

School of Mathematics, Thapar University
Operations Research (UMA-019)
 Tutorial Sheet 5

1. Consider the LPP

$$\text{Maximize } z = 3x_1 + 5x_2 + 4x_3$$

$$\text{Subject to } 2x_1 + 3x_2 \leq 8, 2x_2 + 5x_3 \leq 10, 3x_1 + 2x_2 + 4x_3 \leq 15, x_1, x_2, x_3 \geq 0.$$

- (a) Solve the LPP.
- (b) Find the range over which b_2 can be changed maintaining the feasibility of the solution.

2. Consider the problem, $\text{Max } z = 3x_1 + 2x_2 + 5x_3$

$$\text{s.t. } x_1 + 2x_2 + x_3 \leq 430, 3x_1 + 2x_3 \leq 460,$$

$$x_1 + 4x_2 \leq 420, x_1, x_2, x_3 \geq 0.$$

Given that x_2, x_3, x_6 (slack variable corresponding to constraint 3) form the optimal basis and inverse of the optimal basis is, row-wise; $\frac{1}{2}, -1/4, 0; 0, \frac{1}{2}, 0; -2, 1, 1$. Form the optimal table based on this information.

3. In problem 2, find the optimal solution if the objective function is changed to

$$(i) \quad z = 4x_1 + 2x_2 + x_3$$

$$(ii) \quad z = 3x_2 + x_3$$

4. In problem 2, a fourth variable is added with the technological (constraint) coefficients as 3, 2 and 4. Determine the optimal solution if the profit per unit of the new variable is given as 5 and 10.

5. Consider the following LPP, $\text{Max } z = 5x_1 + 2x_2 + 3x_3$ s.t. $x_1 + 5x_2 + 3x_3 = 30, x_1 - 5x_2 - 6x_3 \leq 40, x_1, x_2, x_3 \geq 0$. Solve this problem using M-method.

6. In problem 5, find the optimal solution, using sensitivity analysis if the objective function is changed to

$$(i) \quad \text{max } z = 12x_1 + 5x_2 + 2x_3$$

$$(ii) \quad \text{min } z = 2x_2 - 5x_3$$

7. In problem 5, suppose that the technological coefficients of x_2 are $(5 - a, -5 + a)$ instead of $(5, -5)$, where a is a nonnegative parameter. Find the value of a so that the solution remains optimal.

8. In problem 5, suppose that the right hand side of the constraint becomes $(30 + a, 40 - a)$, a is nonnegative parameter. Determine the values of a so that the solution of the problem remain optimal.

9. Solve the LPP: $\text{Maximize } z = 3x_1 + x_2 + 5x_3$

$$\text{Subject to } 6x_1 + 3x_2 + 5x_3 \leq 25, \quad 3x_1 + 4x_2 + 5x_3 \leq 20, \quad x_1, x_2, x_3 \geq 0.$$

Also, discuss the effect on the optimal solution if a new constraint

$$2x_1 - 3x_2 + 4x_3 = 15 \text{ is added.}$$

10. Consider the LPP: Maximize $z=3x_1+4x_2+x_3+7x_4$

Subject to $8x_1+3x_2+4x_3+x_4\leq 7$, $2x_1+6x_2+x_3+5x_4\leq 3$

$x_1+4x_2+5x_3+2x_4\leq 8$, $x_1, x_2, x_3, x_4\geq 0$.

- a) Solve the LPP.
- b) What will be the optimal solution if a new constraint $2x_1+3x_2+x_3+5x_4\leq 4$ is added?