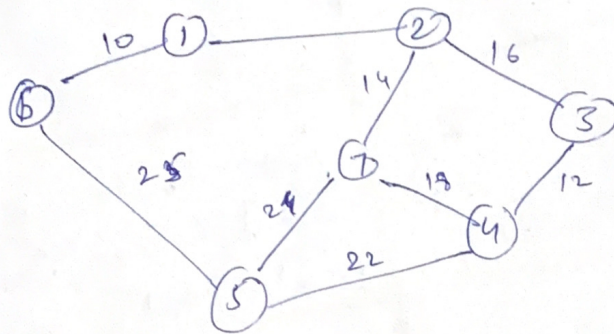


## Prim's algorithm



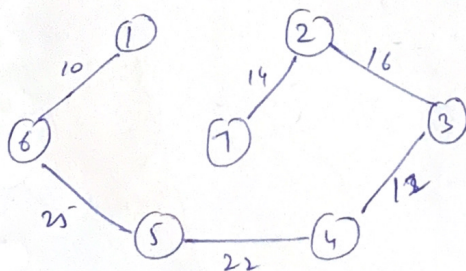
the cost adjacency matrix for the above graph is:

|   | 1        | 2        | 3        | 4        | 5        | 6        | 7        |
|---|----------|----------|----------|----------|----------|----------|----------|
| 1 | 0        | 28       | $\infty$ | $\infty$ | $\infty$ | 10       | $\infty$ |
| 2 | 28       | 0        | 16       | $\infty$ | $\infty$ | $\infty$ | 14       |
| 3 | $\infty$ | 16       | 0        | 12       | $\infty$ | $\infty$ | $\infty$ |
| 4 | $\infty$ | $\infty$ | 12       | 0        | 22       | $\infty$ | 18       |
| 5 | $\infty$ | $\infty$ | $\infty$ | 22       | 0        | 25       | 24       |
| 6 | 10       | $\infty$ | $\infty$ | $\infty$ | 25       | 0        | $\infty$ |
| 7 | $\infty$ | 14       | $\infty$ | 18       | 24       | $\infty$ | 0        |

| tree vertices     | Remaining vertices   | Resulting graph |
|-------------------|--|-----------------|
| 1. 1(-,-)         | 2(1,28)    4(1, $\infty$ ) <u>6(1,10)</u><br>3(1, $\infty$ )    5(1, $\infty$ )    7(1, $\infty$ )   |                 |
| 2. <u>6(1,10)</u> | 2(1,28)    2(6, $\infty$ ) <del>3(6,<math>\infty</math>)</del><br>3(1, $\infty$ )    3(6, $\infty$ )<br>4(1, $\infty$ )    4(6, $\infty$ )<br>5(1, $\infty$ ) <u>5(6,25)</u><br>7(1, $\infty$ )    7(6, $\infty$ ) |                 |

|             |   |  |
|-------------|---|--|
| 3. 5(6, 25) | $2(1, 28)$ $2(6, 8)$ $2(5, \infty)$<br>$3(1, \infty)$ $3(6, \infty)$ $3(5, \infty)$<br>$4(1, \infty)$ $4(6, \infty)$ $4(5, 22)$<br>$7(1, \infty)$ $7(6, \infty)$ $7(5, 24)$ |  |
| 4. 4(5, 22) | $2(1, 28)$ $2(6, \infty)$ $2(5, \infty)$ $2(4, \infty)$<br>$3(1, \infty)$ $3(6, \infty)$ $3(5, \infty)$ $3(4, 12)$<br>$7(1, \infty)$ $7(6, \infty)$ $7(5, 24)$ $7(4, 18)$   |  |
| 5. 3(4, 12) | $2(1, 28)$ $2(6, \infty)$ $2(5, \infty)$<br>$7(1, \infty)$ $7(6, \infty)$ $7(5, 24)$<br>$2(4, \infty)$ $2(3, 16)$<br>$7(4, 18)$ $7(3, \infty)$                              |  |
| 6. 2(3, 16) | $7(1, \infty)$ $7(6, \infty)$ $7(5, 24)$<br>$7(4, 18)$ $7(3, \infty)$ $7(2, 14)$  |  |
| 7. 7(2, 14) |   |  |

Minimum spanning tree :



$$\begin{aligned}
 \text{Minimum cost} &= 10 + 25 + 22 + 12 + 16 + 14 \\
 &= 99 \text{ units}
 \end{aligned}$$