ASSIGNMENT 3

➤ Question 1:

Implementation of Merge sort.

TC: O(n Log n)

- > Solution:
 - Source Code:

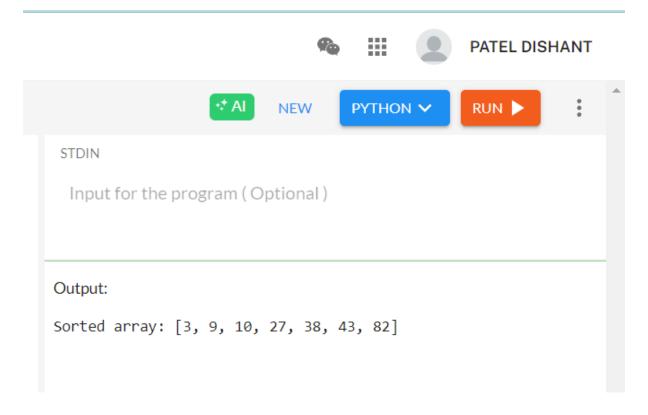
```
def merge(left, right):
  merged = []
  i = j = 0
  while i < len(left) and j < len(right):
     if left[i] <= right[j]:</pre>
       merged.append(left[i])
       i += 1
     else:
       merged.append(right[j])
       i += 1
  while i < len(left):
     merged.append(left[i])
     i += 1
  while j < len(right):
     merged.append(right[j])
     j += 1
  return merged
def merge_sort(arr):
  if len(arr) \leq 1:
     return arr
  mid = len(arr) // 2
  left half = merge sort(arr[:mid])
  right half = merge sort(arr[mid:])
  return merge(left half, right half)
arr = [38, 27, 43, 3, 9, 82, 10]
```

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sorted_arr = merge_sort(arr)
print("Sorted array:", sorted_arr)

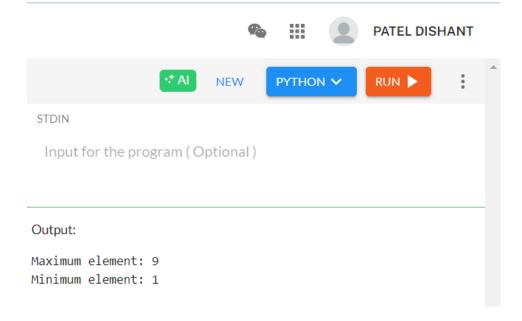


> Question 2:

Implementation of Max-Min by using Divide and Conquer principal TC: O(n)

- > Solution:
 - Source code:

```
def find max min(arr, low, high):
  if low == high:
    return arr[low], arr[low]
  elif high == low + 1:
    if arr[low] > arr[high]:
       return arr[low], arr[high]
    else:
       return arr[high], arr[low]
  mid = (low + high) // 2
  max1, min1 = find max min(arr, low, mid)
  max2, min2 = find max min(arr, mid + 1, high)
  overall max = max(max1, max2)
  overall min = min(min1, min2)
  return overall max, overall min
arr = [3, 5, 1, 8, 9, 2, 7, 6]
n = len(arr)
maximum, minimum = find max min(arr, 0, n - 1)
print(f"Maximum element: {maximum}")
print(f"Minimum element: {minimum}")
```



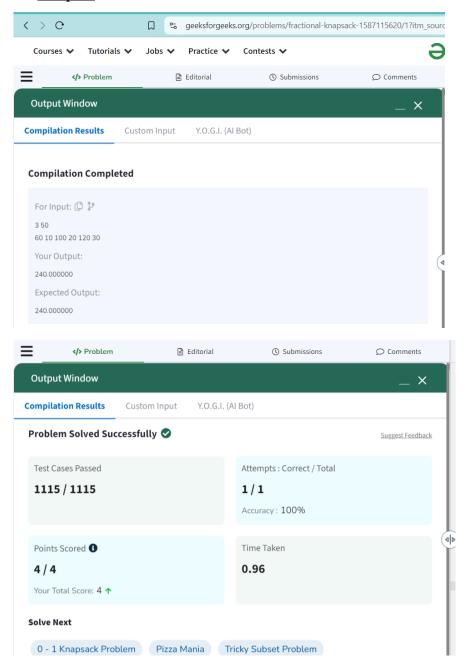
➤ Question 3:

Fractional Knapsack GeeksForGeeks Implementation of Fractional KnapSack TC: O(n log n) (Problem Statement: The weight of N items and their corresponding values are given. We have to put these items in a knapsack of weight W such that the total value obtained is maximized.)

> Solution:

• Source code:

```
class Item:
  def init (self,val,w):
     self.value = val
     self.weight = w
class Solution:
  def fractionalknapsack(self, w,arr,n):
     prof = [arr[i].value / arr[i].weight for i in range(n)]
     items = [[prof[i], arr[i].value, arr[i].weight] for i in range(n)]
     items.sort(key=lambda x: x[0], reverse=True)
     profit = 0
     i = 0
     while w > 0 and i < n:
        if items[i][2] \leq= w:
          profit += items[i][1]
          w = items[i][2]
        else:
           profit += items[i][0] * w
          \mathbf{w} = \mathbf{0}
        i += 1
     return profit
```



➤ Question 4: Implementation of Prim's Algorithm.

> Solution:

```
Source code:
  import heapq
  def prim(graph, start):
    mst = []
    visited = set()
    min heap = [(0, start)]
    total cost = 0
    while min heap:
       cost, node = heapq.heappop(min heap)
       if node in visited:
          continue
       visited.add(node)
       total cost += cost
       mst.append((node, cost))
       for neighbor, weight in graph[node]:
          if neighbor not in visited:
            heapq.heappush(min heap, (weight, neighbor))
    return mst, total cost
  graph = {
    0: [(1, 2), (3, 6)],
     1: [(0, 2), (2, 3), (3, 8), (4, 5)],
    2:[(1,3),(4,7)],
    3: [(0,6), (1,8)],
    4: [(1, 5), (2, 7)]
  mst, total cost = prim(graph, 0)
  print("Minimum Spanning Tree:", mst)
  print("Total Cost:", total cost)
```

Output:



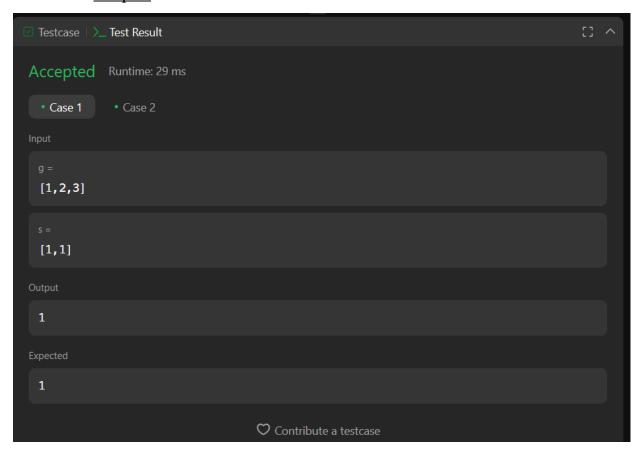
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➤ Question 5:

Assign Cookies. (Assume you are an awesome parent and want to give your children some cookies. But, you should give each child at most one cookie.) Leetcode problem number: 455

- > Solution:
 - Source code:

```
\label{eq:content_children} \begin{split} & \text{def find\_content\_children}(g,\,s) \colon \\ & \text{g.sort}() \\ & \text{s.sort}() \\ & \text{i} = \text{j} = 0 \\ & \text{while i} < \text{len}(g) \text{ and j} < \text{len}(s) \colon \\ & \text{if s[j]} >= \text{g[i]} \colon \\ & \text{i} += 1 \\ & \text{j} += 1 \\ & \text{return i} \end{split} g = [1, 2, 3] \\ s = [1, 1] \\ \text{result} = \text{find\_content\_children}(g,\,s) \\ \text{print}(\text{result}) \\ \end{split}
```



➤ Question 6:

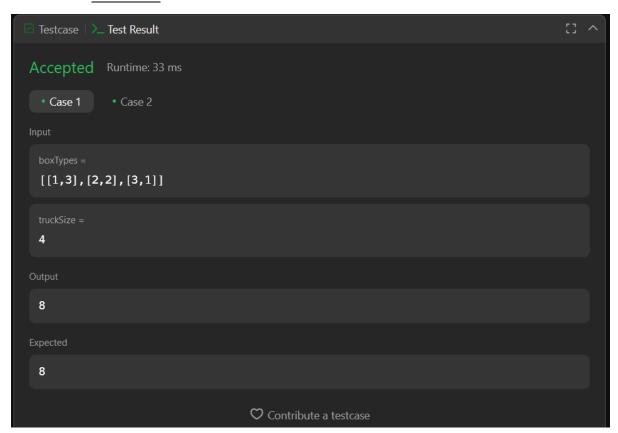
Maximum Units on a Truck. Leetcode problem number: 1710

> Solution:

```
• Source Code:
```

```
class Solution:
    def maximumUnits(self, boxTypes: List[List[int]], truckSize: int) -> int:
        boxTypes.sort(key=lambda x: x[1], reverse=True)
        total_units = 0
        for box_count, units in boxTypes:
            if truckSize == 0:
                break
        if box_count <= truckSize:
                total_units += box_count * units
                truckSize -= box_count
        else:
                total_units += truckSize * units
                truckSize = 0
        return total_units</pre>
```

• Solution:



➤ Question 7:

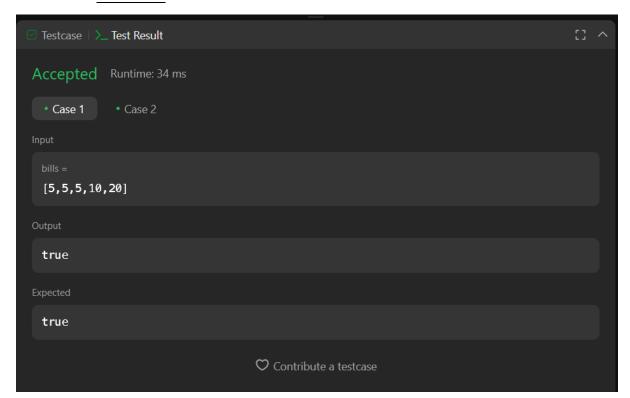
Lemonade Change. Leetcode problem number: 860

> Solution:

```
Source Code:
  class Solution:
     def lemonadeChange(self, bills: List[int]) -> bool:
        five, ten = 0, 0
        for bill in bills:
          if bill == 5:
             five += 1
          elif bill == 10:
             if five > 0:
                five -= 1
                ten += 1
             else:
                return False
          elif bill == 20:
             if ten > 0 and five > 0:
                ten -= 1
                five -= 1
             elif five \geq = 3:
                five -= 3
             else:
                return False
```

• Solution:

return True



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➤ Question 8:

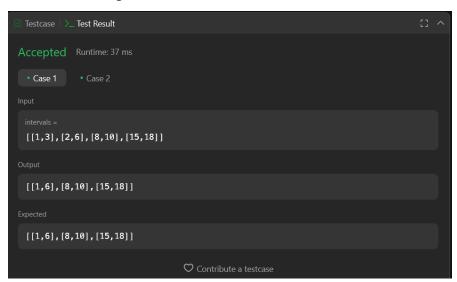
Merge Intervals Leetcode problem number: 56

> Solution:

```
Source Code:
    class Solution:
    def merge(self, intervals: List[List[int]]) -> List[List[int]]:
        intervals.sort(key=lambda x: x[0])
        merged = []

    for interval in intervals:
        if not merged or merged[-1][1] < interval[0]:
            merged.append(interval)
        else:
        merged[-1][1] = max(merged[-1][1], interval[1])</pre>
```

return merged



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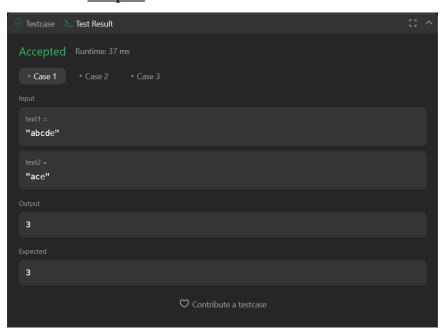
➤ Question 9:

LCS LeetCode problem number 1143

> Solution:

```
• Source Code:
```

```
class Solution:  \begin{aligned} &\text{def longestCommonSubsequence(self, text1: str, text2: str)} \rightarrow &\text{int:} \\ &m, \, n = \text{len(text1), len(text2)} \\ &dp = [[0]*(n+1) \text{ for } \_\text{ in range}(m+1)] \\ &\text{for } i \text{ in range}(1, m+1)\text{:} \\ &\text{for } j \text{ in range}(1, n+1)\text{:} \\ &\text{ if text1}[i-1] == \text{text2}[j-1]\text{:} \\ &dp[i][j] = dp[i-1][j-1] + 1 \\ &\text{else:} \\ &dp[i][j] = \text{max}(dp[i-1][j], dp[i][j-1]) \\ &\text{return } dp[m][n] \end{aligned}
```



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➤ Question 10:

Number of Coins Geeks For Geeks

> Solution:

```
Source Code:
  class Solution:
     def minCoins(self, coins, M, sum):
        k = float("inf")
        dp = [[k \text{ for } \_ \text{ in } range(sum + 1)] \text{ for } \_ \text{ in } range(M + 1)]
        dp[0][0] = 0
        for i in range(1, M + 1):
           for j in range(1, sum + 1):
             if coins[i-1] \le j:
                dp[i][j] = min(dp[i][j - coins[i - 1]] + 1, dp[i - 1][j])
             else:
                dp[i][j] = dp[i - 1][j]
        if dp[M][sum] == k:
           return -1
        return dp[M][sum]
  # Driver code
  if __name__ == "__main__":
     T = int(input())
     for i in range(T):
        v, m = input().split()
        v, m = int(v), int(m)
        coins = [int(x) for x in input().split()]
        ob = Solution()
        ans = ob.minCoins(coins, m, v)
        print(ans)
```

