

INTERMEDIATE CODE GENERATION

4TH PHASE OF COMPILER CONSTRUCTION

1

SECTION 5.1: INTERMEDIATE CODE GENERATION

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INTERMEDIATE CODE GENERATION

Intermediate codes are machine independent codes, but they are close to machine instructions.

- The given program in a source language is converted to an equivalent program in an intermediate language by the intermediate code generator.

Benefits of using a machine-independent intermediate form are:

- Retargeting is facilitated. That is, a compiler for a different machine can be created by attaching a back end for the new machine to an existing front end.
- A machine-independent code optimizer can be applied to the intermediate representation.

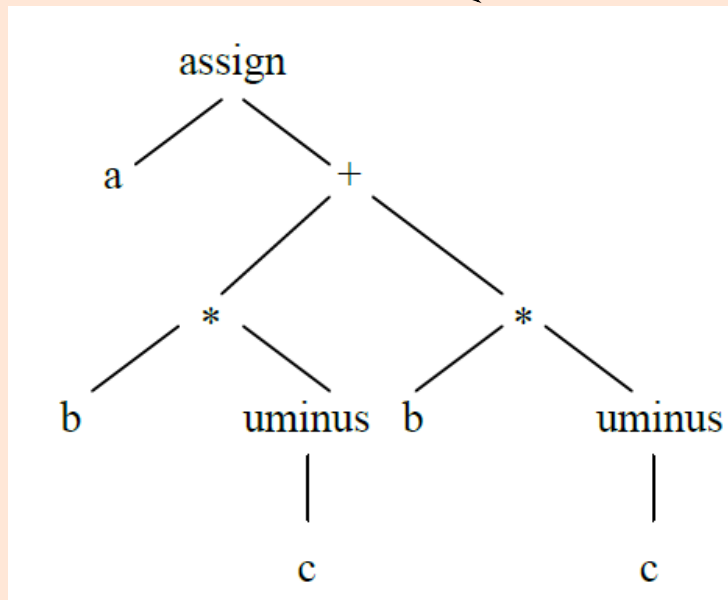
Three ways of intermediate representation:

- Graphical representations(syntax trees)
- Postfix notation (operations on values stored on operand stack; similar to JVM bytecode)
- Three-address code (triples or Quadruples)

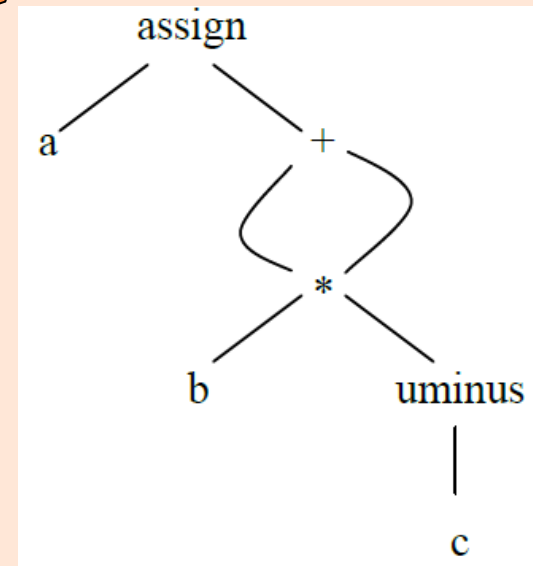
ABSTRACT SYNTAX TREE

- A syntax tree depicts the natural hierarchical structure of a source program. A DAG (Directed Acyclic Graph) gives the same information but in a more compact way because common subexpressions are identified.

a := b * -c + b * -c



Tree



DAG

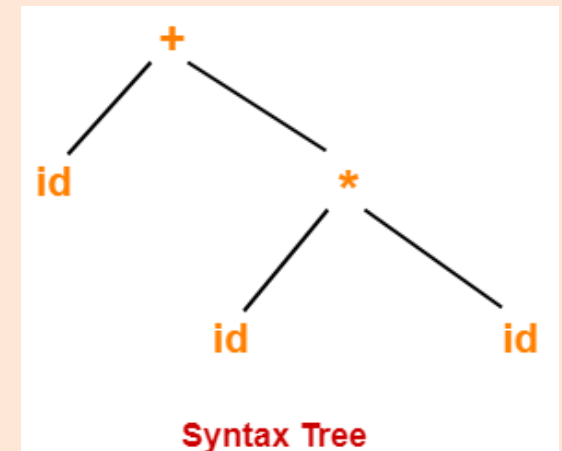
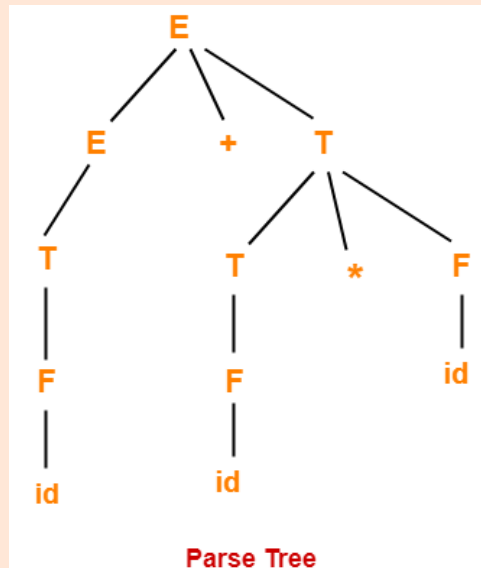
ABSTRACT SYNTAX TREE

- ASTs don't show the whole syntactic clutter, but represent the parsed string in a structured way, discarding all information that may be important for parsing the string, but isn't needed for analyzing it.
- Abstract syntax trees, or simply *syntax trees*, differ from parse trees because superficial distinctions of form, unimportant for translation, do not appear in syntax trees.

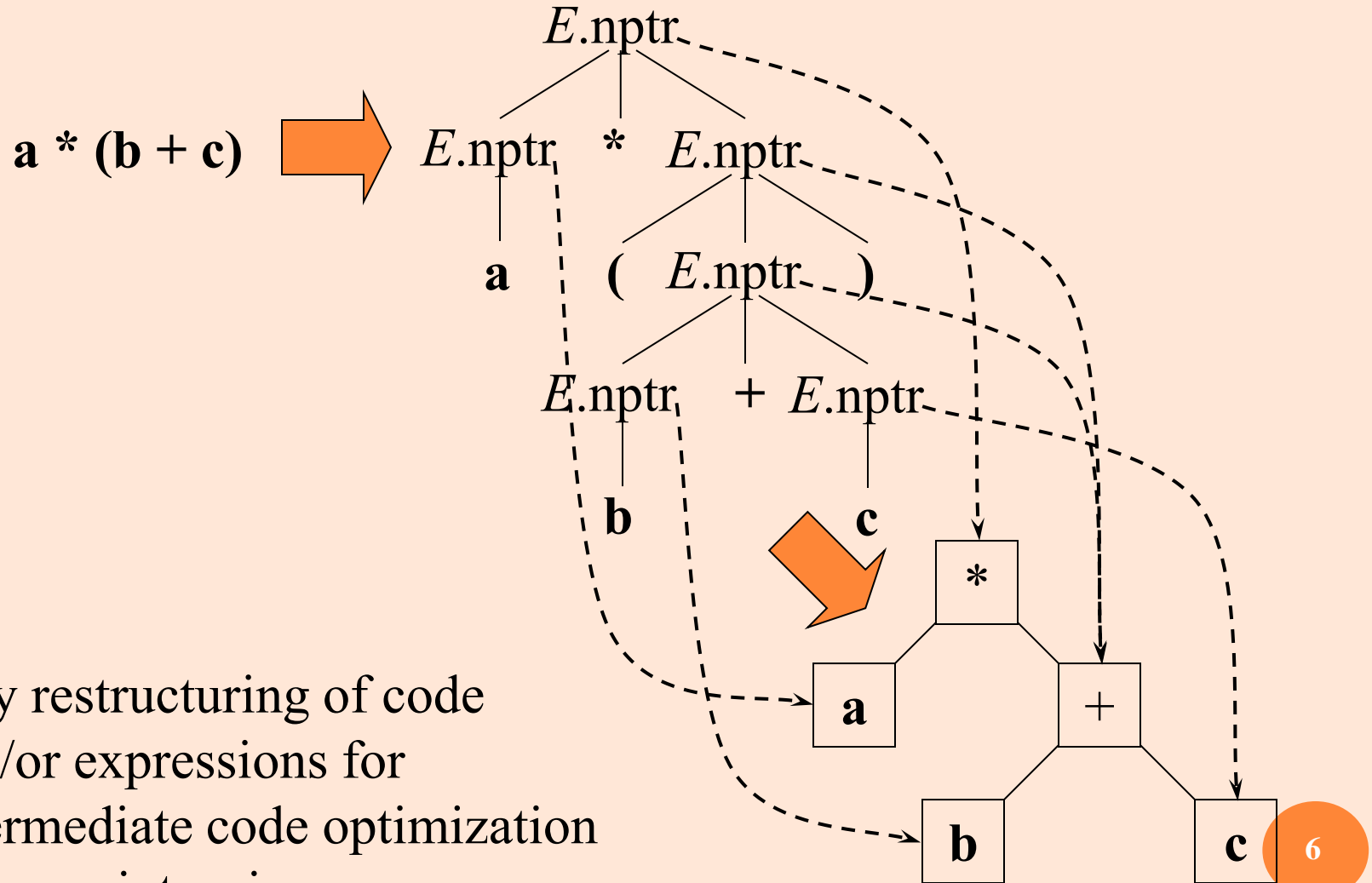
For the Grammar

$$E \rightarrow E + T \mid T$$
$$T \rightarrow T \times F \mid F$$
$$F \rightarrow (E) \mid \text{id}$$

Parse the string 'id + id x id'



ABSTRACT SYNTAX TREES



POSTFIX NOTATION

a := b * -c + b * -c

a b c uminus * b c uminus * + assign

Postfix notation represents
operations on a stack

Pro: easy to generate
Cons: stack operations are more
difficult to optimize

```
iload 2 // push b
iload 3 // push c
ineg // uminus
imul // *
iload 2 // push b
iload 3 // push c
ineg // uminus
imul // *
iadd // +
istore 1 // store a
```

THREE-ADDRESS CODE

Three-address code is a sequence of statements of the general form

$$x := y \text{ op } z$$

where x , y and z are names, constants, or compiler-generated temporaries; op stands for any operator, such as a fixed- or floating-point arithmetic operator, or a logical operator on Boolean valued data. Thus a source language expression like $x + y * z$ might be translated into a sequence

$$t1 := y * z$$
$$t2 := x + t1$$

where $t1$ and $t2$ are compiler-generated temporary names.

Advantages of three-address code:

- The unraveling of complicated arithmetic expressions and of nested flow-of-control statements makes three-address code desirable for target code generation and optimization.
- The use of names for the intermediate values computed by a program allows three address code to be easily rearranged – unlike postfix notation

THREE-ADDRESS CODE (QUADRUPLES)

$a := b * -c + b * -c$



```
t1 := - c
t2 := b * t1
t3 := - c
t4 := b * t3
t5 := t2 + t4
a := t5
```

Linearized representation
of a syntax tree

```
t1 := - c
t2 := b * t1
t5 := t2 + t2
a := t5
```

Linearized representation
of a syntax DAG

COMMON THREE-ADDRESS STATEMENTS

1. Assignment statements of the form $x := y \text{ op } z$, where op is a binary arithmetic or logical operation.
2. Assignment instructions of the form $x := \text{op } y$, where op is a unary operation. Essential unary operations include unary minus, logical negation, shift operators, and conversion operators that, for example, convert a fixed-point number to a floating-point number.
3. Copy statements of the form $x := y$ where the value of y is assigned to x .
4. The unconditional jump $\text{goto } L$. The three-address statement with label L is the next to be executed.
5. Conditional jumps such as $\text{if } x \text{ relop } y \text{ goto } L$. This instruction applies a relational operator ($<$, $=$, $>=$, etc.) to x and y , and executes the statement with label L next if x stands in relation relop to y . If not, the three-address statement following $\text{if } x \text{ relop } y \text{ goto } L$ is executed next, as in the usual sequence.

COMMON THREE-ADDRESS STATEMENTS

6. param x and call p, n for procedure calls and return y, where y representing a returned value is optional. For example,

param x1

param x2

...

param xn

call p,n

generated as part of a call of the procedure $p(x1, x2, \dots, xn)$.

7. Indexed assignments of the form $x := y[i]$ and $x[i] := y$.

8. Address and pointer assignments of the form $x := \&y$, $x := *y$, and $*x := y$.

THREE-ADDRESS STATEMENTS

Binary Operator: `op y, z, result` or `result := y op z`

where `op` is a binary arithmetic or logical operator. This binary operator is applied to `y` and `z`, and the result of the operation is stored in `result`.

Ex:

<code>add</code>	<code>a, b, c</code>
<code>gt</code>	<code>a, b, c</code>
<code>addr</code>	<code>a, b, c</code>
<code>addi</code>	<code>a, b, c</code>

Unary Operator: `op y, , result` or `result := op y`

where `op` is a unary arithmetic or logical operator. This unary operator is applied to `y`, and the result of the operation is stored in `result`.

Ex:

<code>uminus</code>	<code>a, , c</code>
<code>not</code>	<code>a, , c</code>
<code>inttoreal</code>	<code>a, , c</code>

THREE-ADDRESS STATEMENTS (CONT.)

Move Operator: `mov y, , result` or `result := y`
where the content of `y` is copied into `result`.

Ex: `mov a, , c`
 `movi a, , c`
 `movr a, , c`

Unconditional Jumps: `jmp , , L` or `goto L`

Jump to the three-address code with the label `L`, and the execution continues from that statement.

Ex: `jmp , , L1 // jump to L1`
 `jmp , , 7 // jump to the statement 7`

THREE-ADDRESS STATEMENTS (CONT.)

Conditional Jumps: `jmp`***relop*** `y, z, L`

or

`if y relop z goto L`

Jump to the three-address code with the label `L` if the result of `y relop z` is true, and the execution continues from that statement. If the result is false, the execution continues from the statement following this conditional jump statement.

Ex:

<code>jmpgt</code>	<code>y, z, L1</code>	// jump to L1 if <code>y > z</code>
<code>jmpgte</code>	<code>y, z, L1</code>	// jump to L1 if <code>y >= z</code>
<code>jmpe</code>	<code>y, z, L1</code>	// jump to L1 if <code>y == z</code>
<code>jmpne</code>	<code>y, z, L1</code>	// jump to L1 if <code>y != z</code>

Relational operator can also be a unary operator.

<code>jmpnz</code>	<code>y, , L1</code>	// jump to L1 if <code>y</code> is not zero
<code>jmpz</code>	<code>y, , L1</code>	// jump to L1 if <code>y</code> is zero
<code>jmpt</code>	<code>y, , L1</code>	// jump to L1 if <code>y</code> is true
<code>jmpf</code>	<code>y, , L1</code>	// jump to L1 if <code>y</code> is false

THREE-ADDRESS STATEMENTS (CONT.)

Procedure Parameters:

param $x, ,$ or param x

Procedure Calls:

call $p, n, ,$ or call p, n

where x is an actual parameter, we invoke the procedure p with n parameters.

Ex:

param $x_1, ,$

param $x_2, ,$

→ $p(x_1, \dots, x_n)$

param $x_n, ,$

call $p, n, ,$

$f(x+1, y)$ →

add $x, 1, t1$

param $t1, ,$

param $y, ,$

call $f, 2, ,$

THREE-ADDRESS STATEMENTS (CONT.)

Indexed Assignments:

move $y[i], , x$ or $x := y[i]$

move $x, , y[i]$ or $y[i] := x$

Address and Pointer Assignments:

moveaddr $y, , x$ or $x := \&y$

movecont $y, , x$ or $x := *y$

SYNTAX-DIRECTED TRANSLATION INTO THREE ADDRESS CODE

- Use attributes
 - *E.place*: the name that will hold the value of E
 - Identifier will be assumed to already have the place attribute defined.
 - *E.code*: hold the three address code statements that evaluate E (this is the 'translation' attribute).
- Use function *newtemp* that returns a new temporary variable which can be used.
- Use function *gen* to generate a single three address statement given the necessary information (variable names and operations).

SYNTAX-DIRECTED TRANSLATION INTO THREE ADDRESS CODE

$S \rightarrow \mathbf{id} := E$	$S.\text{code} = E.\text{code} \parallel \text{gen}(\text{'mov' } E.\text{place ' ,,' id.place})$
$E \rightarrow E_1 + E_2$	$E.\text{place} = \text{newtemp}();$ $E.\text{code} = E_1.\text{code} \parallel E_2.\text{code} \parallel \text{gen}(\text{'add' } E_1.\text{place ' ,,' } E_2.\text{place ' ,,' } E.\text{place})$
$E \rightarrow E_1 * E_2$	$E.\text{place} = \text{newtemp}();$ $E.\text{code} = E_1.\text{code} \parallel E_2.\text{code} \parallel \text{gen}(\text{'mult' } E_1.\text{place ' ,,' } E_2.\text{place ' ,,' } E.\text{place})$
$E \rightarrow - E_1$	$E.\text{place} = \text{newtemp}();$ $E.\text{code} = E_1.\text{code} \parallel \text{gen}(\text{'uminus' } E_1.\text{place ' ,,' } E.\text{place})$
$E \rightarrow (E_1)$	$E.\text{place} = E_1.\text{place};$ $E.\text{code} = E_1.\text{code}$
$E \rightarrow \mathbf{id}$	$E.\text{place} = \mathbf{id}.\text{place};$ $E.\text{code} = \text{null}$

SYNTAX-DIRECTED TRANSLATION (CONT.)

$S \rightarrow \text{while } E \text{ do } S_1$	$S.\text{begin} = \text{newlabel}();$ $S.\text{after} = \text{newlabel}();$ $S.\text{code} = \text{gen}(S.\text{begin} \text{ ":"}) \parallel E.\text{code} \parallel$ $\quad \text{gen}(\text{'jmpf' } E.\text{place} \text{ ',,' } S.\text{after}) \parallel S_1.\text{code} \parallel$ $\quad \text{gen}(\text{'jmp' '.,,' } S.\text{begin}) \parallel$ $\quad \text{gen}(S.\text{after} \text{ ':'})$
$S \rightarrow \text{if } E \text{ then } S_1 \text{ else } S_2$	$S.\text{else} = \text{newlabel}();$ $S.\text{after} = \text{newlabel}();$ $S.\text{code} = E.\text{code} \parallel$ $\quad \text{gen}(\text{'jmpf' } E.\text{place} \text{ ',,' } S.\text{else}) \parallel S_1.\text{code} \parallel$ $\quad \text{gen}(\text{'jmp' '.,,' } S.\text{after}) \parallel$ $\quad \text{gen}(S.\text{else} \text{ ':'}) \parallel S_2.\text{code} \parallel$ $\quad \text{gen}(S.\text{after} \text{ ':'})$

TRANSLATION SCHEME TO PRODUCE THREE-ADDRESS CODE

$S \rightarrow \mathbf{id} := E$ { $p = \text{lookup}(\text{id.name});$
 if (p is not nil) then $\text{emit}(\text{'mov' } E.\text{place ' , ' } p)$
 else $\text{error}(\text{"undefined-variable"})$ }

$E \rightarrow E_1 + E_2$ { $E.\text{place} = \text{newtemp}();$
 $\text{emit}(\text{'add' } E_1.\text{place ' , ' } E_2.\text{place ' , ' } E.\text{place})$ }

$E \rightarrow E_1 * E_2$ { $E.\text{place} = \text{newtemp}();$
 $\text{emit}(\text{'mult' } E_1.\text{place ' , ' } E_2.\text{place ' , ' } E.\text{place})$ }

$E \rightarrow - E_1$ { $E.\text{place} = \text{newtemp}();$
 $\text{emit}(\text{'uminus' } E_1.\text{place ' , ' } E.\text{place})$ }

$E \rightarrow (E_1)$ { $E.\text{place} = E_1.\text{place};$ }

$E \rightarrow \mathbf{id}$ { $p = \text{lookup}(\text{id.name});$
 if (p is not nil) then $E.\text{place} = \mathbf{id}.\text{place}$
 else $\text{error}(\text{"undefined-variable"})$ }

TRANSLATION SCHEME WITH LOCATIONS

$S \rightarrow \mathbf{id} := \{ E.\text{inloc} = S.\text{inloc} \} E$

 { $p = \text{lookup}(\text{id.name});$

 if (p is not nil) then { $\text{emit}(E.\text{outloc} \text{ 'mov' } E.\text{place} \text{ ',,' } p); S.\text{outloc} = E.\text{outloc} + 1$ }

 else { $\text{error}(\text{"undefined-variable"}); S.\text{outloc} = E.\text{outloc}$ } }

$E \rightarrow \{ E_1.\text{inloc} = E.\text{inloc} \} E_1 + \{ E_2.\text{inloc} = E_1.\text{outloc} \} E_2$

 { $E.\text{place} = \text{newtemp}(); \text{emit}(E_2.\text{outloc} \text{ 'add' } E_1.\text{place} \text{ ', ' } E_2.\text{place} \text{ ', ' } E.\text{place}); E.\text{outloc} = E_2.\text{outloc} + 1$ }

$E \rightarrow \{ E_1.\text{inloc} = E.\text{inloc} \} E_1 * \{ E_2.\text{inloc} = E_1.\text{outloc} \} E_2$

 { $E.\text{place} = \text{newtemp}(); \text{emit}(E_2.\text{outloc} \text{ 'mult' } E_1.\text{place} \text{ ', ' } E_2.\text{place} \text{ ', ' } E.\text{place}); E.\text{outloc} = E_2.\text{outloc} + 1$ }

$E \rightarrow - \{ E_1.\text{inloc} = E.\text{inloc} \} E_1$

 { $E.\text{place} = \text{newtemp}(); \text{emit}(E_1.\text{outloc} \text{ 'uminus' } E_1.\text{place} \text{ ',,' } E.\text{place}); E.\text{outloc} = E_1.\text{outloc} + 1$ }

$E \rightarrow (E_1) \{ E.\text{place} = E_1.\text{place}; E.\text{outloc} = E_1.\text{outloc} + 1 \}$

$E \rightarrow \mathbf{id} \{ E.\text{outloc} = E.\text{inloc}; p = \text{lookup}(\text{id.name});$

 if (p is not nil) then $E.\text{place} = \mathbf{id}.\text{place}$

 else $\text{error}(\text{"undefined-variable"})$ }

BOOLEAN EXPRESSIONS

$E \rightarrow \{ E_1.inloc = E.inloc \} E_1 \text{ and } \{ E_2.inloc = E_1.outloc \} E_2$
 $\{ E.place = newtemp(); \text{ emit}(E_2.outloc \text{ 'and' } E_1.place \text{ ', ' } E_2.place \text{ ', ' } E.place);$
 $E.outloc = E_2.outloc + 1 \}$

$E \rightarrow \{ E_1.inloc = E.inloc \} E_1 \text{ or } \{ E_2.inloc = E_1.outloc \} E_2$
 $\{ E.place = newtemp(); \text{ emit}(E_2.outloc \text{ 'and' } E_1.place \text{ ', ' } E_2.place \text{ ', ' } E.place);$
 $E.outloc = E_2.outloc + 1 \}$

$E \rightarrow \text{not } \{ E_1.inloc = E.inloc \} E_1$
 $\{ E.place = newtemp(); \text{ emit}(E_1.outloc \text{ 'not' } E_1.place \text{ ', ' } E.place); E.outloc = E_1.outloc + 1 \}$

$E \rightarrow \{ E_1.inloc = E.inloc \} E_1 \text{ **relop** } \{ E_2.inloc = E_1.outloc \} E_2$
 $\{ E.place = newtemp();$
 $\text{ emit}(E_2.outloc \text{ **relop**.code } E_1.place \text{ ', ' } E_2.place \text{ ', ' } E.place); E.outloc = E_2.outloc + 1 \}$

TRANSLATION SCHEME(CONT.)

$S \rightarrow \text{while } \{ E.\text{inloc} = S.\text{inloc} \} E \text{ do}$
 { emit(E.outloc 'jmpf' E.place ',', 'NOTKNOWN');
 $S_1.\text{inloc} = E.\text{outloc} + 1$; } S_1
 { emit($S_1.\text{outloc}$ 'jmp' ',', $S.\text{inloc}$);
 $S.\text{outloc} = S_1.\text{outloc} + 1$;
 backpatch(E.outloc, $S.\text{outloc}$); }

$S \rightarrow \text{if } \{ E.\text{inloc} = S.\text{inloc} \} E \text{ then}$
 { emit(E.outloc 'jmpf' E.place ',', 'NOTKNOWN');
 $S_1.\text{inloc} = E.\text{outloc} + 1$; } S_1 else
 { emit($S_1.\text{outloc}$ 'jmp' ',', 'NOTKNOWN');
 $S_2.\text{inloc} = S_1.\text{outloc} + 1$;
 backpatch(E.outloc, $S_2.\text{inloc}$); } S_2
 { $S.\text{outloc} = S_2.\text{outloc}$;
 backpatch($S_1.\text{outloc}$, $S.\text{outloc}$); }

THREE ADDRESS CODES - EXAMPLE

```
x:=1;  
y:=x+10;  
while (x<y) {  
    x:=x+1;  
    if (x%2==1) then y:=y+1;  
    else y:=y-2;  
}
```



```
01: mov    1,,x  
02: add    x,10,t1  
03: mov    t1,,y  
04: lt     x,y,t2  
05: jmpf   t2,,17  
06: add    x,1,t3  
07: mov    t3,,x  
08: mod    x,2,t4  
09: eq     t4,1,t5  
10: jmpf   t5,,14  
11: add    y,1,t6  
12: mov    t6,,y  
13: jmp    ,,16  
14: sub    y,2,t7  
15: mov    t7,,y  
16: jmp    ,,4  
17:
```


IMPLEMENTATION OF THREE-ADDRESS STATEMENTS: QUADS

$a := (-c * b) + (-c * b)$

A quadruple is a record structure with four fields, which are, op, arg1, arg2 and result.

- The op field contains an internal code for the operator. The three-address statement $x := y \text{ op } z$ is represented by placing y in arg1, z in arg2 and x in result (Res).
- The contents of fields arg1, arg2 and result are normally pointers to the symbol-table entries for the names represented by these fields. Temporary names must be entered into the symbol table as they are created.

#	Op	Arg1	Arg2	Res
(0)	uminus	c		t1
(1)	*	b	t1	t2
(2)	uminus	c		t3
(3)	*	b	t3	t4
(4)	+	t2	t4	t5
(5)	:=	t5		a

Quads (quadruples)

Pro: easy to rearrange code for global optimization
Cons: lots of temporaries

IMPLEMENTATION OF THREE-ADDRESS STATEMENTS: TRIPLES

$a := (-c * b) + (-c * b)$

Three-address statements can be represented by records with only three fields: op, arg1 and arg2.

- The fields arg1 and arg2, for the arguments of op, are either pointers to the symbol table or pointers into the triple structure (for temporary values).
- Since three fields are used, this intermediate code format is known as triples

#	Op	Arg1	Arg2
(0)	uminus	c	
(1)	*	b	(0)
(2)	uminus	c	
(3)	*	b	(2)
(4)	+	(1)	(3)
(5)	:=	a	(4)

Triples

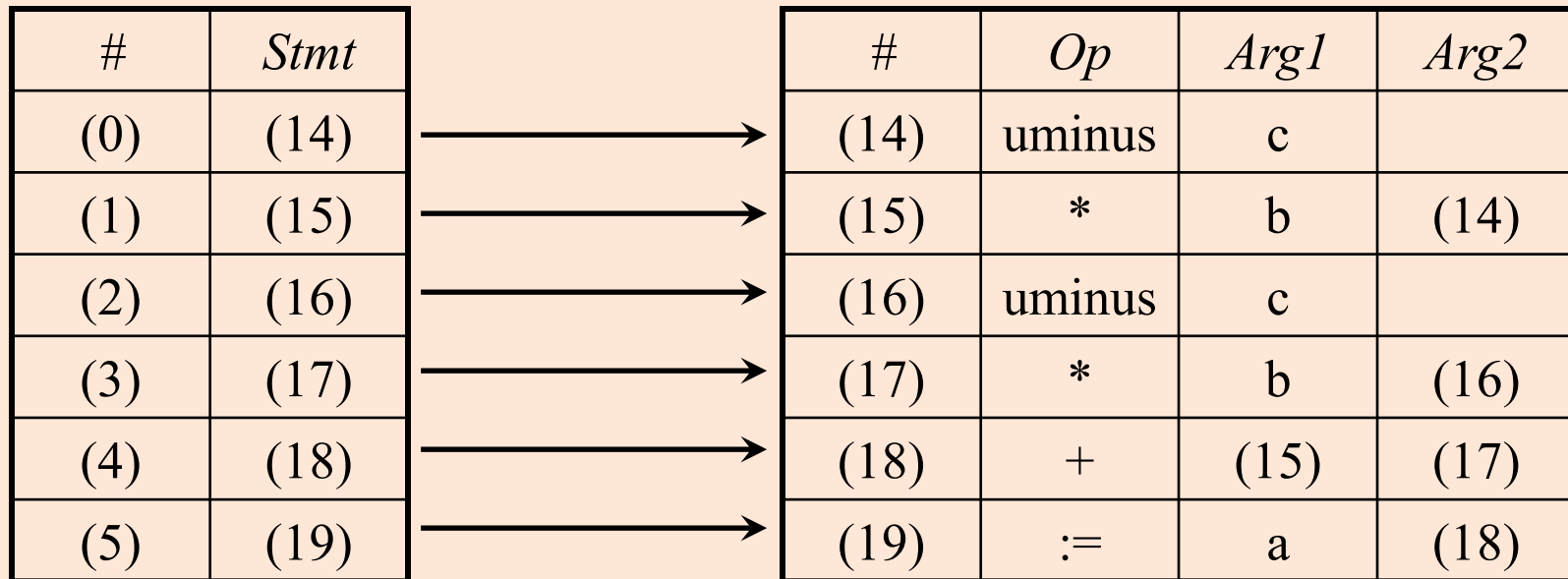
Pro: temporaries are implicit

Cons: difficult to rearrange code

INDIRECT TRIPLES

Listing pointers to triples, rather than listing the triples themselves is called indirect triples.

$a := (-c * b) + (-c * b)$



Program

Triple container

Pro: temporaries are implicit & easier to rearrange code

EXAMPLE

Three address code for $a+b*c - d/(b*c)$

3-address code

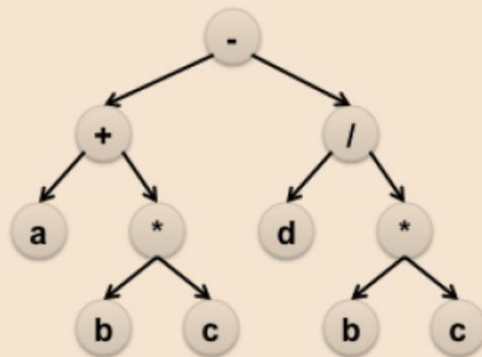
```
1 t1 = b*c
2 t2 = a+t1
3 t3 = b*c
4 t4 = d/t3
5 t5 = t2-t4
```

Quadruples

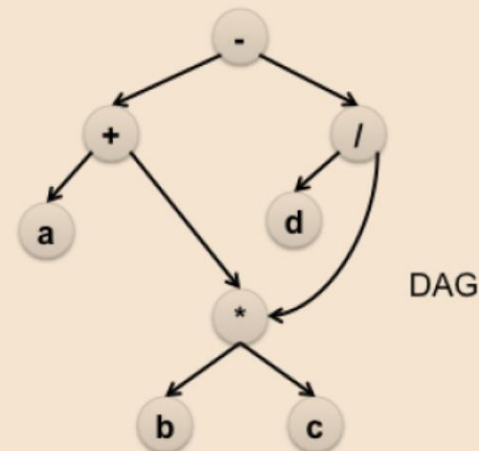
op	arg ₁	arg ₂	result
*	b	c	t1
+	a	t1	t2
*	b	c	t3
/	d	t3	t4
-	t2	t4	t5

Triples

	op	arg ₁	arg ₂
0	*	b	c
1	+	a	(0)
2	*	b	c
3	/	d	(2)
4	-	(1)	(3)



Syntax tree



DAG

SECTION 5.2: TYPE CHECKING

TYPE CHECKING

- A compiler has to do both syntactic and semantic check of the source program
- Semantic Checks can be of two types:
 - **Static** – done during compilation
 - **Dynamic** – done during run-time
- **Type checking** is one of these static checking operations.
 - we may not do all type checking at compile-time.
 - Some systems also use dynamic type checking too.
- A **type system** is a collection of rules for assigning type expressions to the parts of a program.
- A **type checker** implements a type system.
- A **sound** type system eliminates run-time type checking for type errors because it allow us to determine statically that these errors cannot occur when the target program runs.
- A programming language is **strongly-typed**, if every program its compiler accepts will execute without type errors.
 - In practice, some of type checking operations are done at run-time (so, most of the programming languages are not strongly-typed).
 - Ex: `int x[100]; ... x[i]` → most of the compilers cannot guarantee that `i` will be between 0 and 99

TYPE EXPRESSION

- The type of a language construct is denoted by a *type expression*.
- A *type expression* can be:
 - **A basic type**
 - a primitive data type such as *integer, real, char, boolean, ...*
 - *type-error* to signal a type error
 - *void* : no type
 - **A type name**
 - a name can be used to denote a type expression.
 - **A type constructor applies to other type expressions.**
 - **arrays:** If T is a type expression, then $array(I, T)$ is a type expression where I denotes index range. Ex: $array(0..99, int)$
 - **products:** If T_1 and T_2 are type expressions, then their cartesian product $T_1 \times T_2$ is a type expression. Ex: $int \times int$
 - **pointers:** If T is a type expression, then $pointer(T)$ is a type expression. Ex: $pointer(int)$
 - **functions:** We may treat functions in a programming language as mapping from a domain type D to a range type R . So, the type of a function can be denoted by the type expression $D \rightarrow R$ where D and R are type expressions. Ex: $int \rightarrow int$ represents the type of a function which takes an int value as parameter, and its return type is also int .

A SIMPLE TYPE CHECKING SYSTEM

$P \rightarrow D;E$

$D \rightarrow D;D$

$D \rightarrow \mathbf{id}:T \quad \{ \text{addtype}(\mathbf{id.entry}, T.\text{type}) \}$

$T \rightarrow \mathbf{char} \quad \{ T.\text{type}=\mathbf{char} \}$

$T \rightarrow \mathbf{int} \quad \{ T.\text{type}=\mathbf{int} \}$

$T \rightarrow \mathbf{real} \quad \{ T.\text{type}=\mathbf{real} \}$

$T \rightarrow \uparrow T_1 \quad \{ T.\text{type}=\text{pointer}(T_1.\text{type}) \}$

$T \rightarrow \mathbf{array}[\mathbf{intnum}] \text{ of } T_1 \quad \{ T.\text{type}=\mathbf{array}(1..\mathbf{intnum.val}, T_1.\text{type}) \}$

The prefix operator \uparrow builds a pointer type.
Eg. \uparrow Integer leads to the type expression
`pointer(integer)`

TYPE CHECKING OF EXPRESSIONS

$E \rightarrow \text{id} \quad \{ E.\text{type} = \text{lookup}(\text{id}.\text{entry}) \}$

*Lookup(E) is used to fetch the type saved in the symbol table entry pointed to by e

$E \rightarrow \text{literal} \quad \{ E.\text{type} = \text{char} \}$

$E \rightarrow \text{num}_1 \quad \{ E.\text{type} = \text{int} \}$

$E \rightarrow \text{num}_2 \quad \{ E.\text{type} = \text{real} \}$

*Constants represented by the tokens **literal**, **num₁** and **num₂** have type char, int and real.

$E \rightarrow E_1 + E_2 \quad \{ \text{if } (E_1.\text{type} = \text{int} \text{ and } E_2.\text{type} = \text{int}) \text{ then } E.\text{type} = \text{int}$
else if $(E_1.\text{type} = \text{int} \text{ and } E_2.\text{type} = \text{real})$ then $E.\text{type} = \text{real}$
else if $(E_1.\text{type} = \text{real} \text{ and } E_2.\text{type} = \text{int})$ then $E.\text{type} = \text{real}$
else if $(E_1.\text{type} = \text{real} \text{ and } E_2.\text{type} = \text{real})$ then $E.\text{type} = \text{real}$
else $E.\text{type} = \text{type-error} \}$

TYPE CHECKING OF EXPRESSIONS

$E \rightarrow E_1 [E_2] \quad \{ \text{if } (E_2.\text{type}=\text{int} \text{ and } E_1.\text{type}=\text{array}(s,t)) \text{ then } E.\text{type}=t$
 $\text{else } E.\text{type}=\text{type-error} \}$

*The index expression E_2 , the index expression E_2 must have type integer. The result is the element type t obtained from the type $\text{array}(s,t)$ of E_1 .

$E \rightarrow E_1 \uparrow \quad \{ \text{if } (E_1.\text{type}=\text{pointer}(t)) \text{ then } E.\text{type}=t$
 $\text{else } E.\text{type}=\text{type-error} \}$

*The postfix operator yields the object pointed to by its operand. The type of E is the type t of the object pointed to by the pointer E .

TYPE CHECKING OF STATEMENTS

Assignment Statement

$S \rightarrow \text{id} = E$ { if (id.type=E.type then S.type=void
 else S.type=type-error }

Conditional Statement

$S \rightarrow \text{if } E \text{ then } S_1$ { if (E.type=boolean then S.type= S_1 .type
 else S.type=type-error }

While Statement

$S \rightarrow \text{while } E \text{ do } S_1$ { if (E.type=boolean then S.type= S_1 .type
 else S.type=type-error }

TYPE CHECKING OF FUNCTIONS

$E \rightarrow E_1 (E_2) \quad \{ \text{ if } (E_2.\text{type}=s \text{ and } E_1.\text{type}=s \rightarrow t) \text{ then } E.\text{type}=t$
 $\text{ else } E.\text{type}=\text{type-error } \}$

Ex: **int** f(double x, char y) { ... }

f: double x char \rightarrow **int**

argument types return type

The diagram shows the function signature 'f: double x char → int'. Below 'double x char' is the text 'argument types' with an arrow pointing to the parameter list. Below 'int' is the text 'return type' with an arrow pointing to the return type.

STRUCTURAL EQUIVALENCE OF TYPE EXPRESSIONS

- How do we know that two type expressions are equal?
- As long as type expressions are built from basic types (no type names), we may use structural equivalence between two type expressions

Structural Equivalence Algorithm (sequiv):

if (s and t are same basic types) then return true

else if (s=array(s₁,s₂) and t=array(t₁,t₂)) then return (sequiv(s₁,t₁) and sequiv(s₂,t₂))

else if (s = s₁ x s₂ and t = t₁ x t₂) then return (sequiv(s₁,t₁) and sequiv(s₂,t₂))

else if (s=pointer(s₁) and t=pointer(t₁)) then return (sequiv(s₁,t₁))

else if (s = s₁ → s₂ and t = t₁ → t₂) then return (sequiv(s₁,t₁) and sequiv(s₂,t₂))

else return false

NAMES FOR TYPE EXPRESSIONS

- In some programming languages, we give a name to a type expression, and we use that name as a type expression afterwards.

```
type link = ↑ cell;
```

```
var p,q : link;
```

```
var r,s : ↑ cell
```

p,q,r,s have same types ?

- How do we treat type names?
 - Get equivalent type expression for a type name (then use structural equivalence), or
 - Treat a type name as a basic type.

CYCLES IN TYPE EXPRESSIONS

```
type link = ↑ cell;  
type cell = record  
    x : int,  
    next : link  
end;
```

- We cannot use structural equivalence if there are cycles in type expressions.
- We have to treat type names as basic types.
 - ➔ but this means that the type expression `link` is different than the type expression `↑cell`.