# CS315: DATABASE SYSTEMS SCHEDULES

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- A schedule is serial if all operations of a transaction finish before any other operation of another transaction

- T1 transfers 50 from A to B and then T2 transfers 10% of A to B
- A serial schedule

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;  $A := A - 50$ ;  $w_1(A)$ ;  $r_1(B)$ ;  $B := B + 50$ ;  $w_1(B)$ ;  $r_2(A)$ ;  $t := 0.1A$ ;  $A := A - t$ ;  $w_2(A)$ ;  $r_2(B)$ ;  $B := B + t$ ;  $w_2(B)$ ;

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  - They access the same data item and
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- Intuitively, a conflict enforces a logical temporal order on the instructions
- Consequently, if two instructions do not conflict, they can be interchanged

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- A serial schedule is conflict serializable
- A conflict serializable schedule need not be serial

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- r<sub>1</sub>(a)w<sub>2</sub>(a)w<sub>1</sub>(a)
   is not conflict serializable as
  - It is not conflict equivalent to either of the two serial schedules  $T_1 T_2$  or  $T_2 T_1$

Consider the schedule

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- This leads to view serializability

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  - For each data item x, if a transaction T reads the initial value of x in S, it reads the same initial value of x in S' as well
  - 2 For each data item x, if a transaction T writes the final value of x in S, it writes the final value of a in S' as well
  - If transaction  $T_i$  reads the value of data item x produced by write by transaction  $T_j$  in S, it must read the value written by  $T_j$  in S' as well

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- A schedule S is view serializable if it is view equivalent to a serial schedule

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  - Blind writes: writes to a data item without reading it
- Every view serializable schedule that is not conflict serializable must have blind writes

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- Conflict and view serializable schedules are restrictive
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  - $r_2(B)$ ; B := B 10;  $w_2(B)$ ;  $r_2(A)$ ; A := A + 10;  $w_2(A)$ ; but is neither conflict nor view serializable
- Determining such equivalence requires semantic analysis of operations other than read and write

- Create a precedence graph for the schedule
- Directed graph where each transaction is a vertex
- A directed edge is from transaction T<sub>i</sub> to T<sub>j</sub> if I<sub>i</sub> is before I<sub>j</sub> and they conflict
  - $w_i(x)$  precedes  $r_i(x)$ , or
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- Testing for view serializability is NP-complete
- Practical algorithms
  - Catches all non view serializable schedules
  - But can miss a view serializable schedule

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- Consider  $r_1(a)w_1(a)r_2(a)r_1(b)$
- If  $T_2$  commits just after  $r_2(a)$ , i.e., if the schedule is  $r_1(a)w_1(a)r_2(a)c_2r_1(b)a_1$ , then it is *not* recoverable
  - If  $T_1$  crashes, then  $w_1(a)$  is undone, but  $T_2$  has already read a wrong value of a and committed

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- Order of commits and aborts are important for recoverability
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- Consider  $r_1(a)w_1(a)r_2(a)r_1(b)$
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# Relationship among Schedules

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