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Assignment-1 (EE3025)

EE18BTECH11013 - Divyansh Maduriya

Download all python codes from

https://github.com/Divyansh-28/EE3025-EE18BTECH11013/tree/master/codes

and latex-tikz codes from

https://github.com/Divyansh-28/EE3025-EE18BTECH11013

1 Problem

Compute

$$X(k) \triangleq \sum_{n=0}^{N-1} x(n)e^{-j2\pi kn/N}, \quad k = 0, 1, \dots, N-1$$
(1.0.1)

and H(k) using h(n).

2 Solution

we know that

$$y(n) + \frac{1}{2}y(n-1) = x(n) + x(n-2)$$
 (2.0.1)

Where,
$$x(n) = \left\{ 1, 2, 3, 4, 2, 1 \right\}$$
 (2.0.2)

Taking Z-transform

$$Y(z) = \frac{2(z^2 + 1)}{z(2z + 1)}X(z)$$
 (2.0.3)

and

$$H(z) = \frac{2(z^2 + 1)}{z(2z + 1)}$$
 (2.0.4)

$$H(z) = \left[\frac{1}{1 + \frac{1}{2}z^{-1}} + \frac{z^{-2}}{1 + \frac{1}{2}z^{-1}} \right] z^{-1}$$
 (2.0.5)

Taking Inverse Z-Transform,

$$h(n) = \left[\frac{-1}{2}\right]^{n-2} u(n-2) + \left[\frac{-1}{2}\right]^n u(n) \qquad (2.0.6)$$

From equation 1.0.1

$$X(k) = \sum_{n=0}^{N-1} x(n)e^{-j2\pi kn/N}, \quad k = 0, 1, \dots, N-1$$
(2.0.7)

and

$$H(k) = \sum_{n=0}^{N-1} h(n)e^{-j2\pi kn/N}, \quad k = 0, 1, \dots, N-1$$
(2.0.8)

Plots:

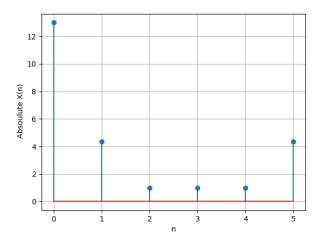


Fig. 0: Abs X(n)

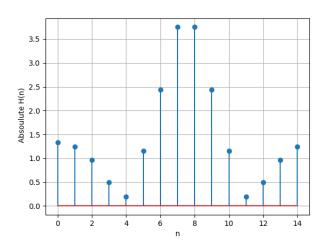


Fig. 0: Abs H(n)

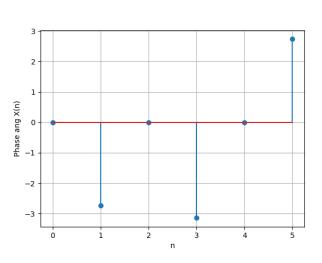


Fig. 0: angle X(n)

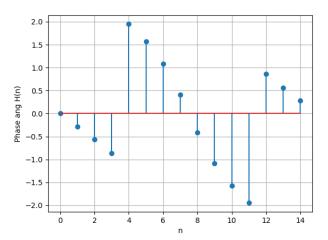


Fig. 0: Phase of h(k)