

STUDENT PORTFOLIO

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Department: Computer Science Engineering
Specialization: Big Data Analytics
Semester: 5

Subject Title: I8CSC30LJ Formal Language & Automata

Handled By: Sharanya S

Assignment – WorkSheet (Unit 1, 2, 3, 4, & 5)

(Write about the assignment questions and how you solved differently)

- Assignment questions were from all topics like Automata, Regular expressions, NFA,DFA,Pumping lemma,CFG,CNF,GNF, PDA,Turing machines. • Questions were of moderate difficulty which induced logical thinking.
- Solving questions was initially difficult. But, over a period it became comparatively easy.
- Overall,these assignment questions helped me to understand the subject better and it gave practice to different types of questions.

Assignment

(what is the most interesting part in the assignment)

- It made me think about how this could be used for real time problem solving.
- Most of the questions were based on the basic understanding which I found the most interesting.
- The questions were designed into the perfect way that tested our understanding and basic concepts in every topic covered in the offline/online classes.

HackerRank Achievements

- Problem Solving certificate Hackerrank
- Python (basic) certificate
- CCC Exit Test

Any other

(Write if you registered or practised apart from Codechef (ex. Hackerrank, Leetcode etc.))

- Hackerrank - registered and started working.
- Leetcode - registered and started working.
- Codechef - registered and started working.

Signature

Note: Enclose the assignment and relevant certificates along with the profile

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WorkSheet - 1

1)

Let $P(n)$ be $2^n - 1$ Basic step: $P(1) = \text{True}$ SD

$$\text{LHS} \rightarrow 2^{2^1} - 1 = 3$$

(C+S) It is divisible by 3.

Inductive step result (C+S) = P

Assume that $\neg P(k)$ is True

$$2^{2^k} - 1 = 3k + \text{SD} \quad (C+S)$$

we have to prove $P(k+1)$ is trueLHS = $2^{2(k+1)} - 1$

$$= 4(3k+1) - 1$$

$$\Rightarrow 12k+3 = 3(4k+1)$$

It is divisible by 3 as = 3 (F)

RHS

$$3(k+1) = 3k+3 = 3(k+1)$$

It is divisible by 3.

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3) $a^2 = 3k$, a^2 is divisible by 3.

$a = (3k+1)$ or $(3k+2)$, a is not divisible by 3.

a^2 is divisible by 3 $\rightarrow a^2 = 3k$

a is divisible by 3 $\rightarrow a = (3k+1)$ or $(3k+2)$

$a^2 = (3k+1)^2$ or $(3k+2)^2$

$\rightarrow 3k+1$ or $3k+1$ is divisible

3) let a & b be integers and assume that $a+b$ is odd but $a+b$ are both even sum of 2 even integers must be even therefore $a+b$ is even

But then $a+b$ both are even (add odd)

which is contradictory.

$$(1+2k) + (1+2l) = 2(1+k+l)$$

4) $P = 2n^2 - 16n + 31$. This always the for all

$n \rightarrow$ taken

$$n=5$$

$$P(5) = 2 \times 25 - (16 \times 5 + 31) = 1$$

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1

$$P(4) = 2 \times 16 - (6 \times 4 + 3) = 1$$

5) Let $P(n)$ for $n \geq 5 \rightarrow 2^n > n^2$

Base steps :-

Assume $P(5)$

$$2^5 > 5^2$$

$$32 > 25$$

Hence, $P(5)$ is true

LHS

$$2^{k+1} > (k+1)^2$$

$$2^k \cdot 2 > k^2 + 2k + 1$$

$$2(2^k) > 2^{k+2}$$

$$6) 1^2 + 2^2 + 3^2 + \dots + k^2 = \frac{k(k+1)(2k+1)}{6}$$

$$\frac{k(k+1)(2k+1)(k+1)^2}{6} = \frac{k(k+1)(2k+1)(2k+3)}{6}$$

$$= \frac{k(k+1)(2k+3)}{6}$$

If it is true $P(k+1)$ is

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FLA Worksheet - 3

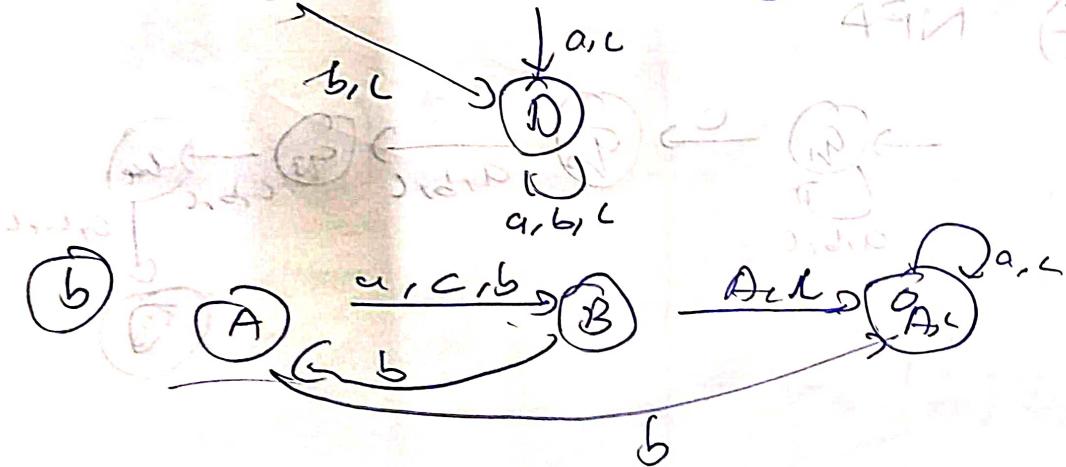
- j) 2(b)
 2) h(a)
 3) 15(c)
 4) increase computation



- 5) 2n
 6) I is false & II is true
 7) DFA is more powerful
 8) S

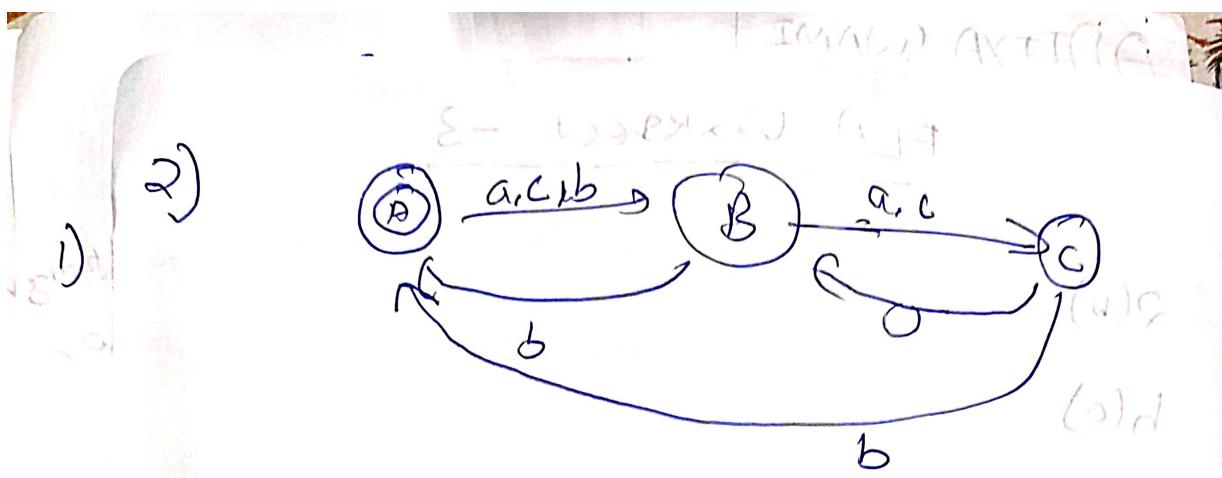
Part - B

- 1) P@S should start with 'a,b'

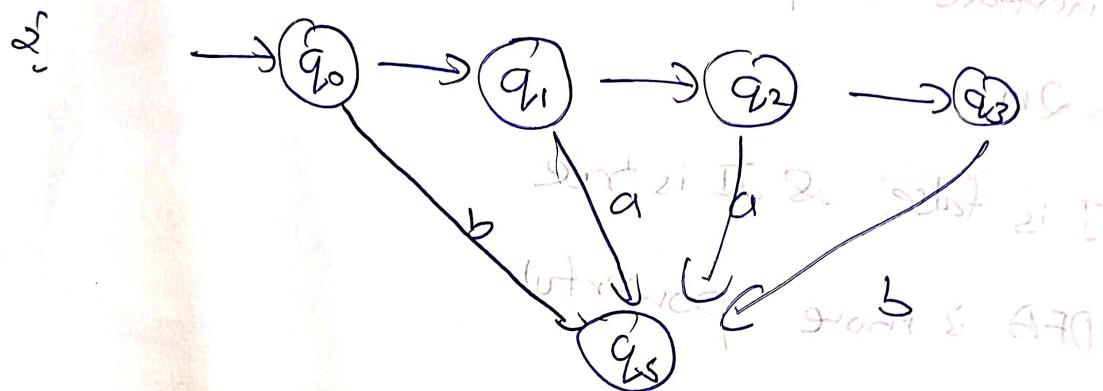


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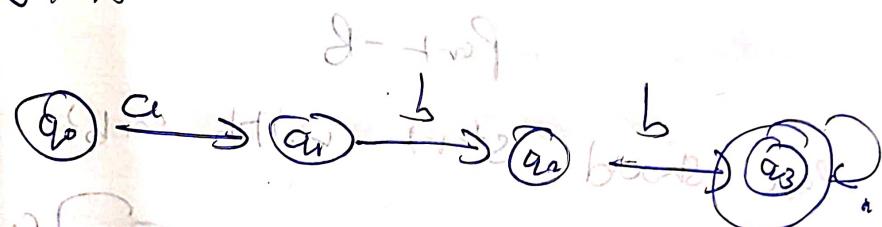
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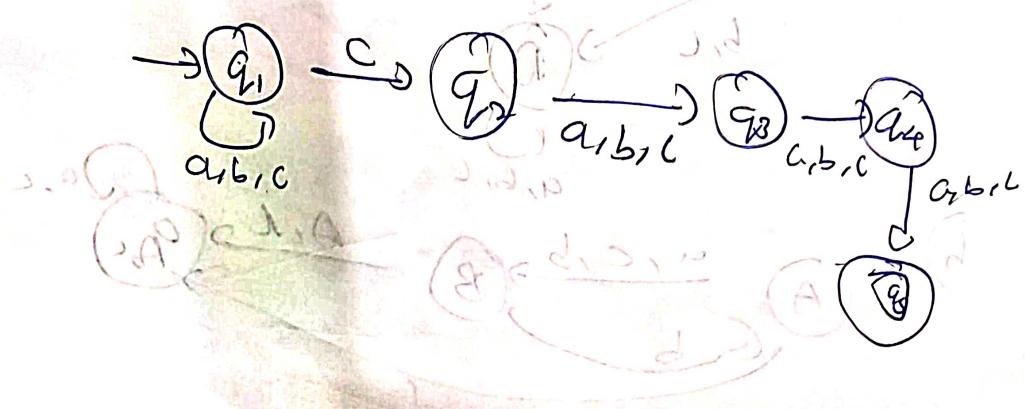
3) DFA



NFA



4) NFA



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Worksheet - 4

- ① In NDFA we get multiple choices. If we have a language satisfying a DFA, it will also satisfy its equivalent NDFA.

$$(d, \epsilon) \text{ word } - 3 = (\phi, \epsilon)^3$$

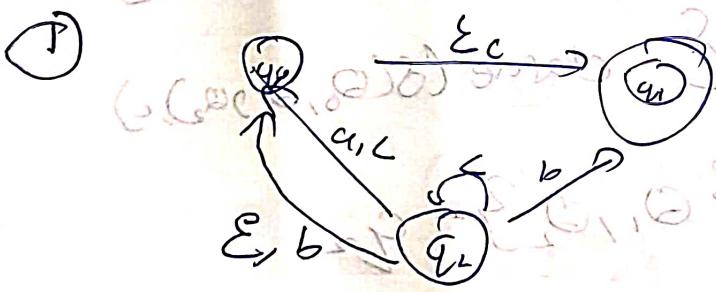
$$2^n = \epsilon - \text{word}$$

$$n \cdot 2^n = (\phi, \epsilon)^n$$

$$f = Q \times (\Sigma \times \Sigma) = P(Q)$$

- ⑤ All the states can reach final states & ϵ -NFA only by reaching on ϵ .

$$\text{Part-B}$$



Transition table:

	a	b	c
Q_0	\emptyset	\emptyset	\emptyset_2, \emptyset_3
Q_1	\emptyset	\emptyset	\emptyset
Q_2	\emptyset_0	\emptyset_1	\emptyset_2

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$$\mathcal{E}\text{-closure}(\phi_0) = \mathcal{E}[\phi_0, \phi_1, \phi_2] - q_2$$

$$\mathcal{E}\text{-closure}(\phi_1) = \mathcal{E}[\phi_0, \phi_1] - q_2$$

$$\mathcal{E}\text{-closure}(\phi_2) = \mathcal{E}[\phi_2] - q_2$$

$$\mathcal{S}'(q_0, a) = \mathcal{E}\text{-closure}(\mathcal{S}(q_0, q_1))$$

$$\Rightarrow \mathcal{E}[\phi_0] - q_2$$

$$\mathcal{S}(q_0, b) = \mathcal{E}\text{-closure}(\mathcal{S}(q_0, b))$$

$$= \mathcal{S}\text{-closure}(\mathcal{S}(Q_0, Q_1, Q_2))$$

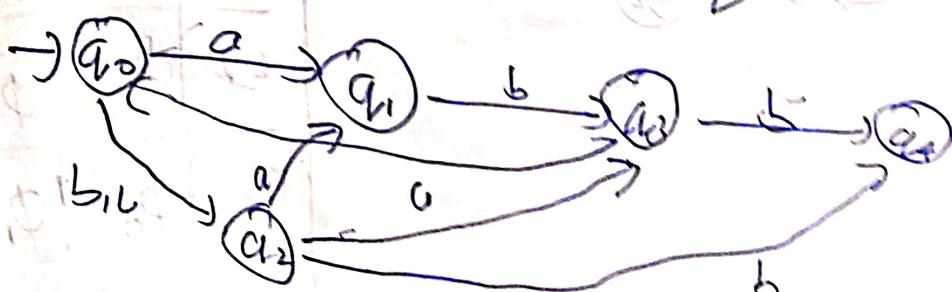
$$= \mathcal{S}\text{-closure}(\mathcal{S}(Q_0, Q_1, Q_2, b))$$

$$\Rightarrow \mathcal{S}(Q_1, Q_2) - q_2$$

$$\mathcal{S}'(q_0, c) = \mathcal{E}\text{-closure}(\mathcal{S}(q_0, c))$$

$$= \mathcal{E}\text{-closure}(\mathcal{S}(Q_0, Q_1, Q_2, c))$$

$$= \mathcal{S}(Q_1, Q_2) - q_2$$

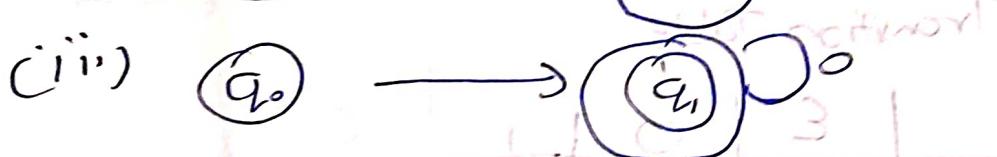
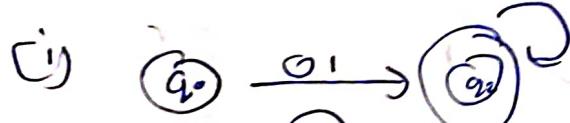


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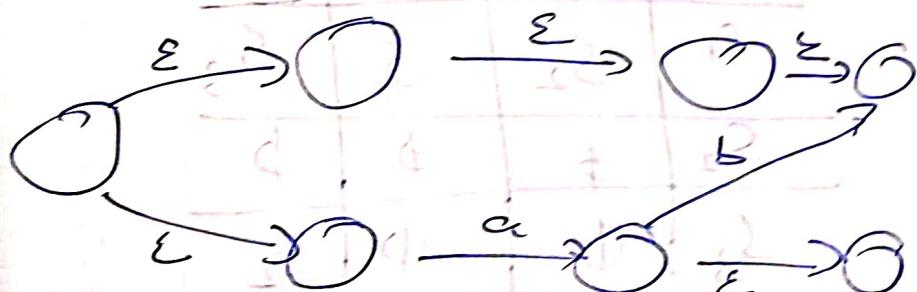
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$$\textcircled{2} \quad L_1 = Q_1^*$$

$$L_2 = Q_1$$



$\textcircled{3}$



$$\Sigma - \text{closure}(1) = \{1, 2, 4, 6\}$$

$$(2) = \{2, 3, 6\}$$

$$(3) = \{3, 6\}$$

$$(4) = \{4\}$$

$$(5) = \{5, 7\}$$

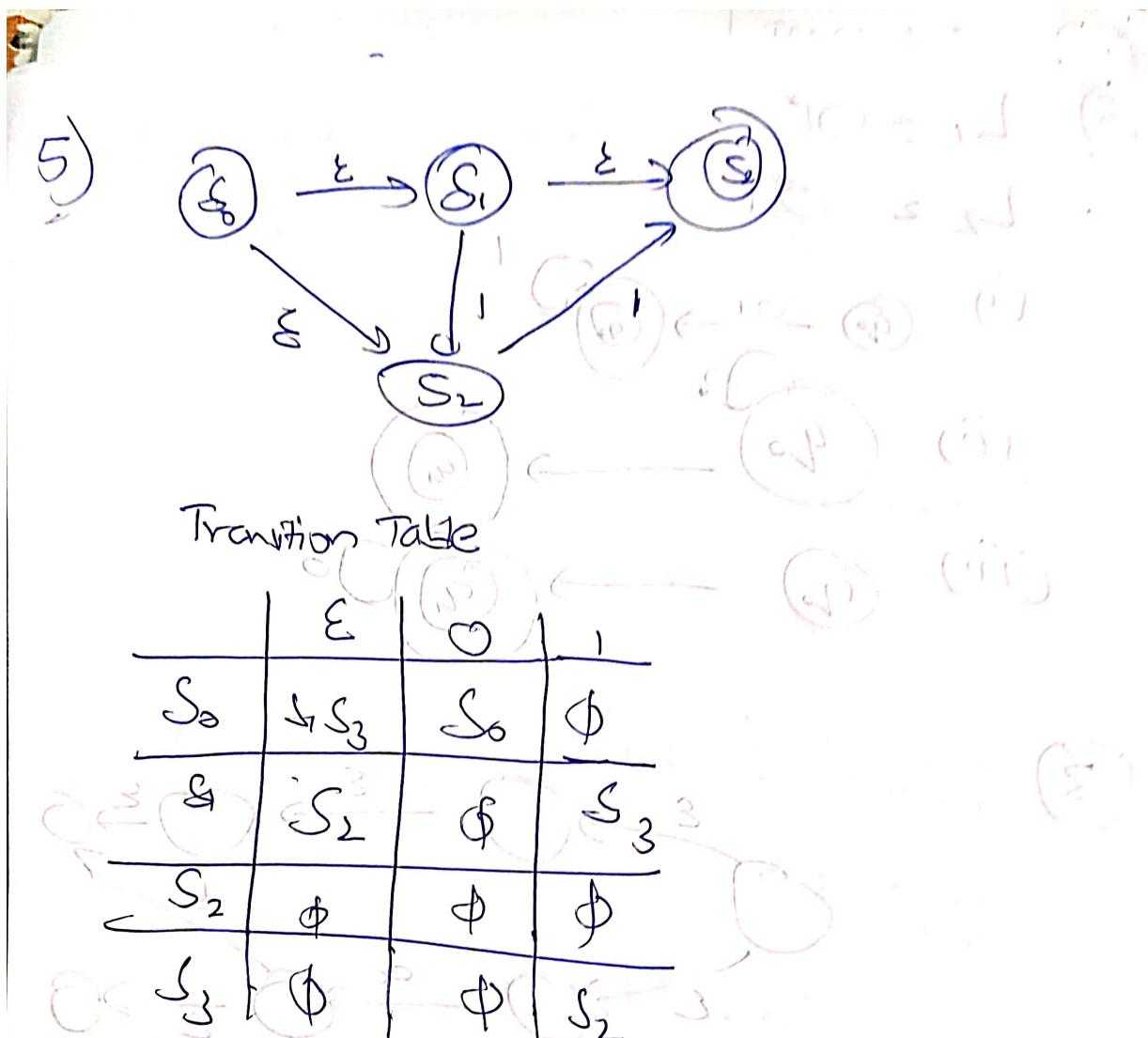
$$(6) = \{6\} = \{0, 2\}'$$

$$(7) = \{7\}$$

$$(8) = \{8\}$$

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ϵ -closures (S_0) = $\{S_0, S_1, S_2, S_3\}$

$(S_1)\epsilon$ -closure = (S_0, S_1, S_2)

$(S_2)\epsilon$ -closure = (S_2)

$(S_3)\epsilon$ -closure = (S_3)

$\delta^*(S_0, 0) = \{ \text{ } \} \cup \epsilon\text{-closure}(\delta(\epsilon\text{-closure}(S_0, 0)))$

= $\epsilon\text{-closure}(\delta(S_0, S_1, S_2, S_3, 0))$

$\Rightarrow \delta\text{-closure}(d_0)$

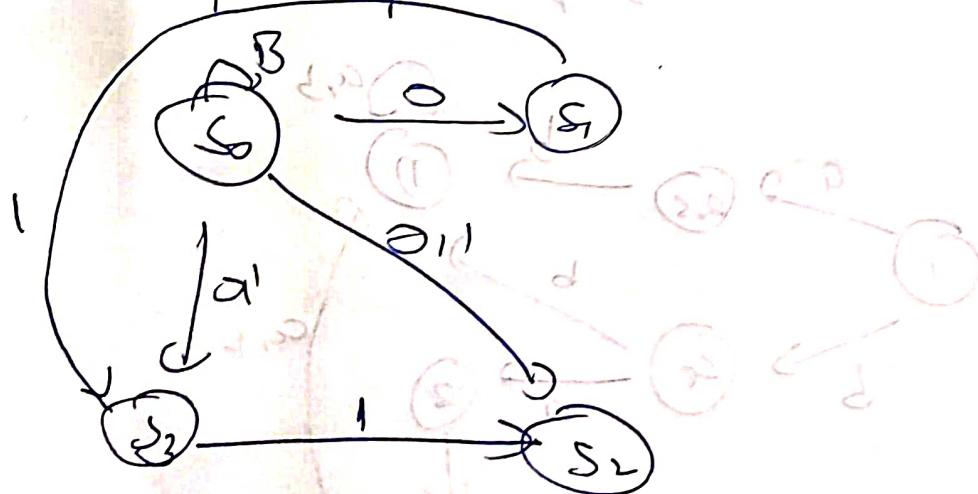
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$$\begin{aligned}
 S'(\{S_0, 1\}) &= \Sigma\text{-closure}(\{S / \Sigma\text{-closure}(S_0, 1)\}) \\
 &= \Sigma\text{-closure}(S_3, S_2) \\
 &\Rightarrow \{S_2, S_3\}
 \end{aligned}$$

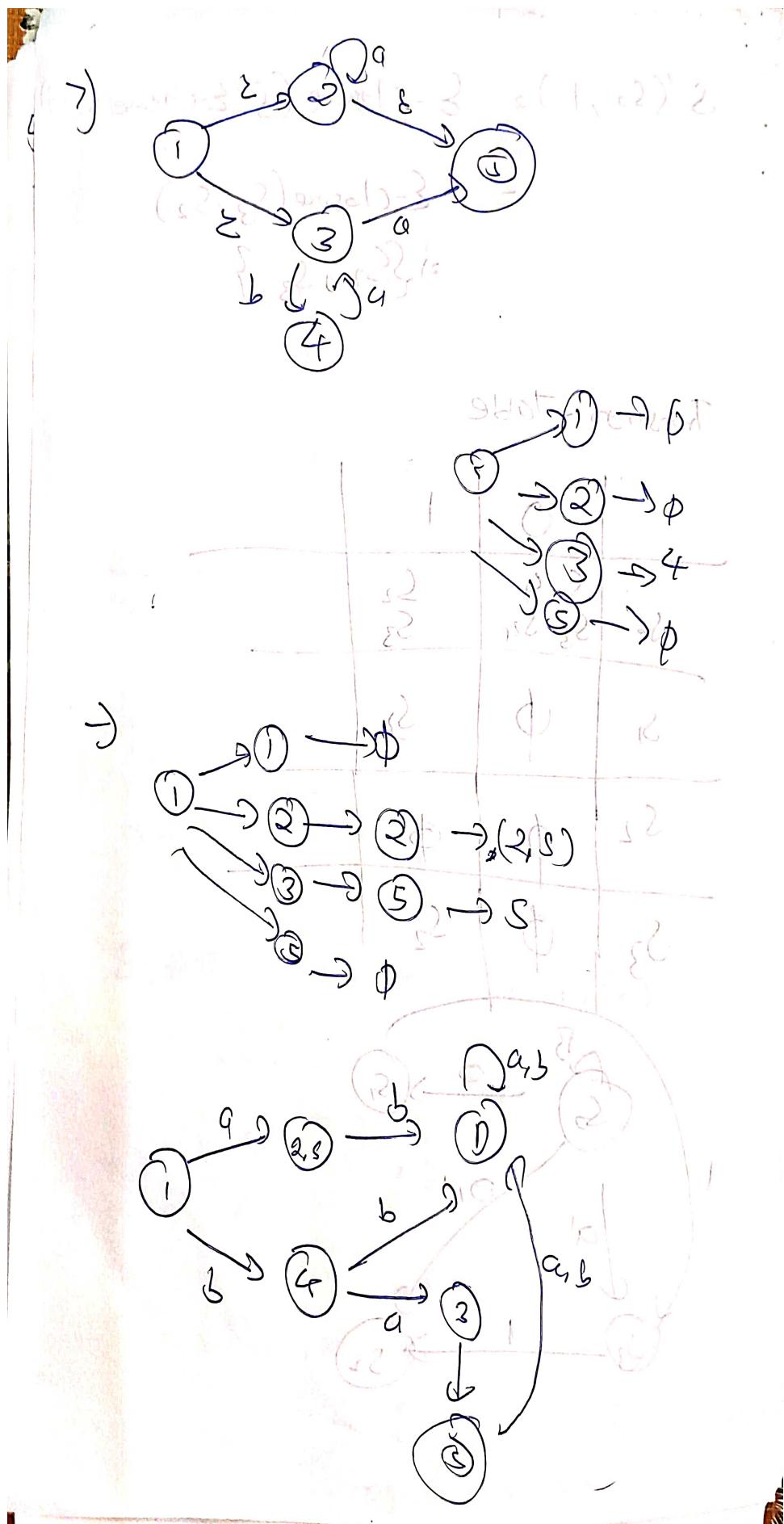
Transition Table

	0	1	
S_0	S_0, S_1 S_3, S_{24}	S_2 S_3	
S_1	\emptyset	S_3	
S_2	\emptyset	\emptyset	
S_3	\emptyset	S_2	



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FLA Worksheet - Set 1

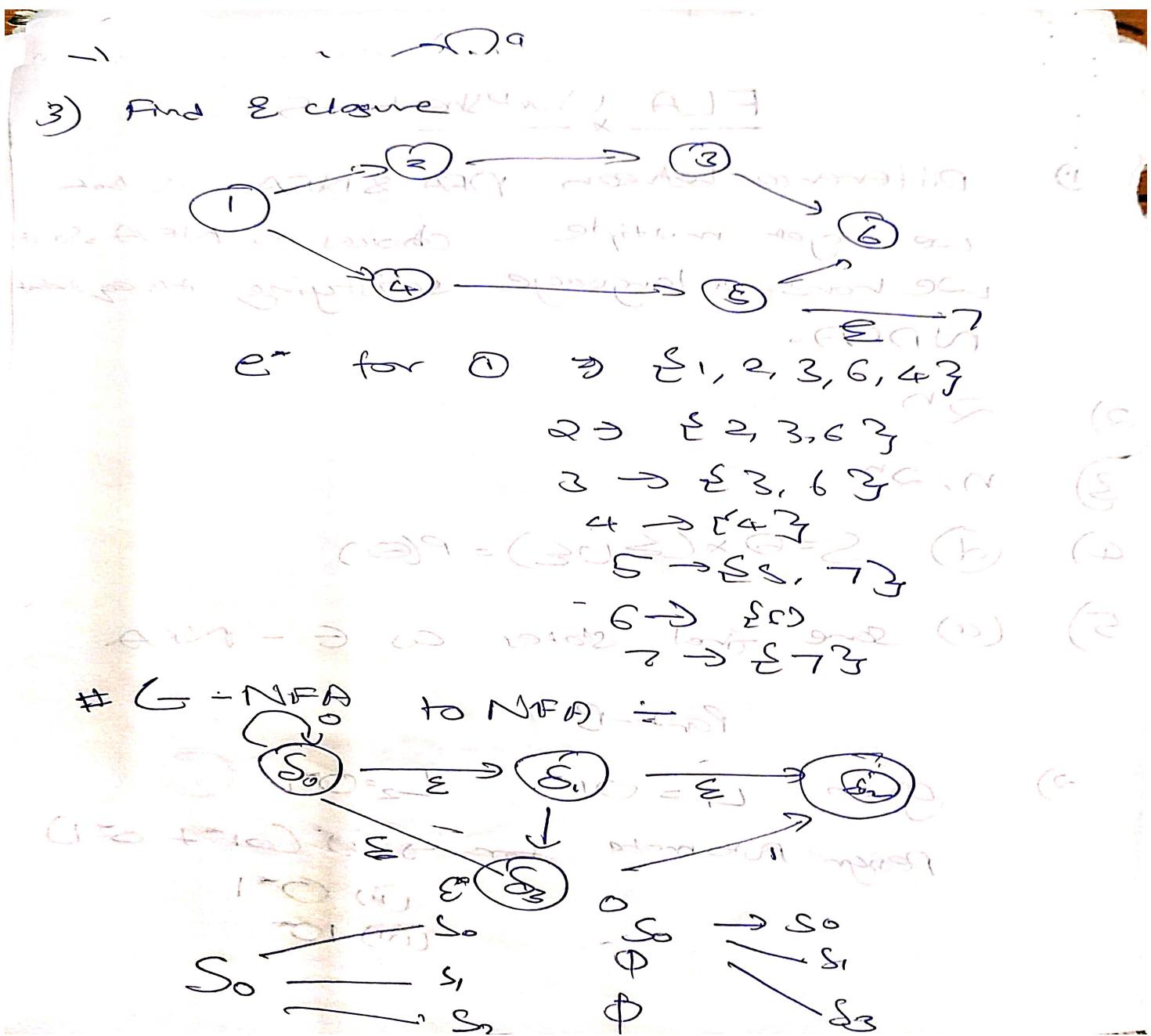
- 1) Difference between DFA & NFA is that we get multiple choices in NFA so it can have a language satisfying its equivalent N DFA.
- 2) 2^n
- 3) $n, 2^n$
- 4) (d) $S = \emptyset \times (\subseteq \cup \epsilon) = P(\emptyset)$
- 5) (a) Some final states can be ϵ -NFA.

Part-B

- 2) Given $L_1 = 0^*$ $L_2 = 0^*1$
Design Automata for $(0^* + 0^*1)$

(i) 0^*
(ii) 0^*1
(iii) 10^*

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Unit -4
Worksheet

- Q-1 Storage capacity
2. Only reads input and two storage tapes.
 3. Turing Machine with stay option.
 4. Non erasing turing machine.
 5. Binary turing machine.

Q-6

A standard turing machine is a machine which on providing an input, moves either to left or right, It may overwrite the existing symbol.

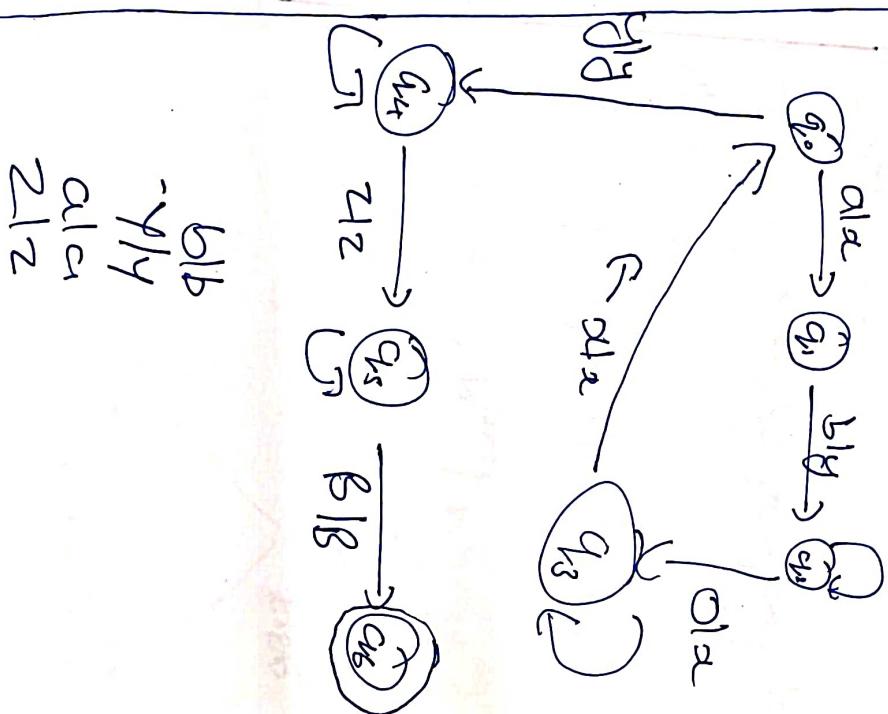
A standard TM is capable of accepting some of language called recursively enumerable language by doing some kind of rectification we can increase no. of language accepted by turing machine.

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Q-7

Design TM for

$$L = a^m b^m c^m \mid m \geq 1$$



Ans) True

2) True

3) 7

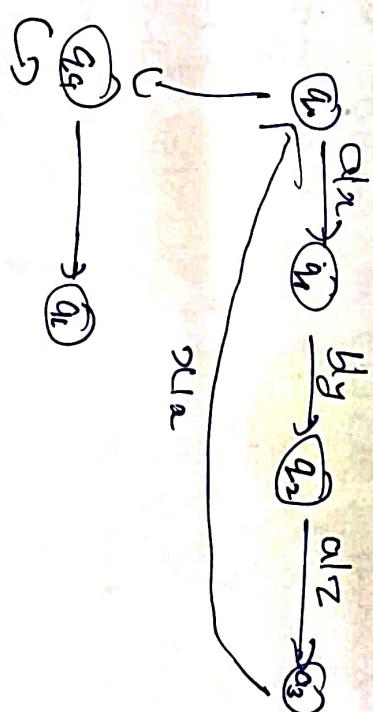
S1, S2, and S3 are same

4) Left

Com'n

7) turing machine

$$L = \{a^m, b^n, c^m\}$$



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- Q) $A = \{0^n 1^n 0^n\} \cup 2^*$ is not context-free language.
- Ans. let P be pumping lemma for CFL and consider string $s = 0^n 1^n 0^n$
- $|s| = 6n > p$, so pumping lemma will hold.
- Their $x, y, z, u, v = 0$
- $F = \{a^{2n}, b^{2n}\} \cup 2^*$
-
- ```

graph LR
 q0((q0)) -- a --> q1((q1))
 q1 -- a --> q2((q2))
 q2 -- a --> q3((q3))
 q3 -- a --> q4(((q4)))
 q0 -- b --> q2
 q1 -- b --> q3
 q2 -- b --> q4
 q3 -- b --> q4
 style q0 fill:none,stroke:none
 style q4 fill:none,stroke:none

```
- and add it to minimum length tree provided the addition does not follow a cycle. Then add with exact lower cost and do on repeat the process until we have selected no longer to make complete spanning tree.

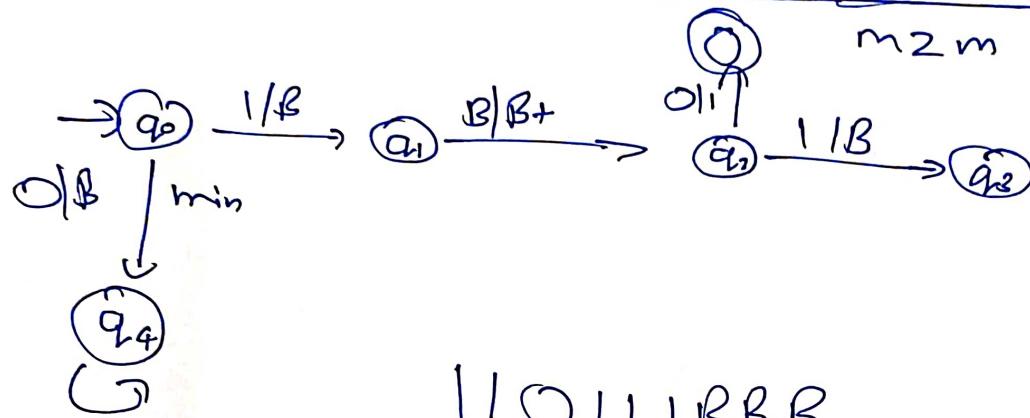
2) Kruskal Algorithm is in class P.  
Kruskal Algorithm works on min. Spanning tree by adding edges one at a time to  $T$ . It is built up by edge rule shown below:

minimum cost if more one cost, we select one of them.

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6)

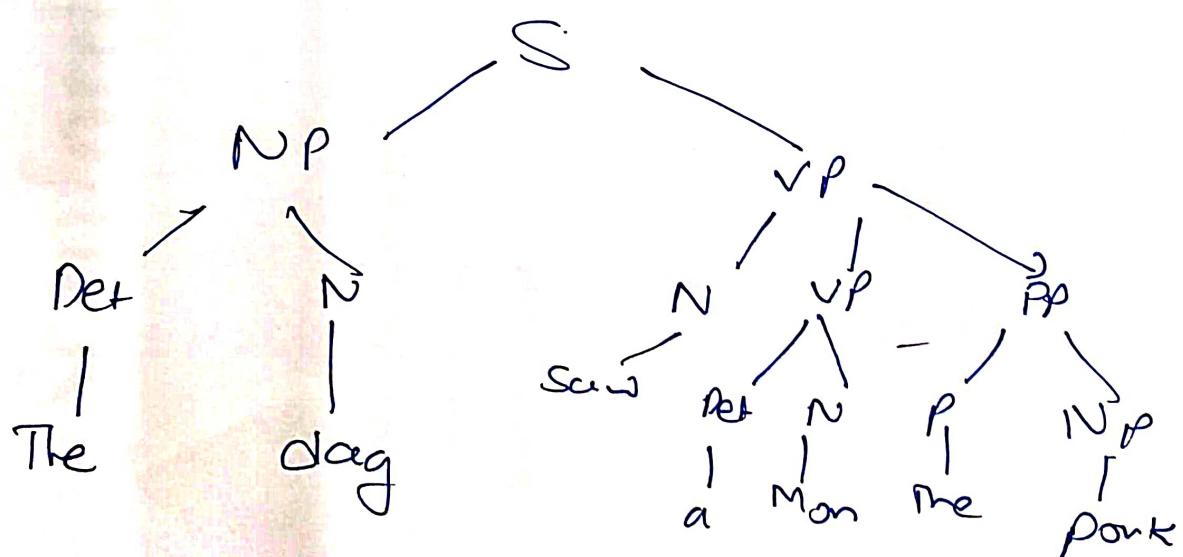


$110111BBB$   
 $B1011BBB$   
 $BB01BBB$   
 $BB1BBB$

participation in the course.

7)

A dog saw a man on park



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ID: 7E269A3FA544



# Certificate

This is to certify that

**DIVYANSH GAUR (RA2011027010090)**

has successfully cleared the assessment for the skill

**Python (Basic)**

**23 Jun, 2022**

Date

A handwritten signature in black ink, appearing to read "J. Harishankaran".

**Harishankaran K**

CTO, HackerRank

ID: BC3C164D3A7D



# Certificate

This is to certify that

**DIVYANSH GAUR (RA2011027010090)**

has successfully cleared the assessment for the skill

**Problem Solving (Basic)**

**09 Dec, 2021**

Date

A handwritten signature in black ink, appearing to read "J. Harishankaran".

**Harishankaran K**

CTO, HackerRank