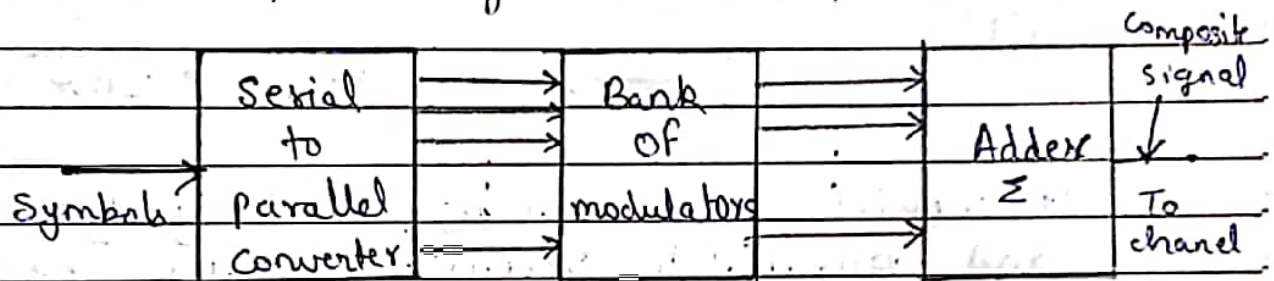


* Test-Ion Unit - 2 *

Q.2 Draw block diagram to describe each components of Multicarrier Modulation transmitter and receiver

→ Multicarrier Modulation Transmitter: -

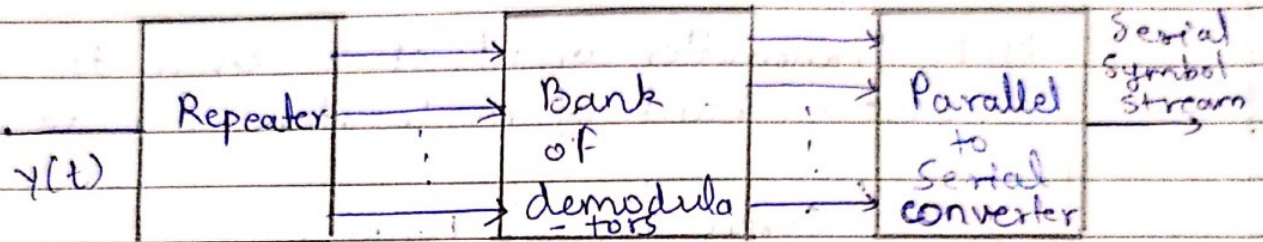
- MCM transmitter consists of a serial-to-parallel converter, bank of modulators and an adder



- Serial to parallel converter is used to transmit the N information symbols to serial. From serial to parallel. Thus there are N numbers of data streams
- The modulator modulates the i^{th} data stream onto the i^{th} subcarrier
- Adder will make the sum of all such subcarriers
- The sum of all the subcarriers will be then transmitted over the channel as composite signal
- Consider the different modulated signals $s_i(t)$ corresponding to the N different subcarriers
- The composite signal $s(t)$ is formed by superposing modulated signals at the transmitter is given by, $s(t) = \sum_i s_i(t)$

- This composite signal $s(t)$ is then transmitted over the wireless channel.
- Thus, in the MCM system N different data streams are transmitted over N subcarriers in parallel.

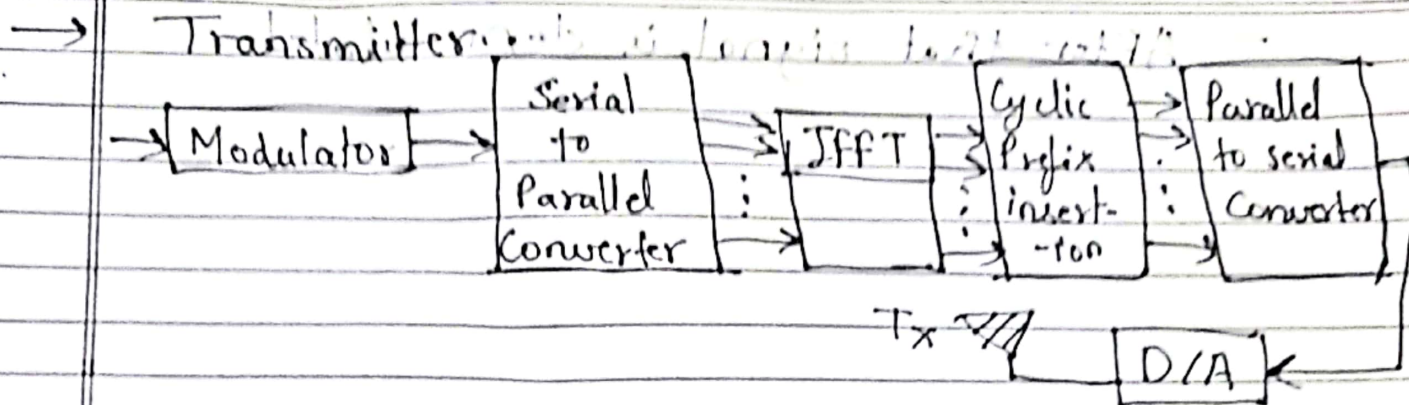
- Multicarrier modulation Receiver :-



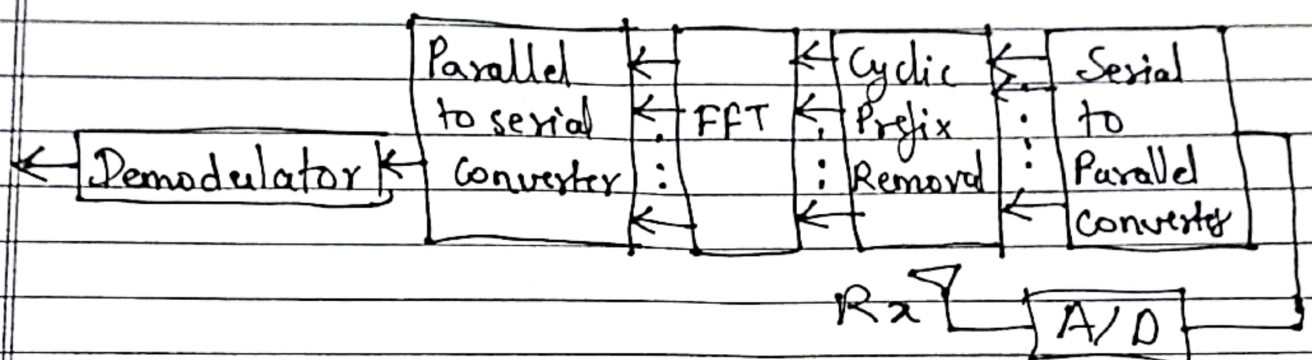
- It consists of a receiver, bank of demodulators and parallel to serial converter. The received signal $y(t)$ is applied to repeater stage. At the receiver end composite signals are amplified first.
- Repeater is an antenna that simultaneously receives, amplifies and transmits a signal.
- It is passed on to the bank of demodulators and the data is converted to serial from parallel forming a symbol stream.

Q.1. Draw neat diagram and explain the working operation of OFDM transmitter and receiver with FFT

→



Receiver :-



- Transmitter :-

- As shown in Fig the OFDM transmitter and receiver consists of IFFT & FFT respectively
- In transmitter the signal is ~~the~~ modulated and passed to convert serial data to parallel
- That data signal is passed to IFFT
- After IFFT the cyclic prefix is inserted to the signal
- And Lastly the data is converted from parallel to serial simultaneously after it digital to analog.
- Receiver :-
- OFDM Receiver acts in opposite as that of transmitter
- Firstly data is converted from digital to analog
- It is converted to parallel
- Here cyclic prefix is removed and applied to FFT

- After it is converted to serial the signal is demodulated

★ Operation :-

- Since we assumed there are N subcarriers allowed for the OFDM transmission, we name them from 0 to $N-1$

- Let $s(t)$ is MCM signal it is Bandlimited to total Bandwidth B

- The eqⁿ is given as:-

Nyquist sampling rate = B

$$\therefore T_s = \frac{1}{B}$$

- Consider complete MCM signal : $\sum_i x_i e^{j2\pi f_i (B/N)t}$

- The u^{th} sample at time instant

$$u T_s = u/B \text{ is given by}$$

$$s(u T_s) = x(u) = \sum_i x_i e^{j2\pi f_i (B/N)(u/B)}$$

$$x(u) = \sum_i x_i e^{j2\pi (f_i u/N)}$$

DFT

- $y_n = h(0)x(n) + \underbrace{h(1)x(n-1) + \dots + h(L-1)x(n-L+1)}_{\text{ISI component}}$

Q.3) Compute the MIMO zero forcing receiver for channel matrix H given as ~~Mar~~

$$H = \begin{bmatrix} 2 & 3 \\ 1 & 3 \\ 4 & 2 \end{bmatrix}$$

$$\rightarrow H^T = \begin{bmatrix} 1 & 2 & 0 & 1 & 4 & 0 \\ 0 & 2 & 3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 2 & 3 \\ 0 & 0 \end{bmatrix}$$

$$H^T H = \begin{bmatrix} 2 & 1 & 4 \\ 3 & 5 & 2 \\ 4 & 2 \end{bmatrix} \begin{bmatrix} 2 & 3 \\ 1 & 2 \\ 0 & 0 \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ 1 & 2 \\ 4 & 2 \end{bmatrix}$$

$$E \cdot I \cdot 0 = \begin{bmatrix} 4+1+16 & 6+3+8 \\ 6+3+8 & 9+9+4 \end{bmatrix} = \begin{bmatrix} 21 & 17 \\ 17 & 22 \end{bmatrix}$$

$$\begin{aligned} H^T H &= \begin{bmatrix} 21 & 17 \\ 17 & 22 \end{bmatrix} \\ &= \frac{1}{21 \times 22 - 17 \times 17} \begin{bmatrix} 22 & -17 \\ -17 & 21 \end{bmatrix} \\ &= \frac{1}{462 - 289} \begin{bmatrix} 22 & -17 \\ -17 & 21 \end{bmatrix} \\ &= \frac{1}{173} \begin{bmatrix} 22 & -17 \\ -17 & 21 \end{bmatrix} \end{aligned}$$

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ 1 & 3 \\ 4 & 2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$y_1 = 2x_1 + 3x_2$$

$$y_2 = x_1 + 3x_2$$

$$y_3 = 4x_1 + 2x_2$$

$$\begin{aligned} \hat{x} &= (H^T H)^{-1} H^T y \\ &= \frac{1}{173} \begin{bmatrix} 22 & -17 \\ -17 & 21 \end{bmatrix} \times \begin{bmatrix} 2 & 14 \\ 3 & 32 \end{bmatrix} \\ &= \frac{1}{173} \begin{bmatrix} -7 & -29 & 54 \\ -29 & 46 & -26 \end{bmatrix} \end{aligned}$$

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} -0.0404 & -0.16761 & 0.3121 \\ -0.1676 & 0.2658 & -0.1502 \end{bmatrix} T \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$$x_1 = \begin{bmatrix} \epsilon & \delta \\ \delta & \epsilon \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} T \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$$x_1 = -0.04 y_1 - 0.17 y_2 + 0.31 y_3$$

$$x_2 = \begin{bmatrix} \delta + \epsilon + \rho & \delta + \epsilon + \delta \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} T \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$$x_2 = -0.17 y_1 + 0.27 y_2 - 0.15 y_3$$

$$\begin{bmatrix} \epsilon & 1 & \delta \\ \delta & \delta & \epsilon \end{bmatrix} = T T^{-1}$$

$$\begin{bmatrix} \epsilon & 1 & \delta \\ 1 & \delta & \epsilon \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = I$$

$$\begin{bmatrix} \epsilon & 1 & \delta \\ 1 & \delta & \epsilon \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = I$$

$$\begin{bmatrix} \epsilon & 1 & \delta \\ 1 & \delta & \epsilon \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = I$$

$$\begin{bmatrix} 1 & \delta \\ \delta & 1 \end{bmatrix} \begin{bmatrix} \epsilon & \delta \\ \delta & \epsilon \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\epsilon \delta + 1 \delta = 1$$

$$\delta \epsilon + 1 \delta = 1$$

$$\epsilon \delta + 1 \delta = 1$$

$$T^{-1} T = I$$

$$\begin{bmatrix} 1 & \delta \\ \delta & 1 \end{bmatrix} \begin{bmatrix} \epsilon & \delta \\ \delta & \epsilon \end{bmatrix} = I$$

$$\begin{bmatrix} 1 & \delta \\ \delta & 1 \end{bmatrix} \begin{bmatrix} \epsilon & \delta \\ \delta & \epsilon \end{bmatrix} = I$$

$$\begin{bmatrix} 1 & \delta \\ \delta & 1 \end{bmatrix} \begin{bmatrix} \epsilon & \delta \\ \delta & \epsilon \end{bmatrix} = I$$

Q.3 For Wimax the total number of subcarriers $N = 256$, with a bandwidth of 15.625 kHz per subcarrier and employs a cyclic prefix which is 12.5% of the symbol time. Find Wimax OFDM symbol ~~at~~ with cyclic prefix.

→ Given $N = 256$

$$BW = 15.625 \text{ kHz} = 15.625 \times 10^3 \text{ Hz}$$

Cyclic prefix length = 12.5% of the symbol time

- Symbol Time :-

$$T_s = \frac{1}{15.625 \times 10^3}$$

$$\therefore T_s = 6.4 \times 10^{-5} = 64 \mu\text{s}$$

- \therefore Cyclic Prefix length = $\frac{12.5 \times 6.4 \times 10^{-5}}{100}$

$$T_{cp} = 8 \times 10^{-6} = 8 \mu\text{s}$$

- Total Symbol Time = $T_s + T_{cp}$
 $= (6.4 \times 10^{-5}) + (8 \times 10^{-6})$

$$T_{\text{total}} = 7.2 \times 10^{-5} = 72 \mu\text{s}$$

- Total symbol samples

$$N_{\text{total}} = T_{\text{total}} \times \text{Sampling Rate}$$

(Symbol rate = 1) (Sampling rate)

$$\therefore N_{\text{total}} = 7.2 \times 10^{-5} \times 1 = \underline{\underline{72 \mu\text{s}}}$$

\therefore Wimax OFDM Symbol with cyclic prefix is 72 μs