Assignment 1

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Abstract - This document contains solution to find the coordinates of a point which divides a line segment internally and Externally

Vector

Question 21: Find the coordinates of the points which divide, internally and externally, the line joining the point (a+b, a-b) to the point (a-b, a+b) in the ratio a: b.

Solution:

Let us consider P be the point which divides the AB line segment in the ratio a: b internally and externally. Given that the coordinates of A point= (a+b, a-b) and coordinates of B point= (a-b, a+b).

So we can write **A** and **B** as product of a constant matrix and a vector,

$$\mathbf{A} = \begin{bmatrix} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} \end{bmatrix}^{\top} = \begin{bmatrix} a+b \\ a-b \end{bmatrix}^{\top} = \begin{bmatrix} a+b & a-b \end{bmatrix}$$
(1)

$$\mathbf{B} = \begin{bmatrix} \begin{pmatrix} 1 & -1 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} \end{bmatrix}^{\top} = \begin{bmatrix} a - b \\ a + b \end{bmatrix}^{\top} = \begin{bmatrix} a - b & a + b \end{bmatrix}$$

and

$$\frac{\mathbf{AP}}{\mathbf{PB}} = \frac{a}{b} \tag{3}$$

For finding internal division coordinates:

$$b\mathbf{AP} = a\mathbf{BP} \tag{4}$$

$$b(\mathbf{A} - \mathbf{P}) = a(\mathbf{P} - \mathbf{B}) \tag{5}$$

Solving the equation we get:

$$\mathbf{P}(a+b) = a\mathbf{B} + b\mathbf{A} \tag{6}$$

$$\mathbf{P} = \frac{a}{a+b} \begin{bmatrix} a-b & a+b \end{bmatrix} + \frac{b}{a+b} \begin{bmatrix} a+b & a-b \end{bmatrix}$$
 (7)

Solving this we get coordinates of P:

$$\mathbf{P} = \begin{bmatrix} \frac{a(a-b)+b(a+b)}{a+b} & \frac{a(a+b)+b(a-b)}{a+b} \end{bmatrix}$$
(8)

For finding external division coordinates:

$$b\mathbf{AP} = a\mathbf{BP} \tag{9}$$

$$b(\mathbf{A} - \mathbf{P}) = a(\mathbf{B} - \mathbf{P}) \tag{10}$$

Solving the equation we get:

$$\mathbf{P}(a-b) = a\mathbf{B} - b\mathbf{A} \tag{11}$$

$$\mathbf{P} = \frac{a}{a-b} \begin{bmatrix} a-b & a+b \end{bmatrix} - \frac{b}{a-b} \begin{bmatrix} a+b & a-b \end{bmatrix}$$
(12)

Solving this we get coordinates of \mathbf{P} :

$$\mathbf{P} = \begin{bmatrix} \frac{a(a-b)-b(a+b)}{a-b} & \frac{a(a+b)-b(a-b)}{a-b} \end{bmatrix}$$
 (13)

Result

Plot of coordinates of the points obtained from Python code considering a= 6, b=3 is shown below

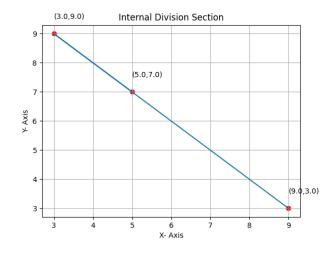


Figure 1: Internal Division Section

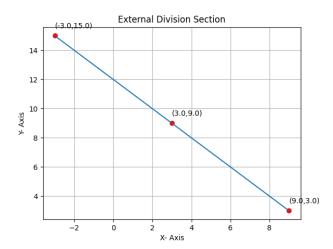


Figure 2: External Division Section