

I Sessional

B.Tech. I Sem.

BEM – C 102

**Sec. A (Attempt any two questions) 6 x 2**

1. Find the  $n$ th derivative of  $\sinh 2x \sin 4x$ .
2. Find the radius of curvature of the cardioid  $r = a(1 + \cos \theta)$  at any point  $(r, \theta)$  on it. Prove that  $\rho^2/r$  is a constant.
3. Evaluate  $\lim_{x \rightarrow \pi/4} \frac{\sec^2 x - 2 \tan x}{1 + \cos 4x}$
4. Expand  $\log x$  in powers of  $(x-1)$  and hence find the value of  $\log_e 1.1$ .

**Sec. B (Attempt any one question) 8 x 1**

1. If  $y = (x^2 - 1)^n$ , prove that  $(x^2 - 1)y_{n+2} + 2xy_{n+1} - n(n+1)y_n = 0$
2. Find all the asymptotes of the curve  $4x^3 - 3xy^2 - y^3 + 2x^2 - xy - y^2 - 1 = 0$