

ESC201T: Introduction to Electronics

HW -10

Date: 19.11.2020

Q.1 Convert the following numbers into the number system indicated:

- a. $(1010.011)_2$ to decimal
- b. $(FA)_{16}$ to decimal
- c. $(101110101101)_2$ into hexadecimal
- d. $(FA)_{16}$ to binary

Q.2 Convert the decimal number 27.25 into a binary number.

Q.3 What is the largest decimal number that you can represent using 8bits? How many bits are required to represent decimal numbers less than or equal to 10^6 ?

Q.4 Determine the number system in which the following arithmetic operations have been carried out. Give justifications for your answer

- a. $24+17=40$
- b. $22 \times 5 = 132$

Q.5 Obtain 1's and 2's complement of the following binary numbers

- a. 10000000
- b. 10101010
- c. 01110101
- d. 10011100

Q.6a What is the minimum number of bits required to represent -32 in 2's complement form?

b. 11011111 is a number in 2's complement. Is it positive or negative? What is its magnitude?

Q.7 Carry out the following four operations using 8bit 2's complement representation:

$$\pm 24 \pm 32$$

Verify that operations have been properly carried out.

Q.8 Show that the Boolean expression $x + \bar{x}.y$ is equivalent to $x + y$ using basic postulates and theorems of Boolean algebra

Q.9 Reduce the following expressions to a minimum number of literals.

a. $f = (x + \bar{y} + \bar{z}).(\bar{y} + \bar{z})$

b. $f = (x + y).(\bar{y} + \bar{x})$

c. $f = ABCD + \bar{A}BD + AB\bar{C}D$

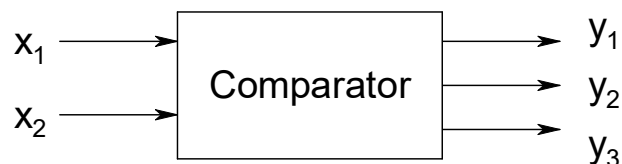
Q.10 Obtain the truth table for the following function: $(x.y+z)(y+x.z)$ and write it as sum of products (SOP) and product of sums (POS).

Q.11 Implement an 8 input OR gate using only 2 input AND and 2 input OR gates.

Q.12 Show that you can implement 2 input AND, 2 input OR and NOT gates using only 2 input NAND gates. Similarly show that you can implement 2 input AND, 2 input OR and NOT gates using only 2 input NOR gates.

Q.13 Implement a 2-input exclusive OR gate with only 2 input NAND gates .

Q.14 Figure below shows a block diagram of a comparator. From the description given , obtain first the truth table for outputs y_1 , y_2 and y_3 , then the Boolean expression and finally the gate netlist. Both inputs are 1-bit.



y_1 is 1 if and only if $x_1 > x_2$

y_2 is 1 if and only if $x_1 = x_2$

y_3 is 1 if and only if $x_1 < x_2$

Q.15 Simplify the following 4-variable functions into sum-of-products form using K-map.

a. $\sum(1,5,6,7,14)$

b. $\sum(0,4,6,8)$

c. $\sum(0,1,4,6,8,9,14)$

d. $\sum(1,4,7,11,13,14)$

Q.16 Simplify the following 4-variable functions into product-of-sums form using K-map

a. $\Pi(1,3,5,7,13,15)$

b. $\Pi(1,3,6,9,11,12,14)$

c. $\Pi (1,3,5,7,9,11,12,13,14,15,)$

d. $\Pi (0,1,3,4,5,7,12,13,15)$

Q.17 Simplify the following expressions into sum-of-products form using the don't care conditions (d) into account.

a. $F(A,B,C,D) = \sum (4,5,7,12,13,14)$
 $d(A,B,C,D) = \sum (1,9,11,15)$

b. $F(A,B,C,D) = \sum (1,2,12,13,14)$
 $d(A,B,C,D) = \sum (8,9,10,11)$

Q.18 For the Boolean expression given below, implement it using two levels of logic first as AND-OR and then as OR-AND.

$$F(a,b,c,d) = (ab + cd)(\bar{a}b + \bar{c}d + a\bar{c})$$

Q.19 Implement the following expression using only 2-input NAND gates and then repeat the problem with only 2 input NOR gates.

$$F(a,b,c,d) = ab + \bar{a}bc + \bar{a}\bar{b}\bar{c}d$$

Q.20 Design a combinational circuit with 3 inputs and 1 output

(a) The output is 1 when the binary value of the inputs is less than 3. The output is 0 otherwise

(b) The output is 1 when the binary value of inputs is an odd number.

Q.21 Design a half subtractor circuit with inputs x and y and outputs Diff. and B_{out}. The circuit subtracts the bits x-y and places the result in Diff. and borrow in B_{out}.