

Roll Number: \_\_\_\_\_

**Thapar Institute of Engineering & Technology, Patiala**

Department of Computer Science and Engineering

**AUXILIARY EXAMINATION**

B. E. (CSE &amp; COE)

Course Code: UCS415

Course Name: Design and Analysis of Algorithms

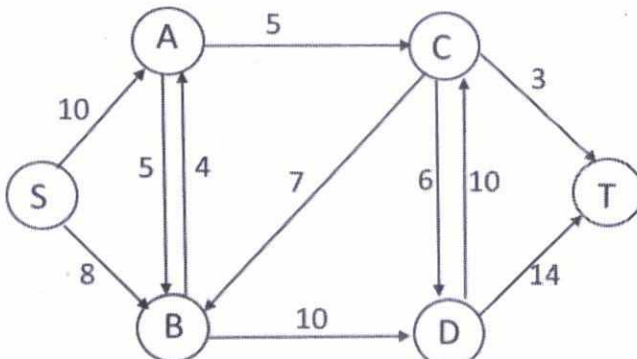
Date: August 17, 2022

Time: 5:30 PM – 7:30 PM

Duration: 2 Hours, M. Marks: 50

Name of Faculty: Dr. Yashwant Singh Patel

**Note: Attempt all questions in a proper sequence with justification.**  
**Assume missing data, if any, suitably.**

Q. 1(a)	Solve the following recurrence relation using recursive tree method.  $T(n) = \begin{cases} T\left(\frac{n}{3}\right) + T\left(\frac{2n}{3}\right) + n & n > 1 \\ 1 & n = 1 \end{cases}$	(5)
Q. 1(b)	Explain the difference between deterministic and non-deterministic algorithm? Also, explain the relationship between P, NP, NP-complete and NP hard class problems with example of each class.	(1+4)
Q. 2(a)	Execute the Ford-Fulkerson algorithm to find the maximum flow for a graph (shown in Fig. 1) from source S to destination T. Show all the intermediate steps of algorithm. Also explain: (a) Augmented path (b) Residual graph (c) Minimum cut (d) Residual capacity.   <b>Fig. 1</b>	(8)
Q. 2(b)	Discuss the time complexity of the Hierholzer's algorithm to determine Euler circuit ?	(2)
Q. 3	Use dynamic programming to fully parenthesize the product of five matrices, i.e. <b>A</b> [4 × 10], <b>B</b> [10 × 3], <b>C</b> [3 × 12], <b>D</b> [12 × 20], <b>E</b> [20 × 7] such that the number of scalar multiplications gets minimized. Show each and every step.	(10)
Q. 4(a)	Discuss the recursive definition/equation employed in dynamic programming solution for 0/1 knapsack problem. Utilize it to maximize the profit for a knapsack having a capacity of <b>W = 7</b> using four items. The respective weight and profit values of the four items are <b>w[ ] : (1, 3, 4, 5)</b> and <b>p[ ] : (1, 4, 5, 7)</b> .	(1+5)
Q. 4(b)	Consider a modification to the activity-selection problem in which each activity $a_i$ has, in addition to a start and finish time, a value $v_i$ . The objective is no longer to maximize the number of activities scheduled, but instead to maximize the total value of the activities scheduled. That is, we wish to choose a set $A$ of compatible activities such that $\sum_{a_k \in A} v_k$ is maximized. Discuss whether a greedy algorithm is possible. If yes, present such an algorithm, and if no, argue why not.	(4)

Q. 5(a)	For string matching, working modulo $q = 13$ , how many spurious hits does the Rabin-Karp matcher encounter in the Text $T = 3141592653589793$  When looking for the pattern $P = 26$ ? Explain your answer with proper implementation of Rabin-Karp algorithm.	(7)
Q. 5(b)	What is backtracking ? Explain 8 queen's problem and how can we solve it using backtracking ?	(3)