eta2
                           1.625467
                                     0.619708
                                                 0.01727
                                                           94.118211
                                                                          0.0
      8
                                                                          0.0
           sk4
                    eta2
                           1.780563
                                     0.695271 0.017746
                                                          100.334697
      9
           sk5
                    eta3
                           1.000000
                                     0.708895
                                                                          0.0
      10
           sk6
                    eta3
                           1.041920
                                     0.566983
                                                  0.0118
                                                           88.300274
      11
           sk7
                    eta3
                           0.571564
                                     0.186279
                                               0.017336
                                                           32.969296
                                                                          0.0
      12
           sk8
                    eta3
                           1.142588
                                     0.548128
                                               0.013232
                                                                          0.0
                                                           86.352139
      13
          eta1
                ~ ~
                    eta1
                           0.141058
                                     1.000000
                                                0.00241
                                                           58.538392
                                                                          0.0
      14
          eta1
                    eta3
                           0.086894
                                     0.583468
                                               0.001321
                                                           65.772745
                                                                          0.0
                ~ ~
      15
                           0.048393
                                     0.592172
                                               0.000754
                                                                          0.0
          eta1
                ~ ~
                    eta2
                                                           64.196223
      16
          eta3
                    eta3
                           0.157234
                                     1.000000
                                               0.002309
                                                           68.099692
                                                                          0.0
                ~ ~
      17
          eta3
                ~ ~
                    eta2
                           0.056983
                                     0.660446
                                               0.000804
                                                           70.900865
                                                                          0.0
      18
          eta2
                ~ ~
                    eta2
                           0.047344
                                     1.000000
                                               0.000794
                                                           59.602994
                                                                          0.0
      19
                     sk8
                           0.477951
                                     0.699556
                                               0.003866
                                                          123.623766
                                                                          0.0
           sk8
                ~ ~
      20
           sk2
                ~ ~
                     sk2
                           0.238696
                                     0.576699
                                               0.002049
                                                          116.507167
                                                                          0.0
      21
           sk7
                ~ ~
                     sk7
                           1.428924
                                     0.965300
                                               0.009713
                                                          147.114692
                                                                          0.0
      22
          sk12
                    sk12 0.439910
                                     0.704283
                                               0.003382
                                                          130.062828
                                                                          0.0
      23
                                                                          0.0
          sk11
                    sk11
                           0.203470
                                     0.477629
                                               0.002053
                                                           99.087724
      24
                                     0.497468
                                                                          0.0
           sk5
                     sk5
                           0.155650
                                               0.001763
                                                           88.276716
```

```
0.0
     25
          sk9 ~~
                   sk9 0.277440 0.662942 0.002203 125.927537
     26
                  sk10 0.593947 0.684449 0.004635 128.145625
                                                                   0.0
         sk10
                                                                   0.0
     27
         sk13
                   sk13 0.699653 0.731120 0.005281
                                                    132.479658
     28
                   sk1
                        0.090112 \quad 0.655568 \quad 0.000715 \quad 125.973925
                                                                   0.0
          sk1
     29
          sk3
                   sk3 0.200634 0.615962 0.001651
                                                    121.53224
                                                                   0.0
     30
                   sk4 0.160409 0.516598 0.001493 107.443359
                                                                   0.0
          sk4
               ~ ~
                   sk6 0.360284 0.678531 0.002981 120.845663
     31
          sk6
                                                                   0.0
[54]:
     semopy.calc_stats(model)
[54]:
            DoF DoF Baseline
                             chi2 chi2 p-value chi2 Baseline
                                                                          CFI \
                                                   0.0 120370.676623 0.939827
     Value
             62
                          78 7300.357081
                GFI
                       AGFI
                                 NFI
                                           TLI
                                                  RMSEA
                                                        AIC
                                                                         BIC \
     Value 0.939351 0.9237 0.939351 0.924299 0.05122 57.671909 310.067302
            LogLik
     Value 0.164046
[]:
```