

## Binary operations on sets

- The **Union** of the sets A and B, denoted  $A \cup B$ , is the set of all objects that are a member of A, or B, or both.  
The union of  $\{1, 2, 3\}$  and  $\{2, 3, 4\}$  is the set  $\{1, 2, 3, 4\}$ .
- The **Intersection** of the sets A and B, denoted  $A \cap B$ , is the set of all objects that are members of both A and B.  
The intersection of  $\{1, 2, 3\}$  and  $\{2, 3, 4\}$  is the set  $\{2, 3\}$ .
- The **Set difference** of U and A, denoted  $U \setminus A$ , is the set of all members of U that are not members of A.  
The set difference  $\{1,2,3\} \setminus \{2,3,4\}$  is  $\{1\}$ , while, conversely, the set difference  $\{2,3,4\} \setminus \{1,2,3\}$  is  $\{4\}$ .
- When A is a subset of U, the set difference  $U \setminus A$  is also called the **complement** of A in U. In this case, if the choice of U is clear from the context, the notation  $A'$  is sometimes used instead of  $U \setminus A$ , particularly if U is a universal set as in the study of Venn diagrams.
- The **Symmetric difference** of sets A and B, denoted  $A \oplus B$ , is the set of all objects that are a member of exactly one of A and B (elements which are in one of the sets, but not in both).  
For instance, for the sets  $\{1,2,3\}$  and  $\{2,3,4\}$ , the symmetric difference set is  $\{1,4\}$ .  
The Symmetric difference is the set difference of the union and the intersection,  $(A \cup B) \setminus (A \cap B)$  or  $(A \setminus B) \cup (B \setminus A)$ .
- The **Cartesian product** of A and B, denoted  $A \times B$ , is the set whose members are all possible ordered pairs (a,b) where a is a

member of A and b is a member of B.

The cartesian product of  $\{1, 2\}$  and  $\{\text{red}, \text{white}\}$  is  $\{(1, \text{red}), (1, \text{white}), (2, \text{red}), (2, \text{white})\}$ .

- The **Power set** of a set A is the set whose members are all possible subsets of A. For example, the power set of  $\{1, 2\}$  is  $\{ \{\}, \{1\}, \{2\}, \{1,2\} \}$ .