



# Memory Protection

- Memory protection implemented by associating protection bit with each frame to indicate if read-only or read-write access is allowed
  - Can also add more bits to indicate page execute-only, and so on
- **Valid-invalid** bit attached to each entry in the page table:
  - “valid” indicates that the associated page is in the process’ logical address space, and is thus a legal page
  - “invalid” indicates that the page is not in the process’ logical address space
  - Or use **page-table length register (PTLR)**
- **Any violations result in a trap to the kernel**





# Valid (v) or Invalid (i) Bit In A Page Table

14 bit  
page size - 2KB → 8 pages

0  
10468

00000	page 0
	page 1
	page 2
	page 3
	page 4
10,468	page 5
12,287	

frame number		valid-invalid bit	
0	2	v	
1	3	v	
2	4	v	
3	7	v	
4	8	v	
5	9	v	
6	0	i	3
7	0	i	3

page table

internal fragmentation

0	
1	
2	page 0
3	page 1
4	page 2
5	
6	
7	page 3
8	page 4
9	page 5
	⋮
	page n





# Shared Pages

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## □ Shared code

- One copy of read-only (**reentrant**) code shared among processes (i.e., text editors, compilers, window systems)
- Similar to multiple threads sharing the same process space
- Also useful for interprocess communication if sharing of read-write pages is allowed

## □ Private code and data

- Each process keeps a separate copy of the code and data
- The pages for the private code and data can appear anywhere in the logical address space





# Shared Pages Example

ed 1
ed 2
ed 3
data 1

process  $P_1$

3
4
6
1

page table  
for  $P_1$

ed 1
ed 2
ed 3
data 2

process  $P_2$

3
4
6
7

page table  
for  $P_2$

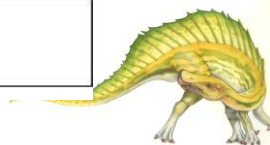
ed 1
ed 2
ed 3
data 3

process  $P_3$

3
4
6
2

page table  
for  $P_3$

0	
1	data 1
2	data 3
3	ed 1
4	ed 2
5	
6	ed 3
7	data 2
8	
9	
10	
11	





# Structure of the Page Table

- ❑ Memory structures for paging can get huge using straight-forward methods  
Consider a 32-bit logical address space as on modern computers
  - ❑ Page size of 4 KB ( $2^{12}$ )
  - ❑ Page table would have 1 million entries ( $2^{32} / 2^{12}$ )
  - ❑ If each entry is 4 bytes -> 4 MB of physical address space / memory for page table alone
    - ▶ That amount of memory used to cost a lot
    - ▶ Don't want to allocate that contiguously in main memory
- ❑ Hierarchical Paging
- ❑ Hashed Page Tables
- ❑ Inverted Page Tables





# Hierarchical Page Tables

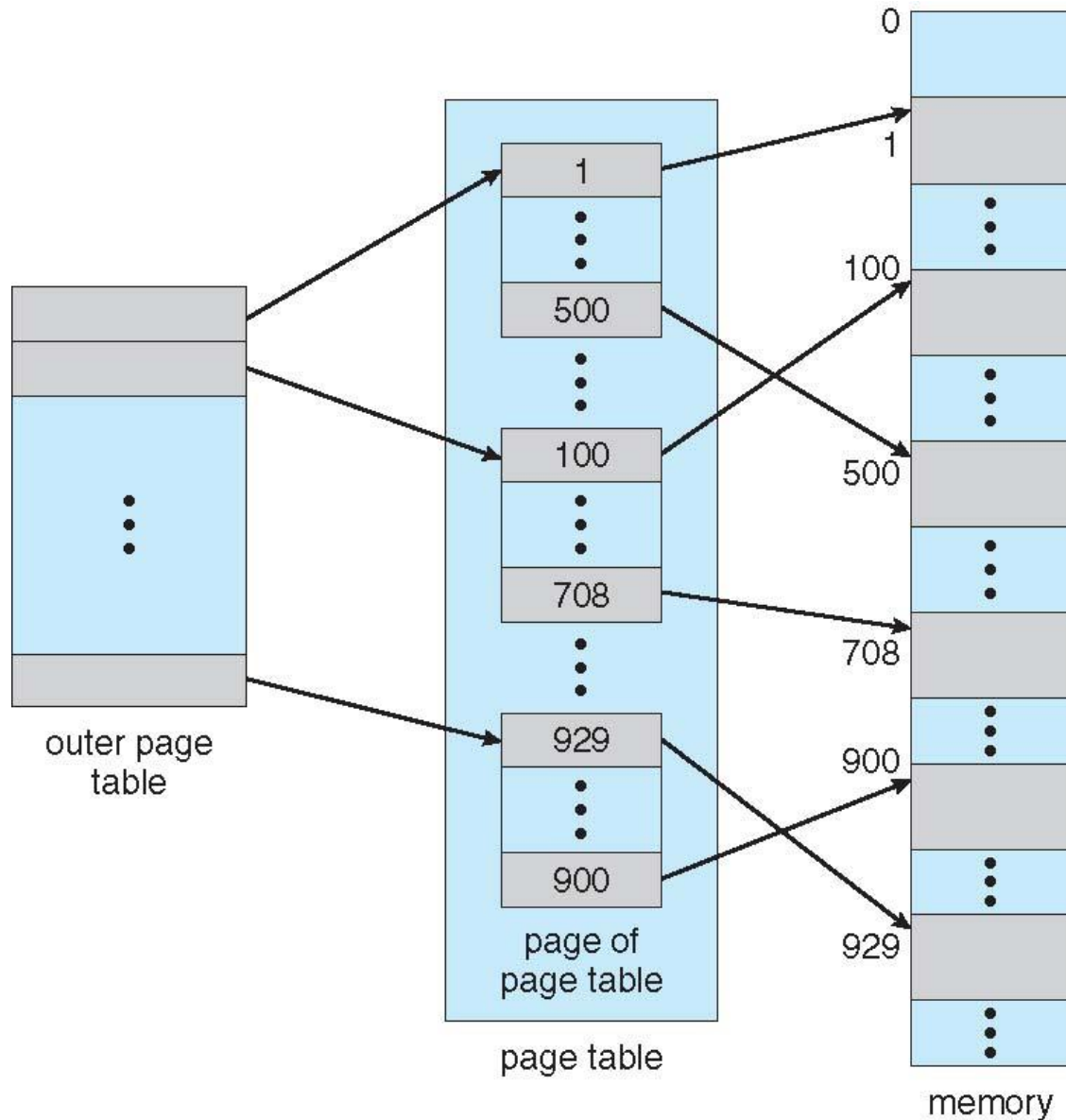
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- Break up the logical address space into multiple page tables
- A simple technique is a two-level page table
- We then page the page table





# Two-Level Page-Table Scheme





# Two-Level Paging Example

- A logical address (on 32-bit machine with 1K page size) is divided into:
  - a page number consisting of 22 bits
  - a page offset consisting of 10 bits
- Since the page table is paged, the page number is further divided into:
  - a 12-bit page number
  - a 10-bit page offset
- Thus, a logical address is as follows:

page number		page offset
$p_1$	$p_2$	$d$
12	10	10

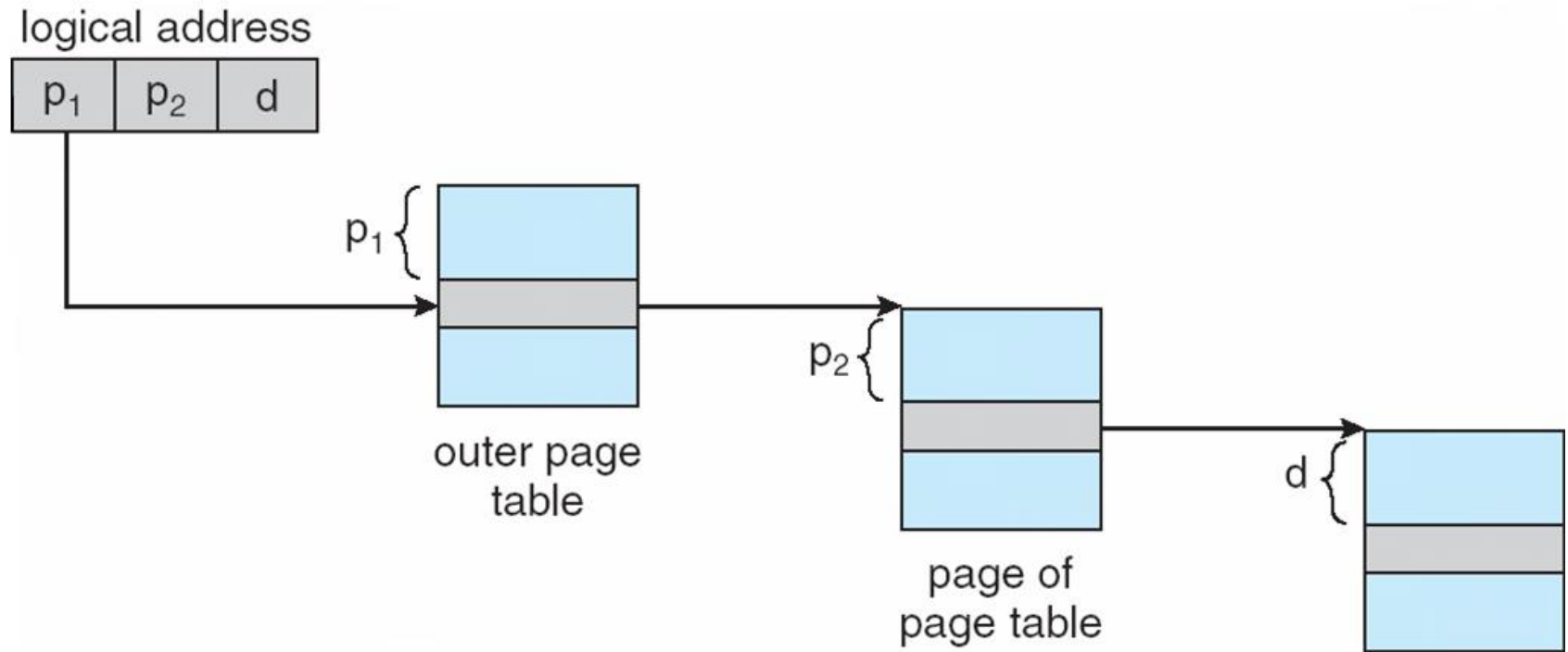
- where  $p_1$  is an index into the outer page table, and  $p_2$  is the displacement within the page of the inner page table
- Known as **forward-mapped page table**







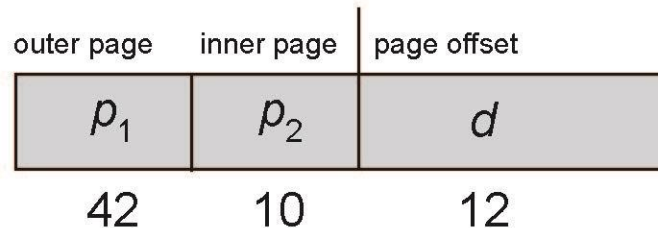
# Address-Translation Scheme





# 64-bit Logical Address Space

- Even two-level paging scheme not sufficient
- If page size is 4 KB ( $2^{12}$ )
  - Then page table has  $2^{52}$  entries
  - If two level scheme, inner page tables could be  $2^{10}$  4-byte entries
  - Address would look like



- Outer page table has  $2^{42}$  entries or  $2^{44}$  bytes
- One solution is to add a  $2^{\text{nd}}$  outer page table
- But in the following example the  $2^{\text{nd}}$  outer page table is still  $2^{34}$  bytes in size
  - ▶ And possibly 4 memory access to get to one physical memory location





# Three-level Paging Scheme

outer page	inner page	offset
$p_1$	$p_2$	$d$
42	10	12

2nd outer page	outer page	inner page	offset
$p_1$	$p_2$	$p_3$	$d$
32	10	10	12





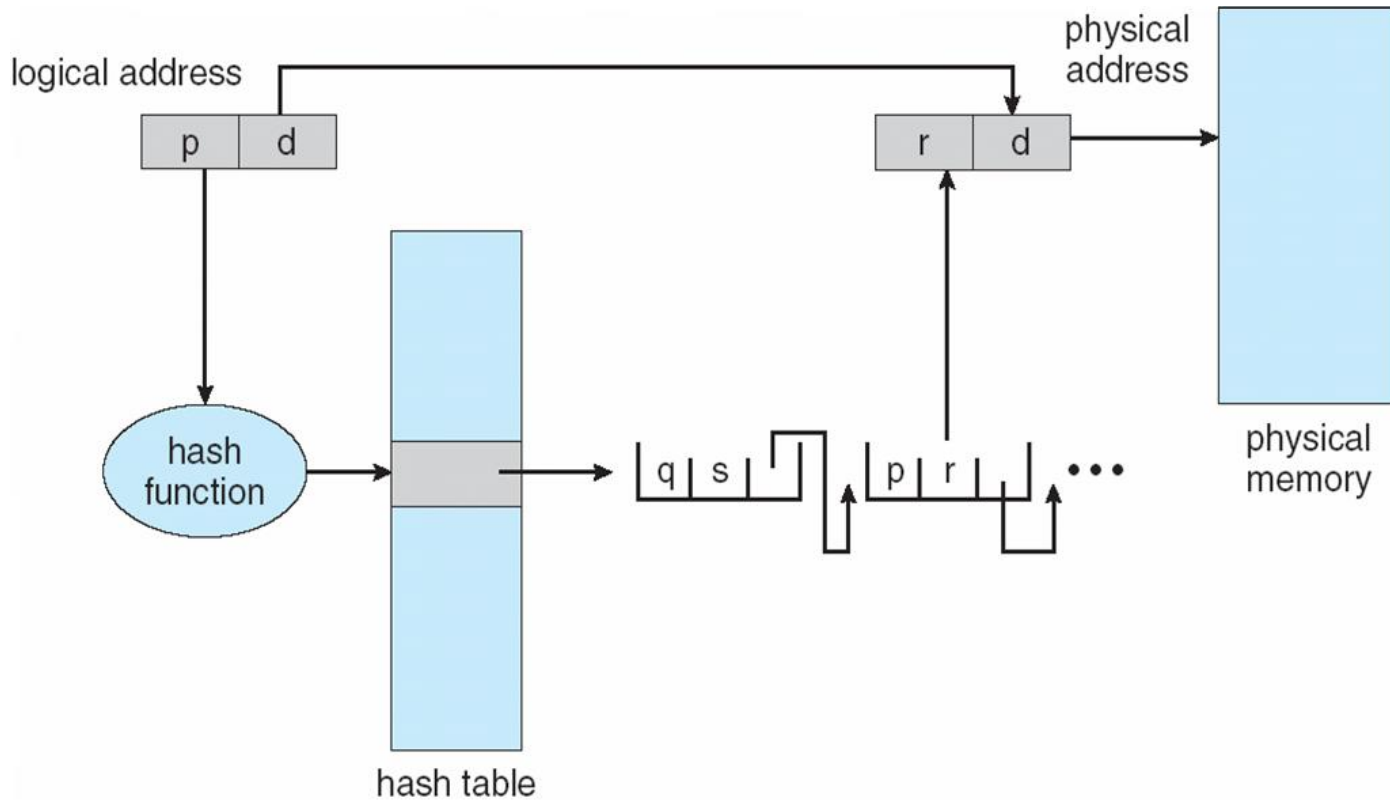
# Hashed Page Tables

- ❑ Common in address spaces  $> 32$  bits
- ❑ The virtual page number is hashed into a page table
  - ❑ This page table contains a chain of elements hashing to the same location
- ❑ Each element contains (1) the virtual page number (2) the value of the mapped page frame (3) a pointer to the next element
- ❑ Virtual page numbers are compared in this chain searching for a match
  - ❑ If a match is found, the corresponding physical frame is extracted
- ❑ Variation for 64-bit addresses is **clustered page tables**
  - ❑ Similar to hashed but each entry refers to several pages (such as 16) rather than 1
  - ❑ Especially useful for **sparse** address spaces (where memory references are non-contiguous and scattered)





# Hashed Page Table





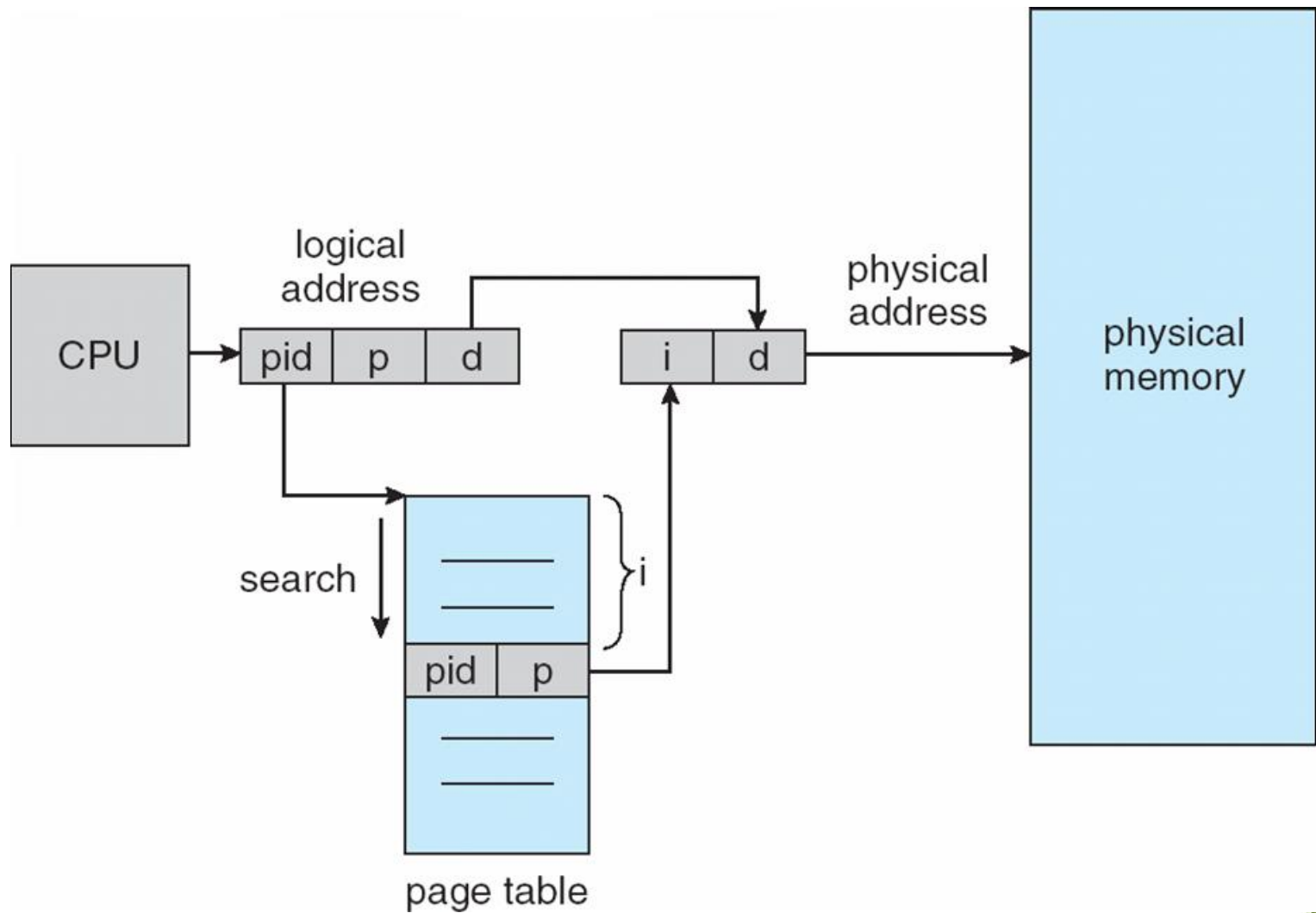
# Inverted Page Table

- ❑ Rather than each process having a page table and keeping track of all possible logical pages, track all physical pages
- ❑ One entry for each real page of memory
- ❑ Entry consists of the virtual address of the page stored in that real memory location, with information about the process that owns that page
- ❑ Decreases memory needed to store each page table, but increases time needed to search the table when a page reference occurs
- ❑ Use hash table to limit the search to one — or at most a few —





# Inverted Page Table Architecture



# End of Chapter 8

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