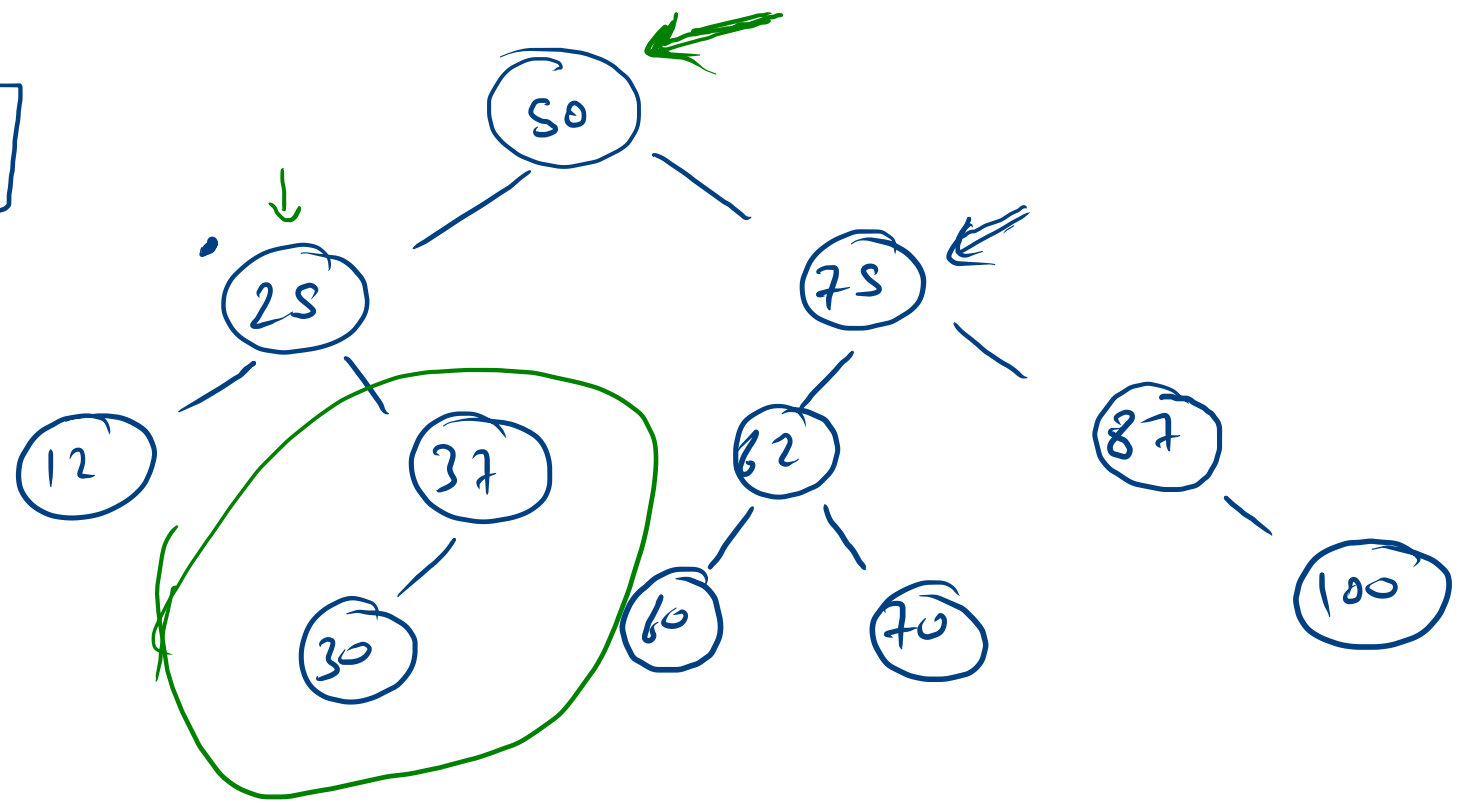


$$fars = 100$$

$$25 \leq 100$$



$$25 + 75$$

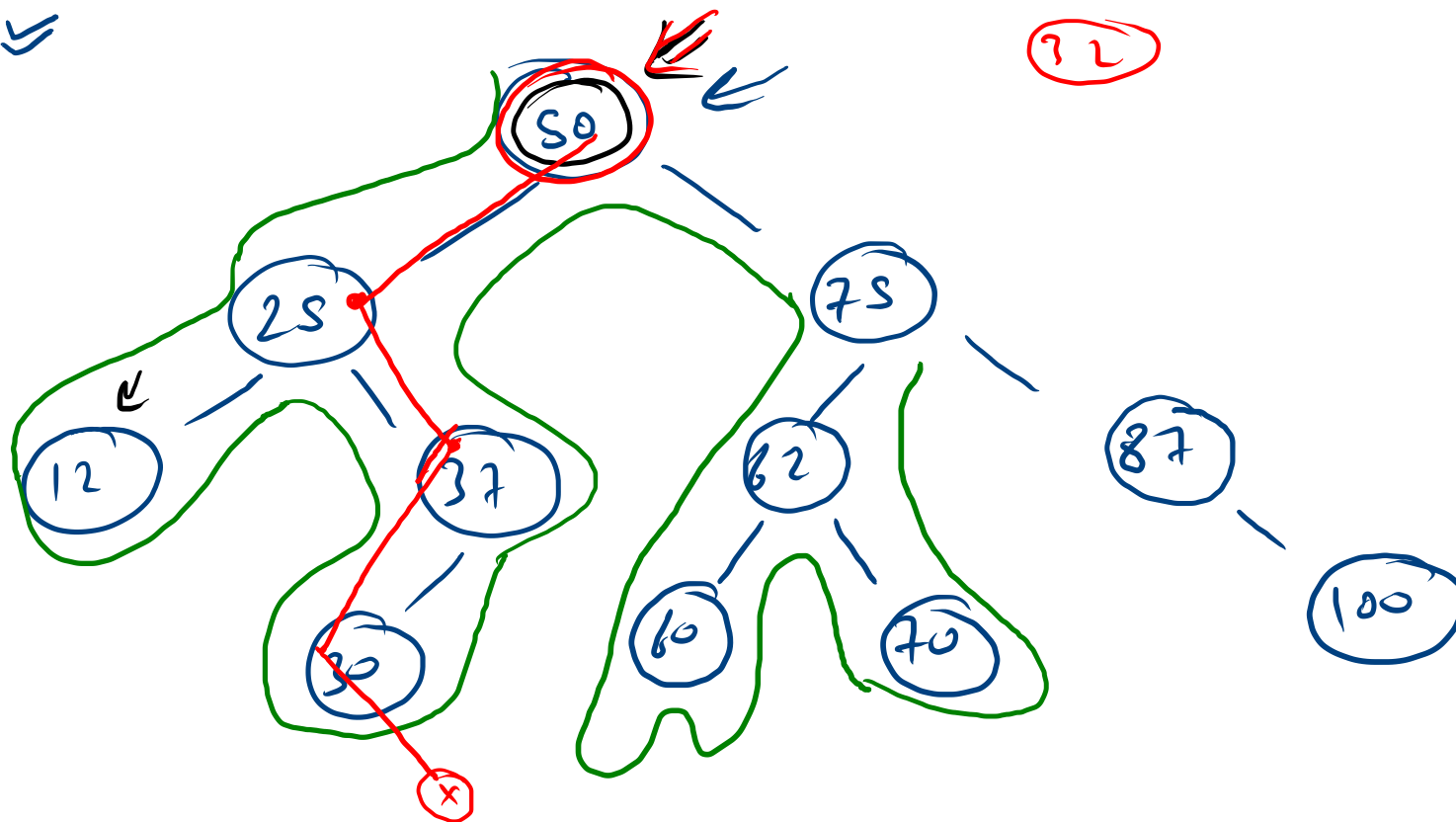
$$30 + 70$$

$$25 \quad 75$$

$$30 \quad 70$$

$$a + b = 100$$

$\log(n) \rightarrow \ln 2 \approx$   
 $\ln \log(n)$



node	comp
$25 < 75$	✓
$30 < 70$	✓
$70 > 30$	✗
$75 > 25$	✗
$50 = 50$	✗

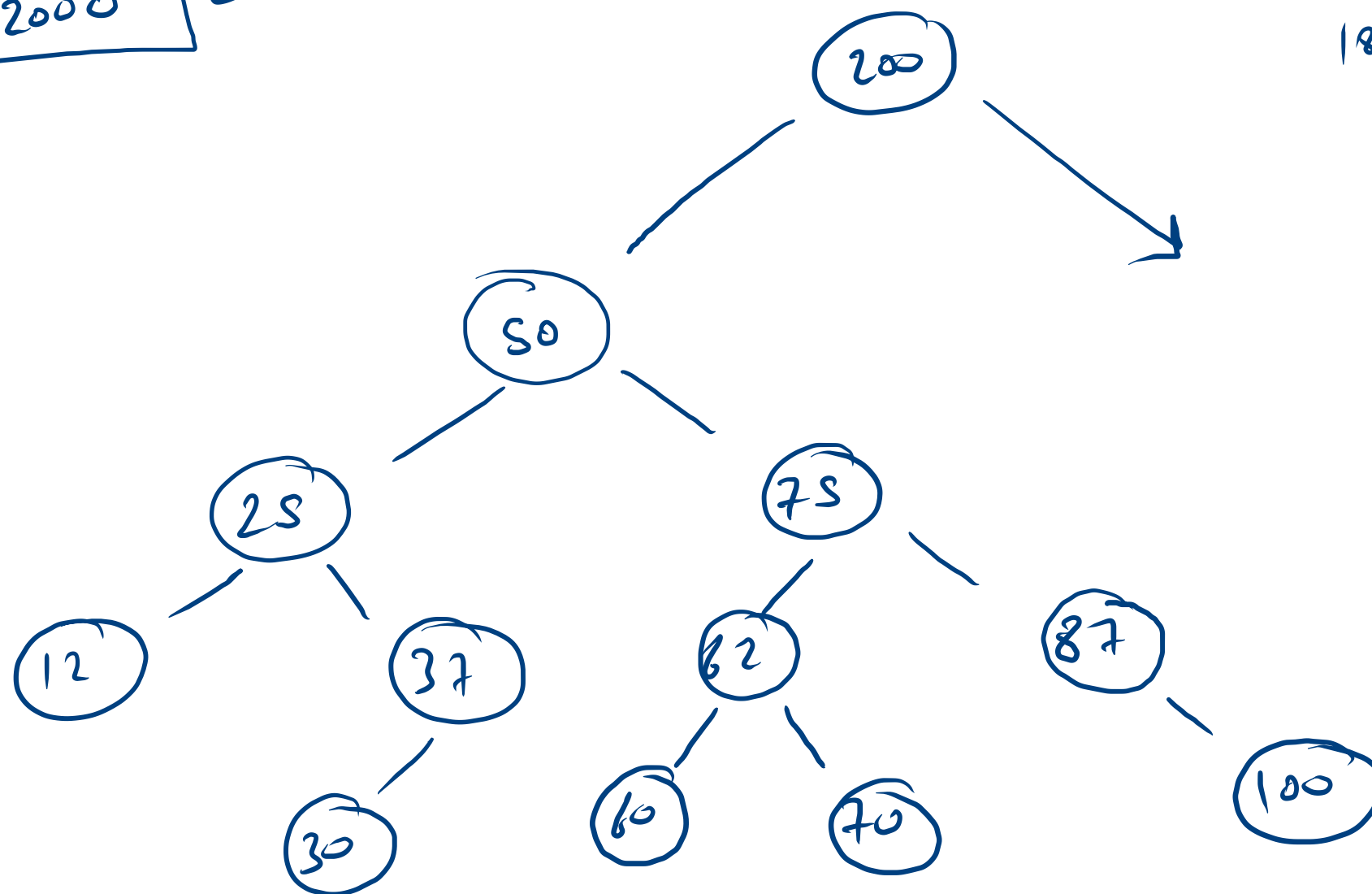
inorder

comp = last - node.data

find (root, comp) ✓ ✗

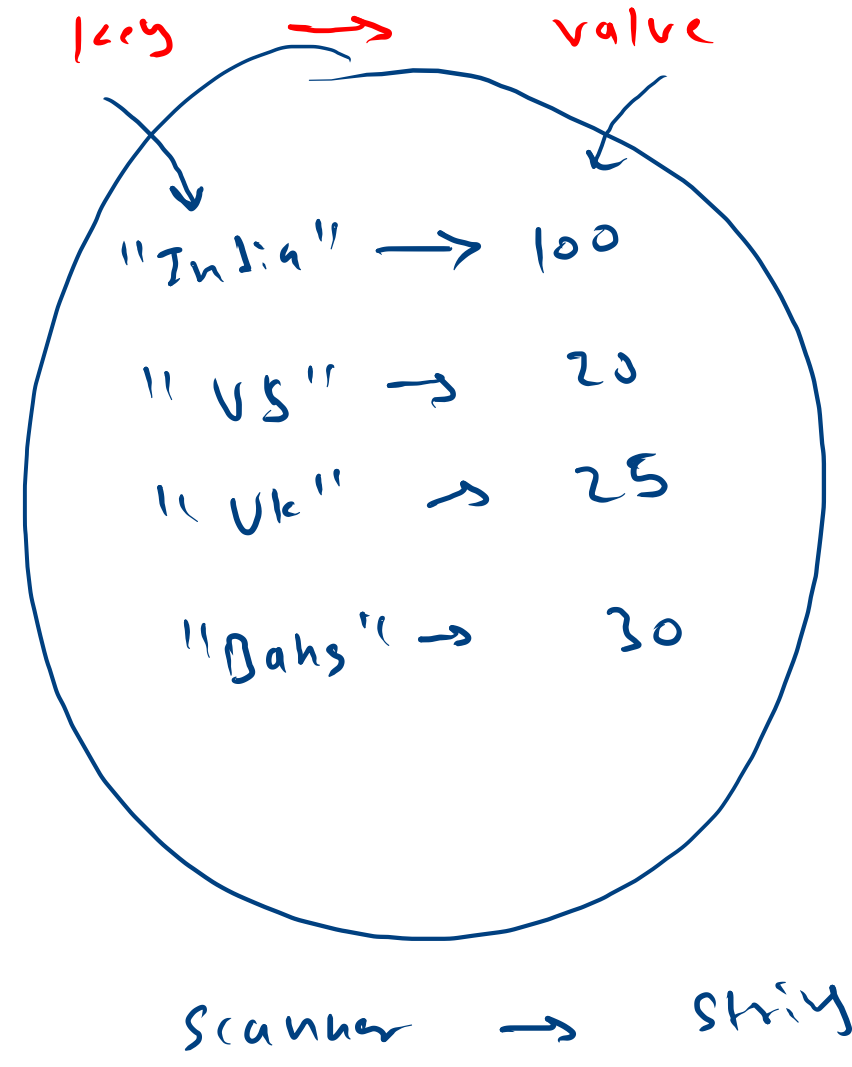
family = 2000 ✓

1800



int	→	?
index	→	?
?	→	?
string	→	string

add / update →  $O(1)$   
remove  $O(1)$



put (key, value)

exist      update  
add      new

value = get (key)

noexist      null

True, False      contains key (key)

remove (key)

zmszeqxllzvheq

2

z 1 2 3

m 1

s 1

e + 2

q + 2

x 1

l → 2

v 1

h 1

↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓  
zmszeqxllzvheq

char  
<Character, Integer>

preget(z)  
pre++  
put(z, pre)

z → x 3

q → x 2

m → 1

x → 1

s → 1

l → x 2

e → x 2

v → 1

h → 1

$$a_1 \rightarrow [5 \quad 5 \quad 9 \quad 8 \quad 5 \quad 5 \quad 8 \quad 0 \quad 3]$$

$$a_2 \rightarrow [9 \quad 7 \quad 1 \quad \textcircled{0} \quad 3 \quad 6 \quad \textcircled{5} \quad 5 \quad 1 \quad 1 \quad 8 \quad 0 \quad 2 \quad 4]$$

9
0
3
5
8



~~5 → f~~  
~~9 → f~~  
~~8 → f~~  
~~0 → f~~  
~~3 → f~~

$a_1 \rightarrow [ \overset{\checkmark}{5} \ \overset{\checkmark}{5} \ \overset{\checkmark}{9} \ \overset{\checkmark}{8} \ \overset{\checkmark}{5} \ \overset{\checkmark}{5} \ \overset{\checkmark}{8} \ \overset{\checkmark}{0} \ \overset{\checkmark}{3} ]$

$a_2 \rightarrow [ \textcircled{9} \ 7 \ 1 \ \textcircled{0} \ \underset{\uparrow}{3} \ \underset{\uparrow}{6} \ \underset{\uparrow}{\textcircled{5}} \ \underset{\uparrow}{9} \ 1 \ 1 \ 8 \ 0 \ 2 \ 4 ]$

0(1)

9
0
3
5
8

$[12 \checkmark \quad 5 \checkmark \quad 1 \checkmark \quad 2 \checkmark \quad 6 \checkmark \quad 10 \checkmark \quad 2 \checkmark \quad 13 \checkmark \quad 7 \checkmark \quad 11 \checkmark \quad 8 \checkmark \quad 9 \checkmark \quad 11 \quad 8 \quad 9 \quad 5 \quad 11]$   
 $-7$

$\star \quad 1 \quad 2$   
 $\star \quad (5) \quad 6 \quad 7 \quad 8 \quad 9 \quad 10 \quad 11 \quad 12 \quad 13$   
 $\uparrow \quad \uparrow$   
 $20 \quad 21$

$len \rightarrow 2$

$len \rightarrow 9$

$len \rightarrow 2$

$\begin{array}{|c|} \hline 1 \\ \hline 20, 21 \\ \hline \end{array}, 2 \quad \star$

$(17) \quad 12 \quad 5 \quad 1 \quad 2 \quad 10 \quad 2$   
 $13 \quad 7 \quad 11 \quad 8 \quad 9 \quad 11 \quad 8$   
 $9 \quad 5 \quad 6 \quad 11$

[12 5 1 2 6 10 2 13 7 11 8 9 11 8 9 5 11]

$\downarrow n$	$o(i)$
12	13
5	7
1	11
2	8
6	9
10	

12  $\rightarrow$  11  $\times$

5  $\rightarrow$  4

sh $\rightarrow$	5	6	7	8	9	10	11	12	13	14
size	$\times$	2	3	4	5	6	7	8	9	$\times$

11

	1	2	3
size	1	2	$\times$

sh  
size  $\leftarrow$

$O(1)$   $O(1)$ 

5	9	12
3	4	3

a + b + c = ...

h

h h

$O(1)$

$O(9)$

8  
1  
2

12  
18  
19

9  
10  
11  
12

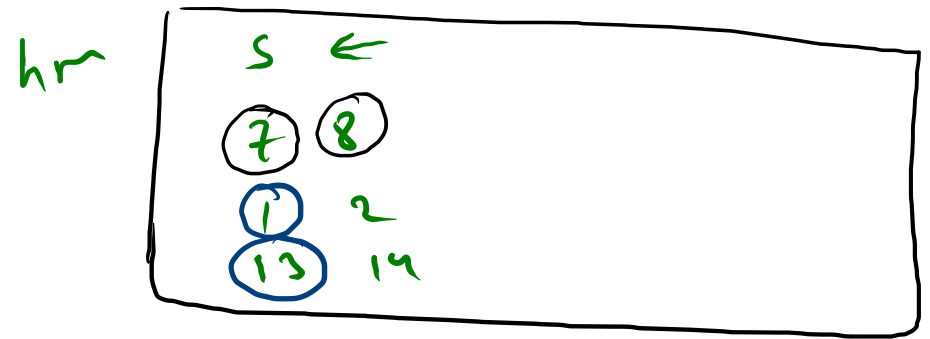
```
HashMap<Integer, Integer> hm = new HashMap<>();
```

```
for(int val: ar){  
    hm.put(val, 1);  
}
```

```
int size=0;  
int start = 0;
```

```
for(Integer key: hm.keySet()){  
    if(hm.containsKey(key-1))continue;  
    ✓ int s = 1;  
    ✓ int f = key+1;  
    while(hm.containsKey(f)){  
        s++;  
        f++;  
    } 2 > 2      2 == 2  13 < 1  
    if(s > size || (size == s && key < start)){  
        start = key;  
        size = s;  
    }  
}
```

```
for(int i=0;i<size;i++){  
    System.out.println(start);  
    start++;  
}
```



size → ~~0~~ ~~1~~ ~~2~~ 2

start → ~~0~~ ~~5~~ ~~7~~ 1

7, 8

→ 1, 2

key = 13

s = 2

f = 14 15

13, 14

[

1 > 0

# Priority Queue

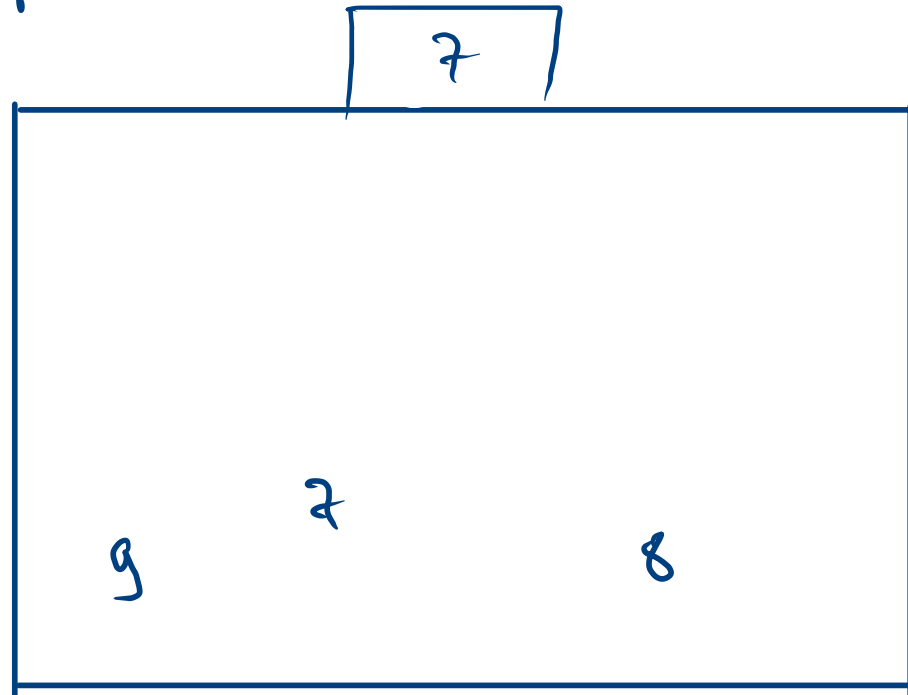
Heap

add(val)  $\rightarrow \log(n)$

remove  $\rightarrow O(\log n)$

peek  $\rightarrow O(1)$

Size



1 2 3 5  
1 3 5

1 2 Rank

100 90 } score

< default  
>

Collections.reverseOrder()

[12, 62, 22, 15, 32, 99, 11, 37, 98, 67, 31, 84]  
99

k = 4

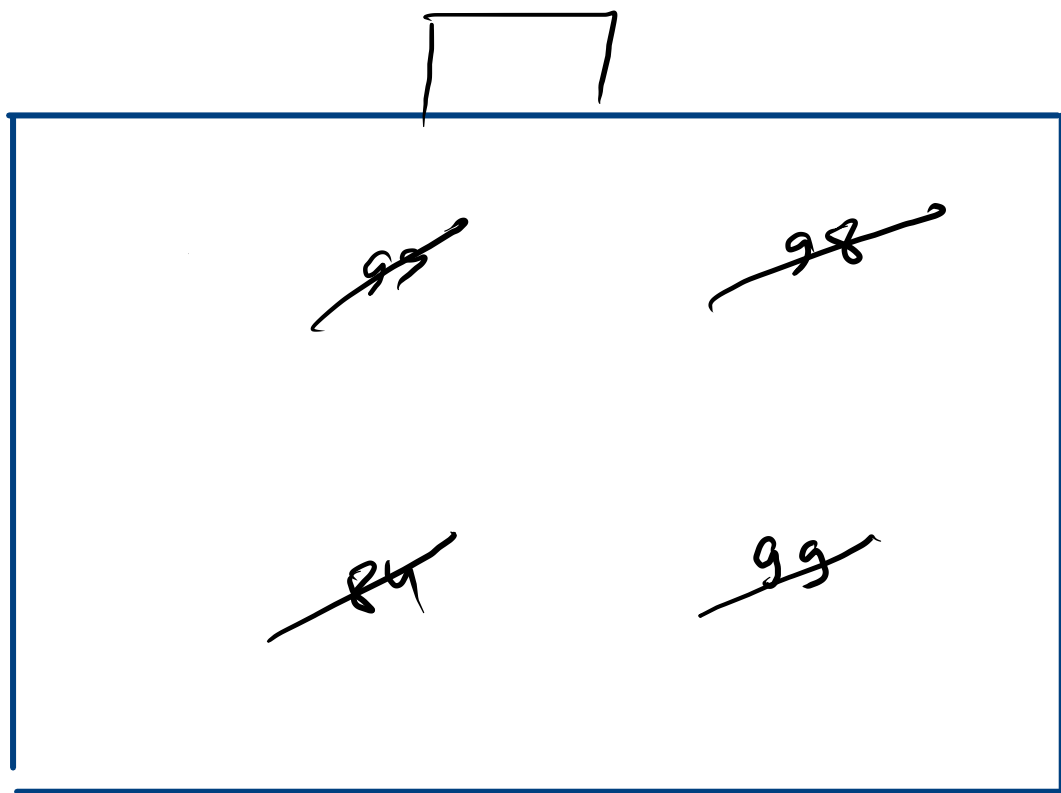
84	
98	←
99	←
99	←

84	99
	98
	99

$\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   $\checkmark$   
 $[12, 62, 22, 15, 37, 99, 11, 37, 98, 67, 31, 84]$   
 $\rightarrow$

$k=4$

smaller  
pq



84  
 98  
 99  
 99



$\alpha$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$        $\downarrow$   
 $[12, 62, 22, 15, 32, 99, 11, 37, 98, 67, 31, 84]$   
 $\xrightarrow{k=4}$   
 $99$

```
PriorityQueue<Integer> pq = new PriorityQueue<>();
```

```
for(int val: arr){
    pq.add(val);
}
```

```
if(pq.size() > k){
    pq.remove();
}
```

```
while(pq.size()>0){
    System.out.println(pq.remove());
}
```

 $\mu_{109}(K)$ 

84

98

95

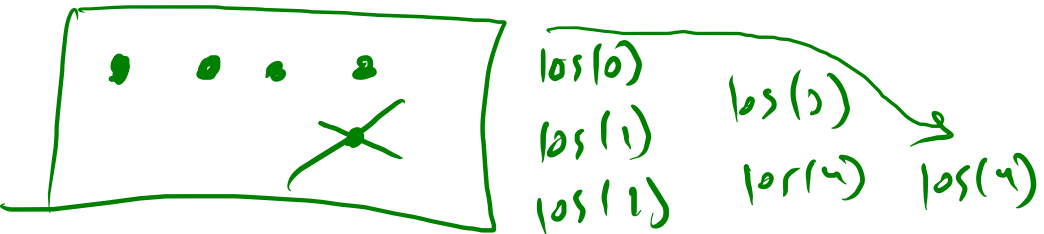
99

pg →

99

99

~~98~~

 $\log(0)$ 

105 (1)

١٥٨١٢٧

los (b)

10514)

105(4)

H.W

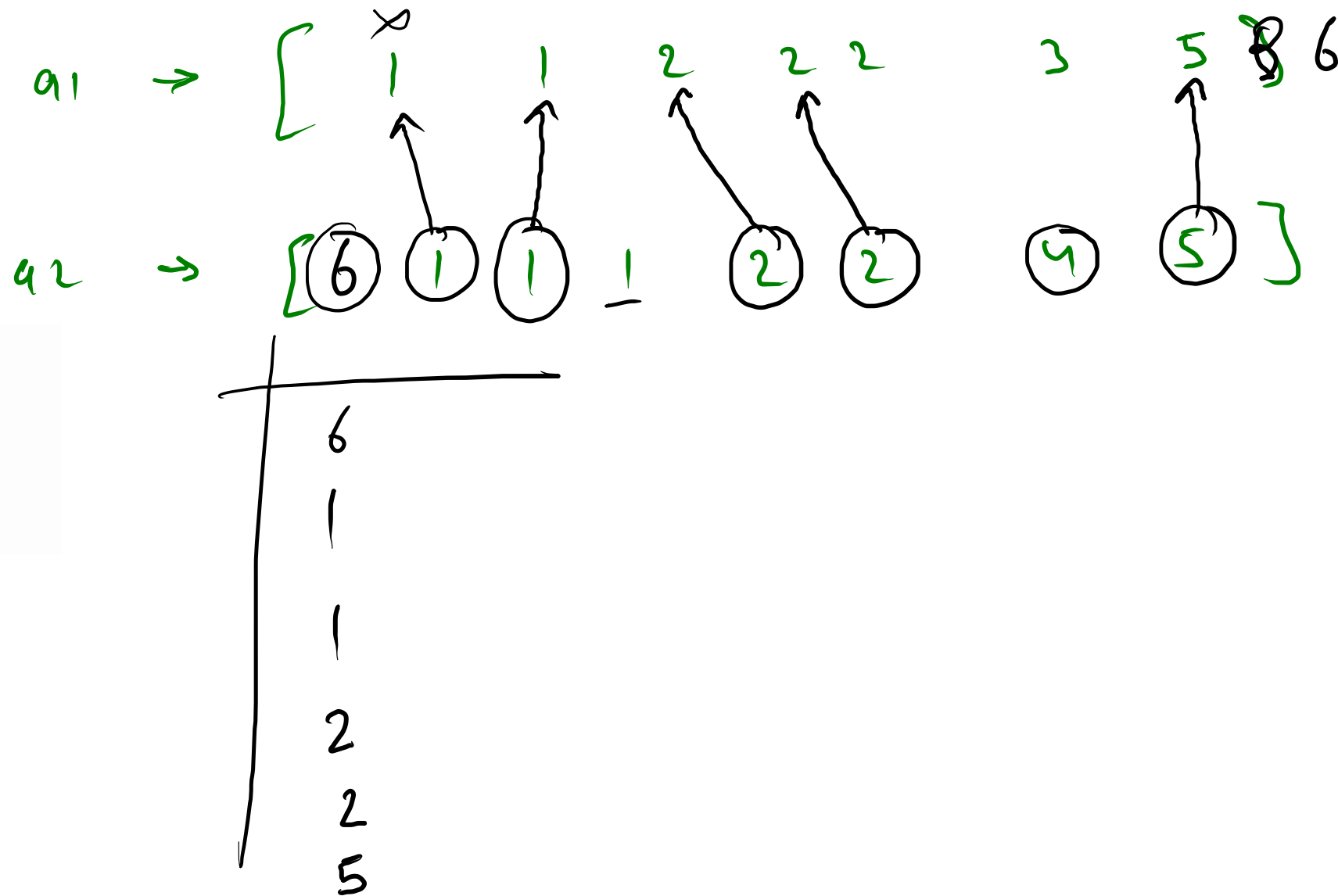
frequency

if a1 -> 1 1 2 2 2 3 5

and a2 -> 1 1 1 2 2 4 5

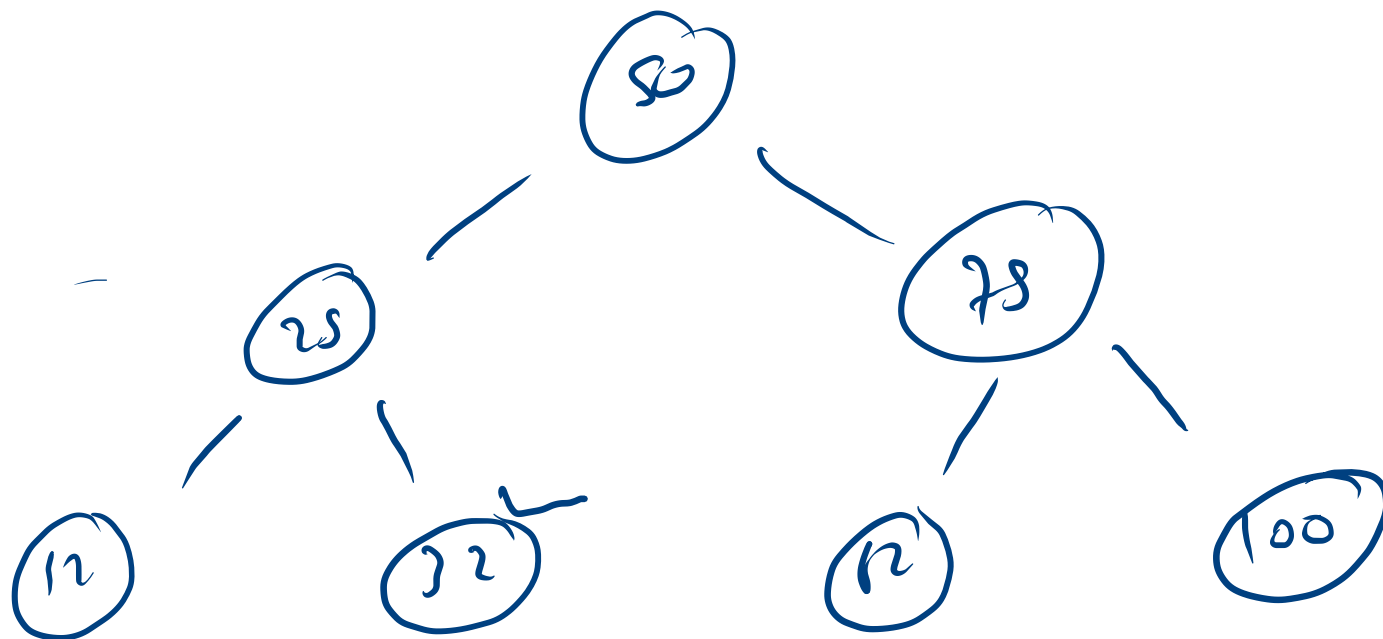
intersection is -> 1 1 2 2 5

Q2 -> or for



N.W.  
PIR

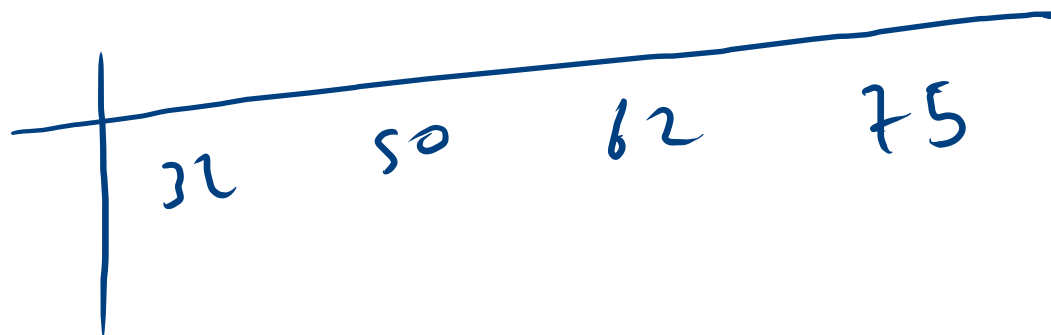
Ascending order



low  $\rightarrow$  32

high  $\rightarrow$  75

[32, 75]  $\rightarrow$



5	7	8	9	10	11
---	---	---	---	----	----

$$n = 6$$

$$\log(6)$$

	5	7	8	9	10	11
i				j		

$$\log(4)$$

[ a, b, c, d, e, f, g ...  
           ↑  ↑  ↑  ↑

(n)

```
for( int val : arr) {
    pq.add(val);
```

```
    if( pq.size() > k)
        pq.remove();
}
```

k=4

log(1)

log(2)

log(3)

log(4)

log(5)

log(5)

all

rem

log(5)

log(5)

log(5)

log(5)

≈ log(k)

$$\boxed{l(1) + l(2) + \dots + l(k)} \neq l(k) + l(k) + l(k) + \dots$$

$$\sim \sqrt{n(\log(k))}$$

a
b
c
d