

**Question 3** (a) Let  $n \in \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$  and let  $p, q$  be the following propositions concerning the integer  $n$ .

$p$ :  $n$  is even;       $q$ :  $n < 5$ .

Find the values of  $n$  for which each of the following compound statements is true.

(i)  $\neg p$ ; (ii)  $p \wedge q$ ; (iii)  $\neg p \vee q$ ; (iv)  $p \oplus q$ .

[4]

(b) (i) Let  $p, q$  be propositions. Construct the truth table for  $p \rightarrow q$ .

[2]

(ii) Use truth tables to prove that  $\neg q \rightarrow \neg p = p \rightarrow q$ .

[2]

(iii) Write the contrapositive of the statement:

If  $n = 23$ , then  $n$  is prime.

END