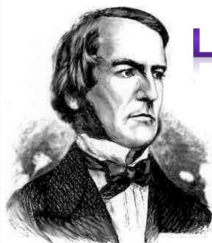


Figure Source:Google



**George Boole,  
(1815-1864)**

# LOGIC GATES

**Did you know?**

**George Boole** Inventor of the idea of logic gates. He was born in Lincoln, England and he was the son of a shoemaker in a low class family. We describe the functions that logic gates use as parts of Boolean Algebra.

All – describe the functions of logic gates. (C)  
Most – construct truth tables for logic gates. (C+)  
Some – Design a circuit to use logic gates to control circuits. (B+)

Figure Source:Google

## • Positive and Negative Logic:

- Binary: Logic "0" state and Logic "1" state.
- Digital systems use two different voltage levels to represent the two states.

⇒ Example: Two voltage levels 0 volts and +5 volts system,

- Positive logic system: "0" state => 0 volts  
"1" state => +5 volts
- Negative logic system: "0" state => +5 volts  
"1" state => 0 volts

- **Logic Gate:** Quite similar to your home door gate.
- Transistor is used as a switch to get functionality like gate.
- The most basic building blocks of any digital system including computers.
- The logic Gates are used to represents the logic functions to design an digital system.

- **Basic building blocks:**

- **Basic Gates:**

- NOT Gate
- AND Gate
- OR Gate

- **Universal Gates:**

- NAND Gate
- NOR Gate

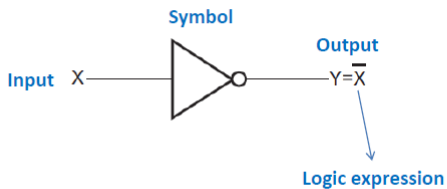
- **Other Gates:**

- XOR Gate

- XNOR Gate

- **XOR and XNOR Gates are used in air thematic circuits, Comparator circuits, code converter etc.**

- NOT Gate:



Truth-table

X	Y
0	1
1	0

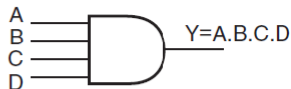
- **AND Gate:**



A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

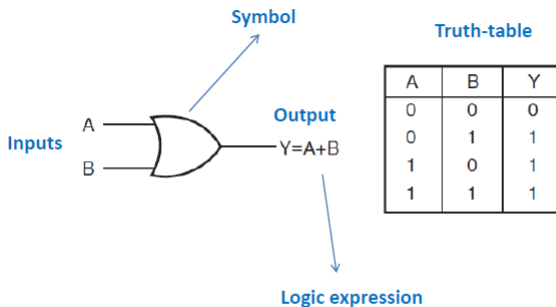


- 3-input and 4-input AND Gate:

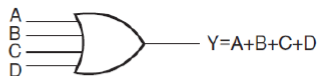
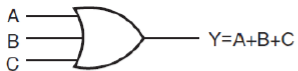


A	B	C	D	Y
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

- **OR Gate:**



- 3-input and 4-input OR Gate:

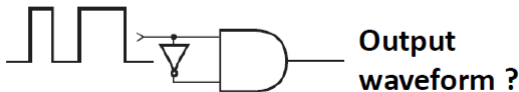


Truth-table of  
3 input OR gate

A	B	C	Y
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

- **Exercise:**
- **Design an 3-input AND gate logic circuit using only 2-input AND gates.**
- **Design an 4-input OR gate logic circuit using only 2-input OR gates.**
- **Design an 4-input AND gate logic circuit using only 2-input AND gates.**
- **Design chain of two inverter logic circuit.**

- Exercise:

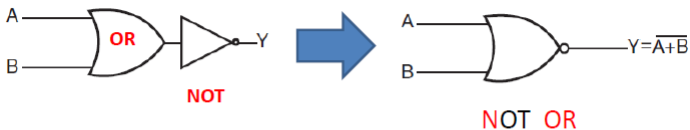


- **NAND Gate:**



A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

- NOR Gate:



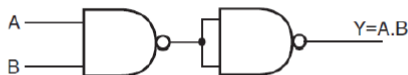
A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

- **NAND Gate: Universal**

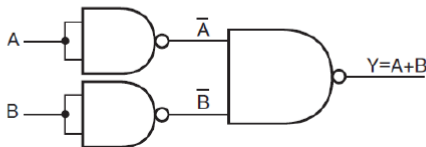
**NOT gate**



**AND gate**



**OR gate**



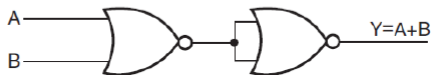


- **NOR Gate: Universal**

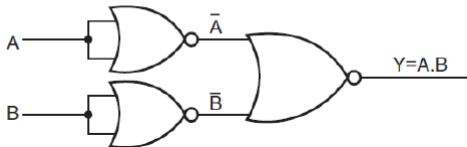
**NOT gate**



**OR gate**



**AND gate**



- **Exercise:**
- **Design an 3-input AND gate logic circuit using only 2-input NAND gates.**
- **Design an 4-input OR gate logic circuit using only 2-input NOR gates.**
- **Design an 4-input NAND gate logic circuit using only 2-input NAND gates.**
- **Design an 4-input OR gate logic circuit using only 2-input NAND gates.**

- **Exclusive-OR Gate or X-OR GATE:**



A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

$$Y = (A \oplus B) = \overline{A}B + A\overline{B}$$

- **Exclusive-NOR Gate or X-NOR GATE:**



A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

$$Y = (\overline{A \oplus B}) = (A.B + \overline{A}.\overline{B})$$

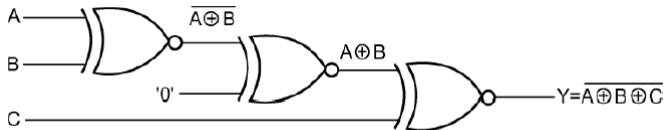
- **Problem (0):**
- **Design an NOT logic circuit using a 2-input Ex-OR gate.**

- **Solution(0):**



- **Problem(1):**
- **Design an 3-input Ex-NOR logic circuit using 2-input Ex-NOR gates.**

- **Solution(1):**





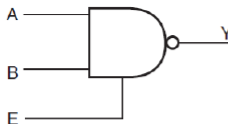
- **Exercise:**
- **Design an 3-input X-OR gate logic circuit using only 2-input X-OR gates.**
- **Design an 4-input X-OR gate logic circuit using only 2-input X-OR gates.**
- **Design an 3-input X-NOR gate logic circuit using only 2-input X-NOR gates.**
- **Design an 4-input X-OR gate logic circuit using only 3-input X-OR gates.**

- **Tristate Gates:**
- **high-impedance state 'Z'.**
- **Active states : Logic '1' and logic '0'.**
- **high-impedance state 'Z' is controlled by an external input known as ENABLE.**

- **ENABLE** decides whether the gate is in active or high-impedance state.
- **An advantage: Inputs and Outputs can be connected in parallel to a common bus line.**

- **Active HIGH ENABLE:**

Active HIGH ENABLE  
NAND gate

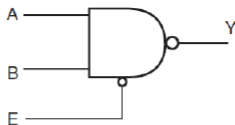


A	B	E	Y
0	0	0	Z
0	0	1	1
0	1	0	Z
0	1	1	1
1	0	0	Z
1	0	1	1
1	1	0	Z
1	1	1	0

Z= High Impedance state

- **Active LOW ENABLE:**

Active LOW ENABLE  
NAND gate



A	B	E	Y
0	0	0	1
0	0	1	Z
0	1	0	1
0	1	1	Z
1	0	0	1
1	0	1	Z
1	1	0	0
1	1	1	Z

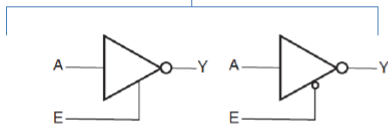
Z= High Impedance state

- **Buffer Circuit:**
- **Load driving capability.**
- **Useful in bus-oriented systems.**
- **Driving capability is higher than logic Gates.**
- **Useful in bus-oriented systems.**
- **Normally, the buffers are tristate devices.**

- **Types: Inverting and Non-inverting.**
- **Driver is even larger load-driving capability than a buffer.**

## • Example:

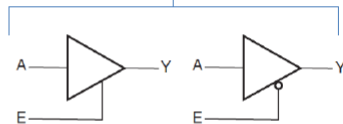
### Inverting buffers



A	E	Y
X	0	Z
0	1	1
1	1	0

A	E	Y
X	1	Z
0	0	1
1	0	0

### Non-inverting Buffers



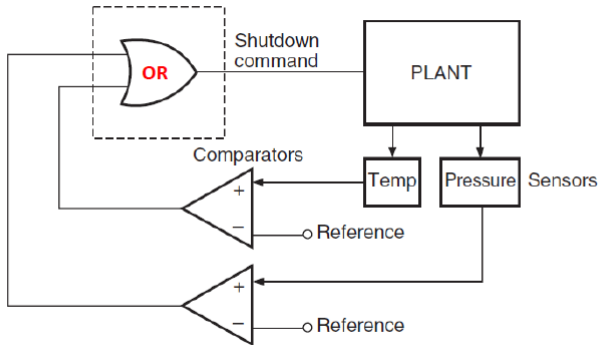
A	E	Y
X	0	Z
0	1	0
1	1	1

A	E	Y
X	1	Z
0	0	0
1	0	1

Z = High Impedance State



- **Application:**



- **Application:**

