

# END SEMESTER EXAMINATION, MARCH-2023

## UNIVERSITY PHYSICS MECHANICS (PHY-1001)

Programme: B. Tech

Full Marks: 60

Semester: 1<sup>st</sup>

Time: 3 Hours

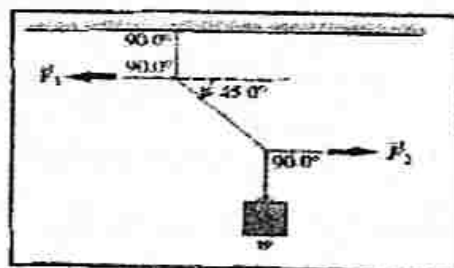
| Subject/Course Learning Outcome | *Taxonomy Level                                  | Ques. Nos. | Marks |
|---------------------------------|--|------------|-------|
| PHY/ a,e                        | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 1          | 6     |
| PHY/ a,e                        | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 2          | 6     |
| PHY/ a,e,g                      | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 3          | 6     |
| PHY/ a,e,g                      | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 4          | 6     |
| PHY/ a,e                        | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 5          | 6     |
| PHY/ a,e                        | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 6          | 6     |
| PHY/ a,e,g                      | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 7          | 6     |
| PHY/ a,e,g                      | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 8          | 6     |
| PHY/ a,e,g                      | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 9          | 6     |
| PHY/ a,e,g                      | L <sub>1</sub> , L <sub>2</sub> , L <sub>3</sub> | 10         | 6     |

\*Bloom's taxonomy levels: Knowledge (L1), Comprehension (L2), Application (L3), Analysis (L4), Evaluation (L5), Creation (L6)

**Answer all questions. Each question carries equal mark.**

- $\vec{A}$  and  $\vec{B}$  are two vectors in x-y plane. Write their scalar and vector product in component form. 2
  - Find the angle between the vectors  $\vec{A} = 2\hat{i} + 3\hat{j} + \hat{k}$  and  $\vec{B} = -4\hat{i} + 2\hat{j} - \hat{k}$  2
  - Vector  $\vec{A}$  has magnitude 2 and vector  $\vec{B}$  has magnitude 3. The angle  $\phi$  between  $\vec{A}$  and  $\vec{B}$  is known to be  $0^\circ$ ,  $90^\circ$ , or  $180^\circ$ . For each of the following situations, state what the value of  $\phi$  must be. (In each situation there may be more than one correct answer.) (a)  $\vec{A} \cdot \vec{B} = 0$  (b)  $\vec{A} \times \vec{B} = 0$  (c)  $\vec{A} \cdot \vec{B} = 6$  (d)  $|\vec{A} \times \vec{B}| = 6$  . 2
- Deduce the relation  $x - x_0 = v_{0x}t + \frac{1}{2}a_x t^2$ . The notations have its usual meaning. 2

- (b) You throw a ball vertically upward from the roof of a tall building. The ball leaves your hand at a point even with the roof railing with an upward speed of  $15.0 \text{ m/s}$ ; the ball is then in free fall. On its way back down, it just misses the railing. Find the ball's position and velocity  $4.0 \text{ s}$  after leaving your hand. 2
- (c) A stone is thrown up vertically with a velocity of  $72 \text{ km/h}$ . Find out the instances at which the magnitudes of its kinetic energy will be half its initial value ( $g = 10 \text{ m/s}^2$ ). 2
3. (a) Derive an expression for the maximum height that can be attained by a projectile. 2
- (b) A batter hits a baseball so that it leaves the bat at speed  $v_0 = 37 \text{ m/s}$ , at an angle  $\alpha_0 = 53.1^\circ$ , at a location where  $g = 9.8 \text{ m/s}^2$ . Find the position of the ball and its velocity at  $t = 2.0 \text{ s}$ . 2
- (c) An airplane's compass indicates that it is headed due north, and its airspeed indicator shows that it is moving through the air at  $240 \text{ km/h}$ . If there is a  $100 \text{ km/h}$  wind from west to east, what is the velocity of the airplane relative to the earth? 2
4. (a) A passenger on a Ferris wheel moves in a vertical circle of radius  $R$  with constant speed  $v$ . The seat remains upright during the motion. Find expressions for the force the seat exerts on the passenger at the top of the circle and at the bottom. 2
- (b) A  $2.49 \times 10^4 \text{ N}$  Rolls-Royce Phantom travelling in the  $+x$ -direction makes an emergency stop; the  $x$ -component of the net force acting on it is  $-1.83 \times 10^4 \text{ N}$ . What is its acceleration? 2
- (c) In the given figure the weight  $w$  is  $60.0 \text{ N}$ . What is the tension in the diagonal string? 2



5. (a) Derive work-energy theorem for a straight-line motion enacted by a constant force. 2
- (b) A  $50.0\text{-kg}$  marathon runner runs up the stairs to the top of Chicago's  $443\text{-m}$ -tall Willis Tower, the tallest building in the United States. To lift herself to the top in  $15.0$  minutes, what must be her average 2



power output? Express your answer in watts, and in horsepower.

- (c) A bullet of 50g and travelling at 80 m/s, hit a sand bag, penetrates it and gets stopped after passing through a distance of 10 cm. Find the force exerted by the sand bag on the bullet. 2
6. (a) Calculate the work done if a spring is elongated by a distance 'x'. 2
- (b) A puck with coordinates  $x$  and  $y$  slides on a level, frictionless air hockey table. It is acted on by a conservative force described by the potential-energy function  $U(x,y) = \frac{1}{2} k (x^2 + y^2)$ . Find a vector expression for the force acting on the puck, and find an expression for the magnitude of the force. 2
- (c) A force of 800 N stretches a certain spring a distance of 0.200 m. What is the potential energy of the spring when it is stretched 0.200 m? 2
7. (a) What is elastic collision? Write general expressions for conservation of kinetic energy and momentum when a body had 1-dimensional elastic collision with another body at rest. 2
- (b) A spring-loaded toy sits at rest on a horizontal, frictionless surface. When the spring releases, the toy breaks into three equal mass pieces, A, B, and C, which slide along the surface. Piece A moves off in the negative  $x$ -direction, while piece B moves off in the negative  $y$ -direction. What are the signs of the velocity components of piece C? 2
- (c) One 110-kg football lineman is running to the right at 2.75 m/s while another 125-kg lineman is running directly toward him at 2.6 m/s. What are the magnitude and direction of the net momentum of these two athletes? 2
8. (a) Analyze static and kinetic friction. 2
- (b) You are trying to move a 500 N crate across a floor. To start the crate moving, you have to pull with a 230 N horizontal force. Once the crate starts to move, you can keep it moving at constant velocity with only 200 N. What are the coefficients of static and kinetic friction. 2
- (c) The flywheel of an engine has moment of inertia 2.50 kg.m<sup>2</sup> about its rotation axis. What constant torque is required to bring it up to an angular speed of 400 rev/min in 8.00 s, starting from rest? 2