CIS 520, Operating Systems Concepts

Lecture 3
Simulation of Asynchronous Processes
(Queuing Systems)



Agenda

- Two paradigms in the design of operating systems
- Queuing model
- Simulation mechanisms
 - Random number generation
 - Event generation
 - Event processing
 - Statistics gathering
- Homework: The First Programming Assignment

Two Paradigms

(after A. Tannenbaum)

```
main()
{
    int ...;

    init();
    do_something();
    read(...);
    do_something_else();
    write(...);
    keep_going();
    exit(0);
}
```

```
main()
event_t event;
while (get_event(event))
   switch (event.type)
                case 1: ...;
                case 2: ...;
                case 3: ...;
```

I: Algorithmic code

II: Event-driven code

The Model

The Customer Queue

Mean rate: μ customers/sec

Arrival, C

<u>Departure</u>

Mean rate: λ customers/sec

The Server

Steady State: $\lambda < \mu$

(takes certain time to process a customer, so the queue is formed)

What does *mean* mean?

Let the probability density of a random variable ξ be $p_{\xi}(x)$ defined on an interval [a, b]

Then the mean $E[\xi]$ is defined as

$$E[\xi] = \int_{a} x p_{\xi}(x) dx$$

For a discrete variable ξ with $p_{\xi}(k) = P(\xi = k)$,

$$E[\xi] = \sum_{i=0}^{\infty} i p_{\xi}(i)$$

The Poisson Distribution

The probability of exactly k arrivals within the interval [0, t] is independent from the previous arrival history:

$$P\{t,k\} = e^{-\lambda t} \frac{(\lambda t)^k}{k!}$$

Inter-arrival Time

• For the *Poisson* distribution, the inter-arrival probability density is distributed exponentially, too:

$$P[inter-arrival\ time < t] = 1 - e^{-\lambda t}$$

Simulations

- Analytical approach does not work very well for all classes of queuing disciplines
- ◆ The low price of computing permits us to use computer simulations of very complex queuing systems (it is equivalent to integrating complex difference-differential equations) on a computer
- Simulations are widely used in modeling (and thus predicting) computer, communications, financial, and biological systems
- From now on, we will use simulations systematically in our homework

First Comes First: Random Number Generation

- Well, one could generate them using Geiger counter, for example, or—better yet—using the data from past experiences
- But very often—and this is what we will do—what is used is *pseudo-random* number generators
- You could download C++ packages from the WWW (e.g., http://www.agner.org/random/, or http://mathworld.wolfram.com/), or check with your local systems administrator for the packages already on your machine. (A good one is available on the class site.)
- If you are interested in the subject, the best place to start (and finish!) is *D. Knuth*, "The Art of Computer Programming," Volume II

Pseudo-Random Number Generation (The *Linear Congruential Method*)

- We start with four natural "magic numbers":
 - \blacksquare m, the modulus
 - a, the multiplier (a < m)
 - c, the increment (c < m)
 - X_0 , the starting value (or seed) ($X_0 < m$)

The desired sequence (which should have a long *period*) is

$$X_{n+1} = (aX_n + c) \mod m, n > 0$$

Pseudo-Random Number Generation (The *Linear Congruential Method*)

• Again, you can find (and you should, if you have time) much better magic numbers, but just for the purpose of the exercise here is a choice of magic numbers (and they don't require the use of long integers):

$$a = 25173$$
, $c = 13849$, $m = 65536$.

Uniformly Distributed Pseudo-Random Numbers

We can obtain a *uniformly-distributed* sequence Y_n in the interval [0, 1] by scaling the sequence

$$X_{n+1} = (aX_n + c) \mod m$$
:

$$Y_{n+1} = X_{n+1} / m$$

Exponentially Distributed Pseudo-Random Numbers

Finally, we can obtain an *exponentially-distributed* sequence Z_n in the interval, with the mean arrival rate λ (or mean inter-arrival rate $1/\lambda$):

$$X_{n+1} = (aX_n + c) \bmod m$$
:

$$Z_{n+1} = -\frac{1}{\lambda} \ln \left(\frac{X_{n+1} + 1}{m} \right)$$

To Make a Long Story Short

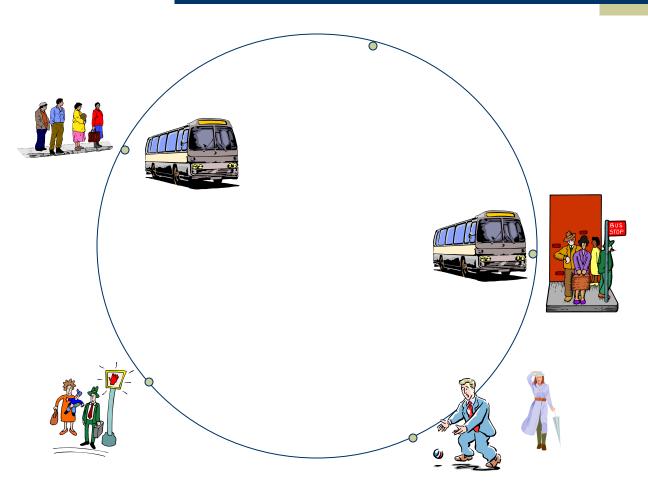
An example:

```
int seed = 1000; /* or, better yet, read it */
float random ()
  float x;
  {
     x = - log ((seed + 1) / 65536);
     seed = (25173 * seed + 13849) % 65536;
         return x;
  }
```

Writing Simulations

- We *create* a data structure (a balanced tree, or simply a doubly-linked ring), which keeps the *events* sorted by time; this is initialized by a dummy event scheduled for time 0
- We *generate* events based on the system we are simulating; as the result, a generated event enters the structure in an appropriate place
- We execute the program by *repeating* the following steps until simulated current time exceeds the defined time limit
 - Take the next event from the event structure and update the current time
 - 2. Process the event; (that will likely generate other events)

We Will Simulate a Bus Service



Three Kinds of Events

- 1. person: A person arrives in the queue at a bus stop

 Action: After a random (exponentially-distributed interarrival) time, another person is scheduled to arrive in the queue
- 2. arrival: A bus arrives at a bus stop

 Action: If there is no one in the queue, the bus proceeds to the next stop, and the event of its arrival there is generated; otherwise, the event to be generated (at present time!) is the first person in the queue boarding the bus;
- 3. boarder: A person boards the bus

 Action: The length of the queue diminishes by 1; If the queue is now empty, the bus proceeds to the next stop, otherwise the next passenger boards the bus

Assumptions

- It takes everyone the same time to enter the bus
- As many people (on average) exit the bus as enter it, and the time to exit the bus is negligible.
 Consequence: we do not consider the exit event in our model
- The stops are equally spaced in a circle
- The buses may not pass one another

The Event Record

This is an entry in the event structure. It contains

- 1. The time of the event
- 2. The type of the event
- 3. The rest of the information, which is event-dependent: the name (number) of the stop, the number of the bus, etc.

The Main Program

```
Initialization();
do
  Get the next event;
  clock = event time;
  switch event_kind
   person:
       update the queue[stop_number];
       generate event (person, stop number, bus number); /* No polymorphism in "C"! */
   arrival: {...} /* board the bus
   boarder: {...}
} while clock < = stop_time
```

Initialization

- Read the *number of buses*, the *number of stops*, the *driving time between stops*, the *boarding time*, the *stop time*, and the *mean arrival rate* from an **initialization file**.
 - For the beginning, assume there are 15 bus stops, 5 buses, the (uniform) time to drive between two contiguous stops is 5 min., mean arrival rate at each stop is 2 persons/min, and boarding time is 3 seconds
- Start with the buses distributed uniformly along the route (by generating appropriate *arrival* events) and generating one *person* event for each stop.

Event Generation

- When the bus *arrival* event occurs, if the queue is empty, generate the *arrival* at the next bus stop at $clock + drive_time$. If the queue is not empty, generate the *boarder* event (at clock)
- When the *boarder* event occurs, if the queue is empty (i.e., the last person boarded), generate the arrival at the next bus stop at *clock* + *drive_time*. If the queue is not empty, generate the *boarder* event (at *clock* + *boarding_time*)
- At the *person* event, generate the next *person* event at the same stop at $clock + (mean_inter-arrival_rate) * random (exponential)$

Note: Keep time in *float* or *double* (a better way of doing things). The *mean_inter-arrival_rate* = 1/ *mean_arrival_rate*

The Goal

- The purpose of the simulation is to observe the behavior of the system, and answer the following questions:
 - Do the distances between two consecutive buses keep uniform? If not, what should be done to ensure they are uniform?
 - What is the average size of a waiting queue at each stop (and what are its maximum and minimum)?
 - Plot the positions of buses as a function of time (you will need to generate periodic snapshots of the system for that)