

# Inverse optimization

Discount

Dec 2019

$$\begin{aligned}
 \sum_{i=1}^m (e_{ij} - f_{ij} + a_{ij}) y_i &= c_j \\
 \sum_{j=1}^n (e_{ij} - f_{ij} + a_{ij}) x_j^0 &\geq b_i \\
 \sum_{i=1}^m b_i y_i &\leq v_0
 \end{aligned} \tag{1}$$

$$T(e, f, y) = \min \sum_i \sum_j (e_{ij} + f_{ij}) + \sum_{j=1}^n \lambda_j g_j(e) + \sum_{i=1}^m \mu_i f_i(e) \tag{2}$$

$$g_j(e, f, y) = \sum_{i=1}^m (e_{ij} - f_{ij} + a_{ij}) y_i - c_j = 0 \tag{3}$$

$$f_i(e, f, y) = b_i - \sum_{j=1}^n (e_{ij} - f_{ij} + a_{ij}) x_j^0 \leq 0 \tag{4}$$

$$h(y) = \sum_{i=1}^m b_i y_i - v_0 \tag{5}$$

$$K(e, f) = e_{ij} f_{ij} \tag{6}$$

$$M(e) = -e_{ij} \tag{7}$$

$$N(f) = -f_{ij} \tag{8}$$

$$V_j = v_j \quad X_i = x_i - q_i x_j \quad = u_j + \sum_{i \neq j} q_i \tag{9}$$

$$V_i = v_i - q_i v_j \quad X_j = x_j \quad U_i = u_i$$