



## DSA - Experiment 1

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**Batch:** A/3

**AIM:** Implement and Analyse Tower of Hanoi

**THEORY:** Tower of Hanoi is a mathematical puzzle where we have three rods (A ,B ,C and ) and N disks. The smallest disk is placed on the top and they are on rod **A**. The objective of the puzzle is to move the entire stack to another rod in the same manner as it was in the start.

**RULES OF THE GAME:**

- Only one disk can be moved at a time.
- Each move consists of taking the upper disk from one of the stacks and placing it on top of another stack i.e. a disk can only be moved if it is the uppermost disk on a stack.
- No disk may be placed on top of a smaller disk.

**Time complexity:  $O(2^n)$**

$$T(n)=2T(n-1)+1$$

Backward substitution:

$$T(n-1) = 2T(n-2) + 2$$

$$T(n-2) = 2T(n-3) + 2$$

$$2T(n-2) = 2^2 T(n-3) + 4$$

$$2^2 T(n-3) = 2^3 T(n-3) + 8$$

$$T(1)=0+2^n$$

General equation is  $T(n)=2^n$

**Space complexity:  $O(n)$**

Space of recursive stack is of order n so space complexity is  $O(n)$

**CODE:**

```
main.c
1  #include<conio.h>
2  #include <stdio.h>
3
4  void tower(int n,char frompeg,char topeg,char auxpeg)
5  {
6      if(n==1)
7      {
8          printf("Move disk 1 form peg %c to peg %c \n",frompeg ,topeg);
9          return;
10     }
11     tower(n-1,frompeg,auxpeg,topeg);    //recall
12
13     printf("Move disk %d form peg %c to peg %c\n",n,frompeg ,topeg);
14     tower(n-1,auxpeg,topeg,frompeg);
15 }
16 int main()
17 {
18     printf("Divyesh khunt\n60009210116\n");
19     int disk;
20     char A,B,C;
21     printf("enter no. of disks\n");
22     scanf("%d",&disk);
23     tower(disk, 'A','C','B' );
24     return 0;
25 }
```

**OUTPUT:**

```
Divyesh khunt
60009210116
enter no. of disks
3
Move disk 1 form peg A to peg C
Move disk 2 form peg A to peg B
Move disk 1 form peg C to peg B
Move disk 3 form peg A to peg C
Move disk 1 form peg B to peg A
Move disk 2 form peg B to peg C
Move disk 1 form peg A to peg C

...Program finished with exit code 0
Press ENTER to exit console.
```



**CONCLUSION:**

Thus the code of tower of hanoi was analysed and implemented.

The time complexity of tower of hanoi is  $2^n - 1$