

# Power Set

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- Determine the power set for the following set

$$***A = \{p, q, r, s\}***$$

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- The Power Set of A , denoted  $\mathcal{P}(A)$  , is an exhaustive list of all subsets of set A.
- The empty set  $\emptyset$  and A are two such subsets.

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- Determine the power set for the following set

$$A = \{p, q, r, s\}$$

- Cardinality of set A is 4
- Cardinality of power set of A is  $2^4$  , i.e. 16

Size of subset	Subsets	Number of subsets
0	$\emptyset$	1
1		4
2		6
3		4
4	{p,q,r,s}	1

Size of subset	Subsets	Number of subsets
0	$\emptyset$	1
1	$\{p\}, \{q\}, \{r\}, \{s\}$	4
2		6
3		4
4	$\{p, q, r, s\}$	1

Size of subset	Subsets	Number of subsets
0	$\emptyset$	1
1	$\{p\}, \{q\}, \{r\}, \{s\}$	4
2		6
3	$\{q,r,s\}, \{p,r,s\}, \{p,q,s\}, \{p,q,r\}$	4
4	$\{p,q,r,s\}$	1

Size of subset	Subsets	Number of subsets
0	$\emptyset$	1
1	$\{p\}, \{q\}, \{r\}, \{s\}$	4
2	$\{p,q\}, \{p,r\}, \{p,s\}, \{q,r\}, \{q,s\}, \{r,s\}$	6
3	$\{q,r,s\}, \{p,r,s\}, \{p,q,s\}, \{p,q,r\}$	4
4	$\{p,q,r,s\}$	1



Size of subset	Subsets	Number of subsets
0	$\emptyset$	1
1	$\{p\}, \{q\}, \{r\}, \{s\}$	4
2	$\{p,q\}, \{p,r\}, \{p,s\}, \{q,r\}, \{q,s\}, \{r,s\}$	6
3	$\{q,r,s\}, \{p,r,s\}, \{p,q,s\}, \{p,q,r\}$	4
4	$\{p,q,r,s\}$	1

# Power Set

## Power Set of A

$$\mathcal{P}(A) = \{ \emptyset, \{p\}, \{q\}, \{r\}, \{s\}, \{p,q\}, \{p,r\}, \{p,s\}, \\ \{q,r\}, \{q,s\}, \{r,s\}, \{q,r,s\}, \{p,r,s\}, \\ \{p,q,s\}, \{p,q,r\}, \{p,q,r,s\} \}$$

# Power Set

- N.B. The number of subsets of size  $k$  are *binomial coefficients*.