

The Hubble tension: approaches, solutions and challenges

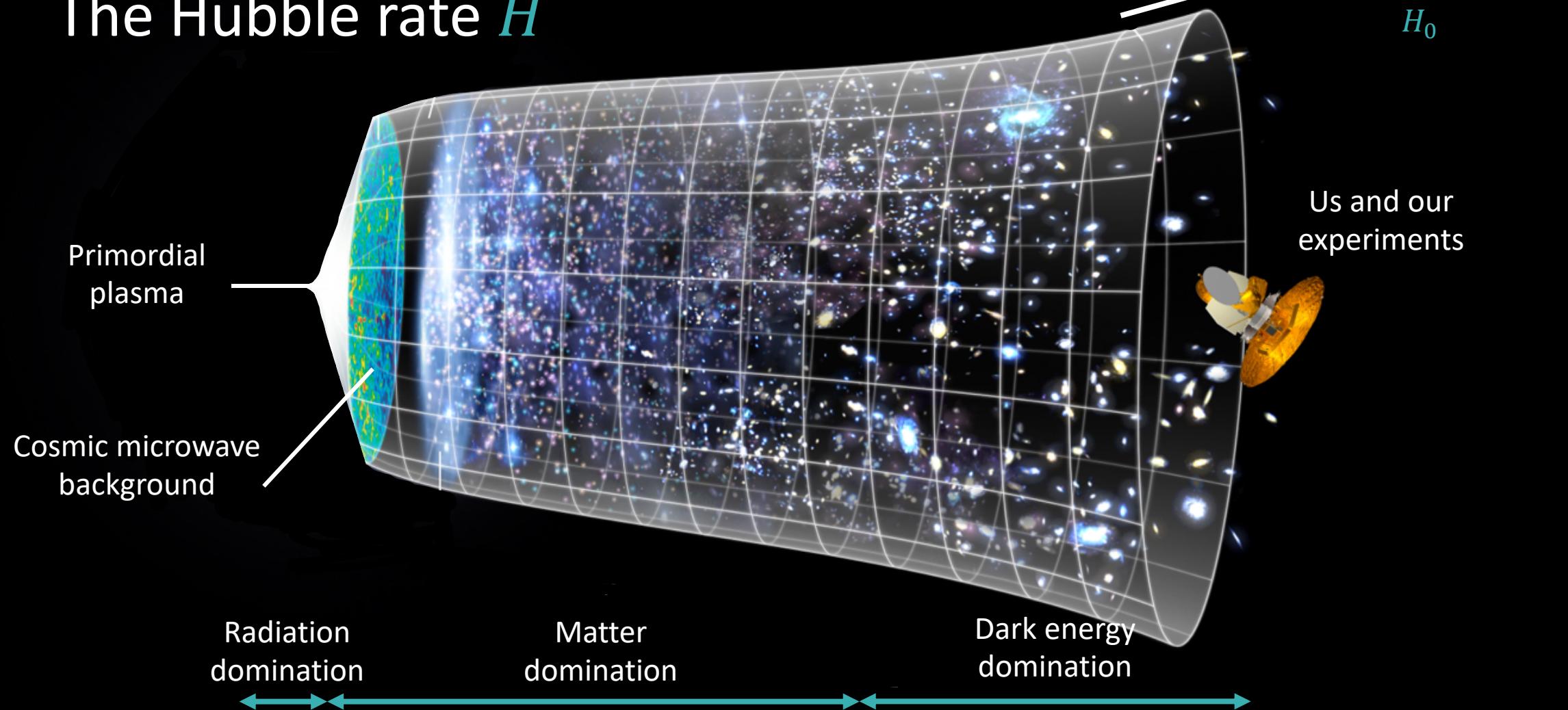
Tanvi Karwal
 Penn

IIT Hyderabad
22nd April, 2021

Based on work with: Vivian Poulin, Tristan L. Smith, Marc Kamionkowski, Daniel Grin, Kim Berghaus, Marco Raveri,
Bhuvnesh Jain, Mark Trodden and Justin Khouri

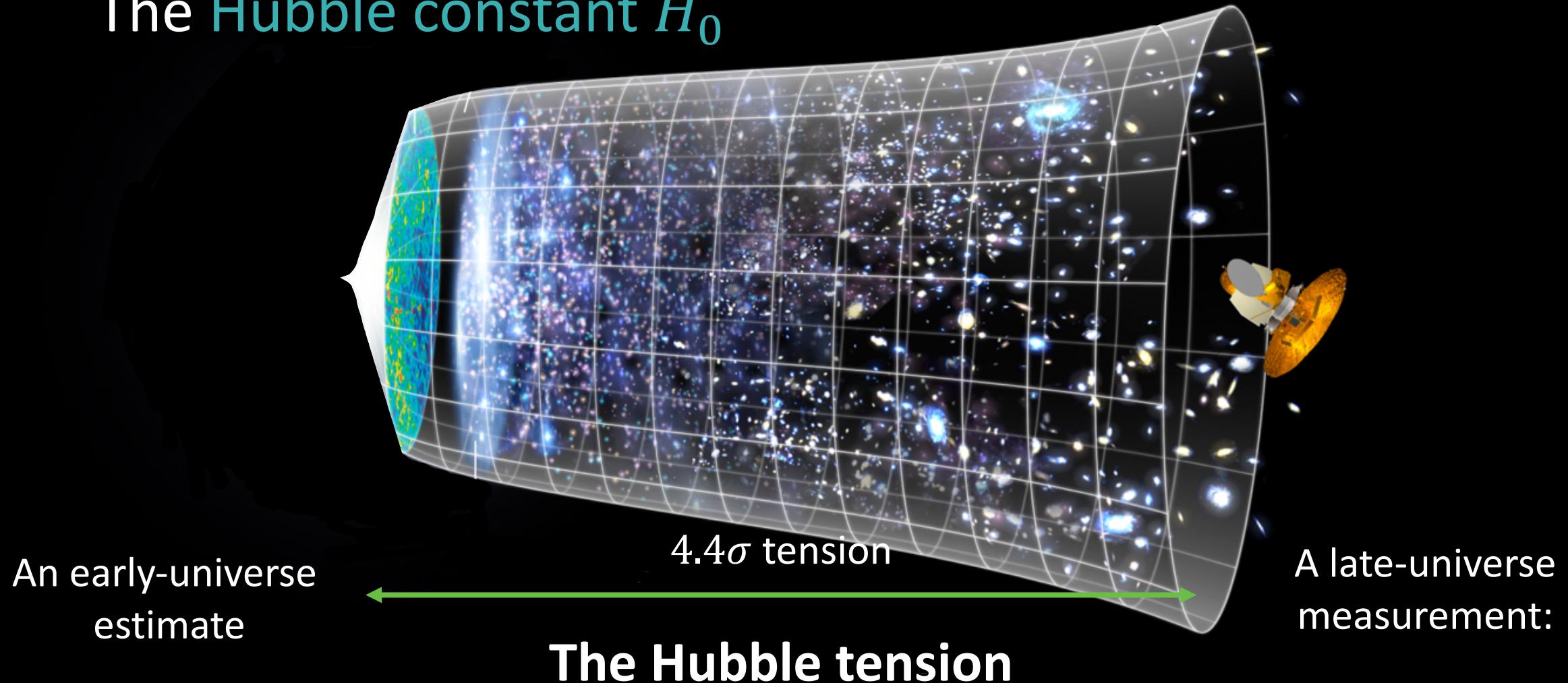
The expansion of the Universe

The Hubble rate H



NASA/WMAP Science Team

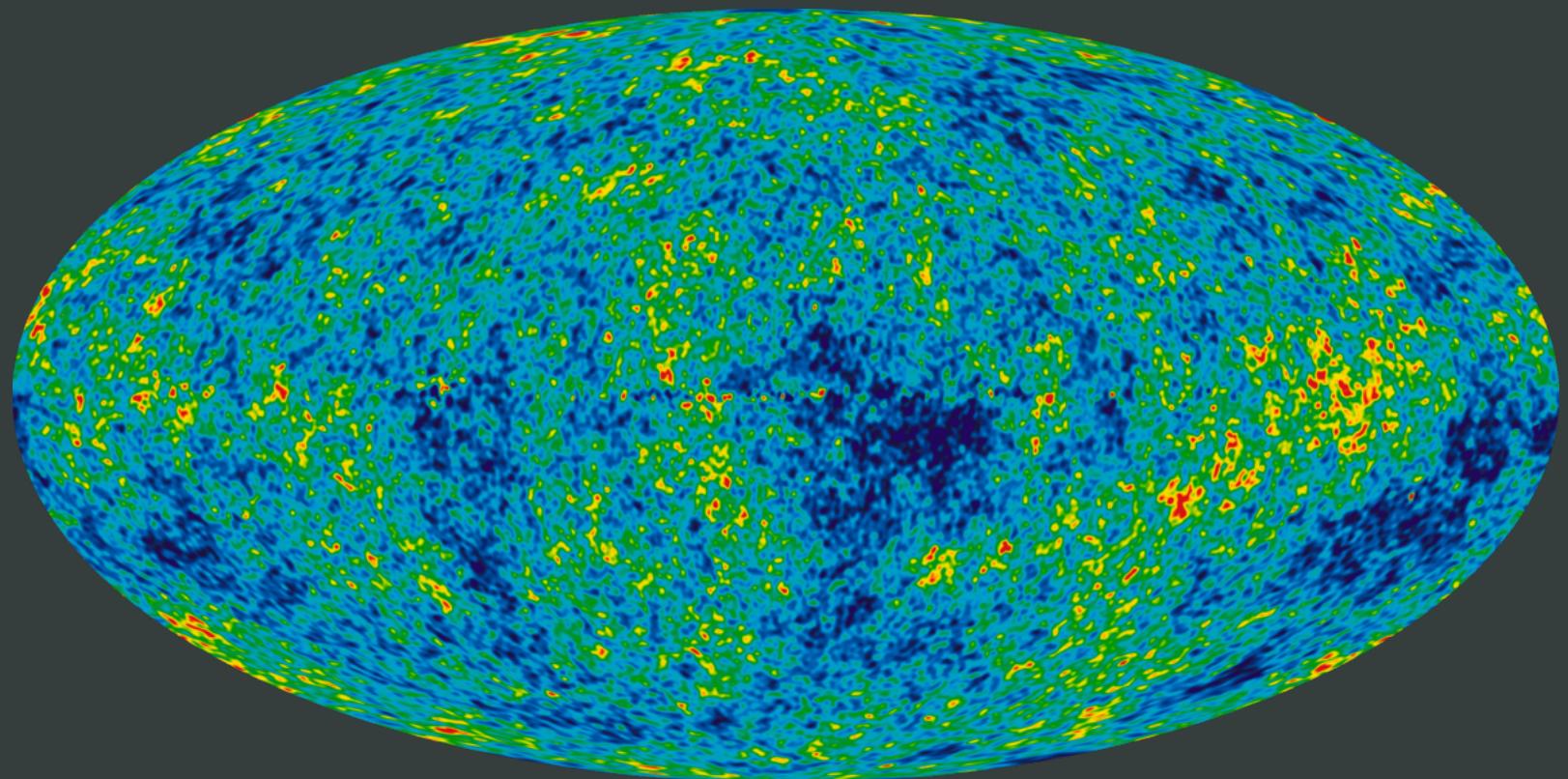
The expansion of the Universe today The Hubble constant H_0



Cosmic microwave background

The oldest light in the Universe

Density imprint
produced by sound
waves in the early
universe



Source: WMAP

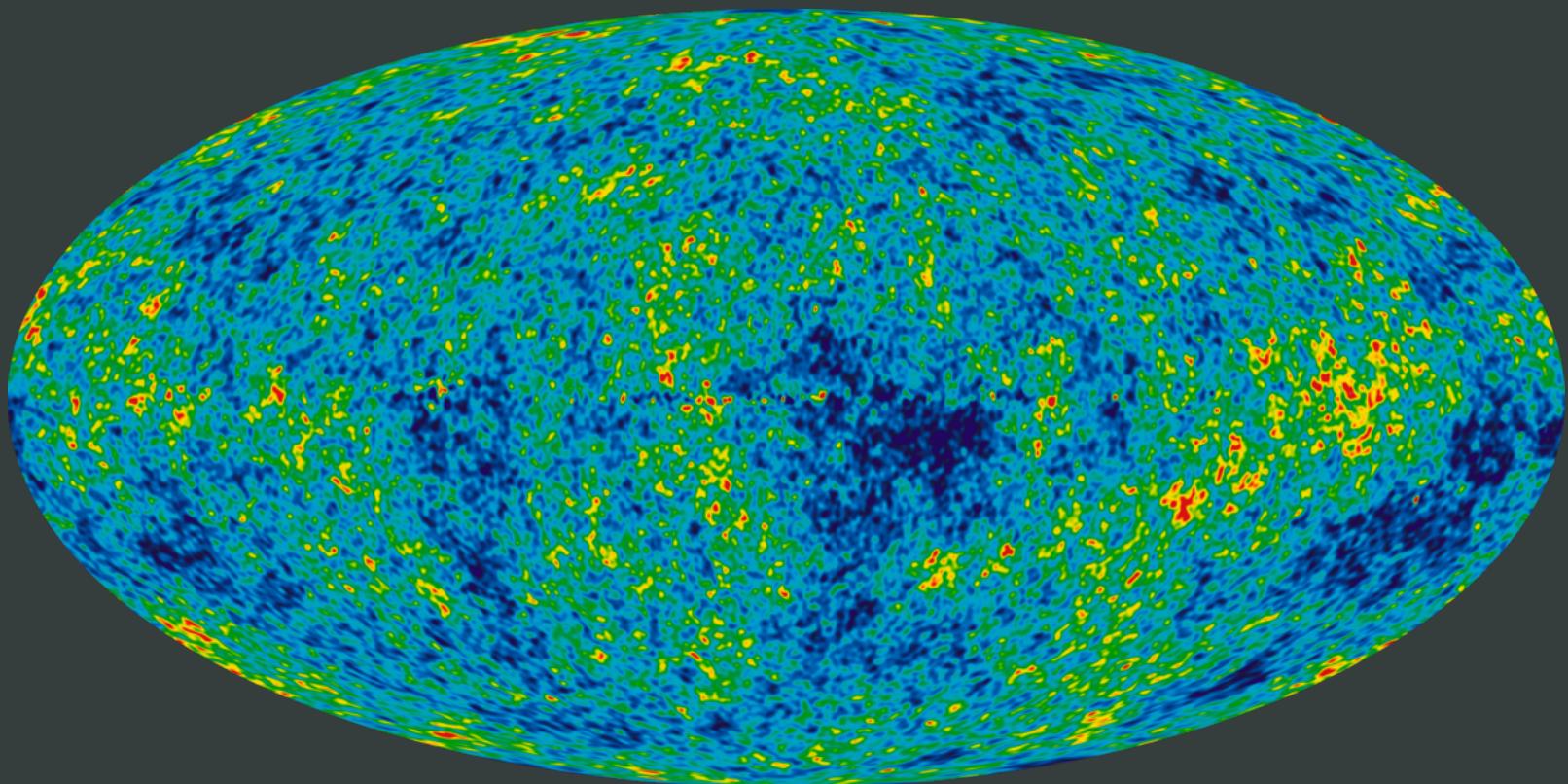
Cosmic microwave background

The oldest light in the Universe

Density imprint
produced by sound
waves in the early
universe

Maximum
variation at
 $\theta_* \sim 1^\circ$ scales

Farthest distance
that sound waves
travelled $\sim r_s$
The sound horizon



Source: WMAP

The standard model of cosmology

Λ CDM

Matter density $\propto z^3$

Cold dark matter

CDM

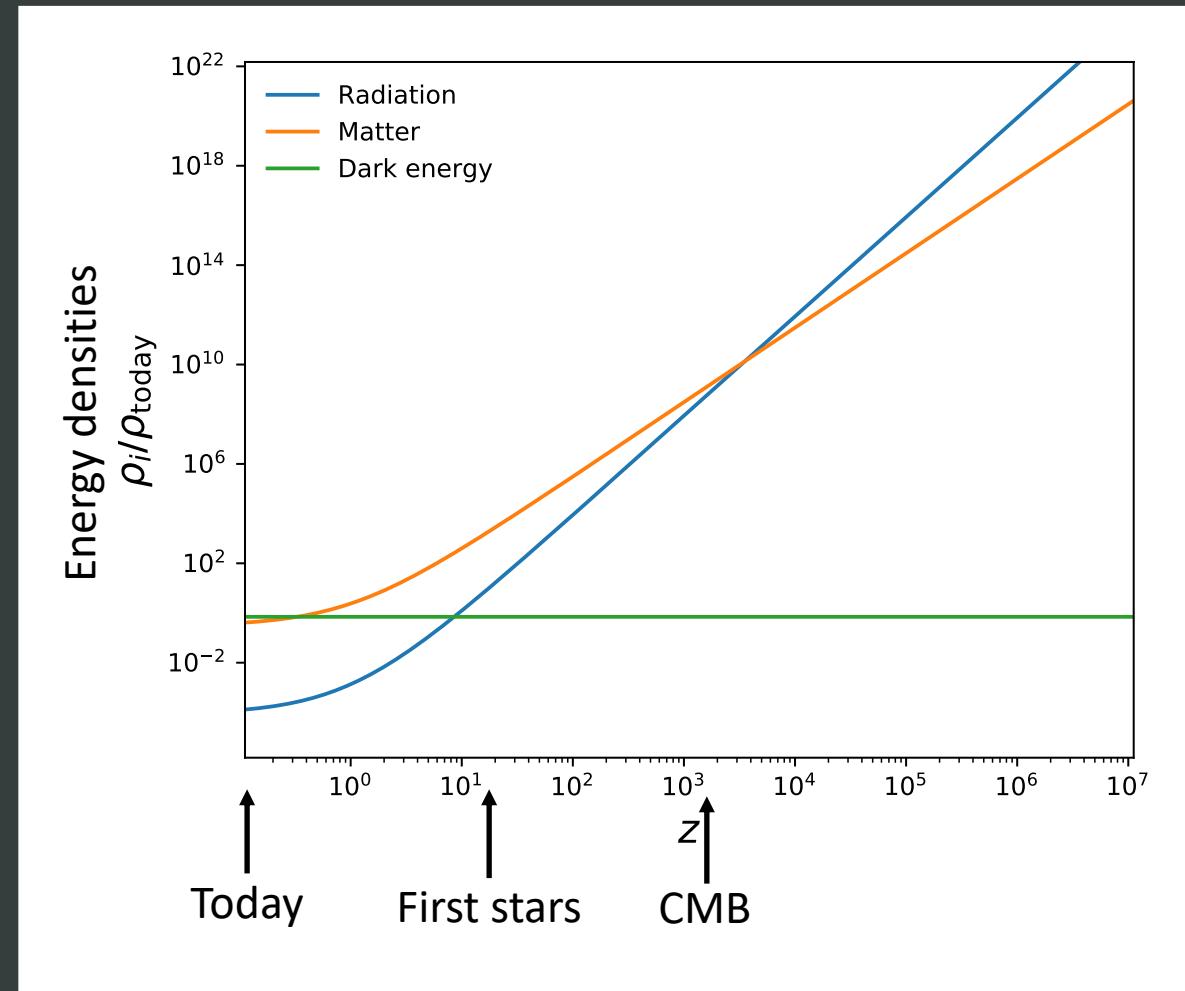
Radiation density $\propto z^4$

Dark energy density $\propto z^0$

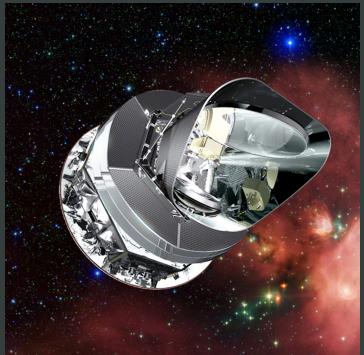
Cosmological
constant Λ

$$H(z) \propto \sqrt{\rho_{tot}(z)}$$

Expansion rate \propto Energy content

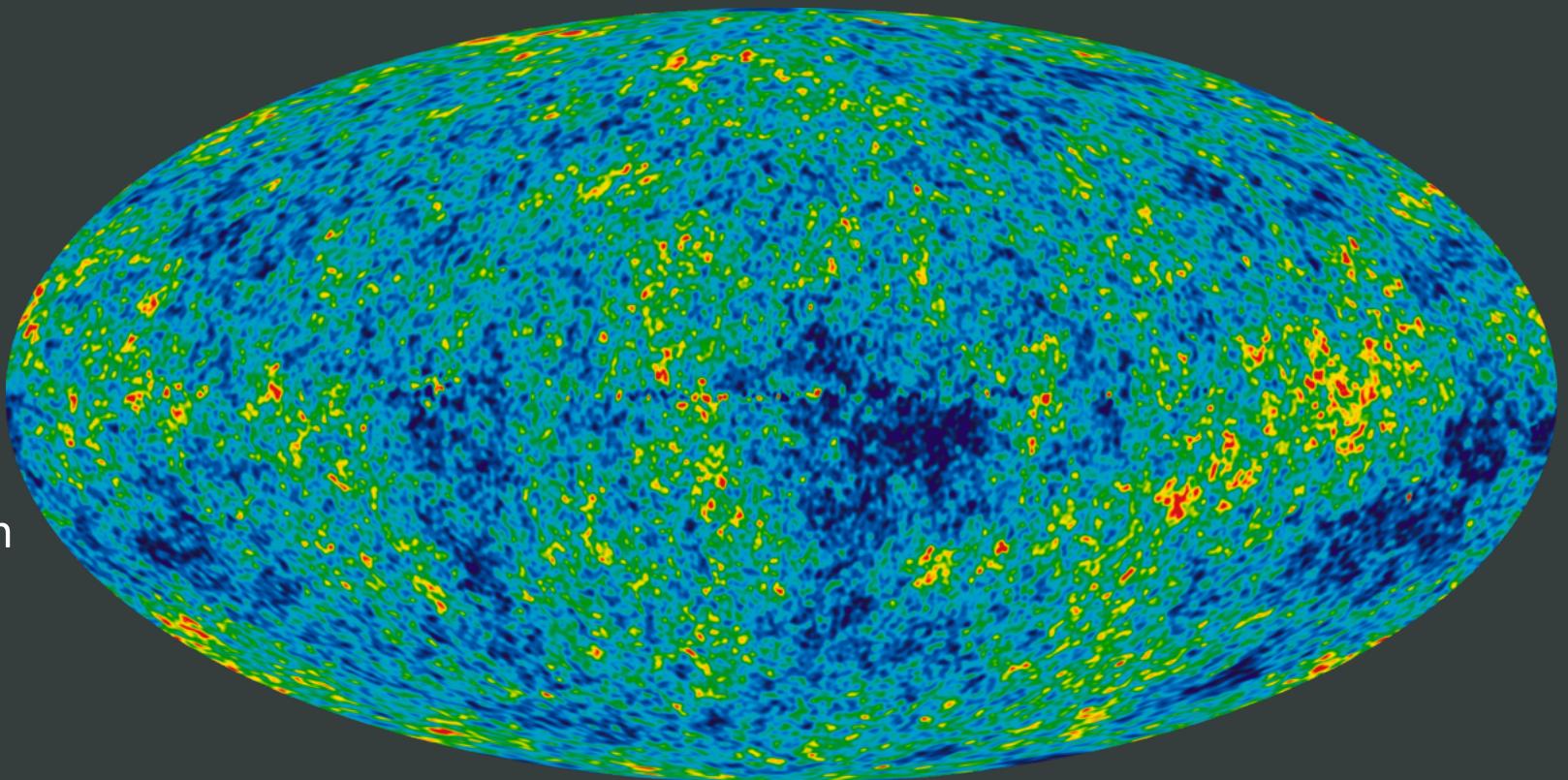


Cosmic microwave background and the Λ CDM model



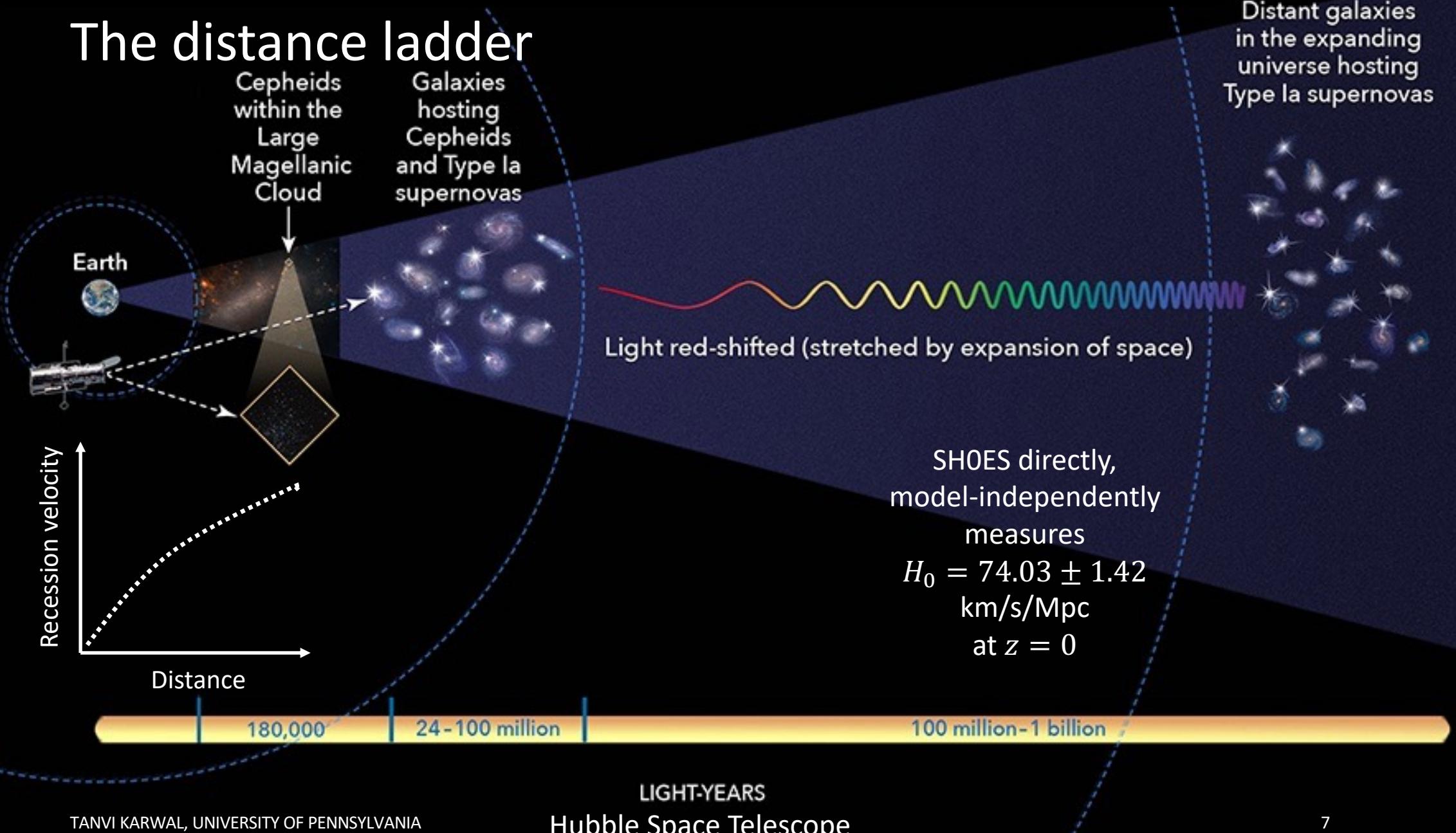
Planck fits Λ CDM to constrain
 $H_0 = 67.4 \pm 0.5 \text{ km/s/Mpc}$
by observing the Universe
at early times

Planck [1807.06209]



Source: WMAP

The distance ladder



Fit Λ CDM to the
early universe
 $H_0 = 67.4 \pm 0.5$
km/s/Mpc

4.4σ tension

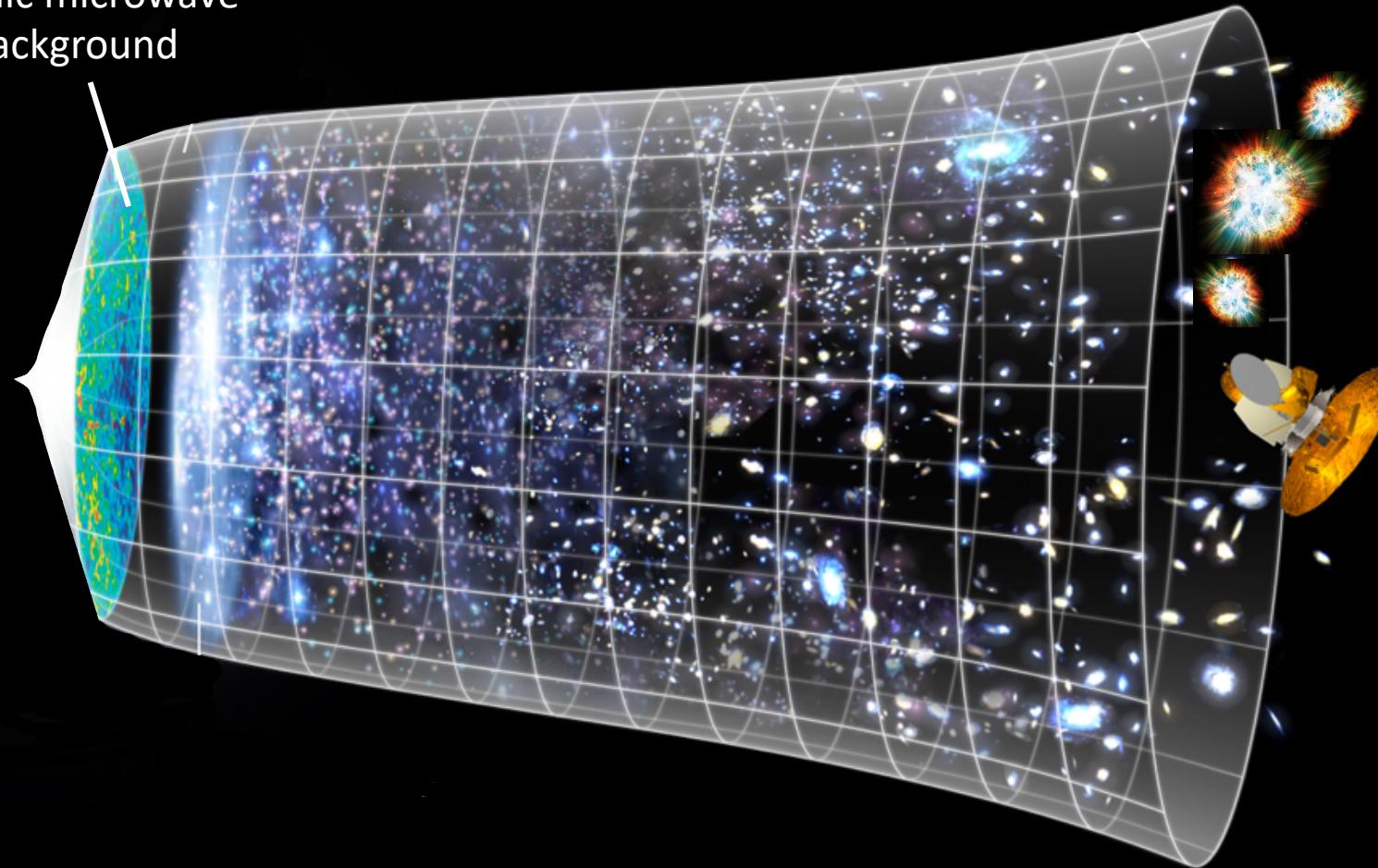
Directly measure in
current universe
 $H_0 = 74.03 \pm 1.42$
km/s/Mpc

The Hubble tension

Early universe +
cosmological
assumptions

Cosmic microwave
background

Late universe +
astrophysical
assumptions



CMB estimation < Direct measurement

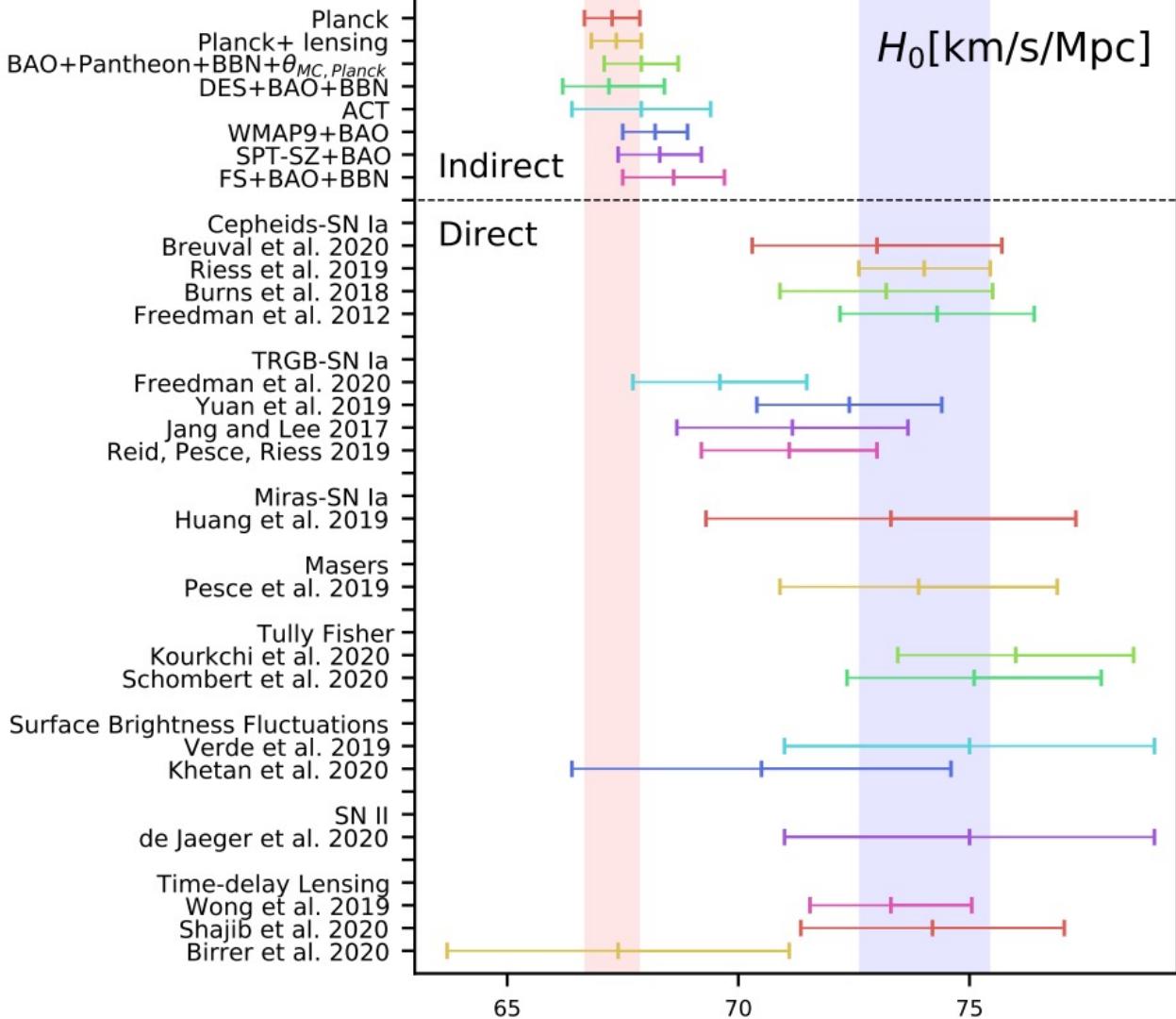
The Hubble tension Current state – headache



Discrepancy between the early and late universe?

Is Λ CDM wrong?

Di Valentino [2011.00246]



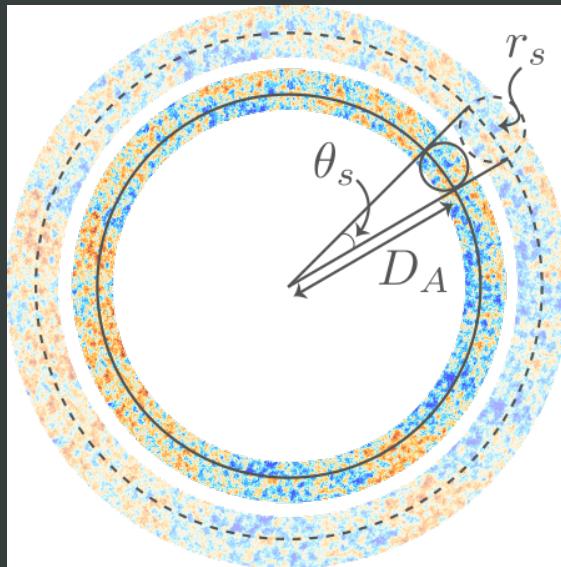
This talk

→ Approaches to theoretically resolving the Hubble tension

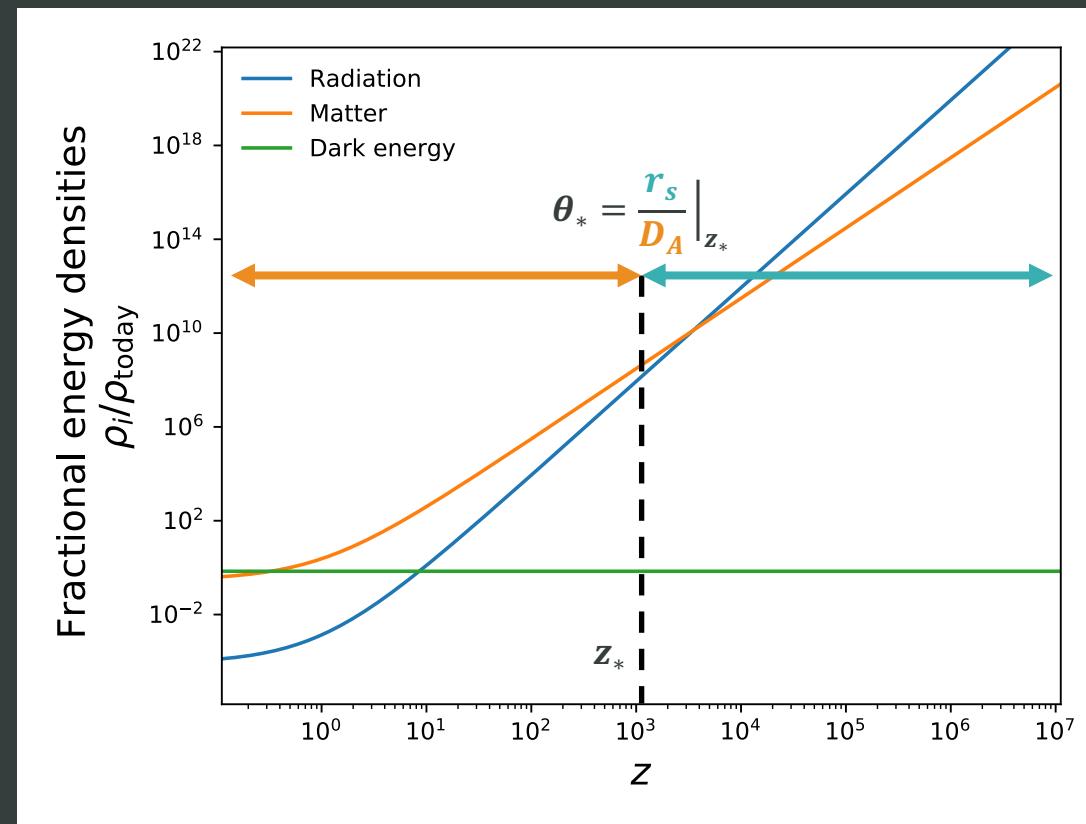
- Solutions to H_0 : early dark energy (EDE) models
- Challenges: the large-scale structure tension

When to add new physics? Early universe

Precisely measured θ_* is an approximate proxy for CMB peak locations



Cartoon by Tristan L. Smith



$$D_A \propto 1/H_{\text{post}}$$

$$\theta_* \sim \frac{r_s}{1/H_{\text{post}}} \sim r_s H_0$$

For constant θ_* ,
 $r_s \propto 1/H_0$

In support of an early universe modification:
Planck [1807.06209]
Bernal et al [1607.05617]
Evslin et al [1711.01051]
Aylor et al [1811.00537]

Hubble tension \leftrightarrow Sound horizon tension

Distance ladder
+ BAO $\rightarrow r_s$

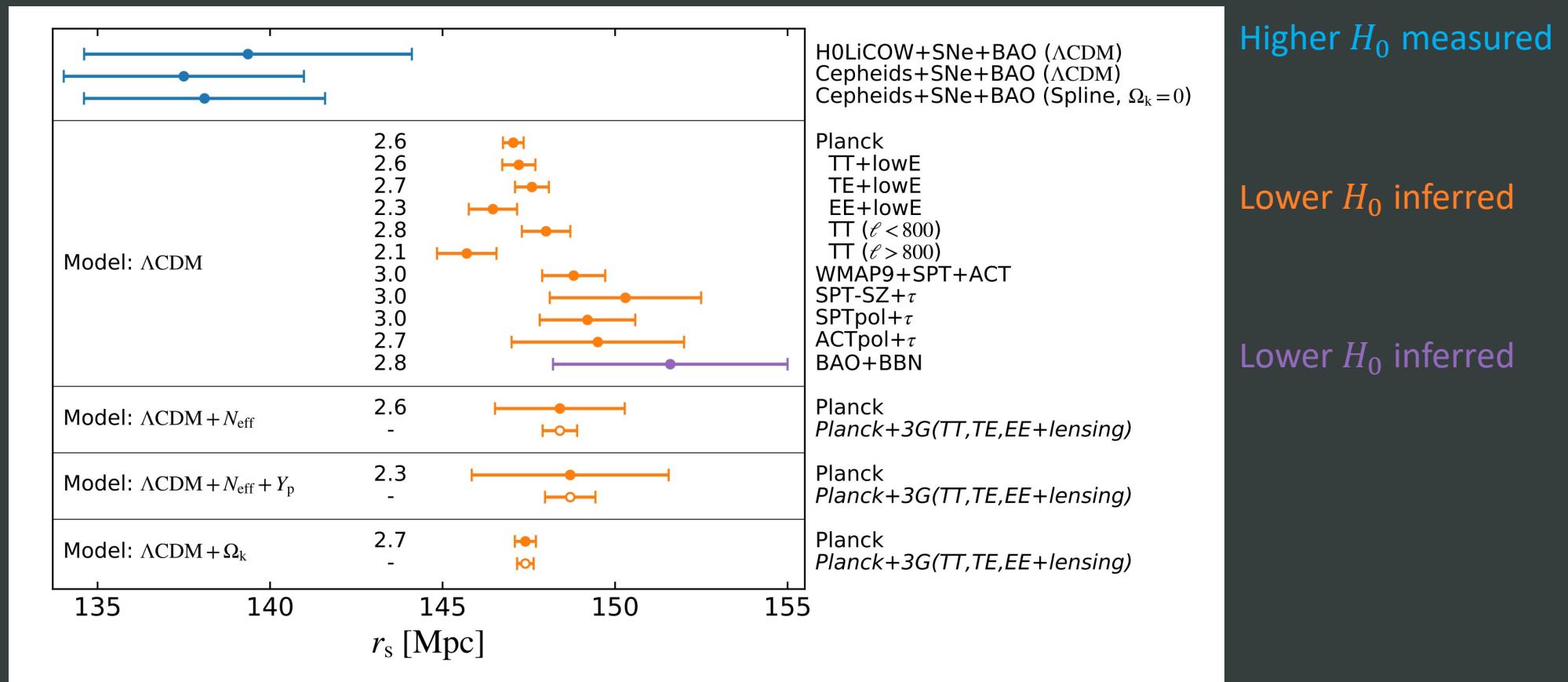
CMB r_s + BAO
 $\rightarrow H_0$

No CMB data

Higher H_0 measured

Lower H_0 inferred

Lower H_0 inferred



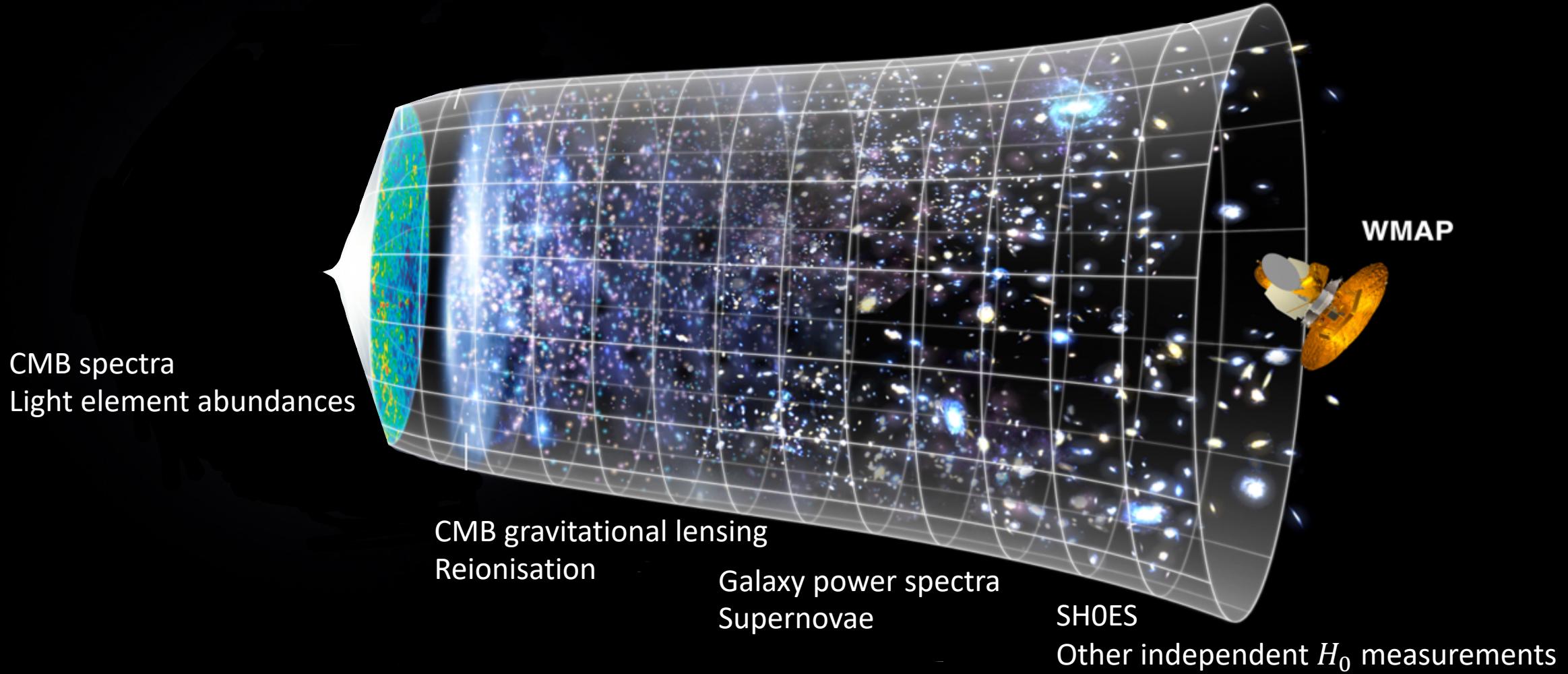
Aylor et al [1811.00537]

Approaches to a solution

Requirements:

- Keep θ_* fixed (or keep CMB peaks fixed) such that $r_s \propto 1/H_0$
- Decrease $r_s \propto 1/H_{pre}(z)$, so increase the pre-CMB expansion rate

How to add new physics?
Leave late universe unchanged



Approaches to a solution

Requirements:

- Keep θ_* fixed (or keep CMB peaks fixed) such that $r_s \propto 1/H_0$
- Decrease $r_s \propto 1/H_{pre}(z)$, so increase the pre-CMB expansion rate
- Leave $D_A \propto 1/H_{post}(z)$ unchanged, so modification must disappear at late times

This talk

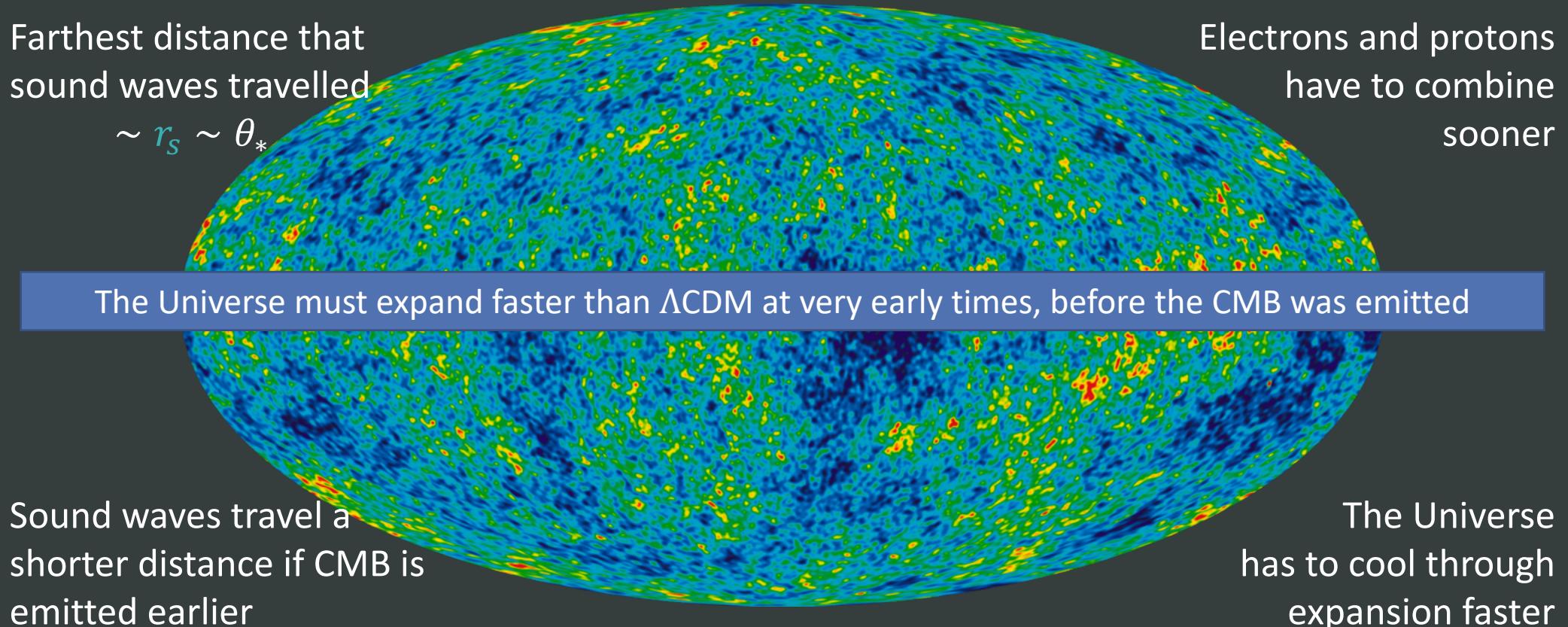
- ✓ Approaches to theoretically resolving the Hubble tension

→ Solutions to H_0 : early dark energy (EDE) models

- Challenges: the large-scale structure tension



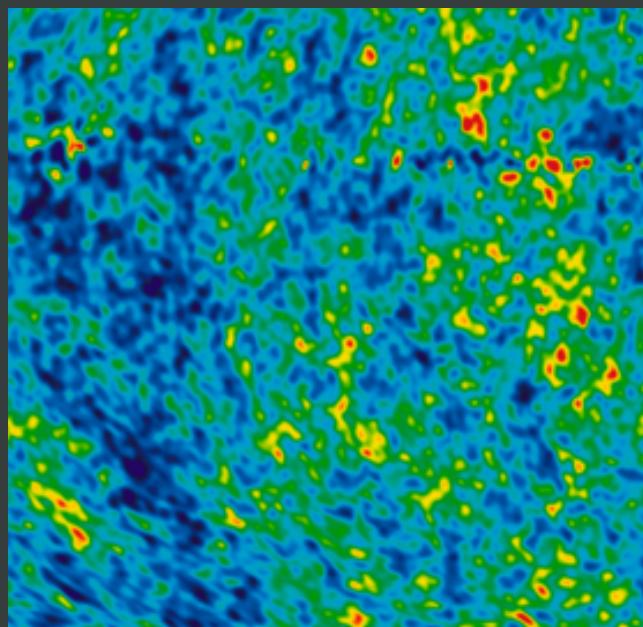
Hubble solutions Reduce r_s



WMAP, NASA

Hubble solutions

Effect of early dark energy



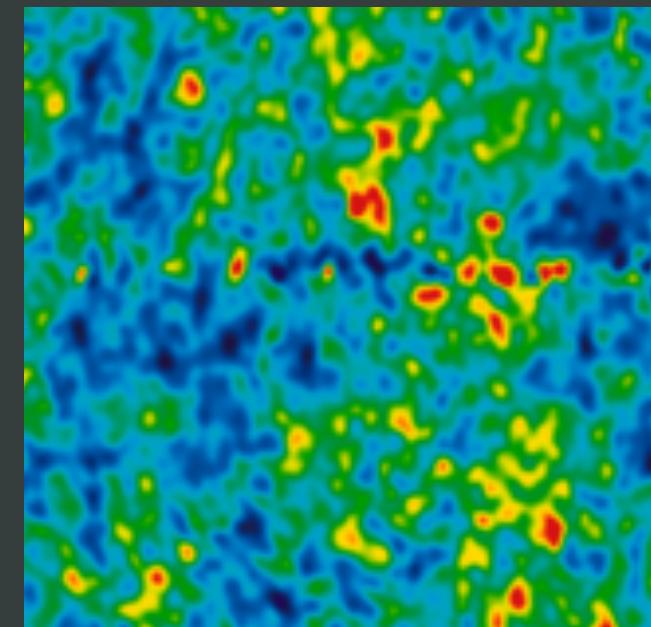
Observed CMB



Increase
 H_0



Decrease
 r_s
Add
early dark energy



Disagreement with
observed CMB

Approaches to a solution

Requirements:

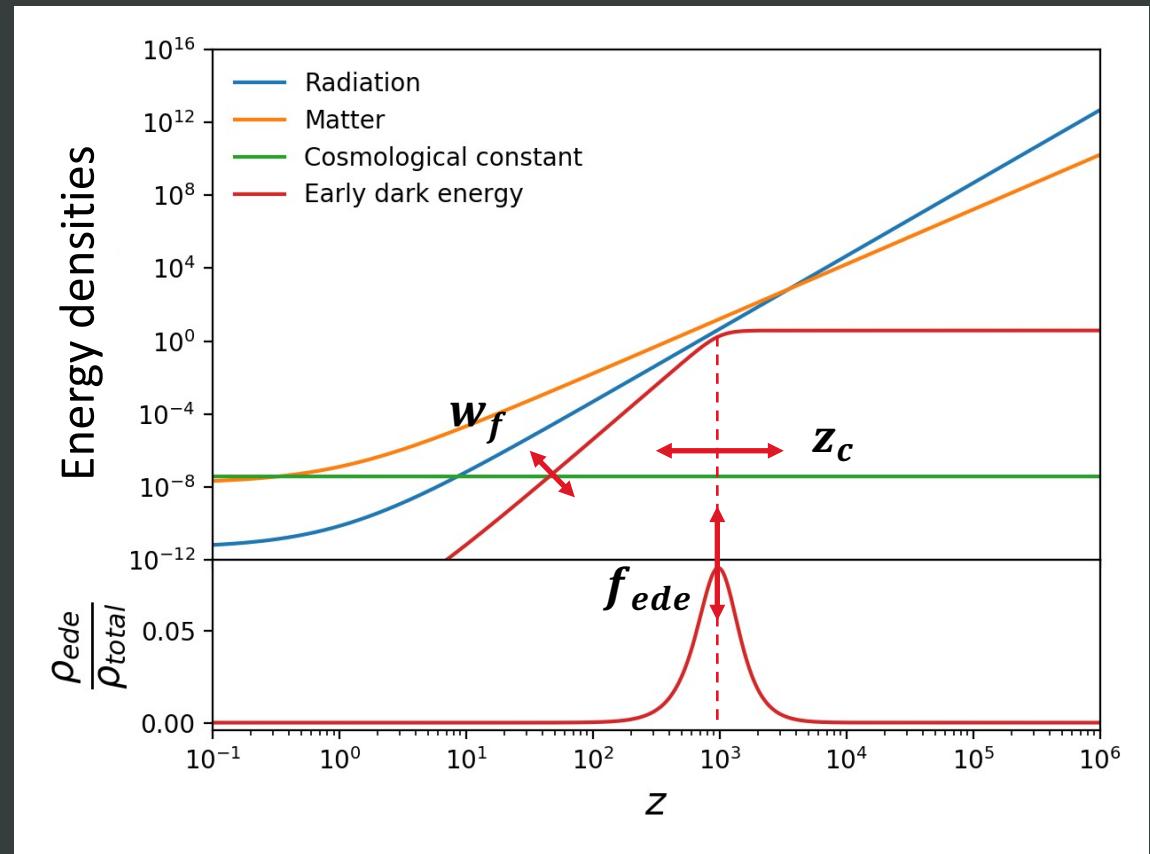
- ✓ Keep θ_* fixed (or keep CMB peaks fixed) such that $r_s \propto 1/H_0$
- ✓ Decrease $r_s \propto 1/H_{pre}(z)$, so increase the pre-CMB expansion rate
- Leave $D_A \propto 1/H_{post}(z)$ unchanged, so modification must disappear at late times

Early dark energy (EDE)

Additional energy component with the properties:

- Λ -like behaviour initially
- Then dilutes faster than matter as w_f
- Localised peak in $f_{ede} = \frac{\rho_{ede}}{\rho_{total}}$ at z_c

f_{ede} - how much EDE
 z_c - when EDE appears
 w_f (or n) - how fast it disappears



Approaches to a solution

Requirements:

- ✓ Keep θ_* fixed (or keep CMB peaks fixed) such that $r_s \propto 1/H_0$
- ✓ Decrease $r_s \propto 1/H_{pre}(z)$, so increase the pre-CMB expansion rate
- ✓ Leave $D_A \propto 1/H_{post}(z)$ unchanged, so modification must disappear at late times

Early dark energy Models

- Dark energy at early times, the Hubble parameter, and the string axiverse
[TK & Kamionkowski \[1608.01309\]](#)
- Cosmological implications of ultralight axionlike fields
Poulin, [TK et al \[1806.10608\]](#)
- Early Dark Energy Can Resolve The Hubble Tension
Poulin, [TK et al \[1811.04083\]](#)
- Thermal Friction as a Solution to the Hubble Tension
Berghaus & [TK \[1911.06281\]](#)
- Dark energy from the string axiverse. Kamionkowski, Pradler & Walker
[1409.0549]
- Rock 'n' Roll Solutions to the Hubble Tension. Agrawal et al
[1904.01016]
- Axion-Dilaton Destabilization and the Hubble Tension. Alexander & McDonough
[1904.08912]
- Acoustic Dark Energy: Potential Conversion of the Hubble Tension. Lin et al
[1905.12618]
- Oscillating scalar fields and the Hubble tension: a resolution with novel signatures. Smith, Poulin, Amin
[1908.06995]
- New Early Dark Energy. Neidermann & Sloth
[1910.10739]
- Early Dark Energy from Massive Neutrinos as a Natural Resolution of the Hubble Tension. Sakstein & Trodden
[1911.11760]
- Unifying Inflation with Early and Late-time Dark Energy in F(R) Gravity. Nojiri et al
[1912.13128]
- Is the Hubble tension a hint of AdS phase around recombination? Ye & Piao
[2001.02451]
- Unified framework for early dark energy from α -attractors. Braglia et al
[2005.14053]
- A novel early Dark Energy model. Garcia, Castaneda, Tejeiro
[2009.07357]
- Neutrino-Assisted Early Dark Energy: Theory and Cosmology. Gonzalez et al
[2011.09895]

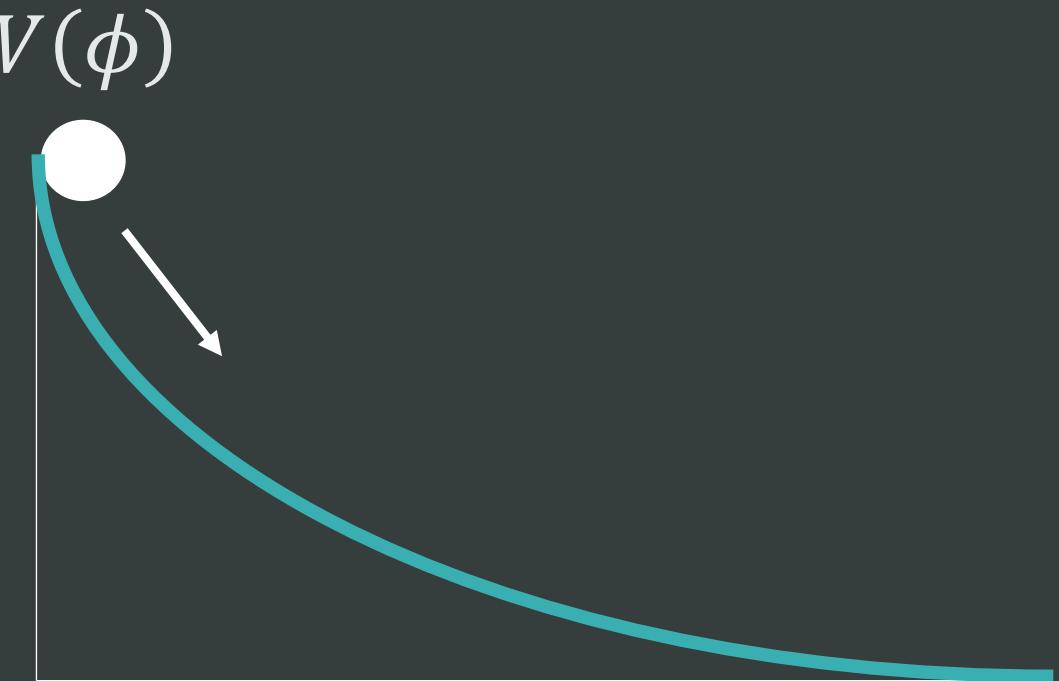
Early dark energy Models

Dissipative axion (DA)

Uncoupled scalar experiences Hubble friction. Uncoupled DR dilutes as $(1 + z)^4$

$$\ddot{\phi} + (3H)\dot{\phi} + V_{\phi} = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr}$$



Berghaus & Karwal [1911.06281]

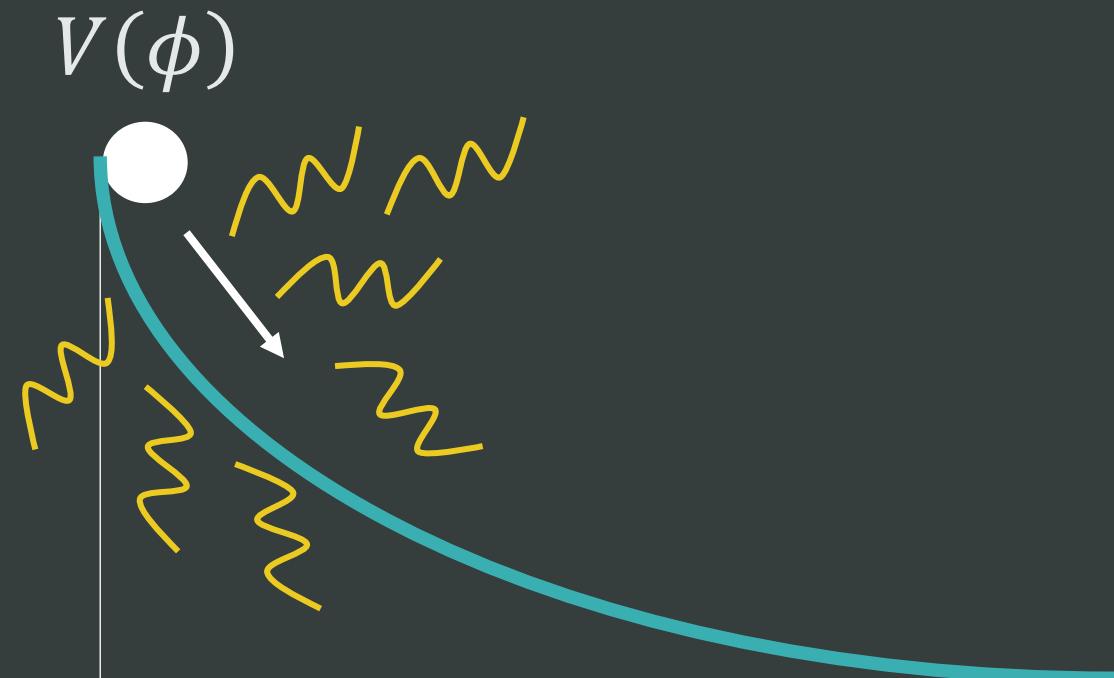
Early dark energy Models

Dissipative axion (DA)

Scalar coupled to DR additionally experiences thermal friction

$$\ddot{\phi} + (3H + \Upsilon(T_{dr}))\dot{\phi} + V_\phi = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon(T_{dr})\dot{\phi}^2$$



Berghaus & Karwal [1911.06281]

Early dark energy Models

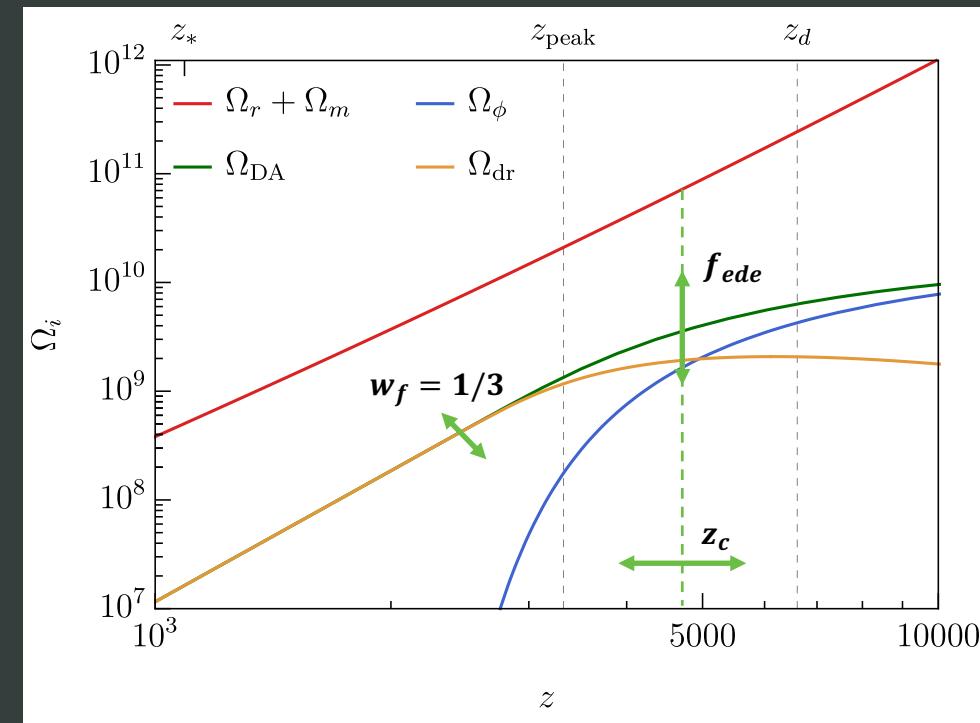
Dissipative axion (DA)

$$\ddot{\phi} + (3H + \Upsilon(T_{dr}))\dot{\phi} + V_\phi = 0$$

$$\dot{\rho}_{dr} = -4H\rho_{dr} + \Upsilon(T_{dr})\dot{\phi}^2$$

$$\begin{aligned} m, \phi_i &\rightarrow f_{ede} \\ m, \Upsilon(T_{dr}) &\rightarrow z_c \\ w_f &= 1/3 \end{aligned}$$

Robust to choice of $V(\phi)$



Berghaus & Karwal [1911.06281]

Early dark energy Models

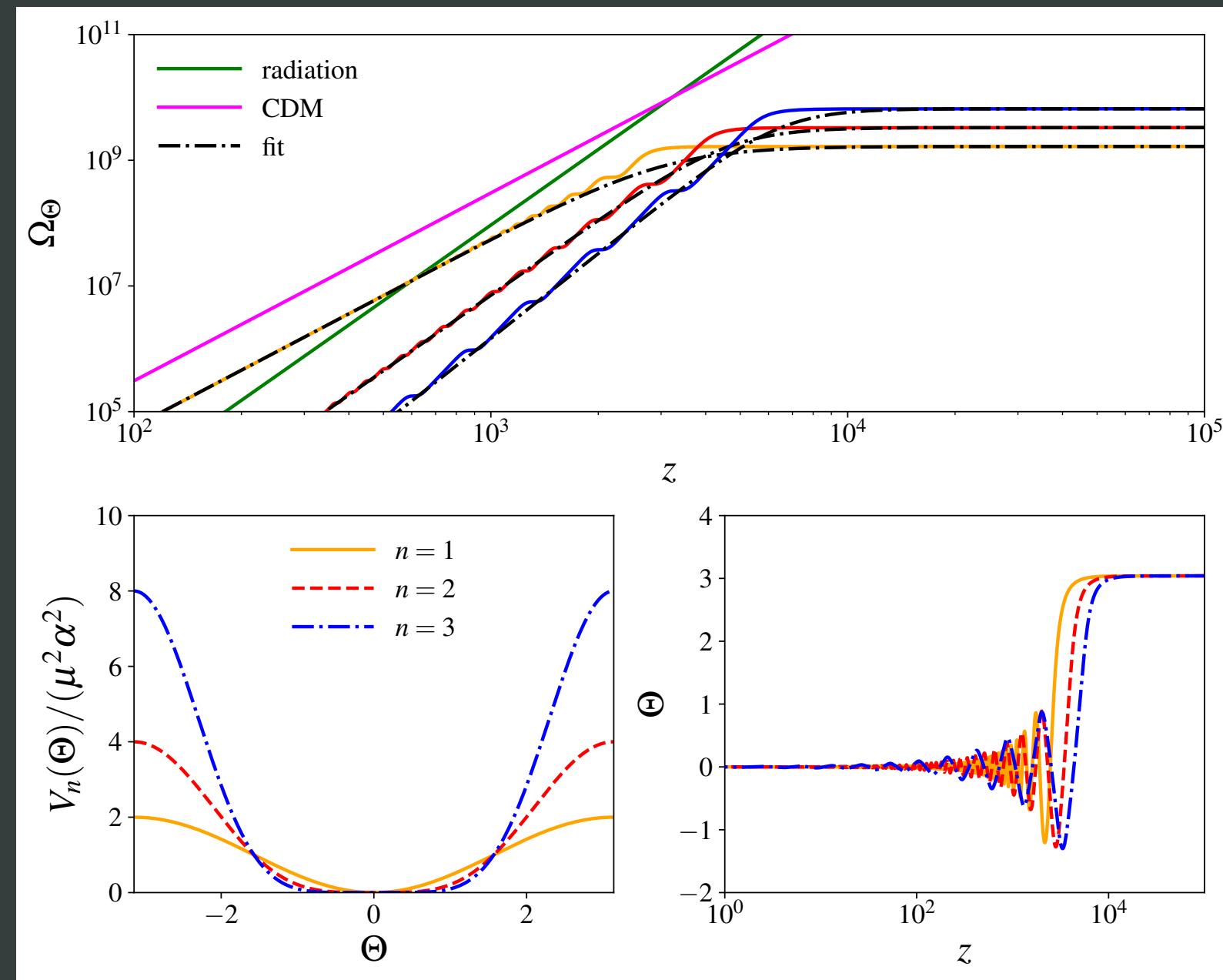
Ultra-light axion-like (ULA)
particles

$$V(\phi) \propto (1 - \cos(\phi))^n$$

$$w_f = \frac{n-1}{n+1}$$

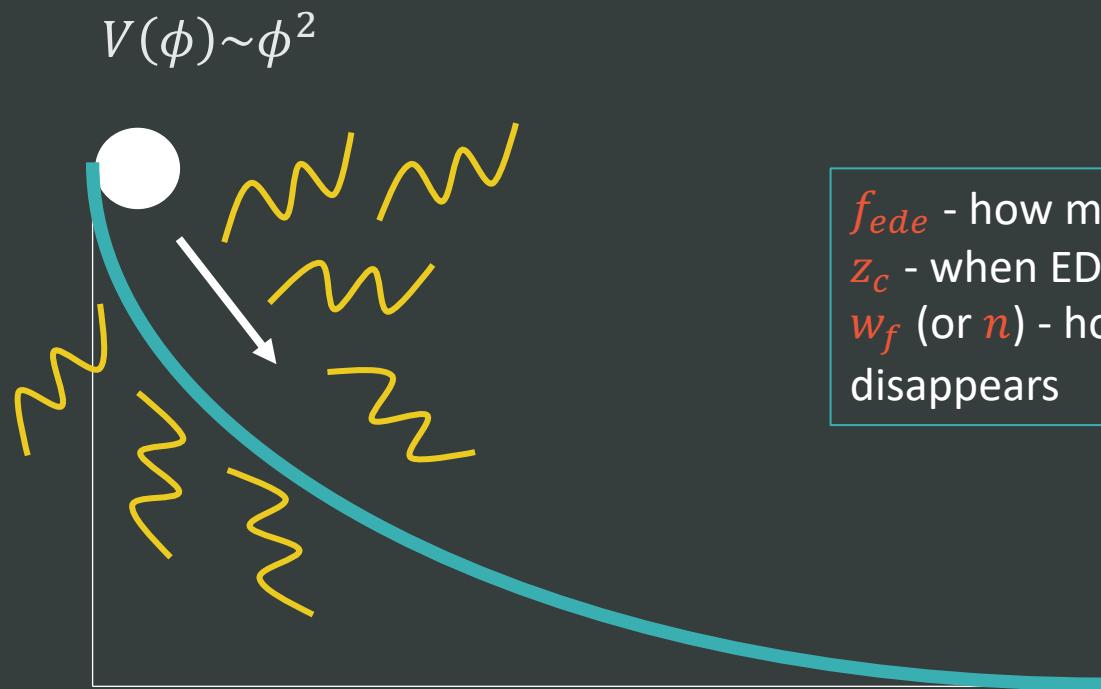
$$\phi_i, f, m \leftrightarrow f_{ede}, z_c$$

Poulin, TK, et al [arxiv:1806.10608]



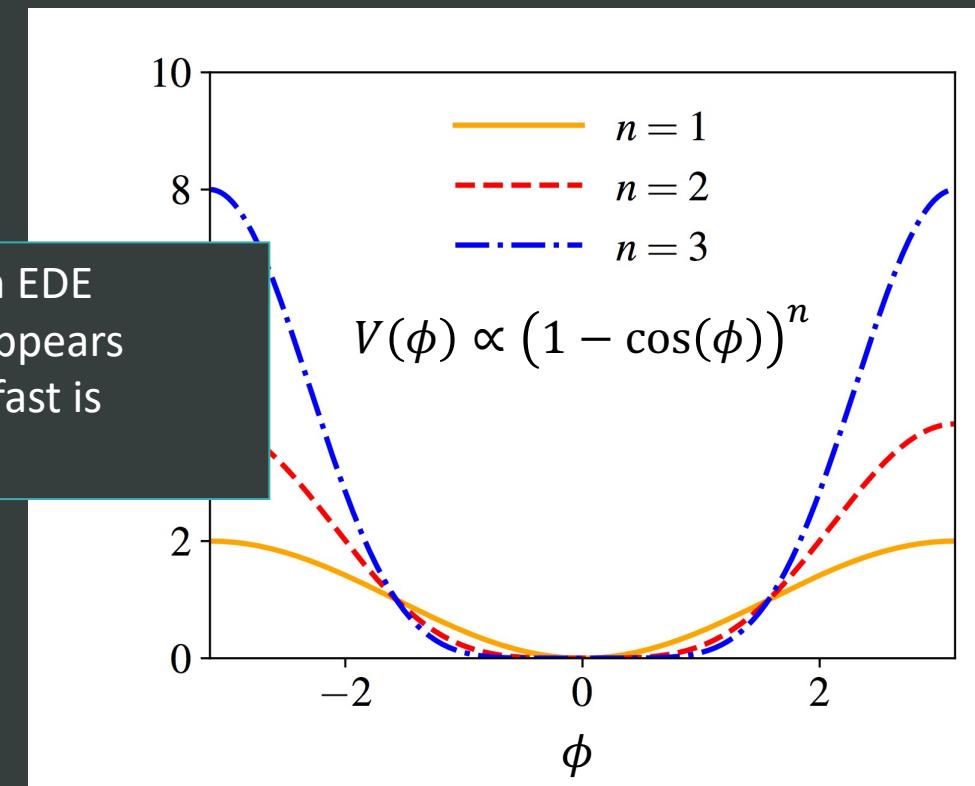
Early dark energy Models

Dissipative Axion



f_{ede} - how much EDE
 z_c - when EDE appears
 w_f (or n) - how fast it disappears

Ultra-light axion inspired (ULA) potential



Early dark energy Solutions

Based on

- CMB temperature, polarisation and lensing data from Planck 2015
- Local Hubble measurement from SHOES 2018
- Baryon acoustic oscillations
- Pantheon supernovae

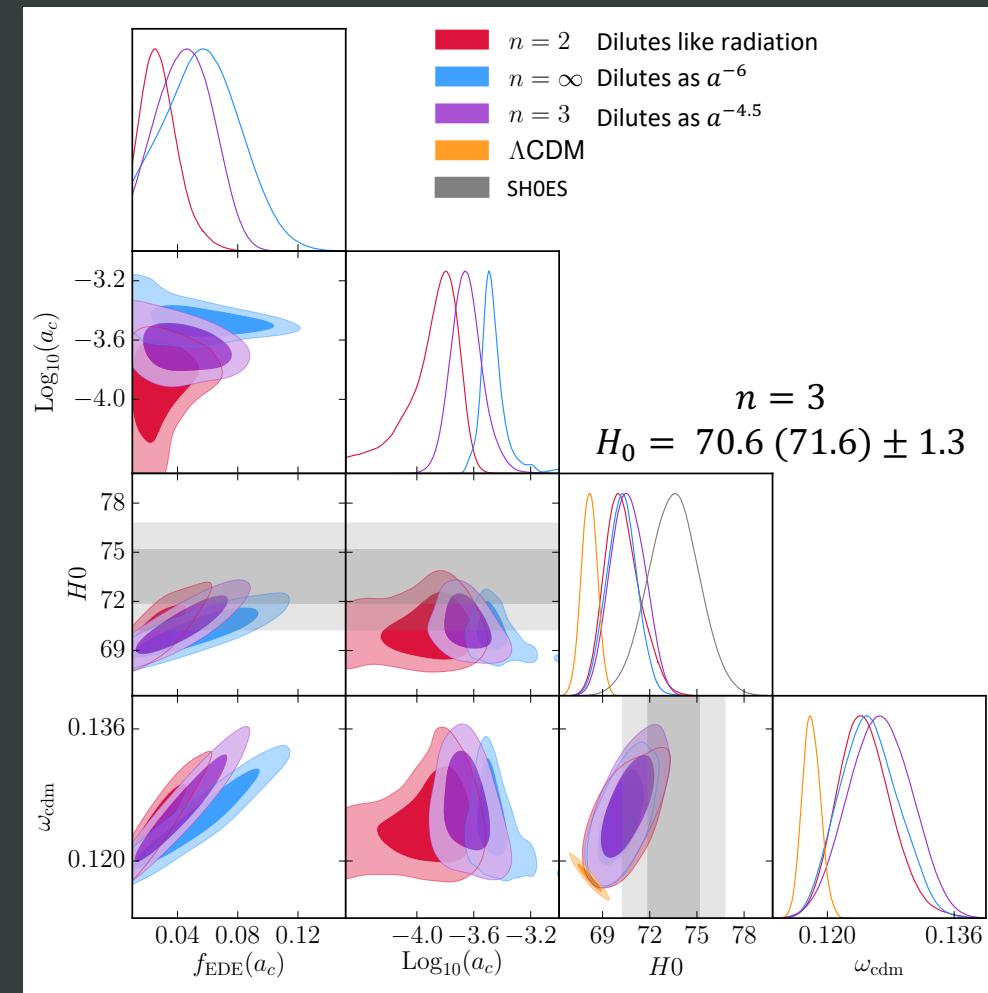
ω_{cdm} = fractional amount of cold dark matter today

$f_{ede}(a_c)$ = fractional energy density in the axion field at critical redshift $z_c \approx 1/a_c$

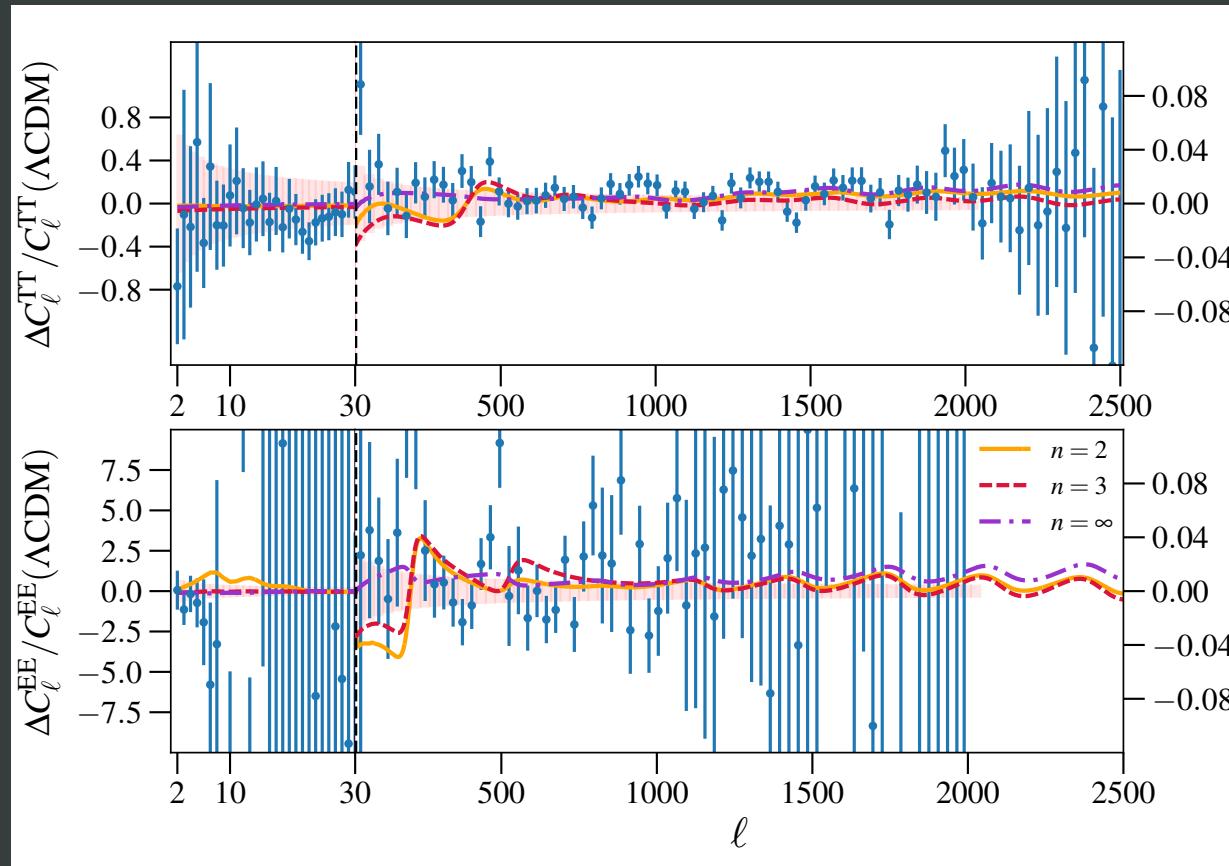
As before, $w_f = \frac{n-1}{n+1}$

Poulin, TK et al [1811.04083]

Phenomenological EDE (ULA fluid)



Early dark energy Detection



Could detect EDE in
cosmic-variance-limited,
high-ell
CMB polarisation data

Poulin, TK et al [1811.04083]

Early dark energy New concordance model?

Cosmologists



This talk

- ✓ Approaches to theoretically resolving the Hubble tension

- ✓ Solutions to H_0 : early dark energy (EDE) models

→ Challenges: the large-scale structure tension

Fit Λ CDM to the
early universe
 $H_0 = 66.93 \pm 0.62$
km/s/Mpc

Cosmic microwave
background

Fit Λ CDM to the
early universe
 $S_8 = 0.832 \pm 0.013$

4.4 σ tension

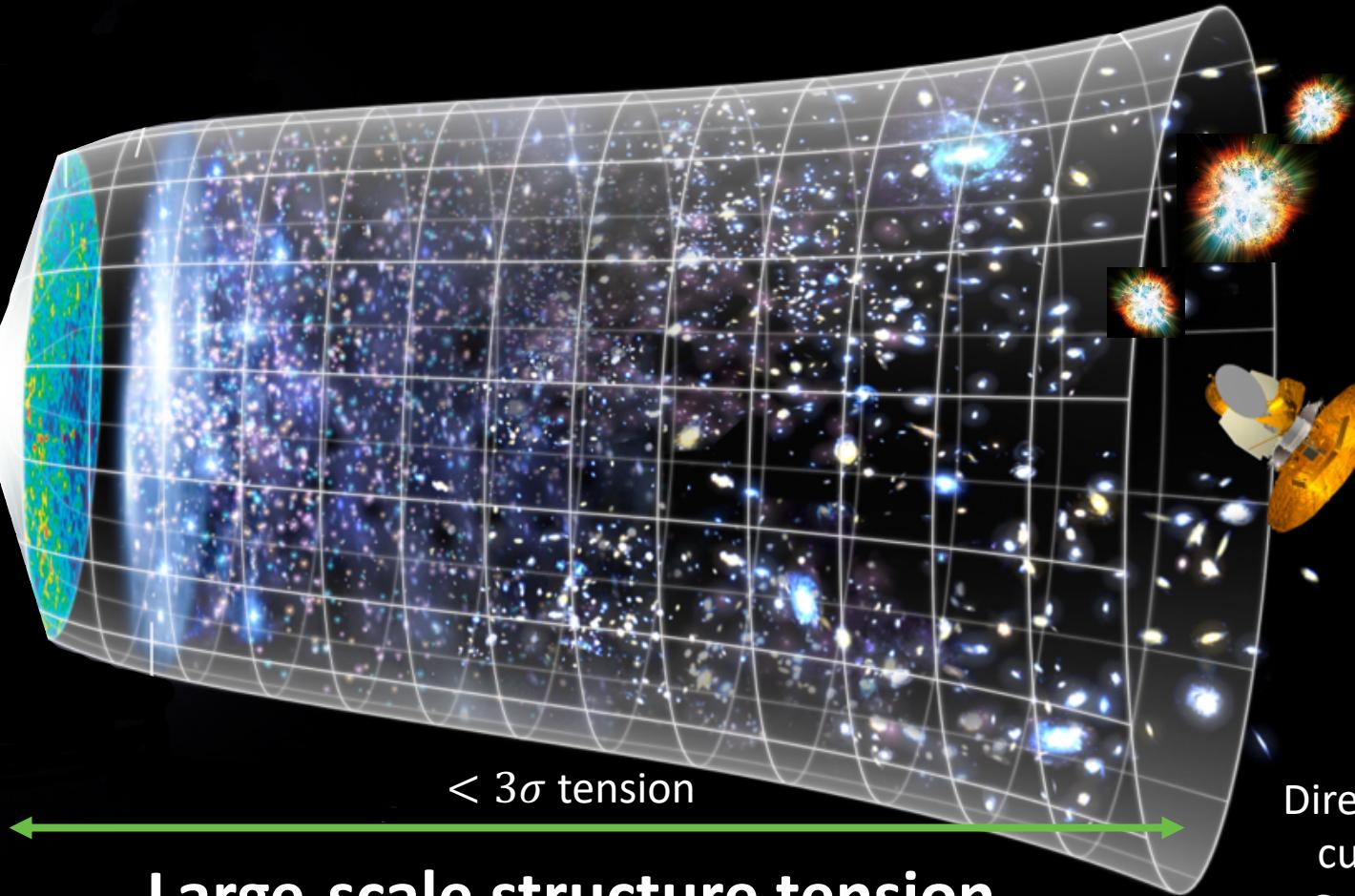
The Hubble tension

Directly measure in
current universe
 $H_0 = 74.03 \pm 1.42$
km/s/Mpc

Directly observe the
current universe
 $S_8 = 0.766^{+0.020}_{-0.014}$

< 3 σ tension

Large-scale structure tension

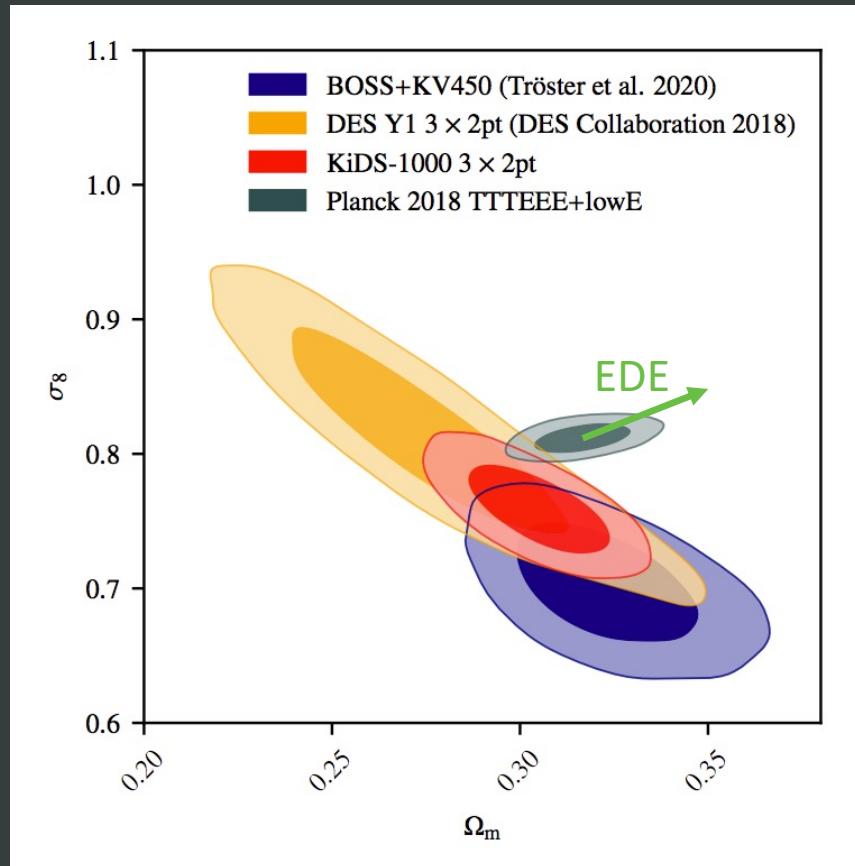


Challenges for EDE

Large-scale structure tension and implications

- Gap in our understanding of how matter clusters?
- Insight into dark matter?
- Relate to the small-scale structure problems of Λ CDM?
 - Λ CDM has difficulty with galaxy evolution
 - Density distribution of some galaxies – see a core but expect a cusp
 - Missing satellites – we expect more sub-halos than observed

Challenges for EDE LSS tension



The S₈ tension

Large-scale structure
(LSS) directly observed
in the late universe

$$S_8 = \sigma_8 \sqrt{\Omega_m / 0.3} < S_8$$

DES Y1 [1708.01530]
KiDS+VIKING-450 [1812.06076]
KiDS-1000 [2007.15632]

Consistent
 2.3σ
 3σ

CMB-inferred value
using Λ CDM

Challenges for EDE LSS tension in EDE and Λ CDM

Effect of LSS tension on EDE is stronger constraints

EDE with CMB

EDE with CMB+LSS

Λ CDM with CMB+LSS

What is the origin of the discrepancy between LSS and CMB?

- Amplitude A_s of the primordial power spectrum

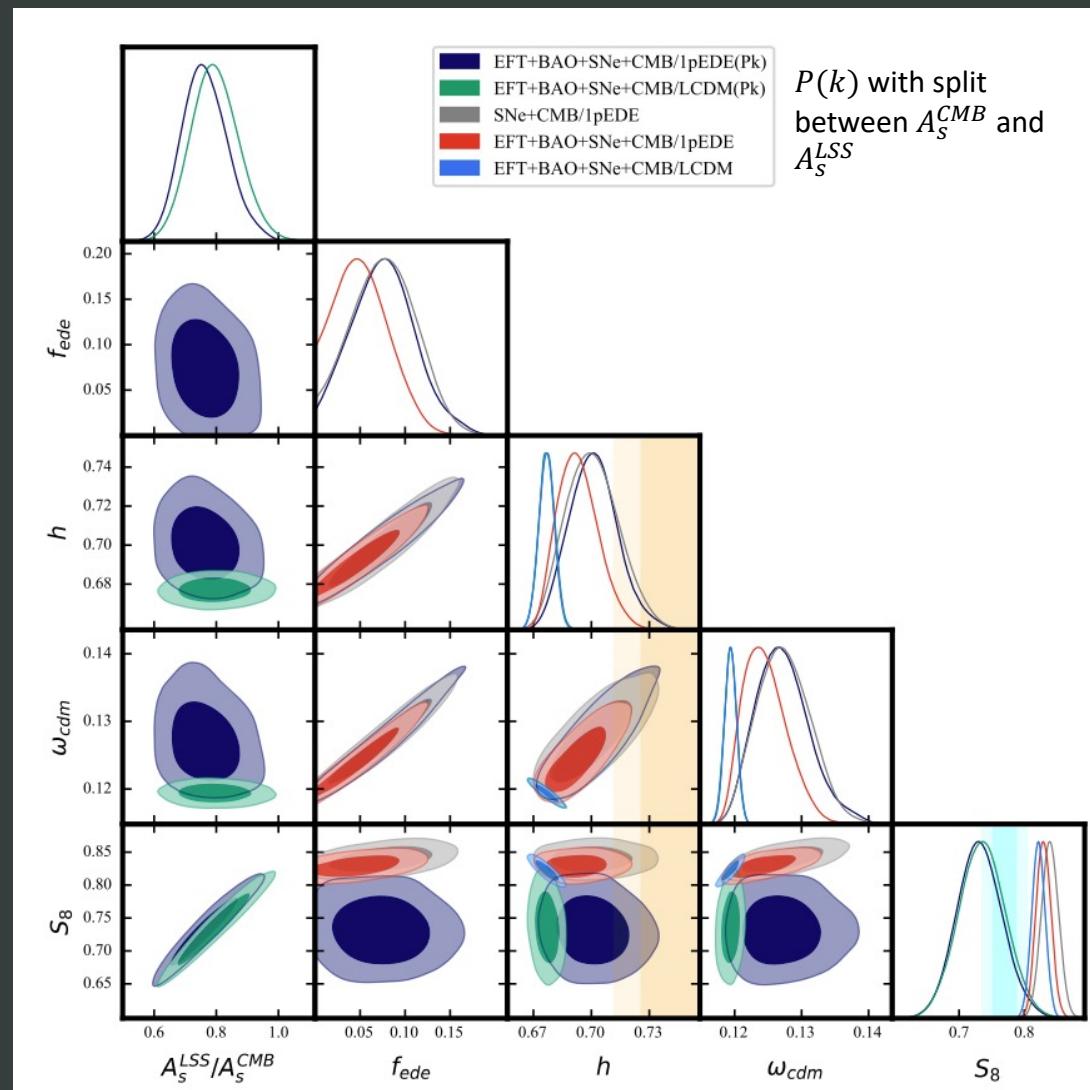
Exercise: allow LSS and CMB different A_s

Λ CDM with CMB+LSS+ A_s split

EDE with CMB+LSS+ A_s split

Tight EDE constraints disappear

Smith et al. [2009.10740]



Towards a new concordance model

Model to replace Λ CDM ?

Model	Tensions
Λ CDM	Both H_0 and LSS
Λ CDM+EDE	Only LSS
New concordance model	Neither

Figure:
a confused dog

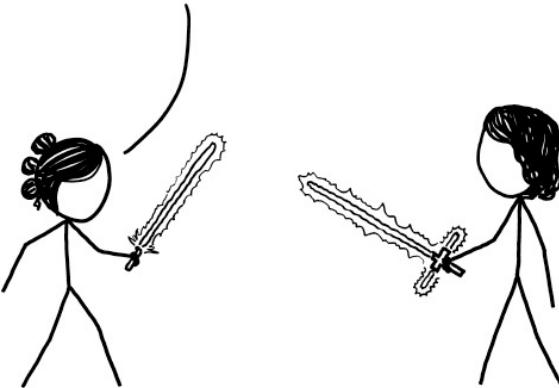


To EDE and beyond

- Does the Hubble tension indicate new physics? Could a solution lie in the early universe?
- Early dark energy can resolve the Hubble tension
 - Several fundamental models for EDE, with varying success at solving the Hubble tension
 - The goodness of fit to cosmological data is not compromised by this addition
 - CMB data from ACT, SPT and CMB-S4 can test EDE
 - EDE faces challenges with the LSS tension [2003.07355] but this tension arises from within Λ CDM and is not introduced because of EDE [2009.10740]
 - Different avatars of EDE have different effects on the large-scale structure tension?
 - New EDE claims to find no tension with EFT of LSS [2009.00006]
 - EDE coupled to neutrinos might have implications for LSS [1911.11760]
 - EDE can be a stepping-stone as we search for the new concordance model of the Universe
 - Two independent solutions required for H_0 and LSS?
 - H_0 depends on background expansion
 - LSS depends on perturbation evolution
 - EDE models can be applied to other eras of cosmic expansion – to explain dark energy or inflation

New LSS, CMB data and further theoretical work might bring insight into the dark sector!

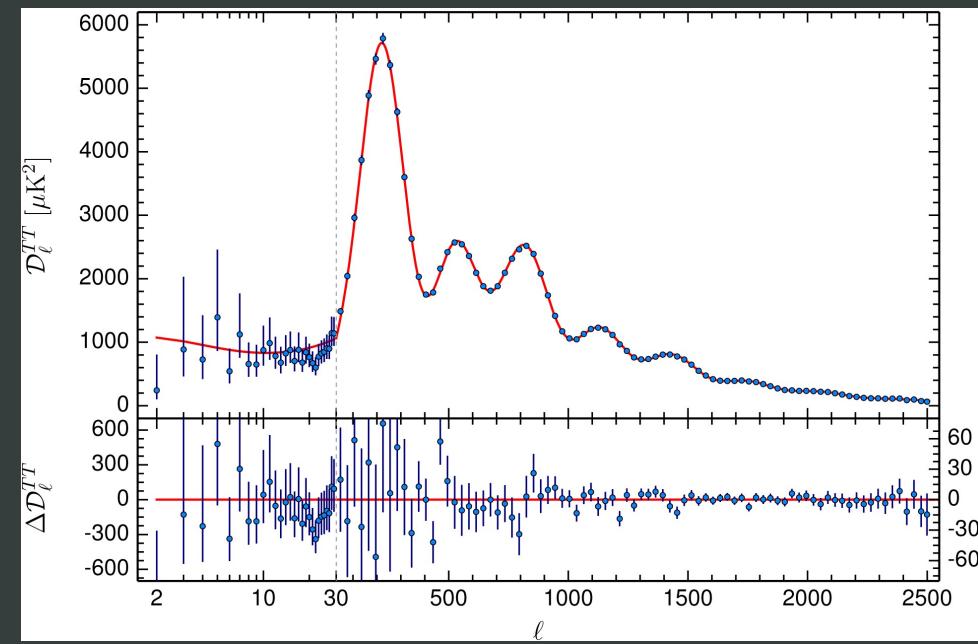
KYLO, WE SHOULDN'T FIGHT! LET'S SET ASIDE OUR DIFFERENCES AND WORK TOGETHER TO MEASURE THE LOCAL PROPERTIES OF SPACE, JUST IN CASE SOMEONE IN THE FAR FUTURE IS WATCHING FROM ANOTHER GALAXY AND WANTS OUR HELP TO CONSTRAIN THE EXPANSION RATE!



Randall Munroe, xkcd

Λ CDM Parameters

- $H_0 = 100h \text{ km s}^{-1}\text{Mpc}^{-1}$ - current value of the Hubble parameter
- $\omega_b = \Omega_b h^2$ - the fractional density of baryons in the Universe
- $\omega_c = \Omega_c h^2$ - the fractional density of cold dark matter in the Universe
- τ - the optical depth due to reionization
- $\ln(10^{10} A_s)$ – amplitude of the primordial power spectrum
- n_s - scalar spectrum power-law index



Source: Ade et al, A&A 2016