

8 Puzzle Problem

using

Greedy Best First Search

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What is 8 Puzzle Problem?

The 8 puzzle consists of an area divided into a grid, 3 by 3 for the 8-puzzle. Thus, there are eight tiles in the 8-puzzle. A tile that is next to the empty grid square can be moved into the empty space, leaving its previous position empty in turn. Tiles are numbered, 1 to 8 for the 8-puzzle, so that each tile can be uniquely identified.

We have to solve it using Greedy Best First Search

Greedy Best First Search

Best-first search is a search algorithm which explores a graph by expanding the most promising node chosen according to a specified rule.

Greedy best-first search expands the node that **appears** to be closest to goal . Here **$f(n) = h(n)$** { where **$h(n)$** is the estimate of cost from node n to goal }

Properties of Greedy best-first search

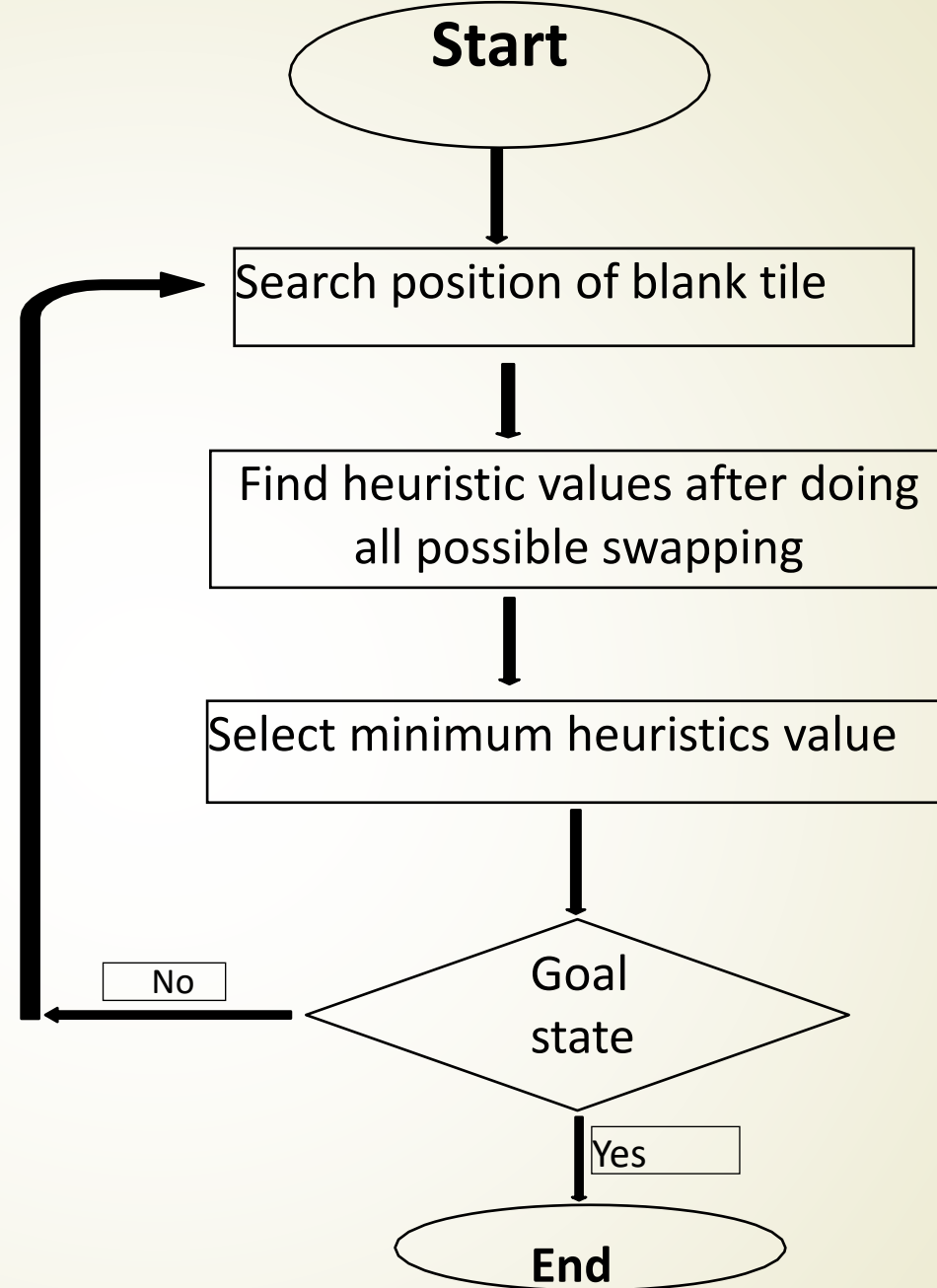
Complete ? No – It can get stuck in loops.

Time ? $O(bm)$, but a good heuristic can give dramatic improvement

Space ? $O(bm)$ - keeps all nodes in memory

Optimal ? No

FLOW CHART:



Pseudo Code of Greedy BFS

Procedure: GreedyBFS

```
insert (state=initial_state, h=initial_heuristic, counter=0) into search_queue;

while search_queue not empty do
    current_queue_entry = pop item from front of search_queue;
    current_state = state from current_queue_entry;
    current_heuristic = heuristic from current_queue_entry;
    starting_counter = counter from current_queue_entry;
    applicable_actions = array of actions applicable in current_state;

    for all index ?i in applicable_actions  $\geq$  starting_counter do
        current_action = applicable_actions[?i];
        successor_state = current_state.apply(current_action);

        if successor_state is goal then
            return plan and exit;
        end if
        successor_heuristic = heuristic value of successor_state;

        if successor_heuristic < current_heuristic then
            insert (current_state, current_heuristic, ?i + 1) at front of search_queue;
            insert (successor_state, successor_heuristic, 0) at front of search_queue;
            break for;

        else
            insert (successor_state, successor_heuristic, 0) into search_queue;
        end if
    end for
end while
exit - no plan found;
```



Figure Shows the initial and goal state of the **8 Puzzle** Problem.
Solve this Puzzle using **Greedy BFS**

Initial State

4	3	
6	7	2
8	1	5

Goal State

	1	2
3	4	5
6	7	8



Here the heuristic function **$h(n)$** is the no. of misplaced tiles (*excluding the blank tile*) with respect to the goal position. We need to solve the above problem using **Greedy Best First Search** algorithm

Initially $h(n)=8$

4	3	
6	7	2
8	1	5



4		3
6	7	2
8	1	5

Move left $h(n)=8$

4	3	2
6	7	
8	1	5

Move down $h(n)=7$

So here the block will move down

Now $h(n)=7$

4	3	2
6	7	
8	1	5



4	3	2
6		7
8	1	5

Move left ; $h(n)=7$

4	3	2
6	7	5
8	1	

Move down ; $h(n)=6$

So here the block will move down

Now $h(n)=6$

4	3	2
6	7	5
8	1	



4	3	2
6	7	5
8		1

Move left ; $h(n)=6$

So here the block will move left

Now $h(n)=6$

4	3	2
6	7	5
8		1



4	3	2
6	7	5
	8	1

Move left ; $h(n)=6$

4	3	2
6		5
8	7	1

Move up ; $h(n)=5$

Here we will move the block up

Initially $h(n)=6$

4	3	2
6		5
8	7	1

4		2
6	3	5
8	7	1

Move up ; $h(n)=5$

4	3	2
	6	5
8	7	1

Move left ; $h(n)=5$

4	3	2
6	5	
8	7	1

Move right ; $h(n)=6$

Here we are getting equal value of heuristic function for two moves , so we will randomly choose any one of the move , lets say UP .

Now $h(n)=5$

4		2
6	3	5
8	7	1



	4	2
6	3	5
8	7	1

Move left ; $h(n)=5$

4	2	
6	3	5
8	7	1

Move right ; $h(n)=6$

Here the block will move left

Now $h(n)=5$

	4	2
6	3	5
8	7	1



6	4	2
	3	5
8	7	1

Move down ; $h(n)=5$

Here the block will move down

Now $h(n)=5$

6	4	2
	3	5
8	7	1



6	4	2
3		5
8	7	1

Move right; $h(n)=4$

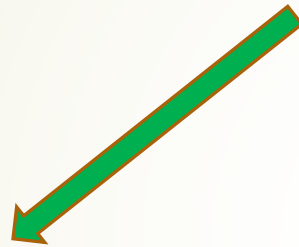
6	4	2
8	3	5
	7	1

Move down ; $h(n)=5$

Here the block will move right

Now $h(n)=4$

6	4	2
3		5
8	7	1



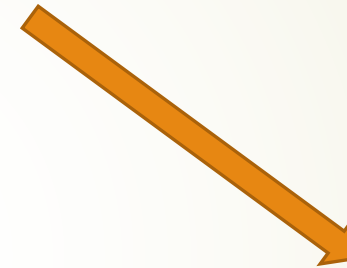
6		2
3	4	5
8	7	1

Move up $h(n)=4$



6	4	2
3	7	5
8		1

Move down ; $h(n)=5$



6	4	2
3	5	
8	7	1

Move right ; $h(n)=5$

Here the block will move up

Now $h(n)=4$

6		2
3	4	5
8	7	1



	6	2
3	4	5
8	7	1

Move left $h(n)=3$

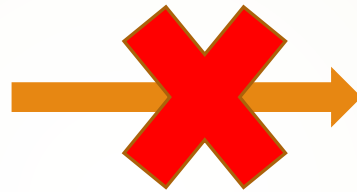
6	2	
3	4	5
8	7	1

Move right ; $h(n)=5$

Here the block will move left

Now $h(n)=3$

	6	2
3	4	5
8	7	1



3	6	2
	4	5
8	7	1

Move down $h(n)=4$

Now from here if we try to move the block down, the value of heuristic function becomes 4 , and so we have no option to move anywhere as Greedy BFS Does not allows us to do so. So this problem cannot be solved completely.

Let's take a look at another example

Example:-

3	2	5
6	1	
7	4	8

Initial state

	1	2
3	4	5
6	7	8

Final state

Initially $h(n) = 7$

3	2	5
6	1	
7	4	8

3	2	
6	1	5
7	4	8

Move up ; $h(n) = 6$

3	2	5
6	1	8
7	4	

Move down ; $h(n) = 7$

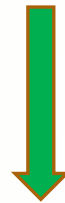
3	2	5
6		1
7	4	8

Move left ; $h(n) = 7$

Here the block will move up

Now $h(n) = 6$

3	2	
6	1	5
7	4	8



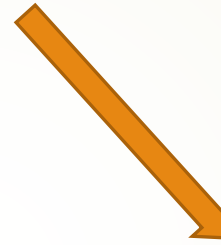
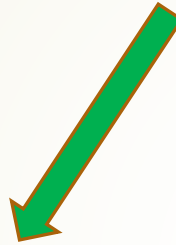
3		2
6	1	5
7	4	8

Move left ; $h(n) = 5$

Here the block will move left

Now $h(n) = 5$

3		2
6	1	5
7	4	8



3	1	2
6		5
7	4	8

Move down; $h(n) = 4$

	3	2
6	1	5
7	4	8

Move up ; $h(n) = 5$

Here the block will move down

Now $h(n) = 4$

3	1	2
6		5
7	4	8

3	1	2
	6	5
7	4	8

Move left ; $h(n) = 4$

3	1	2
6	4	5
7		8

Move down ; $h(n) = 3$

3	1	2
6	5	
7	4	8

Move right ; $h(n) = 5$

Here the block will move down

Now $h(n) = 3$

3	1	2
6	4	5
7		8



3	1	2
6	4	5
	7	8

Move left ; $h(n) = 2$

3	1	2
6	4	5
7	8	

Move right ; $h(n) = 4$

Here the block will move left

Now $h(n) = 2$

3	1	2
6	4	5
	7	8



3	1	2
	4	5
6	7	8

Move up ; $h(n) = 1$

Here the block will move up

Now $h(n) = 1$

3	1	2
	4	5
6	7	8



3	1	2
4		5
6	7	8

Move right; $h(n) = 2$

	1	2
3	4	5
6	7	8

Move up ; $h(n) = 0$

This is the required final state. So here if the block moves up , the $h(n)$ value becomes 0 and we get the result.

CONCLUSION

- **We receive the optimal solution only for some of the specific inputs .**
- **We will not always get optimal solution.**
- **If the value of heuristic function does not decrease, it gets stuck in loops.**



Thank You