

1. Is it possible that an event is independent of itself? If so, when?

ANS: Yes, an event can be independent of itself.

$P(\text{event})=1$ (100% certainty that the event will occur eg death is after birth)

$p(\text{event})=0$ (impossible to happen , eg: 23 hrs in day)

2. Is it always true that if A and B are independent events, then A^c and B^c are independent events? Show that it is, or give a counterexample.

Ans: As A and B are independent

$$P(A \text{ and } B) = P(A) * P(B)$$

$$\text{also } P(A') = 1 - P(A)$$

$$\text{and } P(A \text{ and } B) = P(A \text{ or } B)'$$

$$\text{Thus } P(A' \text{ and } B') = P(A \text{ or } B)'$$

$$= 1 - P(A \text{ and } B)$$

$$= 1 - [P(A) + P(B) - P(A \text{ and } B)]$$

$$= 1 - [P(A) + P(B) - P(A) * P(B)]$$

$$= [1 - P(B)] - P(A)[1 - P(B)]$$

$$= [1 - P(B)] [1 - P(A)]$$

$$= P(B') * P(A')$$

Thus $P(A^c \text{ and } B^c)$ are independent