

## Tutorial #02

EE 100

Q1. The current ' $i$ ' is represented in exponential form as  $i = 20e^{-j2\pi/3}$ . Write its equivalent in

- (i) Rectangular (complex) form  $i = (-10 - j17.32) A$
- (ii) Trigonometric form  $i = 20 [\cos(2\pi/3) - j\sin(2\pi/3)] A$
- (iii) Polar form  $i = 20 \angle -120^\circ A$

Q2. Find the sum of two currents  $i_1 = 5 \angle 30^\circ$  and  $i_2 = 8 \angle -30^\circ$ . Express the sum into

$$i = i_1 + i_2 = 11.26 - j1.5 = 11.35 \angle 7.6^\circ$$

- (i) Rectangular form  $i = 11.26 - j1.5$
- (ii) Trigonometric form  $i = 11.35 [\cos 7.6 + j\sin 7.6]$
- (iii) Exponential form  $i = 11.35 \angle 7.6^\circ$

Q3. A 60-Hz voltage of 115V (rms) is connected to 100- $\Omega$  resistance

(i) Write the time equations for the voltage and the resulting current.

(ii) Show the voltage and current on a time diagram & phasor diagram.

$$(i) \begin{aligned} v(t) &= \sqrt{2} \cdot (115V) \sin[2\pi \cdot 60Hz t] = 115\sqrt{2} \sin(377t) V \\ i(t) &= v(t)/100-\Omega \end{aligned}$$

Q4. A 60Hz voltage of 230V (rms) is connected to 0.265H inductor.

(i) Write the time equations for the voltage and current.

(ii) Show the voltage and current on a time & phasor diagram.

$$\begin{aligned} v(t) &= 230\sqrt{2} \sin(377t) V \\ i(t) &= \frac{230\sqrt{2}}{\omega L} \sin(377t - \pi/2) A \end{aligned}$$



Q5. A 50Hz voltage of 230V (rms) is connected to a 26.5  $\mu\text{F}$  capacitor.

(i) Write the time equations for the voltage and the resultant current.

$$V(t) = 230\sqrt{2} \sin(314t)$$

$$i(t) = 2.71 \sin(314t + \pi/2)$$

(ii) Show the voltage and current on a time & phasor diagram.

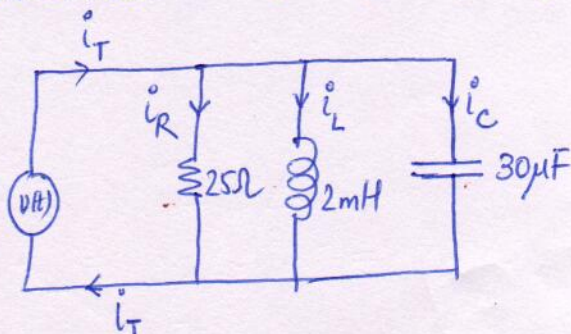
Q6. The voltage applied across 3-branched circuit is given by  $V(t) = 100 \sin(5000t + \pi/4)$ . Calculate the branch currents and the total current.

$$i_R = \frac{V(t)}{R} = 4 \sin(5000t + \pi/4)$$

$$i_L = \frac{1}{L} \int V dt = -10 \cos(5000t + \pi/4)$$

$$i_C = C \frac{dV}{dt} = 15 \cos(5000t + \pi/4)$$

$$i_T = i_R + i_L + i_C$$



Q7. In an alternating circuit, the voltage is given

by  $V = (100 - j50) \text{ V}$  and current is given by

$I = (3 - j4) \text{ A}$ . Determine the real and reactive

power in the circuit.

$$P = 500 \text{ W}$$

$$Q = 250 \text{ VAR}$$

Q8. An inductive circuit draws 10A and 1kW from a 200V, 50Hz a.c. supply. Determine

(i) The impedance of the circuit in Cartesian form ( $a + jb$ );

$$Z = (10 + j17.32) \Omega$$

(ii) The impedance in polar form  $Z \angle \theta$ ;  $Z = 20 \angle 60^\circ$

(iii) The power factor; (iv) The reactive power; (v) The apparent power.

$$\text{pf} = 0.5 \text{ lagging}$$

$$Q = 1732 \text{ VAR}$$

$$S = 2000 \text{ VA}$$



Q9. Two coils 'A' and 'B' are connected in series across a 240V, 50Hz ac supply. The resistance of coil A is  $5\Omega$  and the inductance of coil B is 15mH. If the ~~input~~ real and reactive power supply are 3kW and 2kVAR respectively, determine the inductance of coil A and resistance of coil B. Also determine the voltage across each coil.

$$L_A = 13.2\text{mH (approx.)}; R_B = 8.3\Omega$$

$$V_A = 97.5\text{V}; V_B = 143.5\text{V}$$

Q10. Assume that the voltage applied to a load is  $V = 208\angle -30^\circ\text{V}$  and the current flowing through the load is  $I = 5\angle 15^\circ\text{A}$ .

- (i) Calculate the complex power  $S$  consumed by this load.  $S = 1040\angle -45^\circ\text{VA}$  or  $S = 735(1-j)\text{VA}$
- (ii) Is this load inductive or capacitive? Capacitive (Since  $I$  is leading  $V$ )
- (iii) Calculate the power factor of this load.  $\frac{1}{\sqrt{2}}$
- (iv) Calculate the reactive power consumed or supplied by this load. Does the load consume reactive power from the source or supply it to the source?  $Q = -735.5\text{VAR}$   
Supply to the source. (Since the load is capacitive)