AMATH 522: Problem Set 2

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1 Theory

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2 Simulating Dwell times

```
% Dwell times
     clear all; close all;
rng('shuffle')
     numsteps = 1000000 ; %number of timesteps simulated
     A = [0.98, 0.1, 0;
     0.02, 0.7, 0.05;
     0 , 0.2 , 0.95;] ;
10
     \%list of states on this realization. xlist(k)=1 means in state 1 at
11
12
    %timestep k, etc
     states=zeros(1, numsteps);
13
14
15
    %initial state
     states(1)=1;
17
     for k=1:numsteps-1
18
19
     %uniformly distributed random number - will use for transitions from
20
     \%timestep k to current timestep k+1
21
     rd=rand ;
22
23
     if rd < A(1, states(k)) % for transition FROM states(k) to state 1
24
25
     states(k+1)=1;
     elseif rd \langle A(2, states(k)) + A(1, states(k)) \rangle % for transition FROM states(k) to
       state 1=2
     states(k+1)=2;
28
     states(k+1)=3;
29
     end
30
31
     end;
32
33
34
     figure
35
     set (gca, 'FontSize', 18)
36
     plot (1: numsteps, states, '.', 'MarkerSize', 20) xlabel ('timestep', 'FontSize', 16) ylabel ('state', 'FontSize', 16)
37
38
39
40
     rstates= 2*ones(1,numsteps);
41
     Ind= find(states==1 | states ==2);
42
43
     rstates(1, Ind)=1;
     figure;
```

```
rstates(states)=1;
45
46
     plot(rstates);
     strt = states(1);
47
48
     time=1;
     dwellist1 = [\,]\,;
49
     dwellist2 = [];
50
51
52
     for k=2:length(rstates)
     if rstates(k) = strt
53
54
55
     dwell = k-time;
56
57
     if strt ==1
58
     dwellist1 = [dwellist1 dwell];
59
60
     dwellist2 = [dwellist2 dwell];
61
62
     end;
     strt =rstates(k);
63
     time=k;
64
65
     end;
66
67
     end;
68
     figure;
     [counts, centers] = hist(dwellist2,70);
set(gca, 'FontSize',18)
69
70
71
     bar(centers, counts);
     xlabel('bins', 'FontSize',16)
72
     ylabel ('Histogram of dwell times', 'FontSize', 16)
73
74
     figure
     f = fit (centers', counts', 'exp1');
75
     set(gca, 'FontSize',18);
76
     plot(f, centers, counts);
77
78
     xlabel('bins','FontSize',16)
ylabel('Exponential fit','FontSize',16)
79
80
81
```

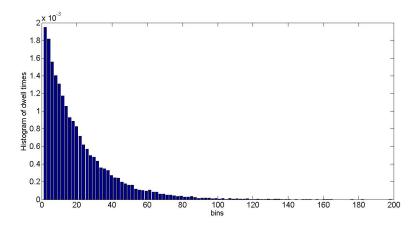


Figure 1: The histogram of dwell times

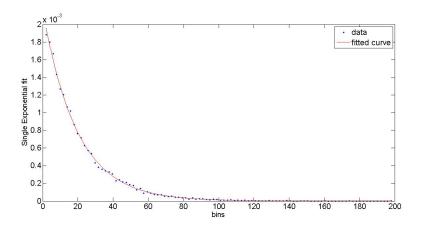


Figure 2: The single exponential fit to the histogram

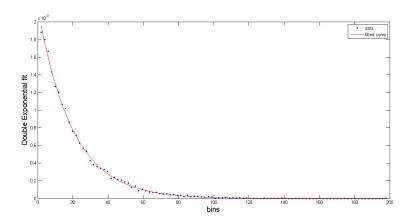


Figure 3: The double exponential fit to the histogram

Obviously, the single exponential function is not a good fit because there are two eigenvalues for the system staying in the closed state.

3 Neural Spiking

```
% Neural Spiking
        clear all;
        parpool; % Parallel computing because this takes a while
       A = [0.98, 0.1, 0;
       0.02, 0.7, 0.05;
       0 , 0.2 , 0.95; ;
       [T,L] = eigs(A);
       prb =T(:,1);
       probin = [prb(1)+prb(2); prb(3);];
12
       probin =probin./sum(probin);
13
       \mathbf{B} = [0.9 \ 0.1 \ 0; \ 0.1 \ 0.6 \ 0.1; \ 0 \ 0.3 \ 0.9;];
15
16
        [T,L] = eigs(B);
       \mathbf{prb} = \mathbf{T}(:,1);
```

```
probout = [prb(1)+prb(2); prb(3);];
20
         probout =probout./sum(probout);
21
         Popenout= 0.4;
22
23
         Popenin = 0.6;
         Nin = 100;
24
         {\color{red}Nout} \ = 50;
25
26
         parfor T=0:1:Nin-1
27
           sum=0;
28
            for w = 0:1:Nout
               sum=sum+ binopdf(w, Nout, Popenin)*(1-binocdf(T+w, Nin, Popenout));
29
               if T+w>Nin
30
31
                  break;
               end
32
            \quad \text{end} \quad
33
           p(T+1) = sum;
34
35
         end
         Nin = 10;
36
         Nout =5;
37
         parfor T=0:1:Nin-1
38
39
            sum = 0;
            for w = 0:1:Nout
40
               \color{red} sum = sum + \hspace{1mm} binopdf(w, \hspace{1mm} Nout, Popenin) * (1 - binocdf(T + w, \hspace{1mm} Nin, Popenout)); \\
41
42
                 break;
43
               end
45
            end
           p2(T+1) = sum;
46
47
         \quad \text{end} \quad
48
         \frac{Nin}{}=1000;
49
50
         Nout =500;
         parfor T=0:1:Nin-1
51
52
            sum = 0;
            for w = 0:1:Nout
53
               \color{red} sum = sum + \hspace{0.1cm} binopdf(w, \hspace{0.1cm} Nout, Popenin) * (1 - binocdf(T + w, \hspace{0.1cm} Nin, Popenout)); \\
54
55
               if T+w>Nin
56
                  break;
               end
57
58
            \quad \text{end} \quad
            p3(T+1) = sum;
59
60
         end
61
```

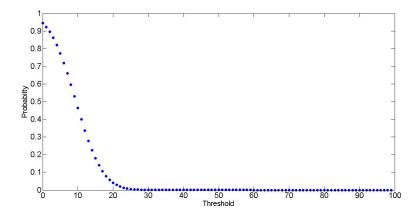


Figure 4: Distribution with $N_{inward} = 100$ and $N_{outward} = 50$

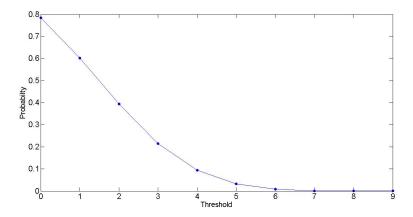


Figure 5: Distribution with $N_{inward}=10$ and $N_{outward}=5$

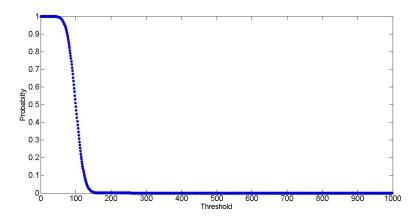


Figure 6: Distribution with $N_{inward} = 1000$ and $N_{outward} = 500$

As we increase the number of channels, the distribution begins to look more and more like a guassian distribution, a good representation of the coin flipping.