

ASSIGNMENT-1

MATH 111

BRANCH-BCA 1st YEAR

ROLL No - Int-820-10720

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1. What is the Probability that the total of two dice will be greater than 9, given that the first die is a 5?

Let X = first die is 5

Let B = total of two dice is greater than 9

$$P(A) = \frac{1}{6}$$

Possible Outcomes for X and B : $\{(5,5), (5,6)\}$

$$P(A \text{ and } B) = \frac{2}{36} = \frac{1}{18}$$

$$P(B|A) = \frac{P(A \cap B)}{P(A)}$$

$$= \frac{1}{18} \times 6$$

$$= \frac{1}{3}$$

2. A bag Contains red and blue marbles. Two marbles are drawn Without Replacement. The Probability Of Selecting a red marble and then a blue marble is 0.28. The Probability Of Selecting a red marble On the first draw is 0.5. What is the Probability Of selecting a blue marble On the Second draw, given that the first marble drawn was red ?

Let A be the event where red marble is selected on the first draw.

Let B be the event where blue marble is selected on the second draw.

Given,

$$P(A) = 0.5 \quad \text{or } \frac{1}{2}$$

$$P(B) = 0.28 \quad \text{or } \frac{28}{100}$$

$$= \frac{7}{25}$$

$$\therefore P(B/A) = \frac{P(A \cap B)}{P(A)}$$

$$P(B/A) = \frac{0.28}{0.5}$$

$$= \frac{28}{50}$$

$$= 0.56$$

3. Find the Probability of Selecting a black Card or a "6" from a deck of 52 Cards.

Total Outcomes = 52

Favourable Outcomes = 26 Black + 2 Six of Hearts and Diamond = 28

So the Probability of selecting a black Card or a 6 from a deck of 52 Card is = $\frac{28}{52}$
 $= \frac{7}{13}$

4. A box contains 4 chocobars and 4 ice creams. Tom eats 3 of them one after another. What is the probability of sequentially choosing 2 chocobars and 1 icecream?

$$\begin{aligned} \text{Probability of choosing 1 chocobar} \\ = \frac{4}{8} = \frac{1}{2} \end{aligned}$$

~~After~~ After taking out 1 chocobar the total number is 7

$$\text{Probability of choosing 2nd chocobar} = \frac{3}{7}$$

$$\begin{aligned} \text{Probability of choosing 1 ice cream out} \\ \text{of a total of 6} = \frac{4}{6} = \frac{2}{3} \end{aligned}$$

So the final probability of choosing 2

$$\begin{aligned} \text{chocobar and 1 icecream} &= \frac{1}{2} \times \frac{3}{7} \times \frac{2}{3} \\ &= \frac{6}{42} \\ &= \frac{1}{7} \end{aligned}$$

5. A single coin is tossed 5 times. what is the probability of getting at least one head?

A single coin is tossed five times
if A, B, C, D, E denotes the number of
getting tails in toss

$$\begin{aligned}
 \text{So the Probability of getting one tail} \\
 &= P(A \cap B \cap C \cap D \cap E) \\
 &= P(A) \cdot P(B) \cdot P(C) \cdot P(D) \cdot P(E) \\
 &= \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \\
 &= \frac{1}{32}
 \end{aligned}$$

$$\begin{aligned}
 \therefore \text{Probability of getting atleast one head} \\
 &= 1 - (\text{Probability of getting one tail}) \\
 &= 1 - \frac{1}{32} \\
 &= \frac{31}{32}
 \end{aligned}$$

6. A Pack Contains 4 blue, 2 red and 3 black Pens.
 If 2 Pens are drawn at random from the Pack,
NOT replaced and then another pen is drawn. What
 is the Probability of drawing 2 blue pens and 1
 black Pen ?

$$\text{Total blue Pens} = 4$$

$$\text{Total Red Pens} = 2$$

$$\text{Total Black Pens} = 3$$

$$\begin{aligned}\text{Total Pens} &= 4 + 2 + 3 \\ &= 9\end{aligned}$$

$$\begin{aligned}\text{Probability of drawing 2 blue pens} &= \frac{{}^4C_2}{{}^9C_2} \\ &= \frac{4 \times 3}{9 \times 8} \\ &= \frac{1}{6}\end{aligned}$$

After this the pen are not replaced which
 reduces the no of pen in the packet
 to 7

(7)

So the Probability of drawing 1 black pen from Pack of 7 pen is

$$\frac{{}^3C_1}{{}^7C_1}$$

$$= \frac{3}{7}$$

Probability of drawing 2 blue and 1

black Pen = $\frac{1}{6} \times \frac{3}{7}$

$$= \frac{3}{42}$$

$$= \frac{1}{14}$$

