

End Point of the rp Process on Accreting Neutron Stars

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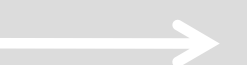
And Introduction to X-ray binary pulsars

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核天体物理

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I. General Introduction
II. Paper's Introduction
III. Method
IV. Result
V. Discussion

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Contents

I. General Introduction: Neutron stars & X-ray binaries

Neutron stars: compact celestial object with $M \sim 1.4 M_{\text{sun}}$, $R \sim 10 \text{ km}$.

• Landau 1932: “gigantic nucleus”

considerations)¹. We expect that this must occur when the density of matter becomes so great that atomic nuclei come in close contact, forming one gigantic nucleus.

(in between: Chadwick 1932: neutron’s discovery)

• Baade & Zwicky 1934: “neutron star”
(result from supernovae)

super-nova now confronts us. With all reserve we advance the view that a super-nova

represents the transition of an ordinary star into a *neutron star*, consisting mainly of neutrons.

Such a star may possess a very small radius and an extremely high density. As neutrons can be

• Oppenheimer & Volkoff 1939: Tolman-Oppenheimer-Volkoff Equations
(GR spherical static ideal fluid: gravity v.s. pressure)

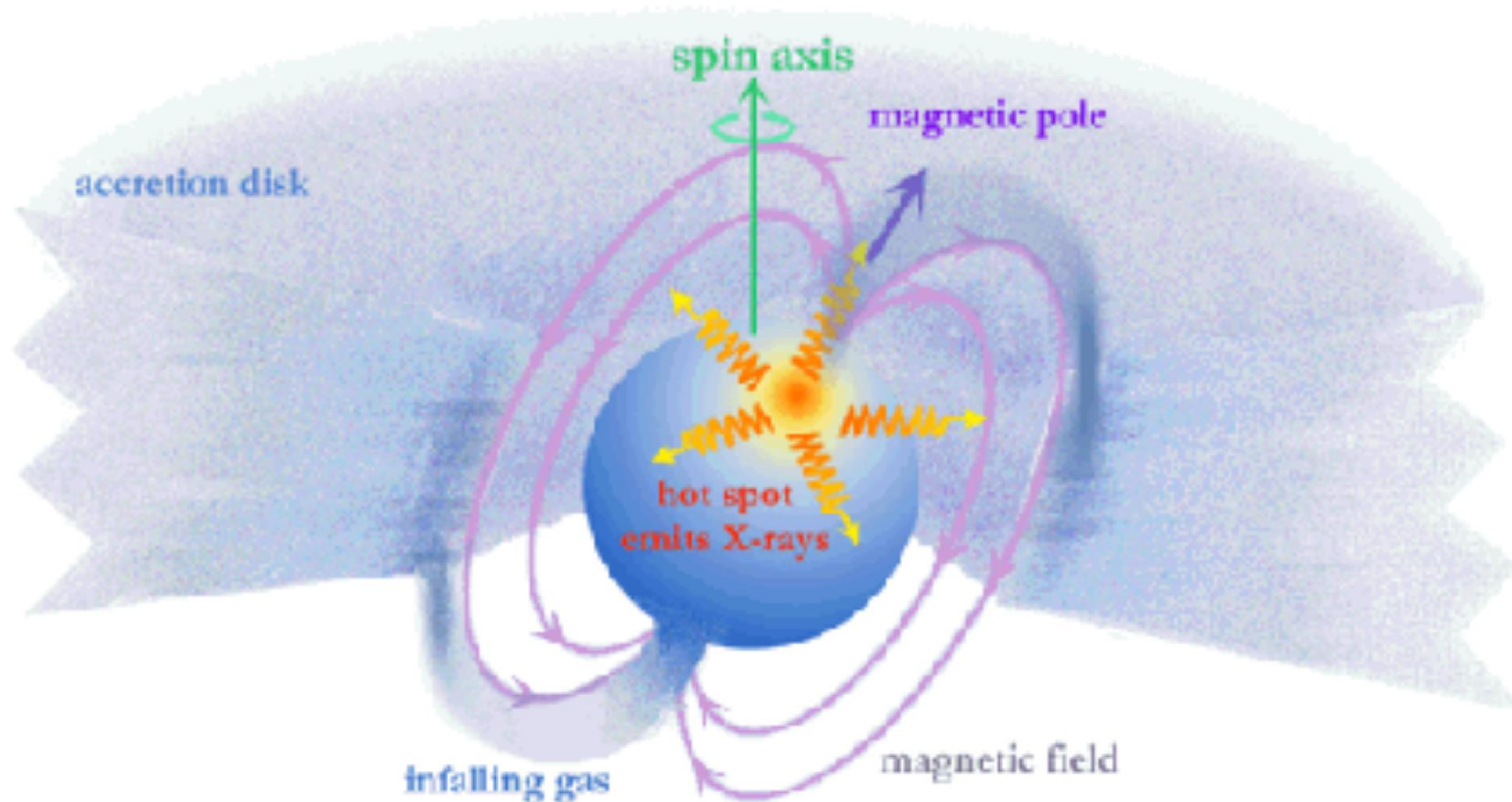
$$\frac{du}{dr} = 4\pi\rho(p)r^2$$

$$\frac{dp}{dr} = -\frac{p + \rho(p)}{r(r - 2u)} [4\pi p r^3 + u]$$

What is $\rho(p)$? $\Rightarrow \Rightarrow$ Equation of State problem.

Neutron stars' electromagnetic radiation:
——From radio, optical, X-ray, to gamma ray.

An example: accreting neutron star (NS) in a binary.
→→ can cause thermal X-ray emission.



A sketch for accreting neutron star's X-ray emission.
https://chandra.harvard.edu/xray_sources/neutron_stars.html

NS accretes matter from
the companion star



NS surface $\rho \uparrow$, $T \uparrow$, $p \uparrow$



Thermonuclear burning
High-energy photons emission

Stable

Unstable

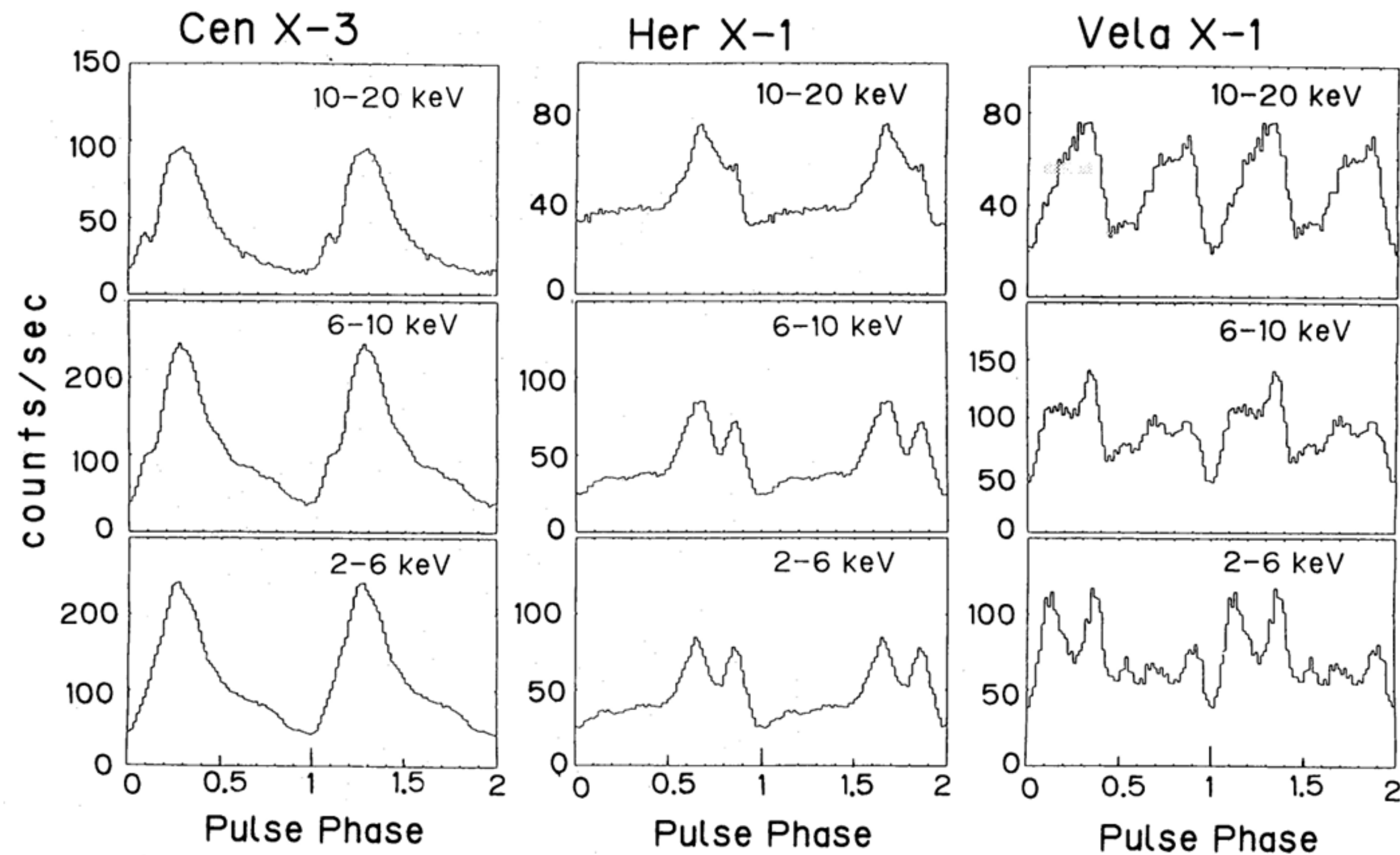
Accreting
X-ray **pulsars**
(AXPs)

Giacconi et al. 1971
ApJ, 167, 67.

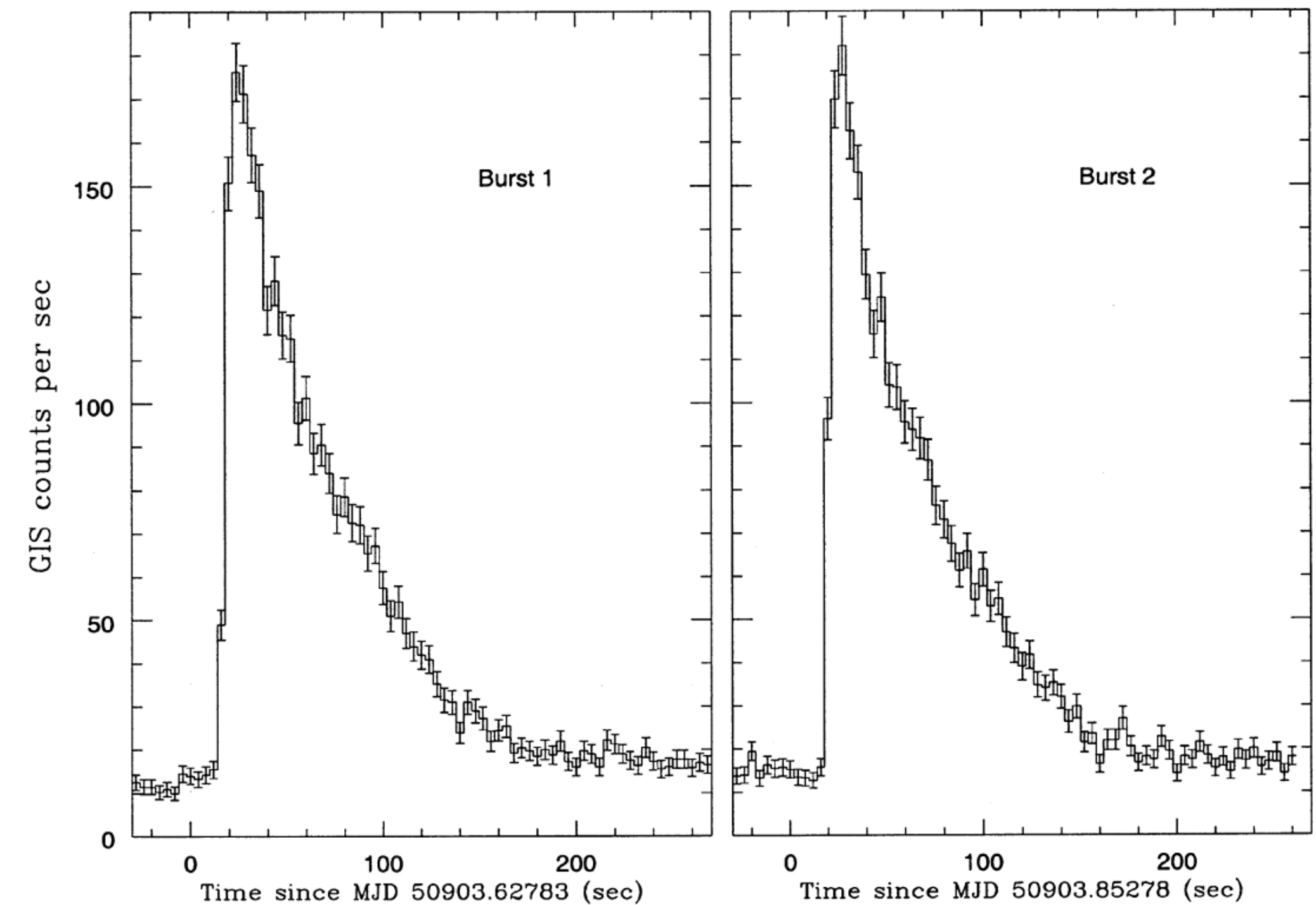
Type-I
X-ray **burst**

Babushkina et al. 1975
Soviet Astronomy Letters, 1, 32

Examples of X-ray light curves.



Accreting X-ray pulsars
(Nagase 1989, *PASJ*, 41, 1)



Type-I X-ray bursts
(Kong et al. 2000, *MNRAS*, 311, 2)

Let's see what has been done
in Schatz et al. 2001 →→→

II. Paper's Introduction

Accreting material: Hydrogen rich.

→ rapid proton capture process (rp-process: $X + p \rightarrow Y + \dots$)
(Wallace & Woosley 1981, *ApJS*, 45, 398)

Hydrogen → rp-process + beta decay → heavier elements

This paper's finding: a natural termination of this process.

Importance: understanding X-ray lightcurves

→ Reveal NS crust properties (thermal & electrical)

→ → Figure out **Magnetic field** evolution, **quiescent luminosity** (when no burst)

(Brown & Bildsten 1998, *ApJ*, 496, 2; Brown, Bildsten & Rutledge 1998, *ApJ*, 504, 2)

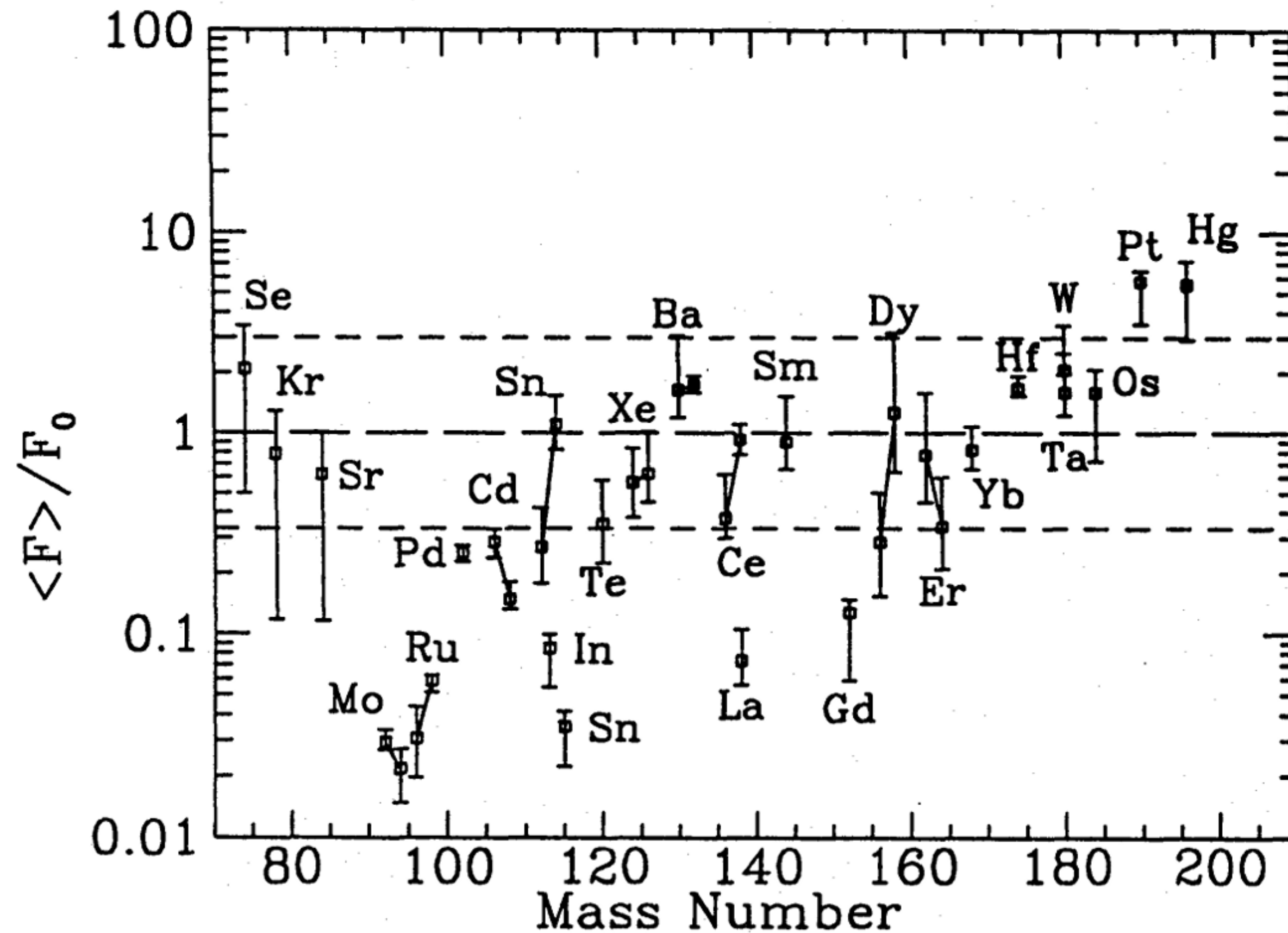
→ Understand **Gravitational Waves** from deformed crust

(Bildsten 1998, *ApJ*, 501, 1; Ushomirsky, Bildsten & Cutler 2000, *MNRAS*, 319, 3)

→ Understand nucleosynthesis of some light p nuclei $^{92,94}\text{Mo}$ $^{96,98}\text{Ru}$

→ Nucleosynthesis of some proton-rich nuclei: if **only** through p-process in Type II Supernovae:

(Rayet et al. 1995, *A&A*, 298, 517)



Mean p-process layer overproduction factor (with respect to solar):

$$\langle F_i \rangle(M) = m_i(M) / (M_p(M) X_{i, \odot})$$

$$F_0(M) = \sum_i \langle F_i \rangle(M) / 35$$

A severe **underproduction** of Mo, Ru p-isotopes.

→ Need to be solved.
(Other routines?)

Dash line: range of solar system composition.

•Previous rp(p)-process simulation on X-ray bursts:
Review the end points...

Many early studies: based on ending up at ^{56}Ni .

The nonstandard nuclear burning has led to the unexpected result that in the regime of high mass accretion rates, $\dot{M} \gtrsim 2 \times 10^{-9} M_{\odot} \text{ yr}^{-1}$, no carbon and little helium is produced. Hydrogen burning proceeds via proton capture onto heavy nuclei, perhaps leading ultimately to the buildup of iron-group species. We believe that this type of nuclear processing proceeds in X-ray pulsars where current models (Davidsen and Ostriker 1973) attribute the pulses as arising from the accretion of matter onto the polar caps. Since the high

Taam & Picklum 1978, *ApJ*, 224, 210

Several later studies: larger networks ending in **Kr-Y** region.
(e.g., Wallace & Woosley 1981, *ApJS*, 45, 398)

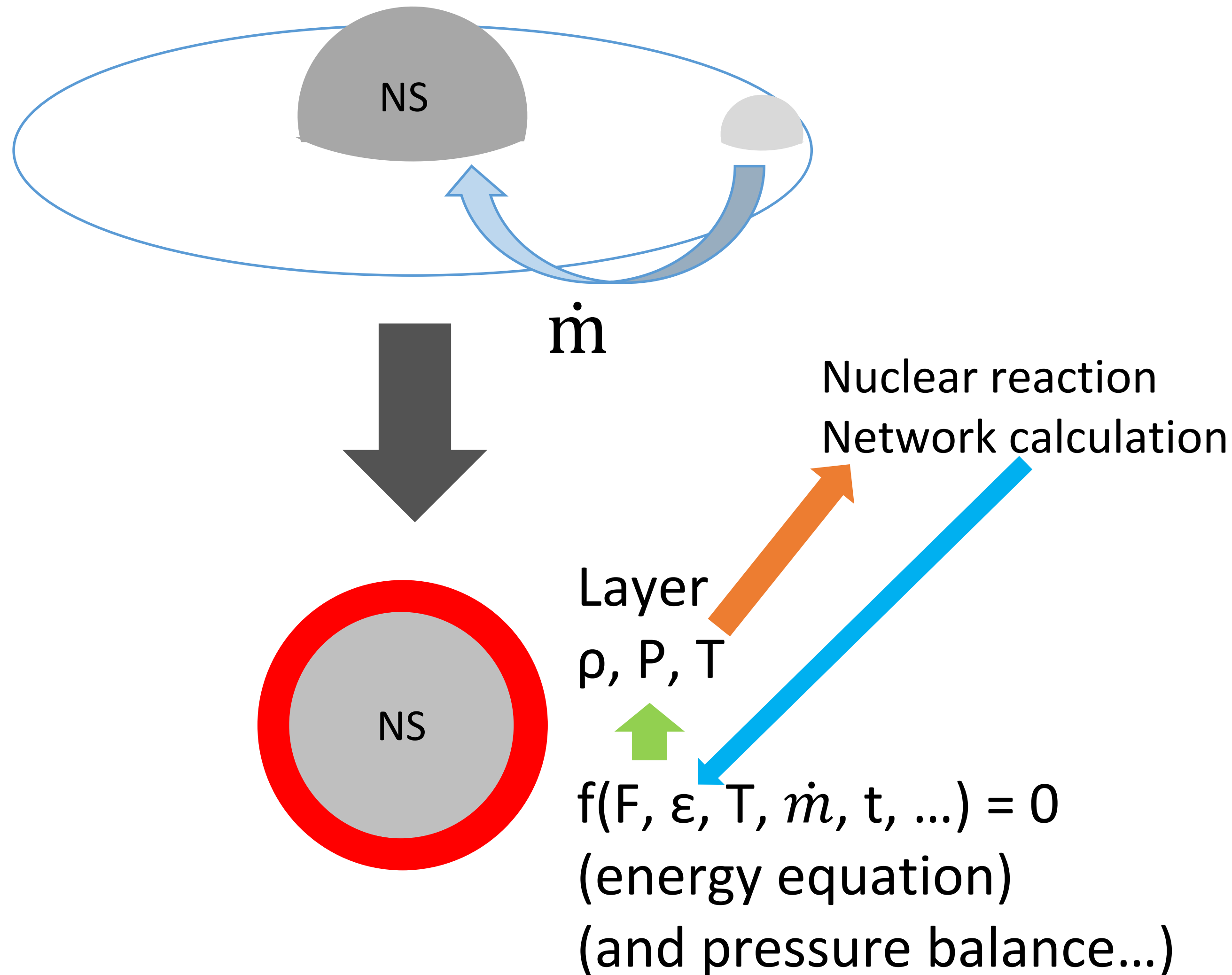
or a simplified 16 nuclei network → **Cd**
(e.g., Wallace & Woosley 1984, AIP Conference Proceedings, 115, 319)

More recent: the network has been extended to **Sn** (Schatz et al. 1998, *PhR*, 294, 167).

(The introduction to network calculation lies in Method section later.)

III. Methods

(i) Physical models:



$$\dot{m}_{\text{Edd}} = 8.8 \times 10^4 \text{ g/cm}^2/\text{s}$$

Initial conditions:

X-ray burst: $Z = 0.001$, $\dot{m} = 0.1 \dot{m}_{\text{Edd}}$

Crust out flow: 0.15MeV/accreted nucleon.

AXP: XYZ=solar, $\dot{m} = 40 \dot{m}_{\text{Edd}}$

$$g = 1.9 \times 10^{14} \text{ cm/s}^2$$

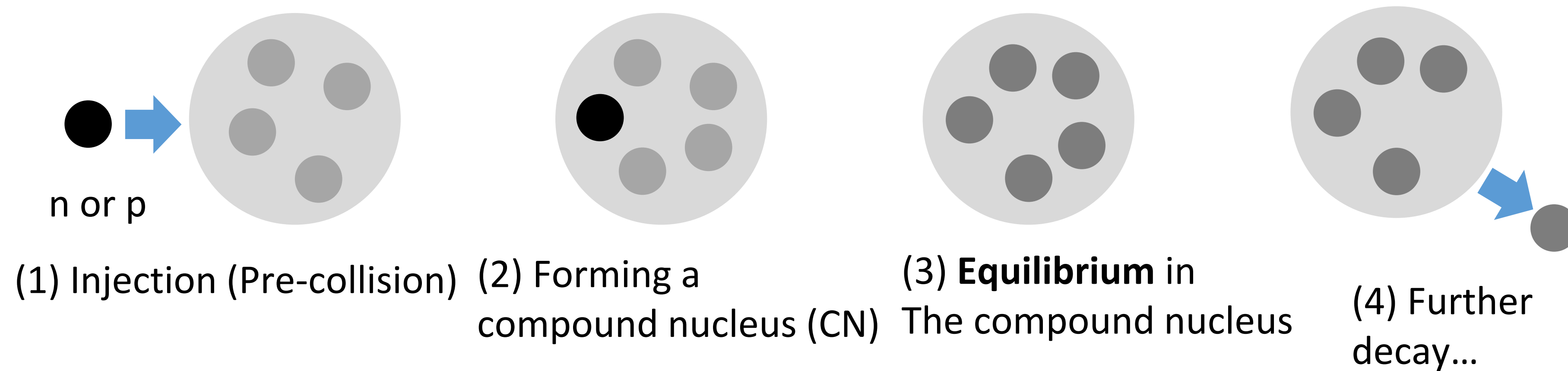
$$P = gy \quad dy = -\rho \, dz \quad g \approx GM/R^2$$

Schatz et al. 1999, *ApJ*, 524, 2

$$\frac{\partial F}{\partial y} + \epsilon = C_p \left(\frac{\partial T}{\partial t} + \dot{m} \frac{\partial T}{\partial y} \right) - \frac{C_p T \dot{m}}{y} \nabla_{\text{ad}}$$

L. Bildsten in *The Many Faces of Neutron Stars*

(ii) Nuclear reaction network calculation: Wolfenstein-Hauser-Feshbach approach (Bohr 1936; Wolfenstein 1951; Hauser & Feshbach 1952)



$$A + a \rightarrow C \rightarrow \begin{cases} B_0 + b_0 \\ B_1^* + b_1 \\ \dots \\ B_n^* + b_n \\ \dots \end{cases} \quad \beta$$

α

$$\sigma_{\alpha\beta,l} = \sigma_{CN,l}(\alpha) G_b \quad \left\{ \begin{array}{l} \sigma_{CN,l}(\alpha) = \pi \lambda_\alpha^2 T_\alpha g_\alpha \\ G_b = \frac{\Gamma_b}{\Gamma} \end{array} \right. \quad \begin{array}{l} T: \text{transmission coef} \\ \text{Decay **possibility** through } \beta \end{array}$$

$$\Sigma_i G_i = \Sigma_i \frac{\Gamma_i}{\Gamma} = 1$$

$$\Gamma: \text{energy level width} = \hbar/\tau = \hbar W = \hbar(W_1 + W_2 + W_3 + \dots)$$

Refer to 《原子核物理学》卢希庭 9.9节

Nuclear reaction network calculation: Wolfenstein-Hauser-Feshbach approach (Bohr 1936; Wolfenstein 1951; Hauser & Feshbach 1952)

$$\sigma_{\alpha\beta,l} = \sigma_{CN,l}(\alpha) G_b \quad \left\{ \begin{array}{l} \sigma_{CN,l}(\alpha) = \pi \lambda_\alpha^2 T_\alpha g_\alpha \\ G_b = \frac{\Gamma_b}{\Gamma} \end{array} \right. \quad \begin{array}{l} \text{T: transmission coef} \\ \text{calculated} \end{array}$$

$$A + a \rightarrow C \rightarrow \left\{ \begin{array}{l} B_0 + b_0 \\ B_1^* + b_1 \\ \dots \\ B_n^* + b_n \\ \dots \end{array} \right. \quad \begin{array}{l} \beta \\ \alpha \end{array}$$

$$g_\alpha = \frac{2I_C + 1}{(2I_a + 1)(2I_A + 1)} \quad \Sigma_i G_i = \Sigma_i \frac{\Gamma_i}{\Gamma} = 1 \quad \text{Decay possibility through } \beta$$

Detailed balance:
(散射矩阵元对角项相等) $\frac{\sigma_{CN,l}(\alpha) p_\alpha^2}{g_\alpha \Gamma_a} = \frac{\sigma_{CN,l}(\beta) p_\beta^2}{g_\beta \Gamma_b}$ p: momentum

H-F equation: $\sigma_{\alpha\beta,l} = \pi \lambda_\alpha^2 T_\alpha g_\alpha \frac{\sigma_{CN,l}(\beta) p_\beta^2 / g_\beta}{\Sigma_i \sigma_{CN,l}(i) p_i^2 / g_i} = \pi \lambda_\alpha^2 T_\alpha T_\beta g_\alpha / \Sigma_i T_i$

In this paper, the calculations are done with a code **NON-SMOKER**.
(Rauscher & Thielemann 2000, *ADNDT*, 75, 1)

IV. Results

(i) Nuclear reaction network

From He to the Sc region:

3α -reaction, (α, p) , (p, γ) processes

(Follow Wallace & Woosley 1981, ApJS, 45, 398).

Ignition density: $1.1 \times 10^6 \text{ g/cm}^3$

Peak temperature: 1.9 GK

Rise timescale: 4s

Cooling phase: 200s

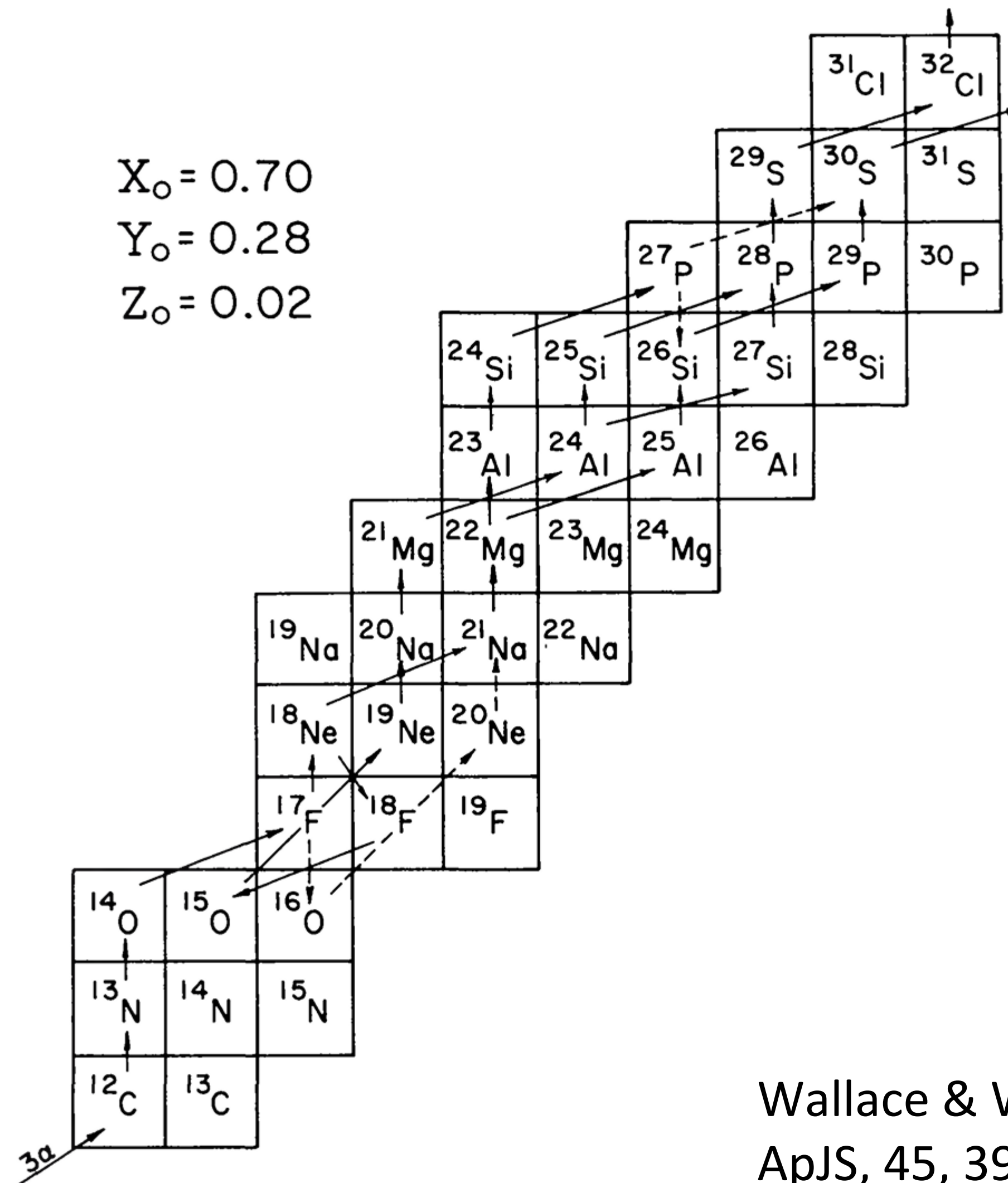


FIG. 10.— The dominant nuclear flows during a thermonuclear runaway of the hydrogen-helium shell on the surface of an accreting neutron star (model B). Flows are evaluated when the runaway has progressed to a temperature $T_9 \approx 0.8$, and density $\rho = 6.1 \times 10^5 \text{ g cm}^{-3}$ ($t \approx 6308 \text{ s}$). Two major chains of (α, p) and (p, γ) reactions extend from ^{18}Ne to ^{30}S and from ^{19}Ne to ^{29}S and beyond.

Beyond Fe: (p, γ), (α ,p), EC/ β^+ decay, reaches (99-101)Sn \sim 80s after burst peak.

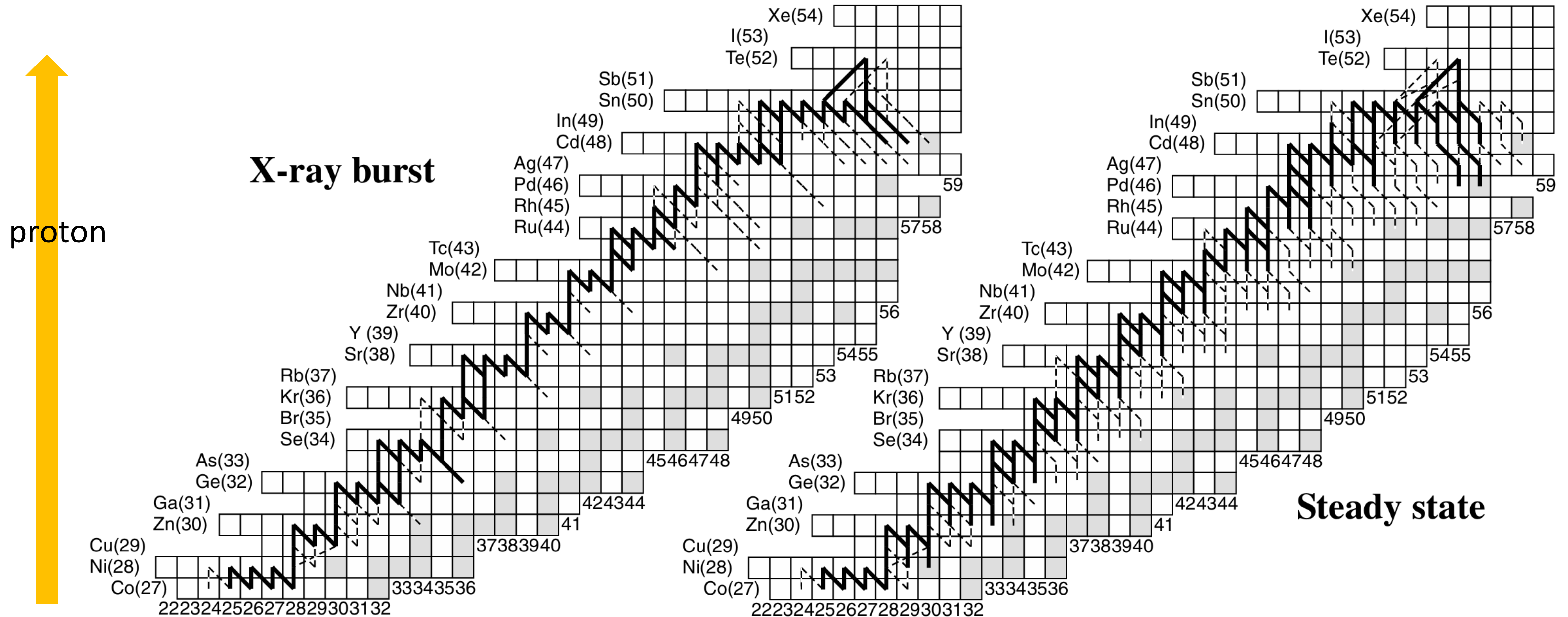


FIG. 1. The time integrated reaction flow above Ga during an x-ray burst and for steady-state burning. Shown are reaction flows of more than 10% (solid line) and of 1%–10% (dashed line) of the reaction flow through the 3α reaction.

Beyond Sn: $105\text{ Sn}(p,\gamma)106\text{ Sb}(p,\gamma)107\text{ Te}(\gamma,\alpha)103\text{ Sn}$

105Sn 32.7 s $\epsilon = 100.00\%$ $\epsilon p = 0.01\%$	106Sb 0.6 s ϵ	107Te 3.1 ms $\alpha = 70.00\%$ $\epsilon = 30.00\%$
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Credit:
NNDC

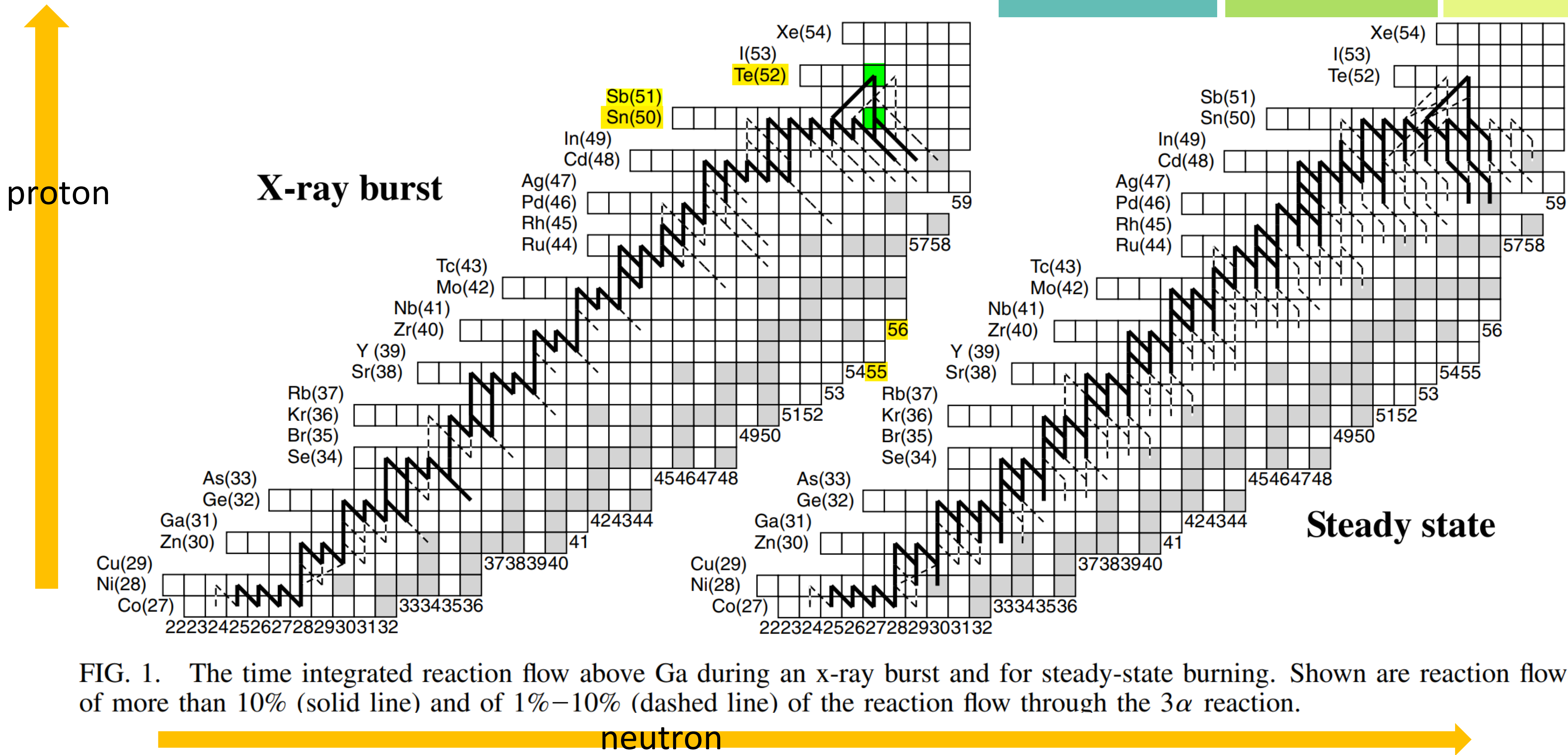
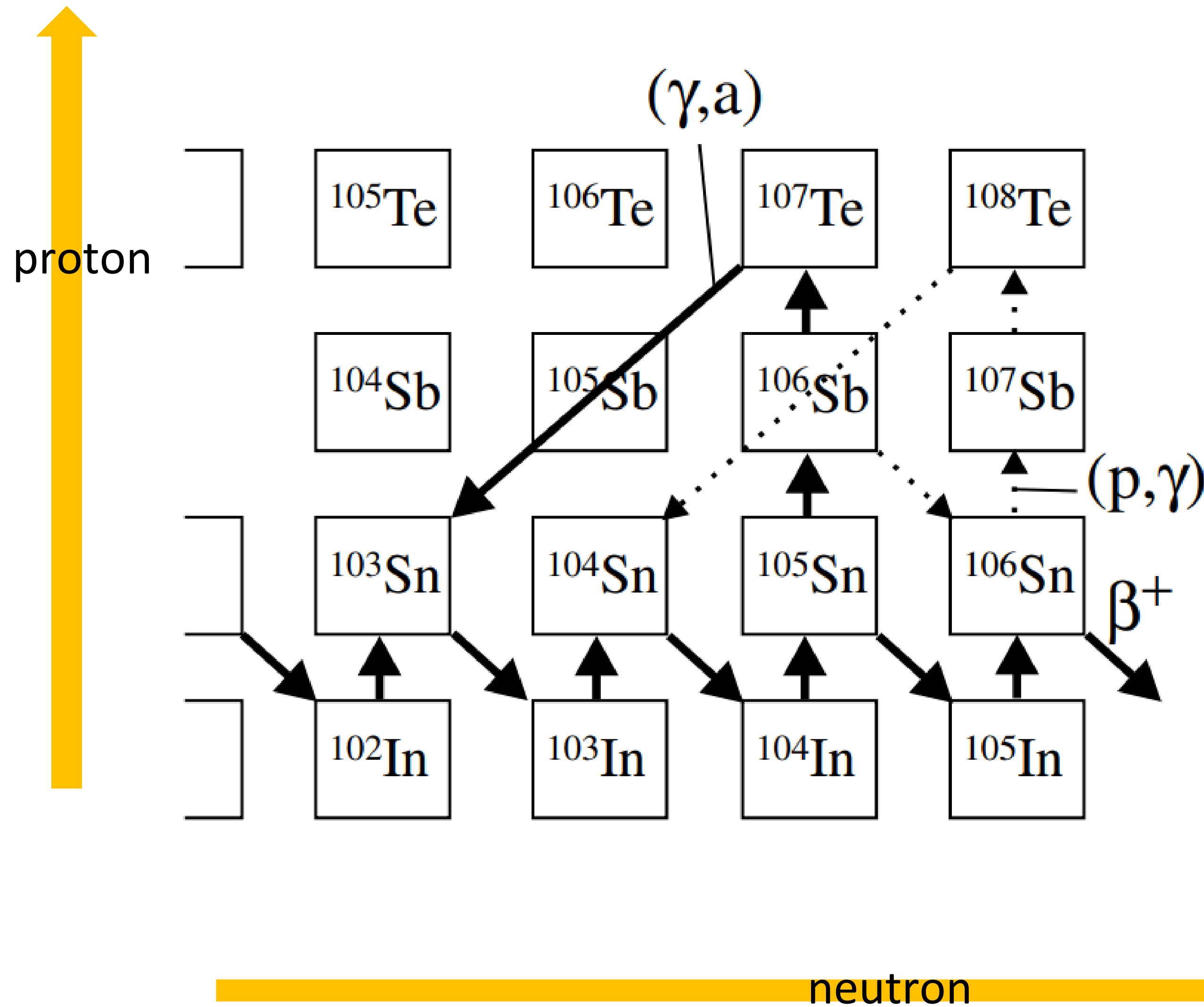


FIG. 1. The time integrated reaction flow above Ga during an x-ray burst and for steady-state burning. Shown are reaction flows of more than 10% (solid line) and of 1%–10% (dashed line) of the reaction flow through the 3α reaction.

106-108 Te: α unbounded by $\sim 4\text{MeV}$ (Page et al. 1994, *PRC*, 49, 6).

107 Te: a known ground state α emitter (Schardt et al. 1979, *NuPhA*, 326, 1).



SnSbTe cycles: two cycles

(1) $105\text{ Sn}(p,\gamma)106\text{ Sb}(p,\gamma)107\text{ Te}(\gamma,\alpha)103\text{ Sn}$

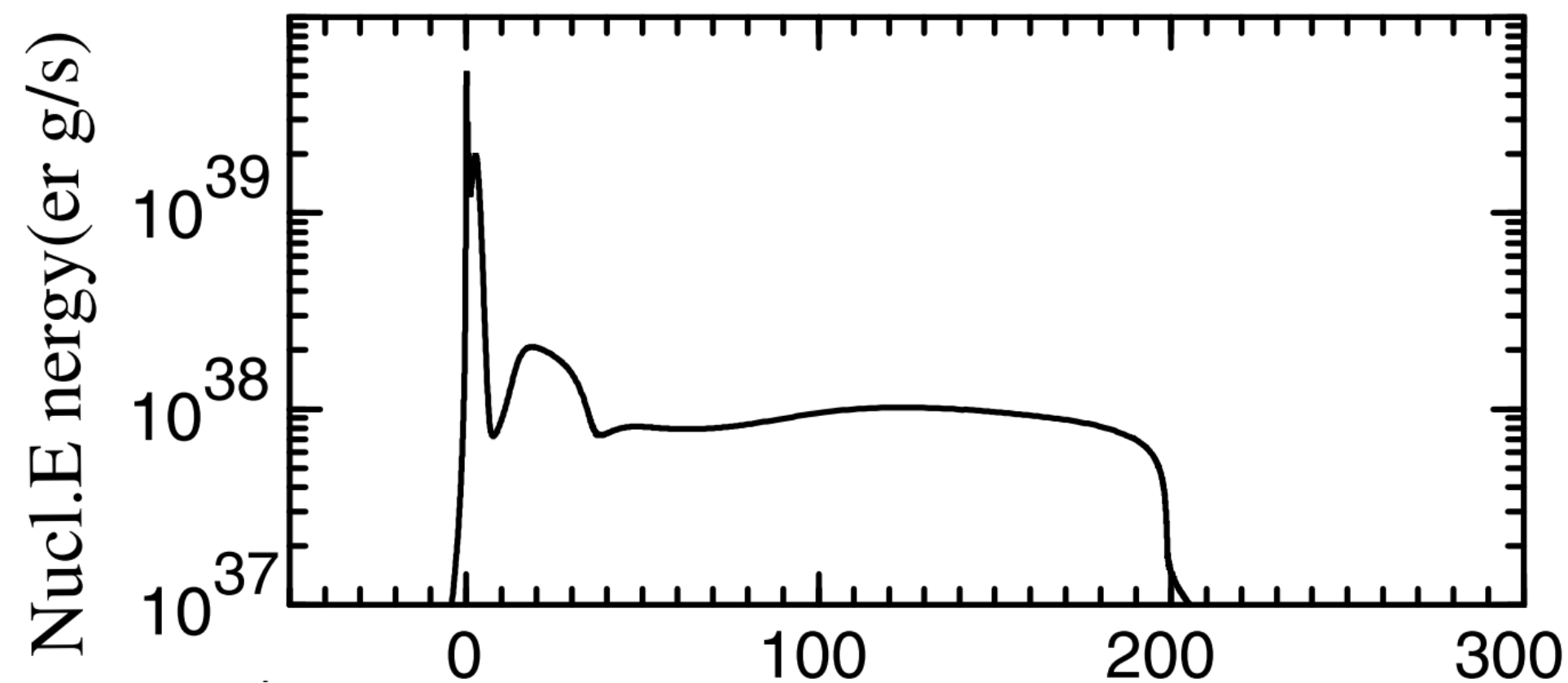
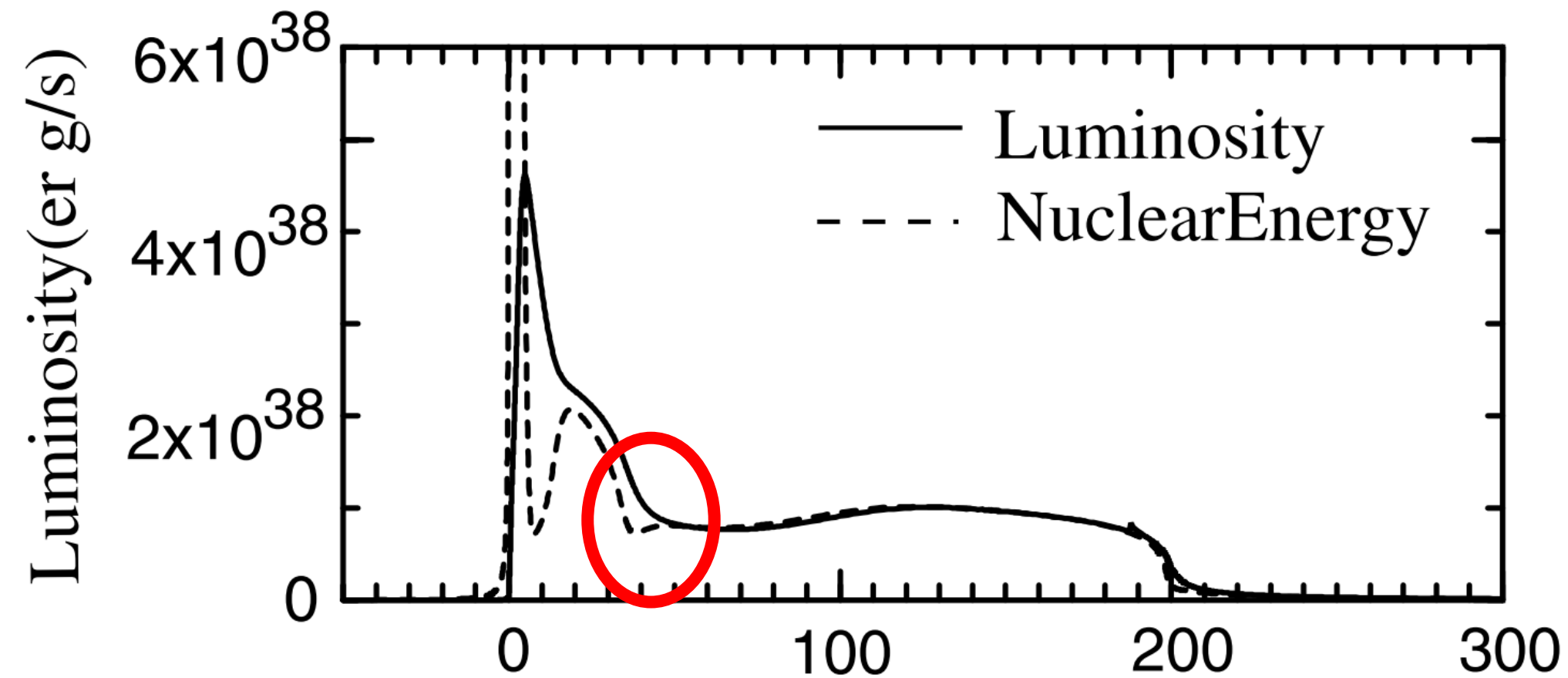
(2) $106\text{ Sn}(p,\gamma)107\text{ Sb}(p,\gamma)108\text{ Te}(\gamma,\alpha)104\text{ Sn}$

(1) is stronger than (2).

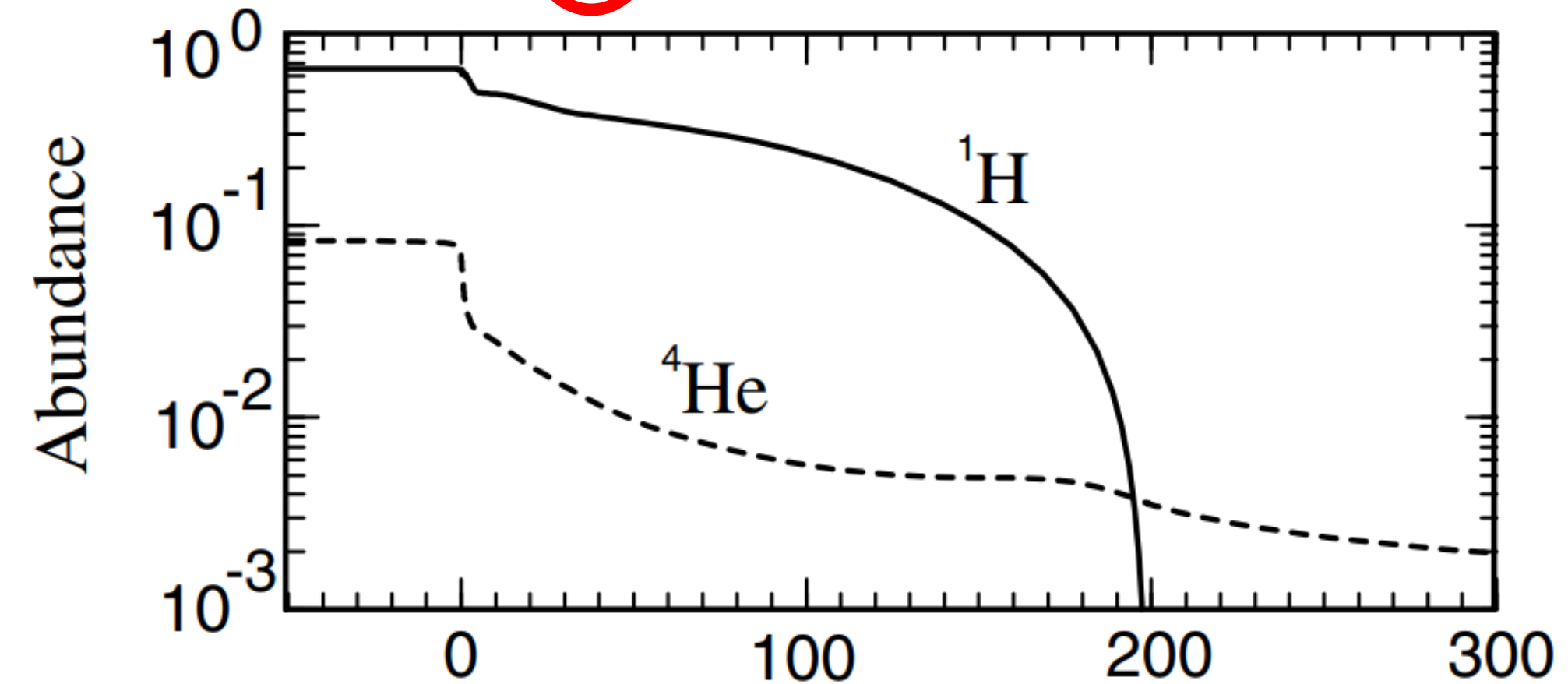
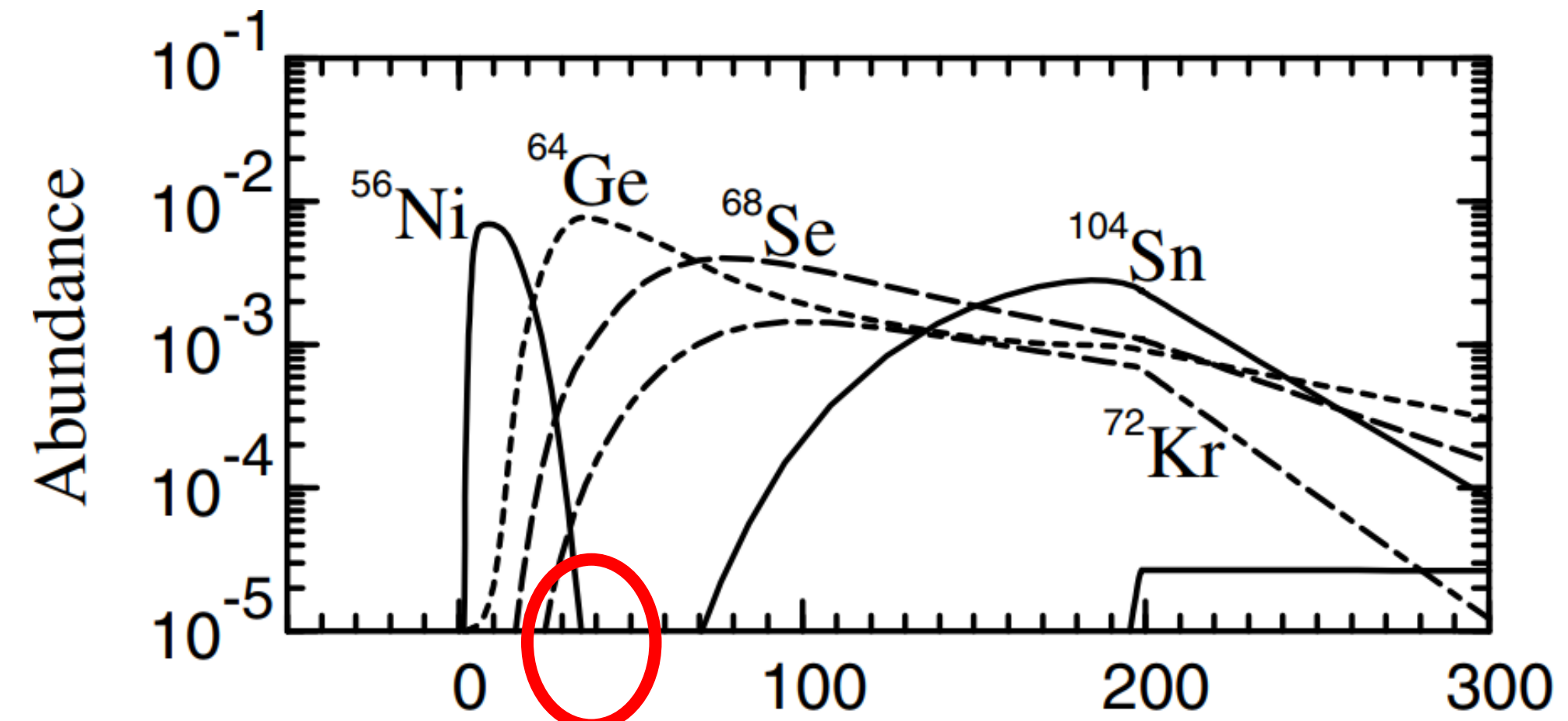
Change initial conditions:
can not beyond SnSbTe.

(ii) Light curves, changes of energy & Abundance

Some long-lived “waiting point” nuclei.



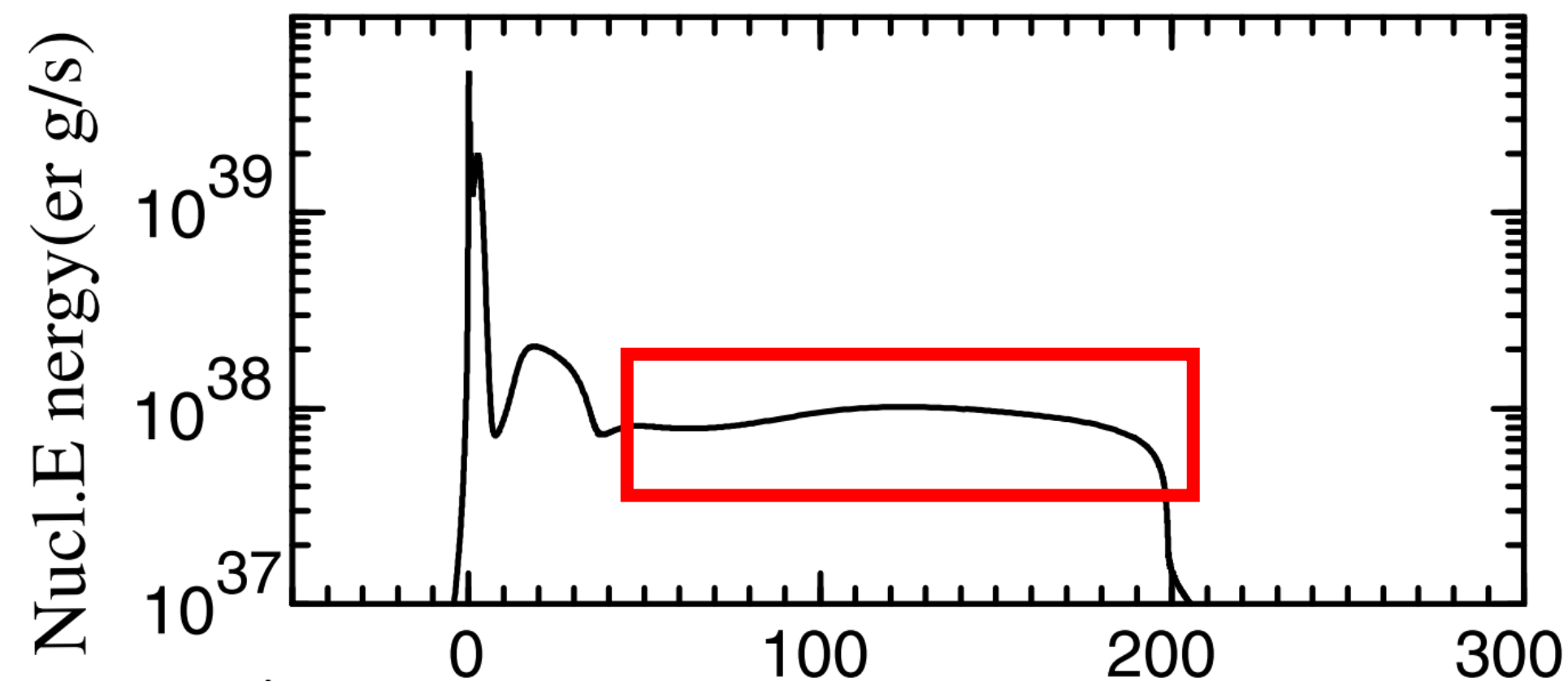
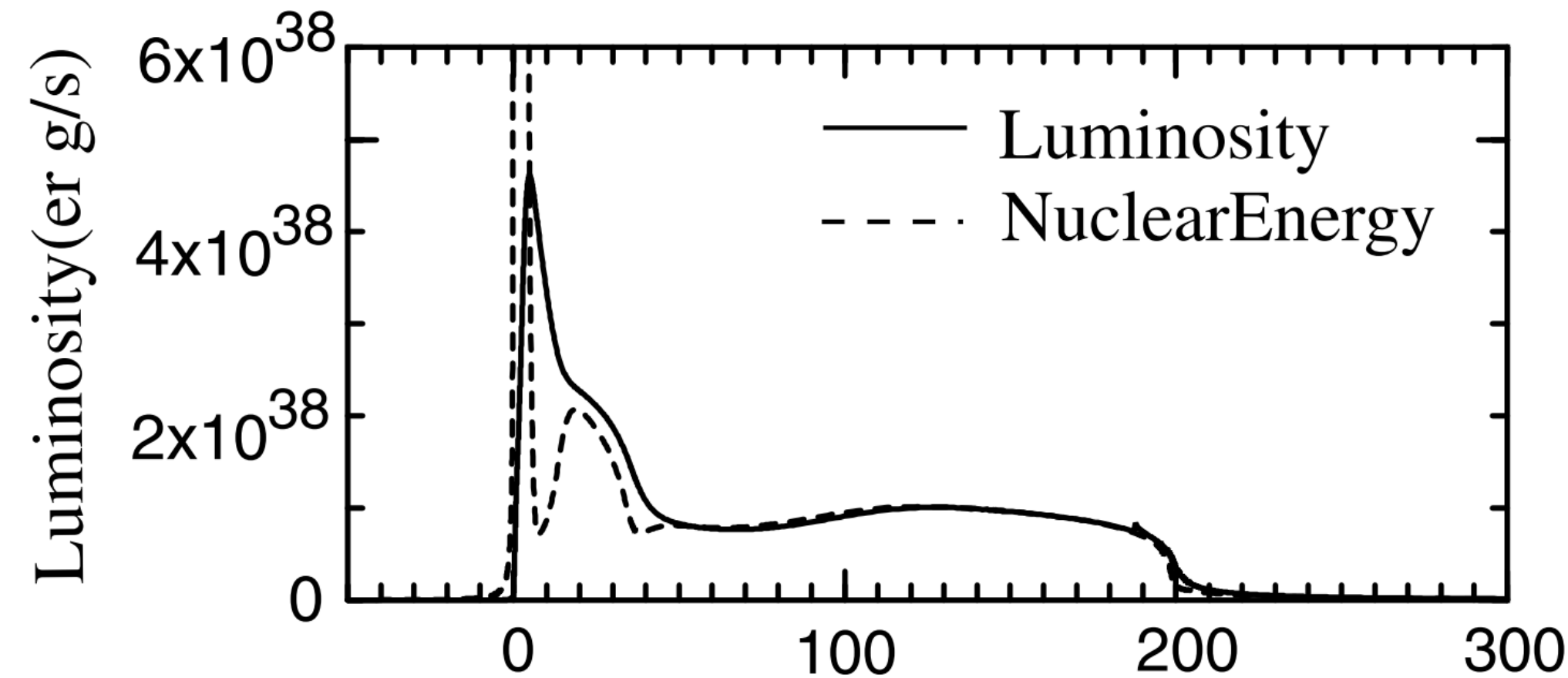
Time (s)



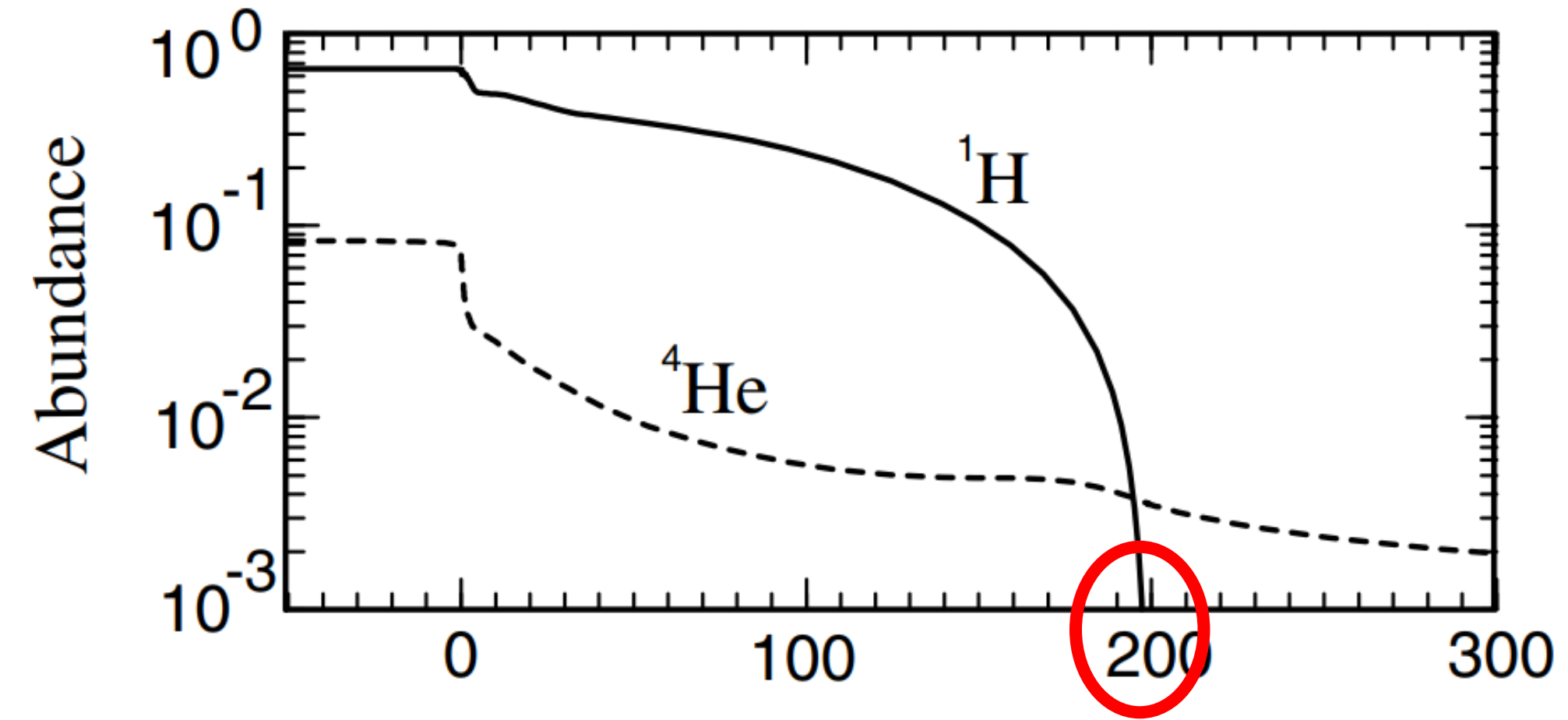
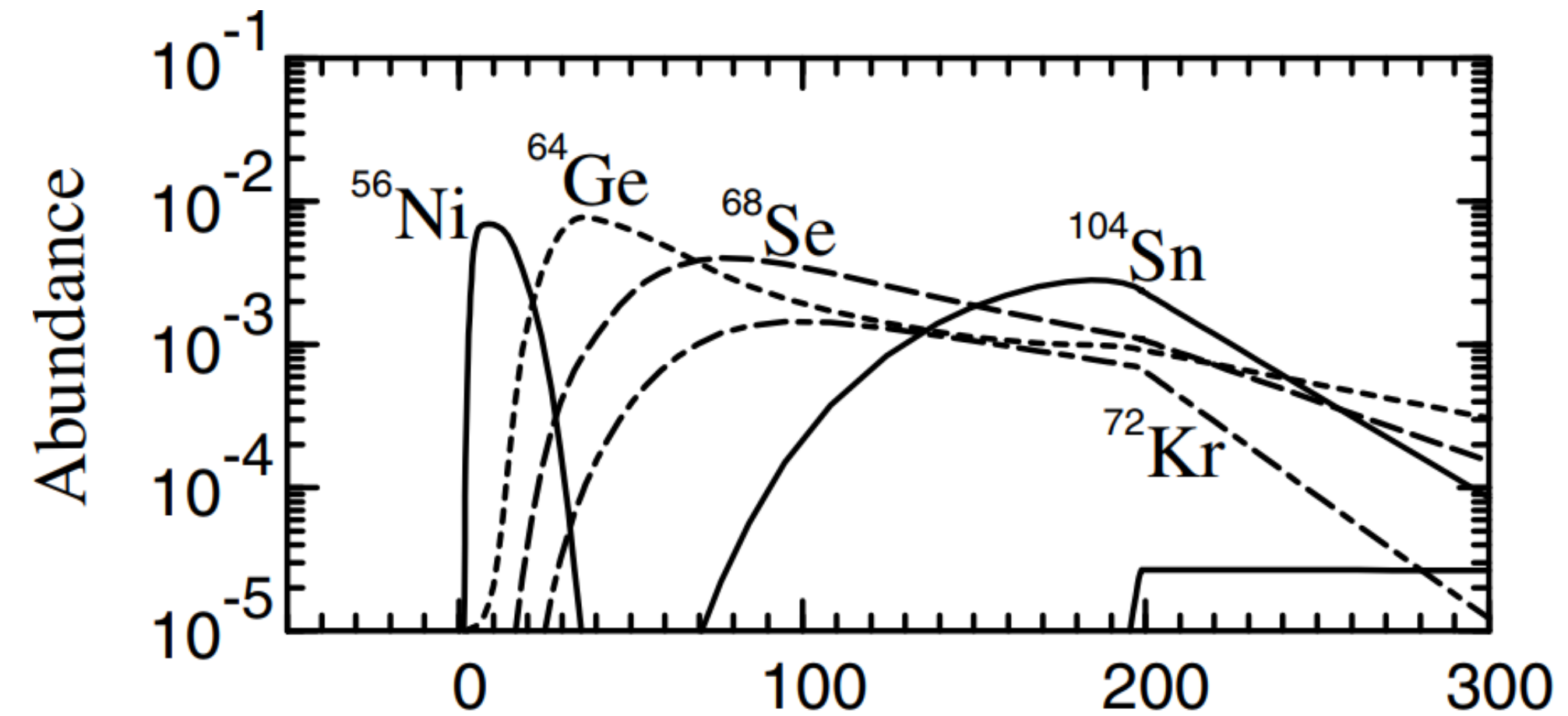
Time (s)

Burning beyond ^{56}Ni → Extended burst tail.

Some long-lived “waiting point” nuclei.



Time (s)

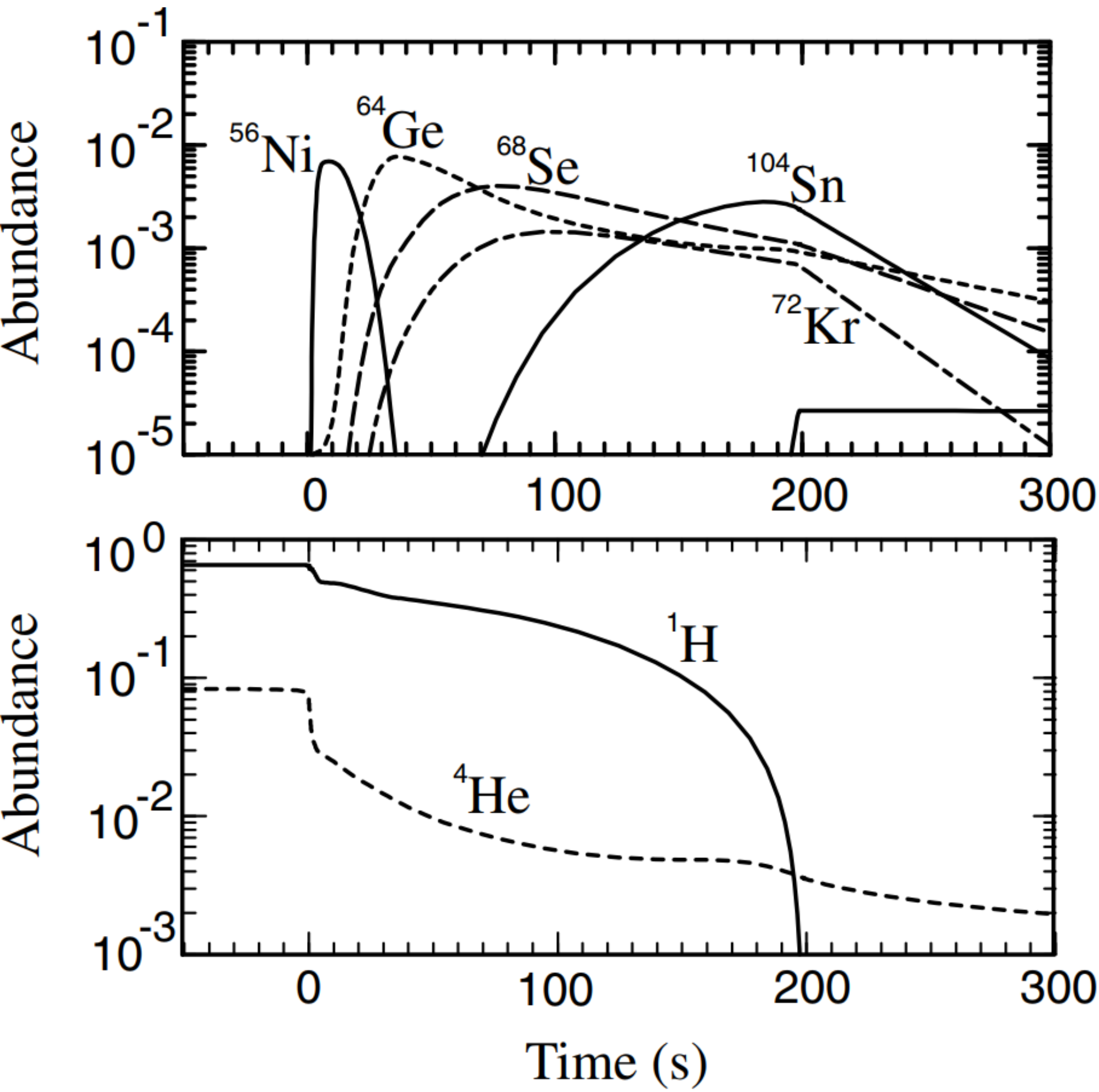


Time (s)

SnSbTe cycle: produce ^{104}Sn mostly ($\tau = 20.8\text{s}$).

produce $\alpha \rightarrow 3\alpha$ increase \rightarrow energy release \rightarrow Hydrogen completely burned.

Some long-lived “waiting point” nuclei.



^{56}Ni
6.075 d
 $\epsilon = 100.00\%$

^{64}Ge
63.7 s
 $\epsilon = 100.00\%$

^{68}Se
35.5 s
 $\epsilon = 100.00\%$

^{72}Kr
17.1 s
 $\epsilon = 100.00\%$
 $\epsilon p < 1.0\text{E-}6\%$

^{104}Sn
20.8 s
 $\epsilon = 100.00\%$

^{103}Sn
7.0 s
 $\epsilon = 100.00\%$
 $\epsilon p = 1.20\%$

^{105}Sn
32.7 s
 $\epsilon = 100.00\%$
 $\epsilon p = 0.01\%$

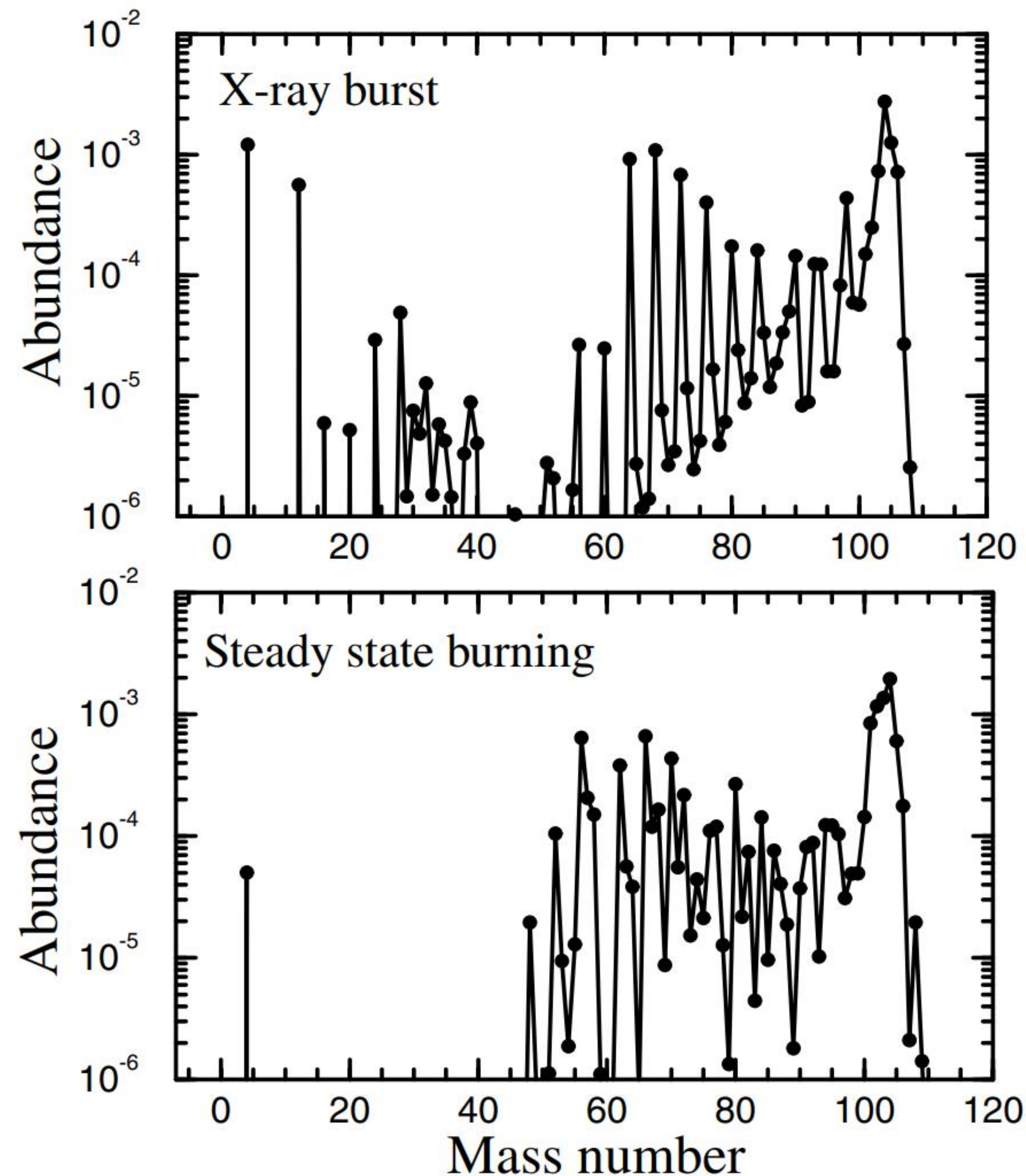
^{106}Sb
0.6 s
 ϵ

^{107}Sb
4.0 s
 $\epsilon = 100.00\%$

^{107}Te
3.1 ms
 $\alpha = 70.00\%$
 $\epsilon = 30.00\%$

Credit:
NNDC

Final abundance (rp process ashes):



(1) Lack of nuclei with $A > 107$.

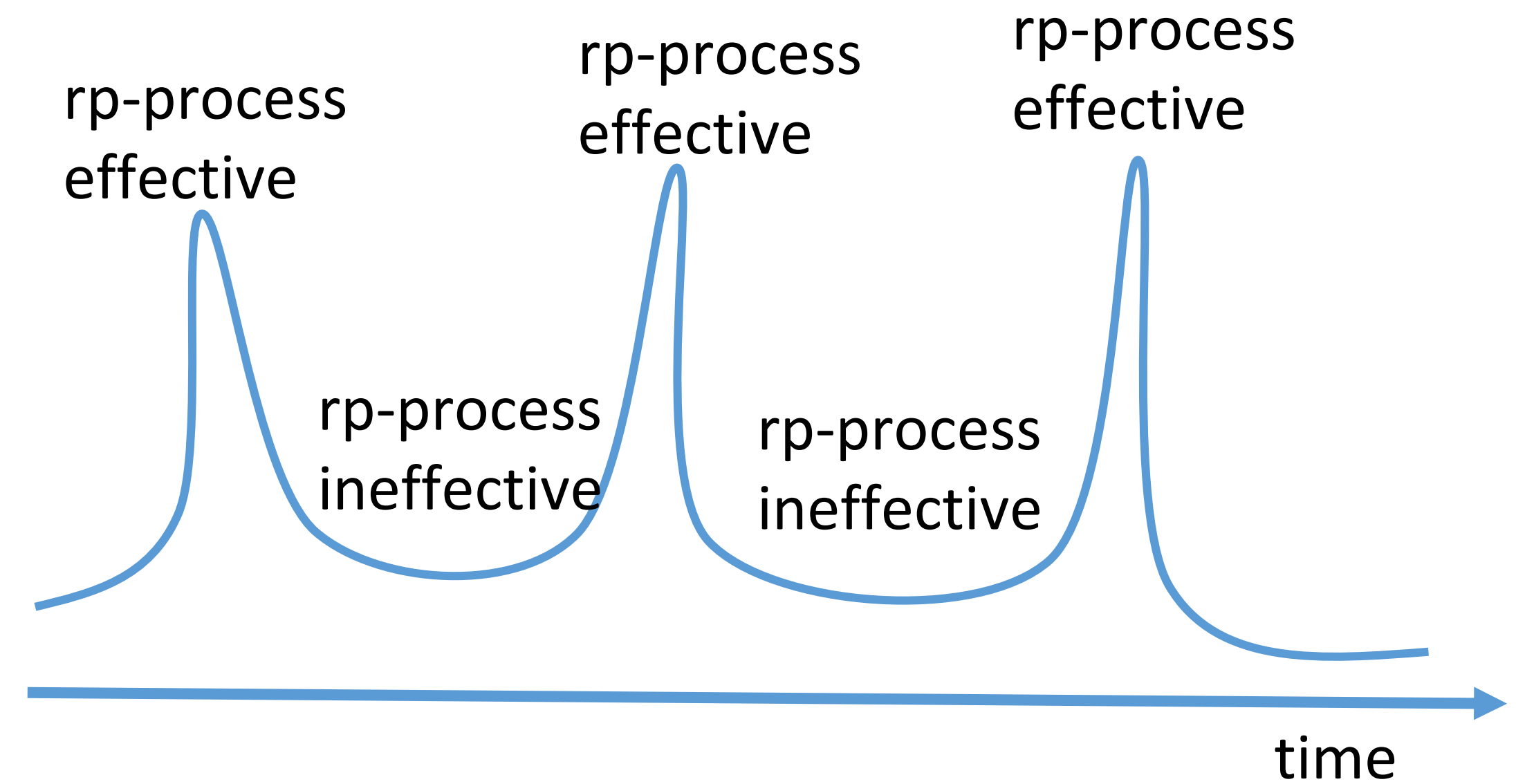
(2) Broad distribution of $64 < A < 107$.
(due to long-lived waiting nuclei & enough helium)

V. Discussion

(i) To bypass SnSbTe cycle?

Only way: a pulsed rp-process.

Between pulses, matter decay to stable nuclei.



→ Need reignition of ashes ← unburned Hydrogen (or) extensive vertical mixing (of nuclei)
(Fujimoto et al. 1987, *ApJ*, 319, 902)

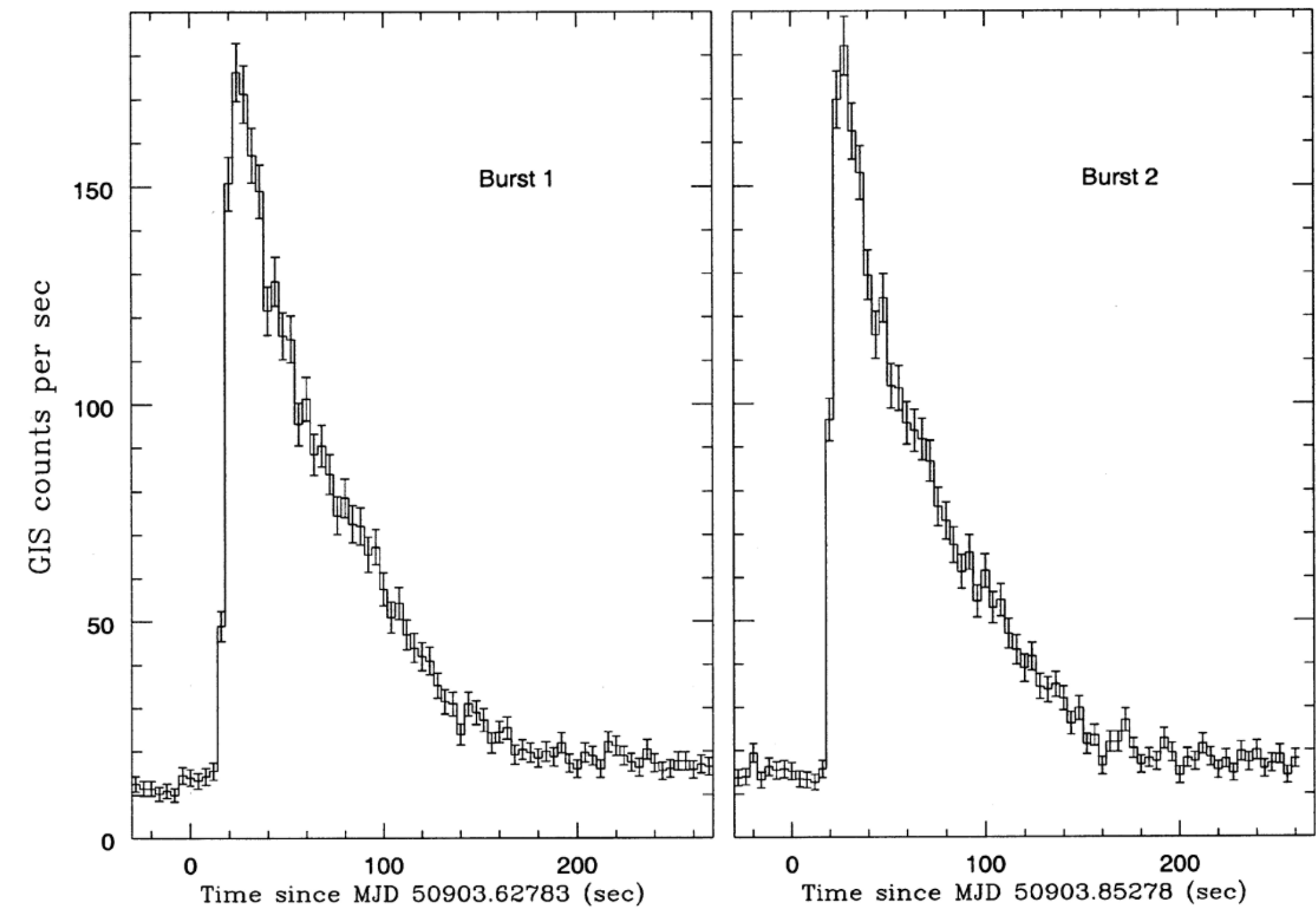
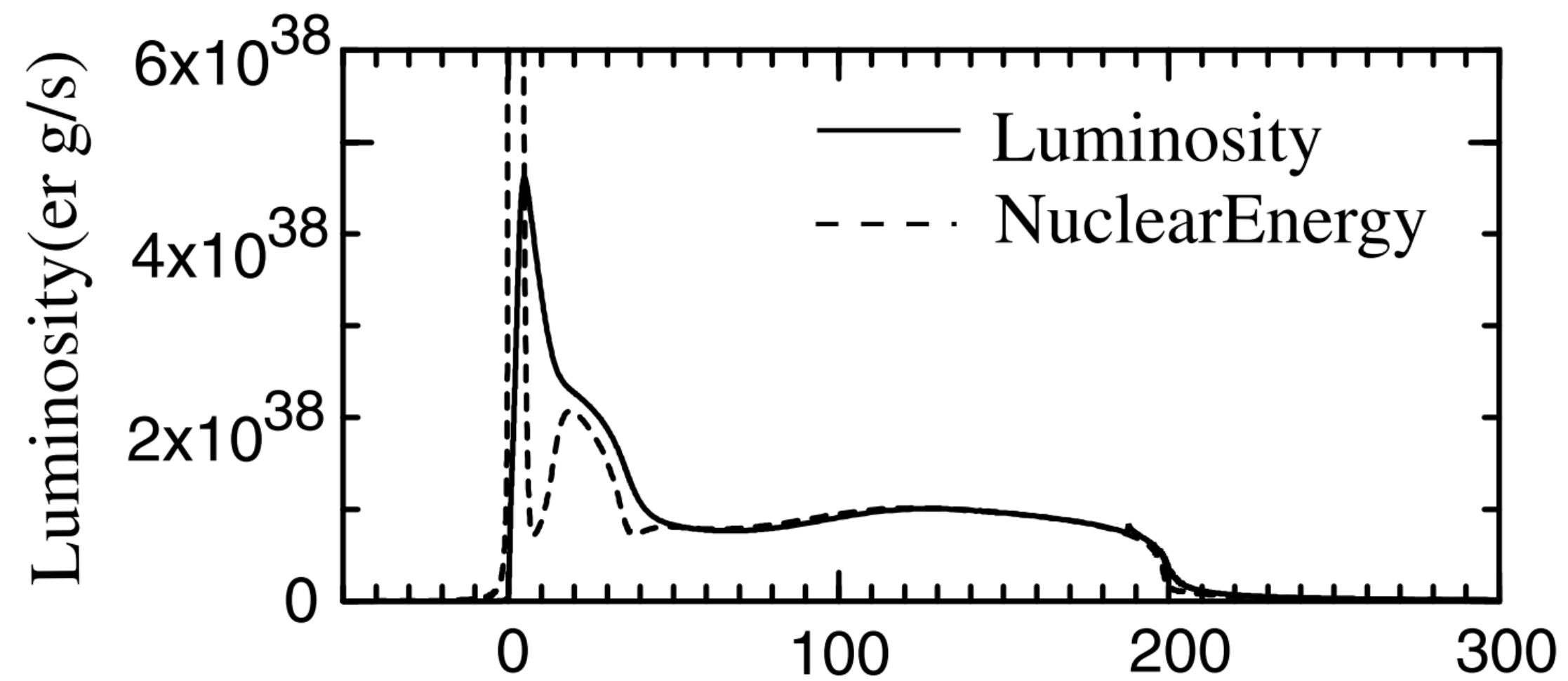


“Dwarf Bursts”
(Taam et al. 1993
ApJ, 413, 324)
Lower luminosity...



Little unburned Hydrogen
in this paper’s calculation.

(ii) Duration of a burst:
Long enough to match observations.



Type-I X-ray burst example (Kong et al. 2000
MNRAS, 311, 2)

(iii) Nucleosynthesis:

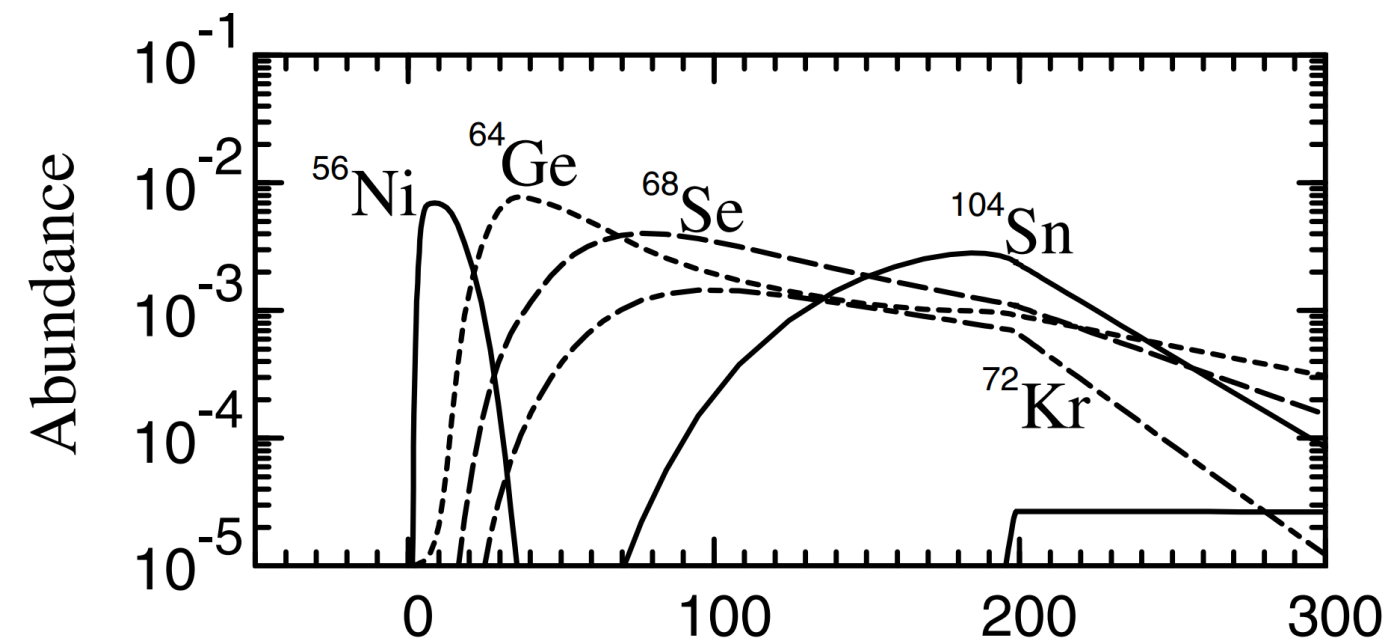
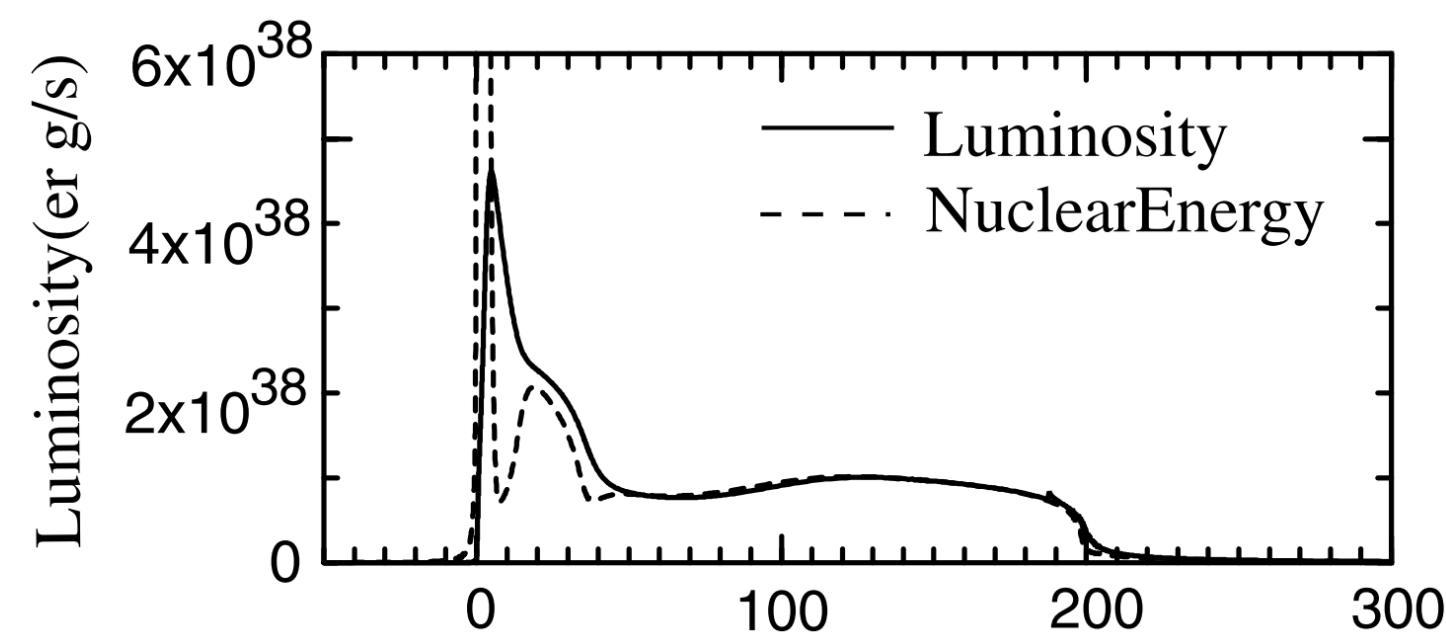
Large overproduction factors ($>10^9$ *solar)
of p nuclei ^{98}Ru , ^{102}Pd , ^{106}Cd .

➔ To explain solar system abundance' origin

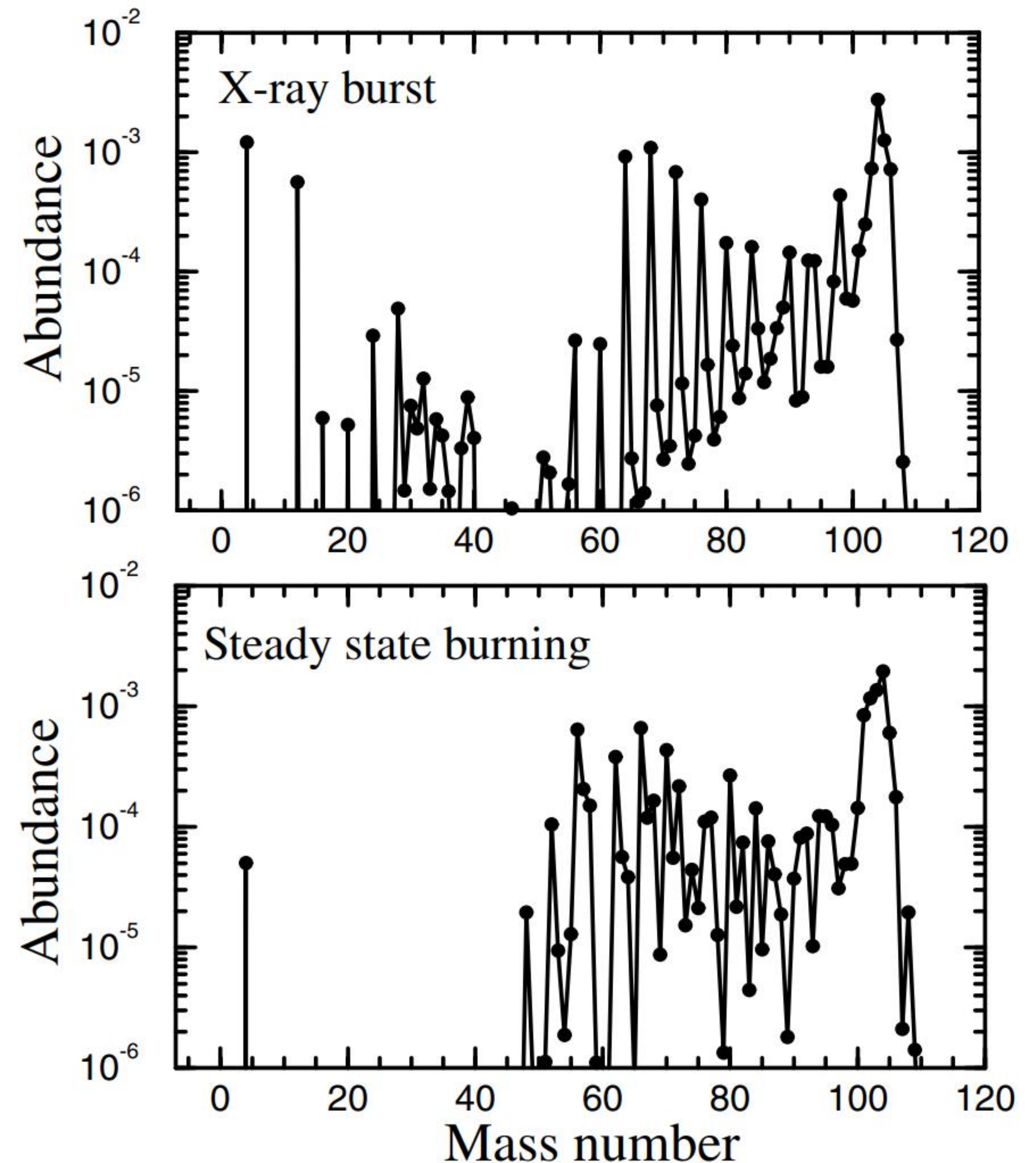
➔➔ 1% of them are ejected

(Schatz et al. 1998, *PhR*, 294, 167)

➔➔➔ The ejection mechanism...(not sure)



• Synthesis of p-nuclei
most likely related to
long burst tails...



The rp-process on accreting NS ends at SnSbTe cycle.

→ Long (~200s) burst duration & long tail.

→ Effective synthesis of $65 < A < 107$ nuclei.

→ More p-nuclei produced (than if only SNe II).

Thank you for your attention 😊