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Math 314  
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## COSC/MATH - 314

### Assignment 2

**Problem 1: Exercise 10, page 56** (to convert to numbers, use  $a=0$ ,  $b=1$ ). Suppose there is a language that has only the letters  $a$  and  $b$ . The frequency of the letter  $a$  is  $.1$  and the frequency of  $b$  is  $.9$ . A message is encrypted using a Vigenere cipher (working mod 2 instead of mod 26). The ciphertext is BABABAAABA.

- (a.) Show that the key length is probably 2.
- (b.) Using the information on the frequencies of the letters, determine the key and decrypt the message.

Solution:

**Problem 2: Exercise 13, page 56** (if you want to compute the inverse of the matrix, see section 3.8). The ciphertext YIFZM A was encrypted by a Hill cipher with the matrix

$$\begin{bmatrix} 9 & 13 \\ 2 & 3 \end{bmatrix}$$

Find the plaintext.

Solution:

**Problem 3: Exercise 14, page 56** . (Note: The matrix  $M$  has 4 entries, so there are 4 unknowns, and to determine them you need 4 equations.) Since the given cipher-text/plaintext pair has 6 letters, you can form 6 equations. You need to choose 4 of them, so that the system that results can be solved.) The ciphertext text GEZXDS was encrypted by a Hill cipher with a  $2 \times 2$  matrix. The plaintext is solved. Find the encryption matrix  $M$  .

Solution:

**Problem 4:** The following ciphertext has been obtained by Vigenere encryption.

ocwyikoooniwugpmxwktzdwgtssayjzwyemdlbnqaaavsuwdvbrflauplooubfgq  
hgcscmgzlatoedcsdeidpbhtmuovpiekifpimfnoamvlpqfxejsmxmpgkccaykwfzp  
yuavtelwhrhmwkbbvgtguvtefjlodfefkvpxsgrsorgtajbsauhzrzalkwuowhgedef  
nswmrciwcpaaavogpdnfpktdbalsisurlnpsjyeatcuceesohhdarkhwotikbroqrdm  
zghgucebvgwcdqxgpbqqlpbdylooqdmuhbdqgmyweuik

- (a.) Use displacement of 5 and 6. Which displacement produces the largest number of coincidences?
- (b.) Find the key.
- (c.) Find the plaintext.

Solution: