

[10 20 30 40 50]

[~~5~~ ~~4~~ ~~9~~ 11 19 55 57]

[~~1~~ ~~2~~ ~~3~~] *

[32 39]

[1 2 3 5 8 9]

$k \rightarrow 4$

$$[\overset{\bullet}{10} \quad 20 \quad 30 \quad 40 \quad 50]$$

k

$$[\overset{\bullet}{5} \quad 7 \quad 9 \quad 11 \quad 19 \quad 55 \quad 57]$$

$\theta(h, k)$

$$[\cancel{10} \quad \cancel{12} \quad \cancel{13}]$$

$$[\overset{\bullet}{32} \quad 39]$$

$$[\quad 1 \quad 2 \quad 3 \quad]$$

[10 20 30 40 50]

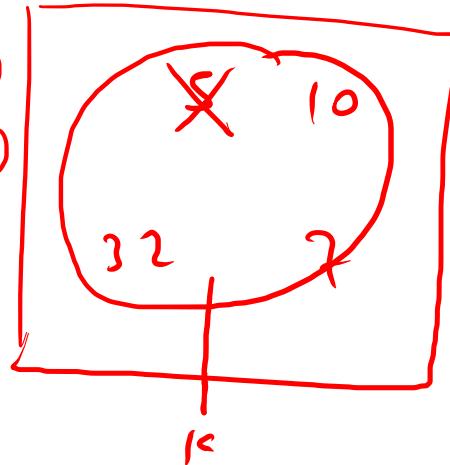
[5 7 9 11 19 55 57]

→ [1 2 3]

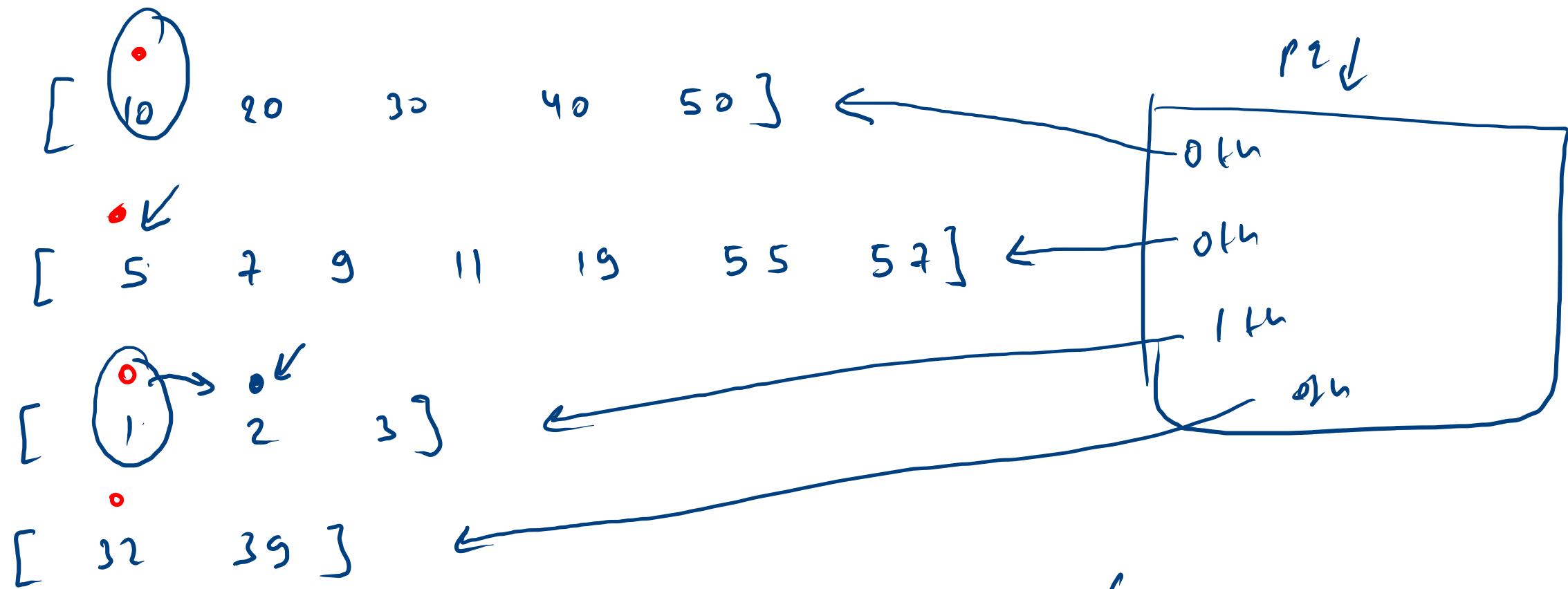
[32 39]

$\log(k)$

$a \propto \log(k)$
remove $\log(k)$



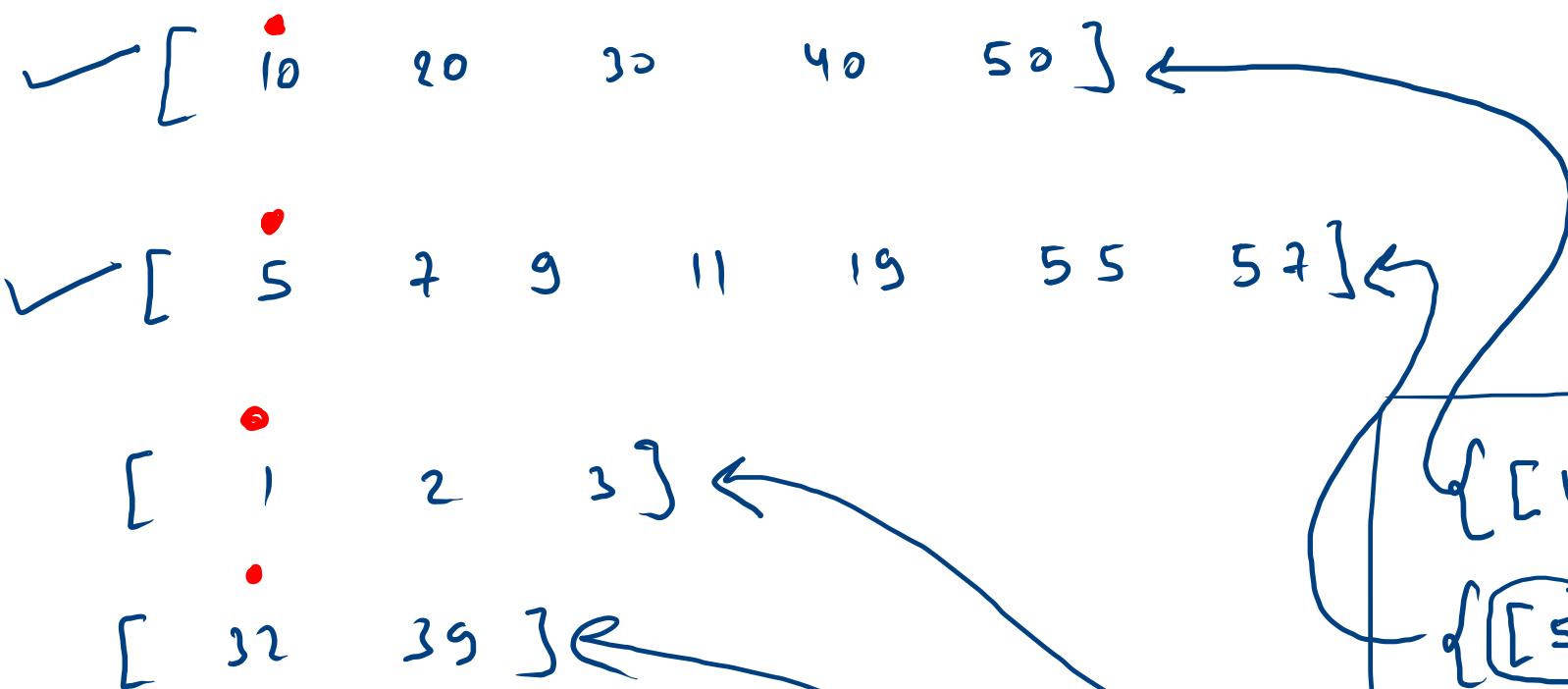
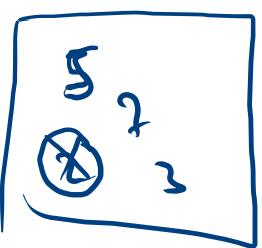
[1 2 3 5]



pair L
 Array1,32
 int idx

3

min



```
PriorityQueue<Pair> pq = new PriorityQueue<Pair>();  
for(ArrayList<Integer> inner: lists){  
    Pair p = new Pair(inner, 0);  
    pq.add(p);  
}
```

p : { [1, 2, 3], 0 }

[10 20 30 40 50] ←

[5 7 9 11 19 55 57] ←

[1 2 3] ←

[32 39] ←

```
while(pq.size() > 0){  
    pair p = pq.remove();  
    int val = p.list.get(p.idx);  
    rv.add(val);  
  
    p.idx++;  
    if(p.idx < p.list.size()) {  
        pq.add(p);  
    }  
}
```

{ [10 20 ... 50], 6 }

{ [5 7 ... 57], 0 }

{ [1, 2, 3], 1 }

{ [32, 39], 0 }

p =

```

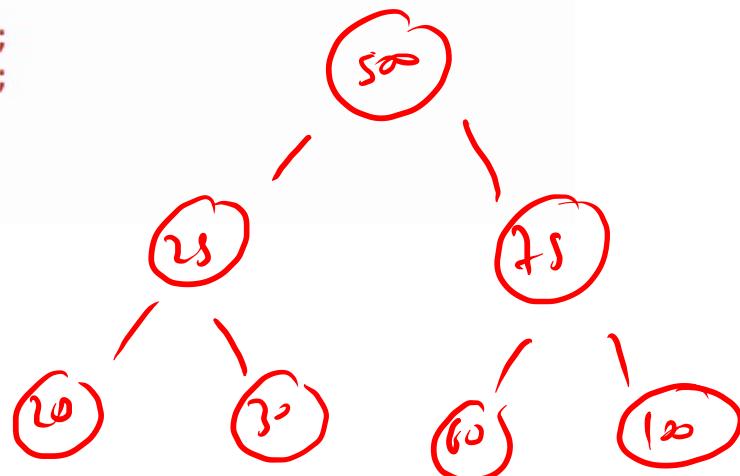
public static class Pair implements Comparable<Pair> {
    ArrayList<Integer> list;
    int idx;
    Pair(ArrayList<Integer> l, int i){
        list = l;
        idx = i;
    }

    public int compareTo(Pair b){
        Pair a = this;

        int x = a.list.get(a.idx);
        int y = b.list.get(b.idx);

        if(x < y) return -1;
        if(x > y) return +1;
        return 0;
    }
}

```



```

public static ArrayList<Integer> mergeKSortedLists(ArrayList<ArrayList<Integer>> lists) {
    ArrayList<Integer> rv = new ArrayList<Integer>();
    PriorityQueue<Pair> pq = new PriorityQueue<Pair>();

    for(ArrayList<Integer> inner: lists){
        Pair p = new Pair(inner, 0);
        pq.add(p);
    }

    while(pq.size() > 0){
        Pair p = pq.remove();
        int val = p.list.get(p.idx);
        rv.add(val);

        p.idx++;
        if(p.idx < p.list.size()){
            pq.add(p);
        }
    }

    return rv;
}

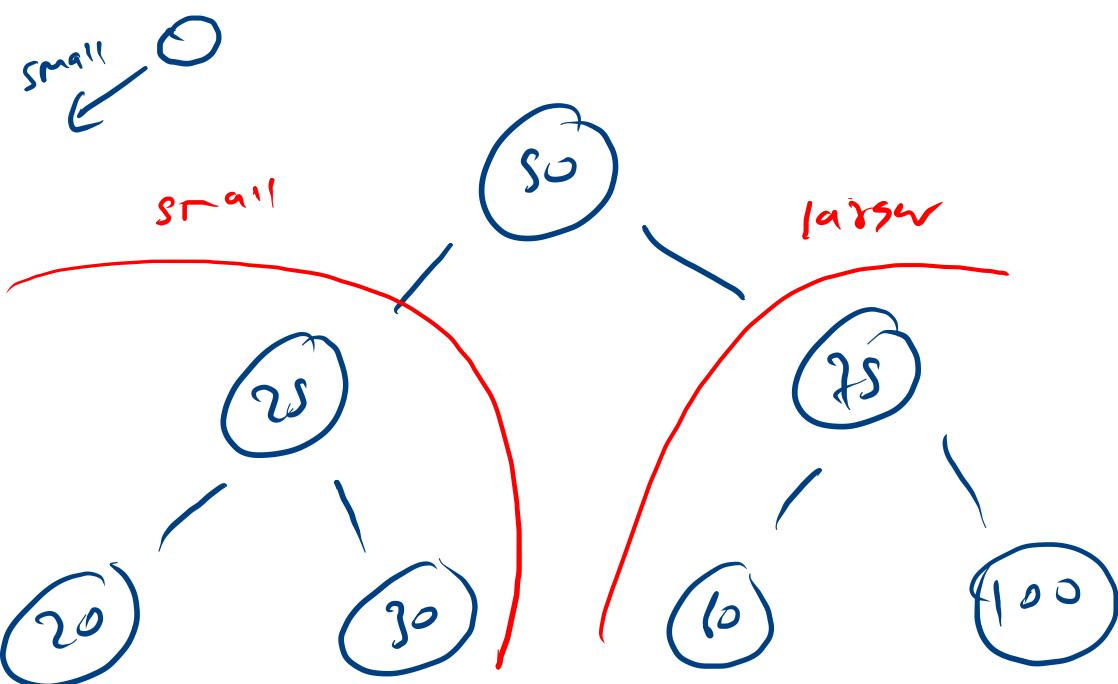
```

PQ → Priority Queue

		✓
add	$O(1)$	$\log(n)$
remove	$O(n)$	$\log(n)$
peek	$O(n)$	$\log(n)$
size		

$n \log(n)$ [$\text{for } (\text{int } val : ar) \leftarrow O(n)$
 $\quad pq.\text{add}(val)$]

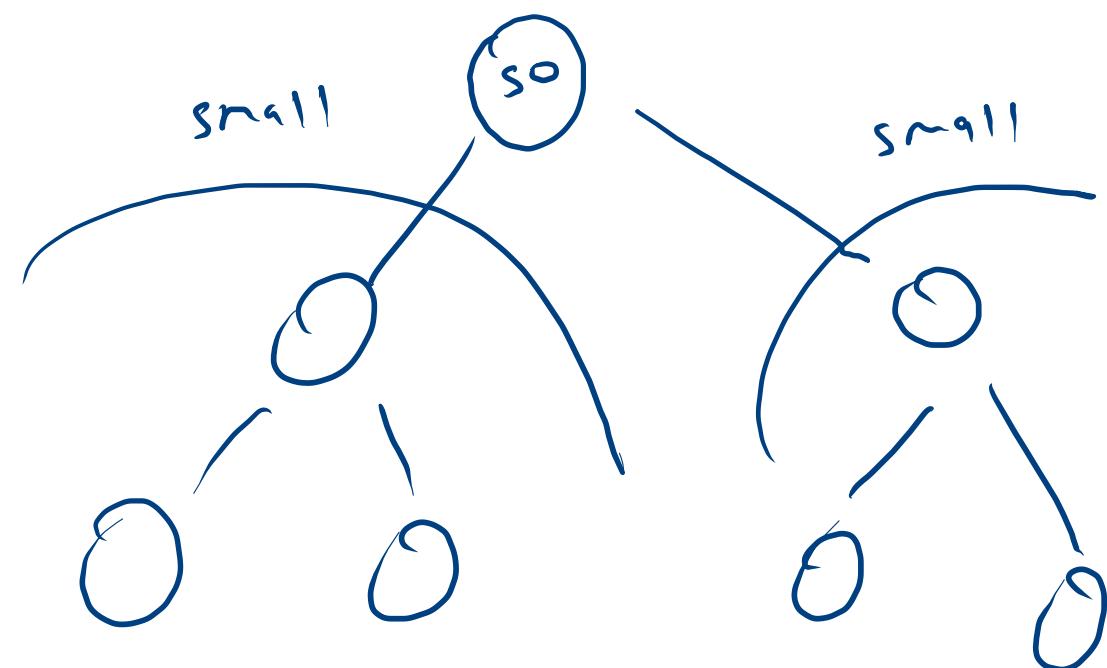
$n \log(n)$ [$\text{while } (pq.\text{size}() > 0)$
 $\quad \text{print } (pq.\text{peek}())$
 $\quad \text{print } (pq.\text{remove})$] $O(n^2)$



$\text{add} \rightarrow \log(n)$

$\text{remove} \rightarrow \log(n)$

$\text{pick} \rightarrow \log(n)$



$\text{add} \rightarrow ?$

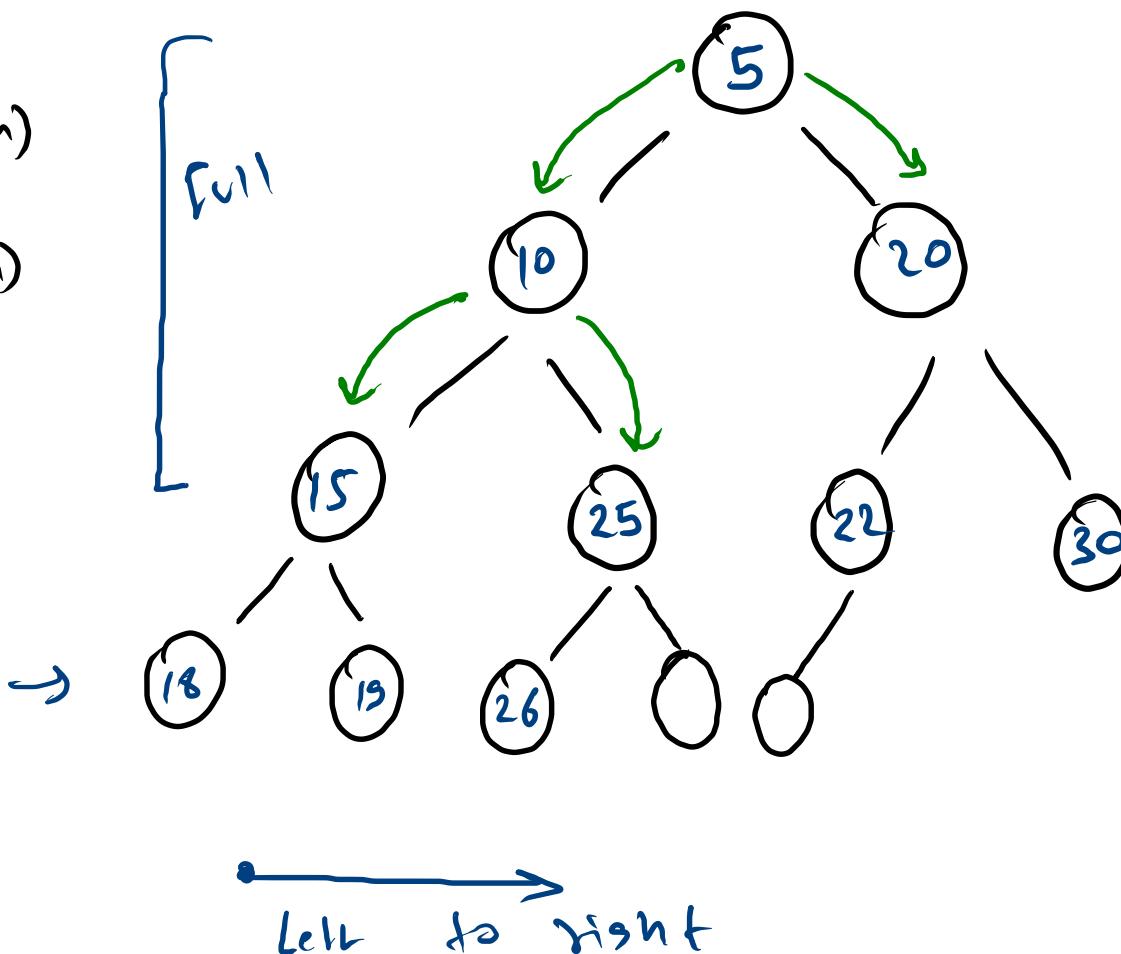
$\text{remove} \rightarrow ?$

$\text{pick} \rightarrow O(1)$

Heap \rightarrow min priority

add $\log(n)$
remove $\log(n)$

peek $O(1)$

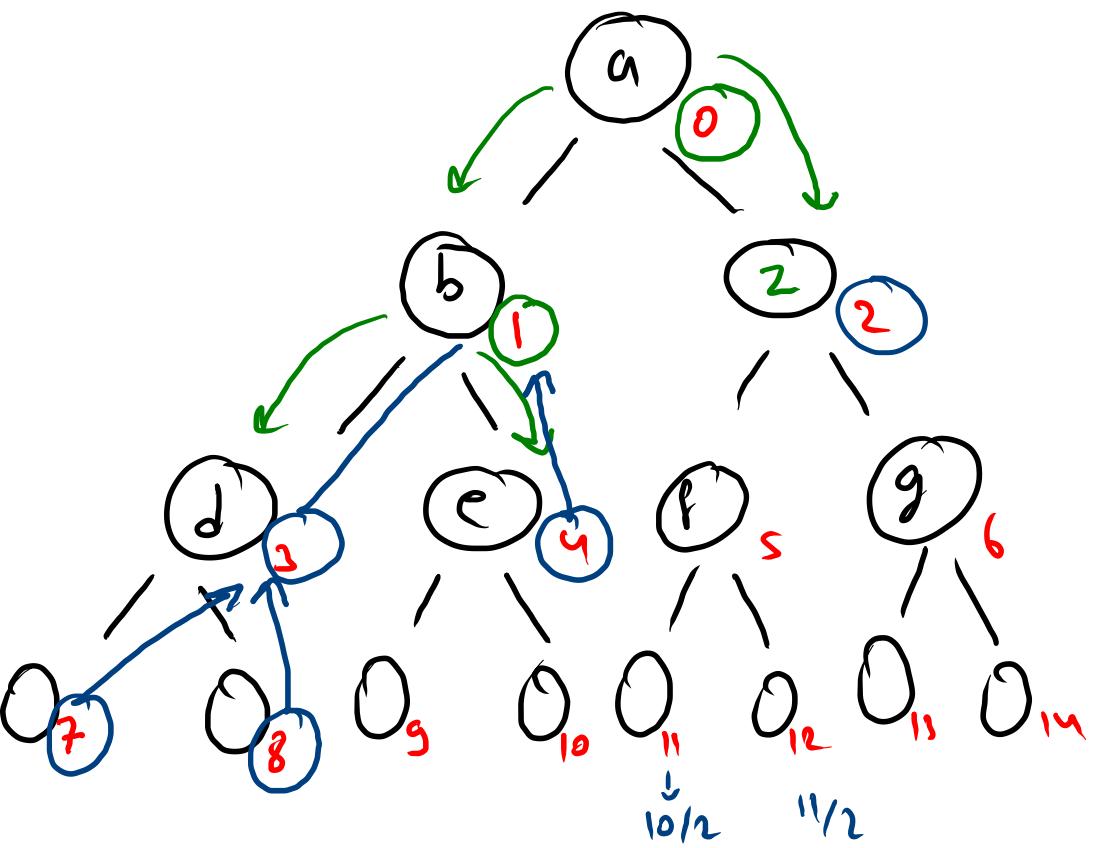


property

- NOP \rightarrow peek
- CBT \rightarrow add, remove

[a , b , 2 , ↓ , e , f , g]

0 → 0 → 0 → 0



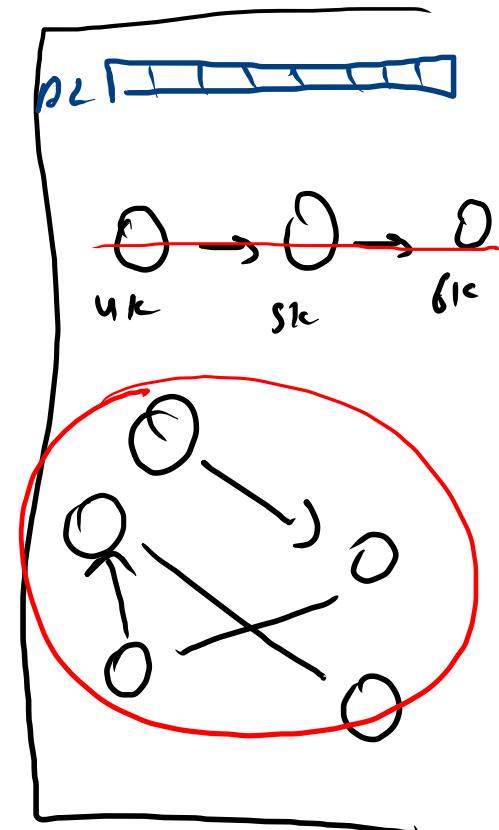
p_i

left $\rightarrow p_i * 2 + 1$

right $\rightarrow p_i * 2 + 2$

i

parent $\rightarrow (i-1)/2$



$$\frac{32}{32} \quad 1 \rightarrow 2^0$$

$$\frac{32}{16} \quad 2 \rightarrow 2^1$$

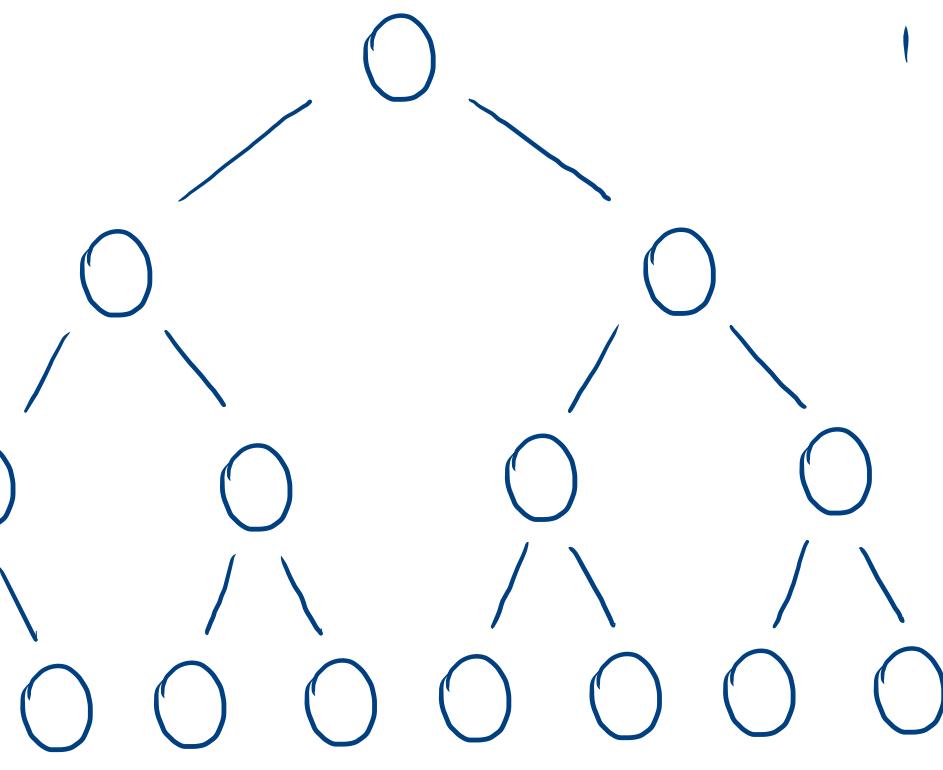
$$\frac{32}{8} \quad 4 \rightarrow 2^2$$

$$\frac{32}{4} \quad 8 \rightarrow 2^3$$

$$\frac{32}{2} \quad 16$$

$$\frac{32}{1} \quad n$$

$$2^m$$



$$\frac{32}{1}$$

$$\boxed{\begin{array}{ccccccc} 32 & & 32 & & 32 & & \\ \hline & 2 & & 4 & & 8 & \\ & \downarrow & & \downarrow & & \downarrow & \\ & 1 & & 1 & & 1 & \\ & & \dots & & & & \end{array}}$$

32

$$n \rightarrow 2^n$$

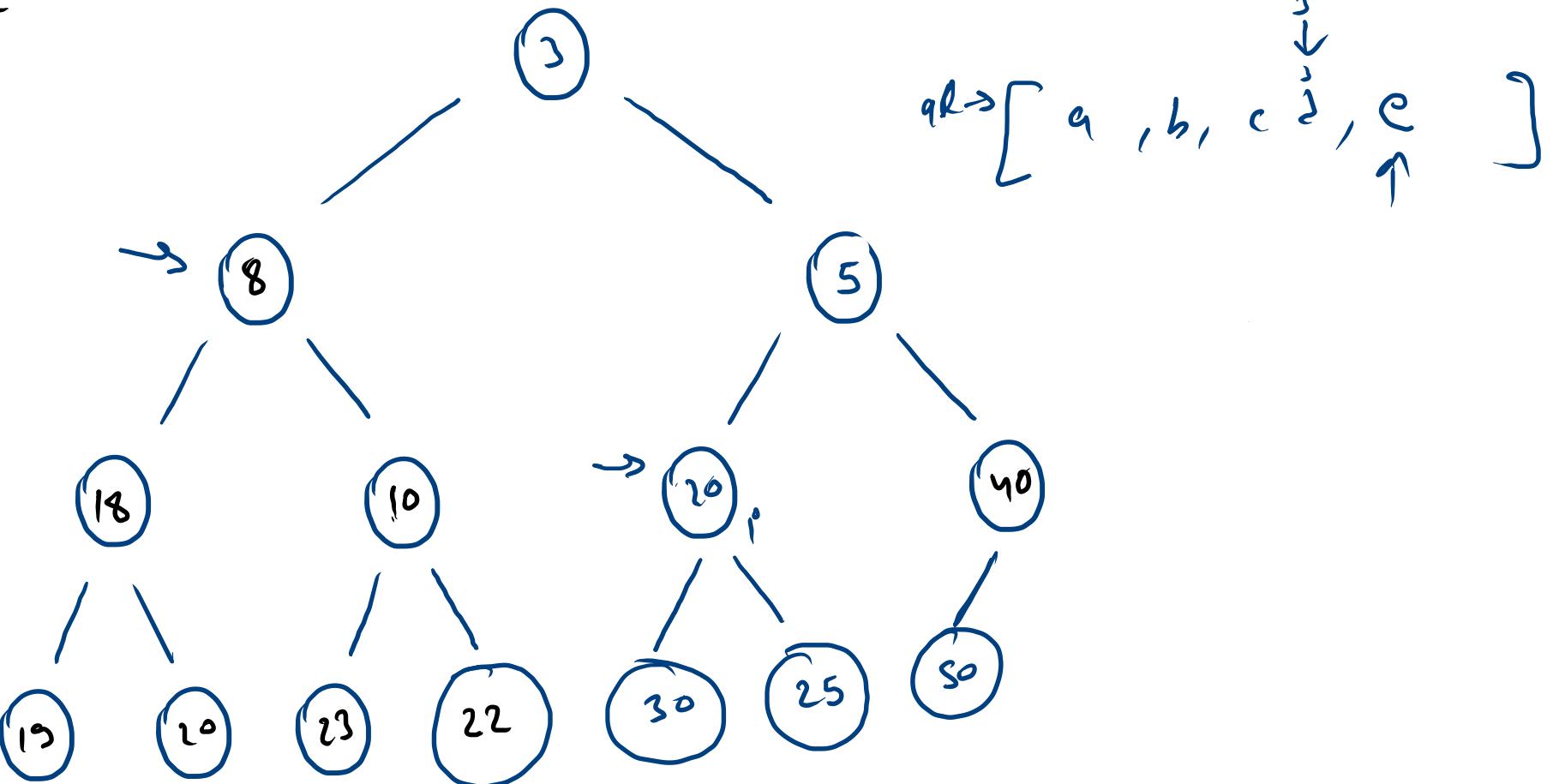
$$2^m = n$$

$$m = \log_2(n)$$

min → max

NO P

a↓↓
a↓↓
8
25



CDF

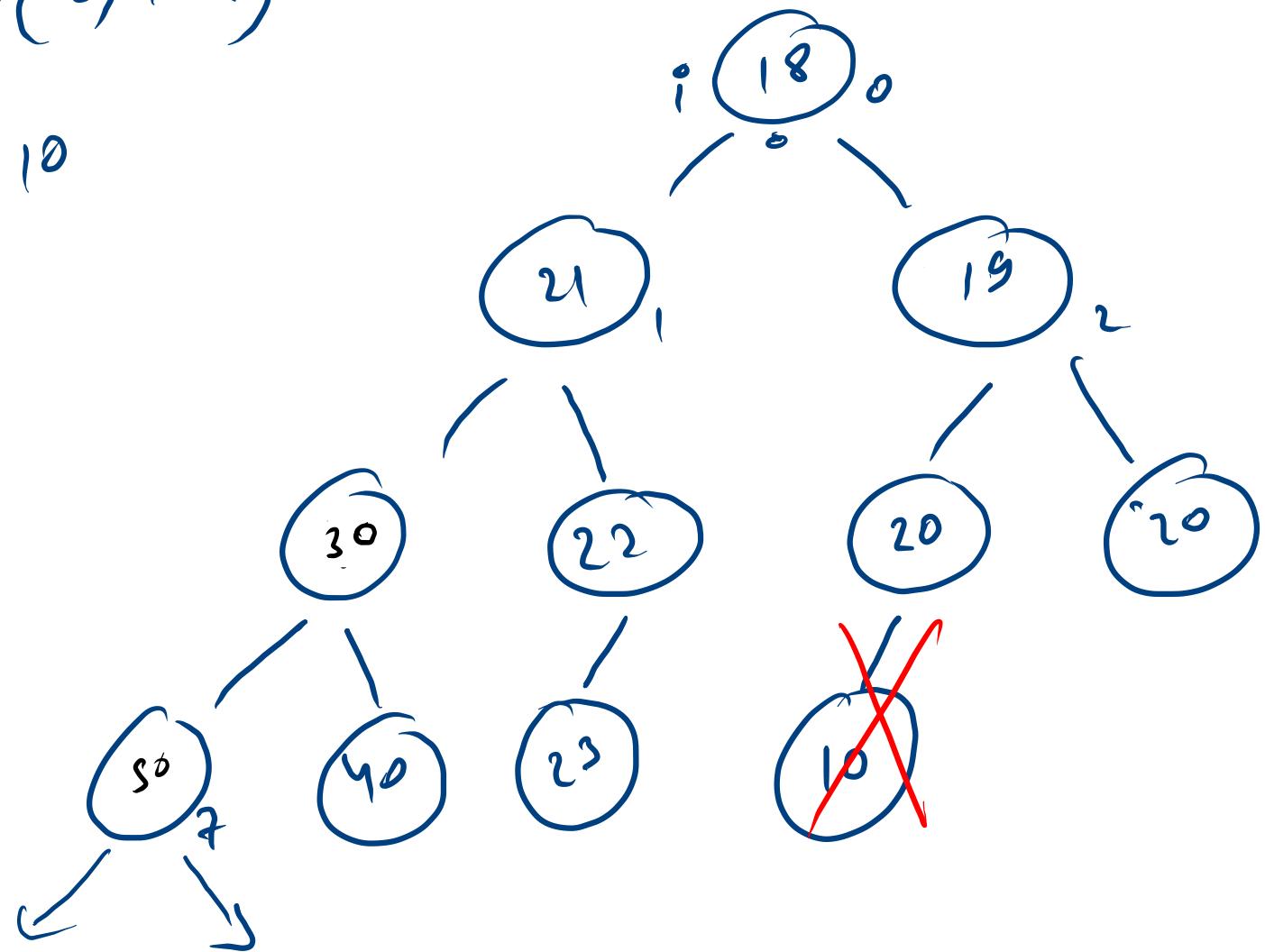
[3 , 8, 5 , 18, 10, 20, 40, 15, 20, 23, 22, 30, 25, 50]

~~remove~~

swap(0, last)

val = 10

~~remove()~~



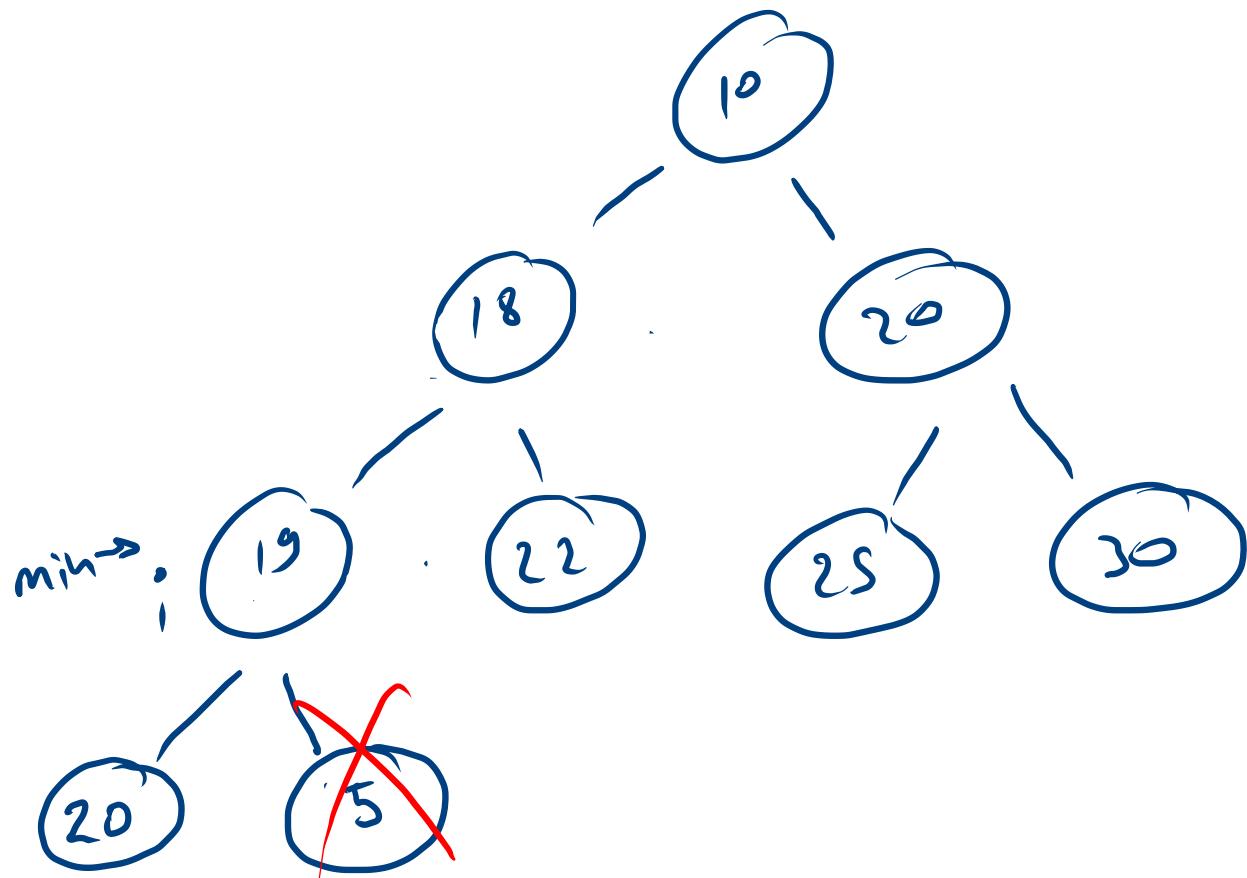
down heapify

NOP

(BT)

dornheaps

val = 5



\cancel{O}	pvt	get	contains	remove	keyset	size
\checkmark	pvt	null	false	null		0
	Update	value	true	value		val
TC.	$\rightarrow O(1)$	$O(1)$	$O(1)$	$O(1)$	$O(n)$	$O(1)$

key	value
India	10050
UK	25
US	20
Bangla	30

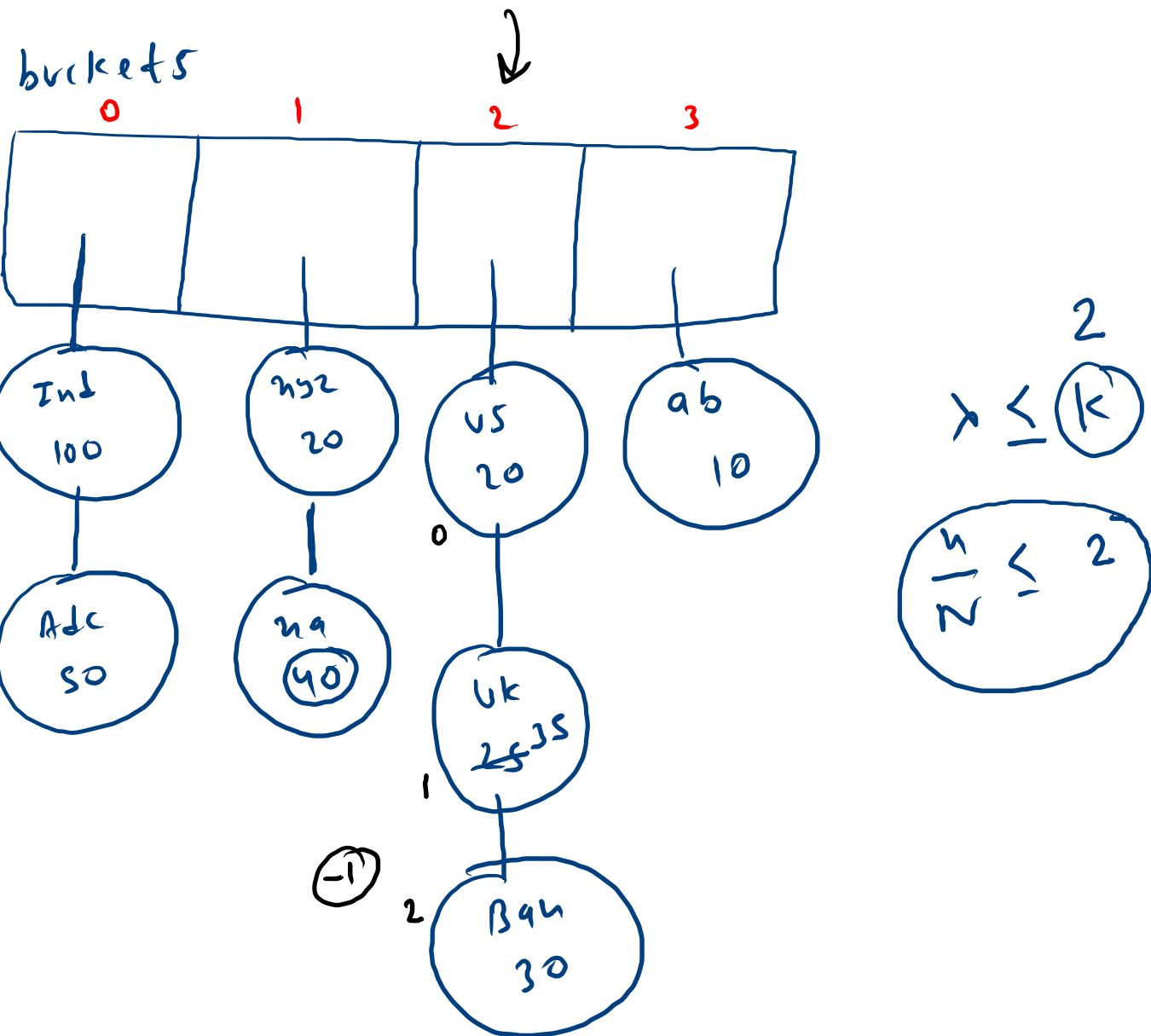
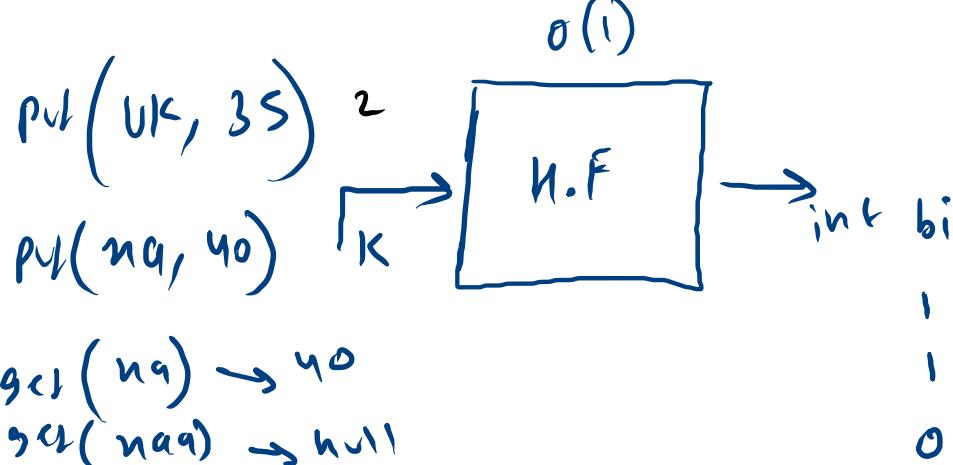
remove (vuk)

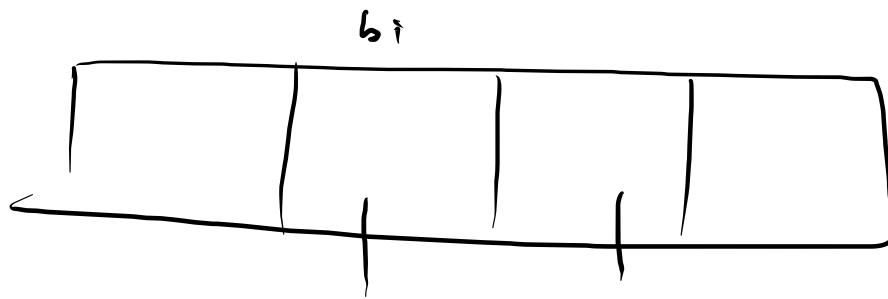
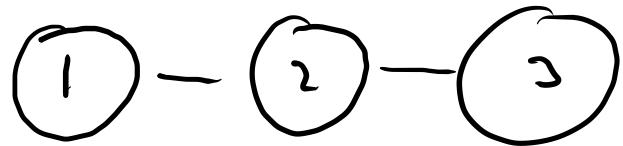
put
 get
 remove
 contains
 keys & size

$$n \rightarrow 8 \text{ size}$$

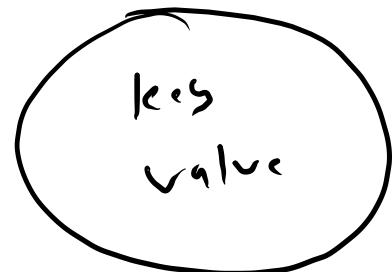
$$N \rightarrow 4$$

$$\lambda \rightarrow \frac{n}{N} \quad \frac{8}{4} = 2$$





HMNode

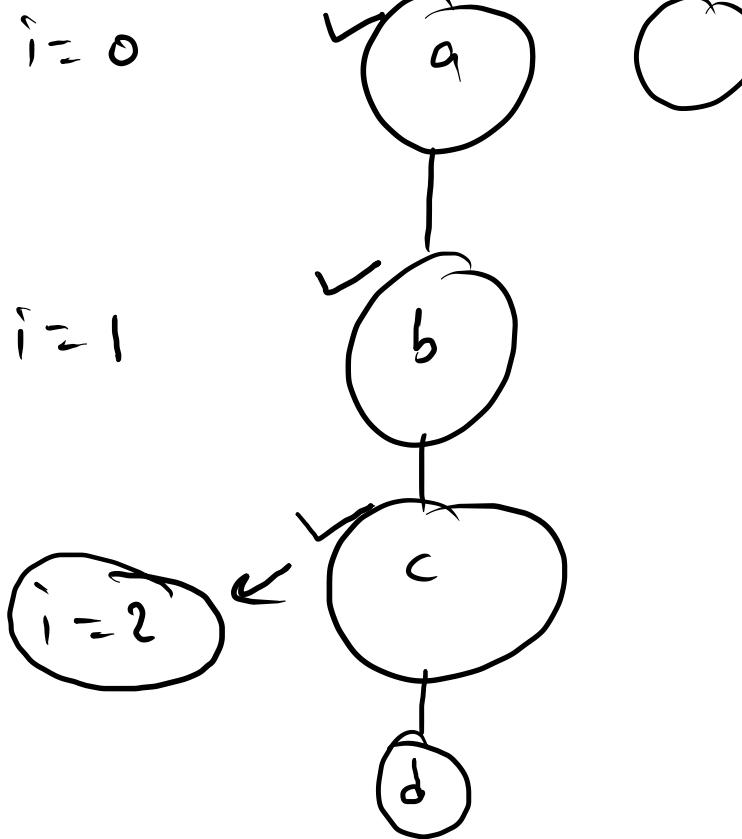


```

private int getKeyInBucket(int bi, K key){
    int i=0;
    for(HMNode node : buckets[bi]){
        if(key.equals(node.key)){// == problem
            return i;
        }
        i++;
    }
    return -1;
}
  
```

key = $\leftarrow 2$

key = $\downarrow \rightarrow -1$



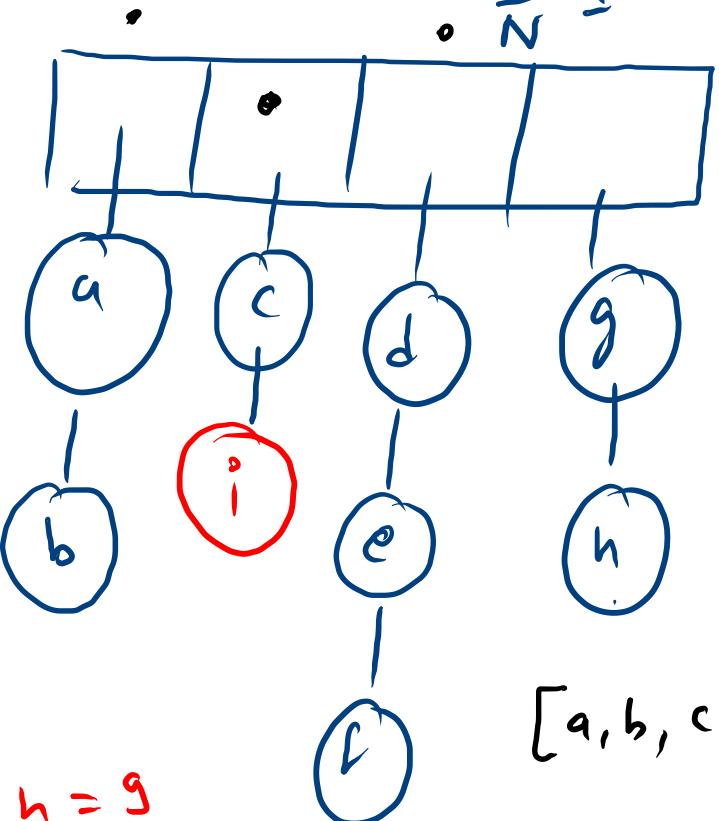
$$h = 8$$

$$N = 4$$

$$k = 2$$

$$\lambda \leq k$$

$$\frac{h}{N} \leq 2$$

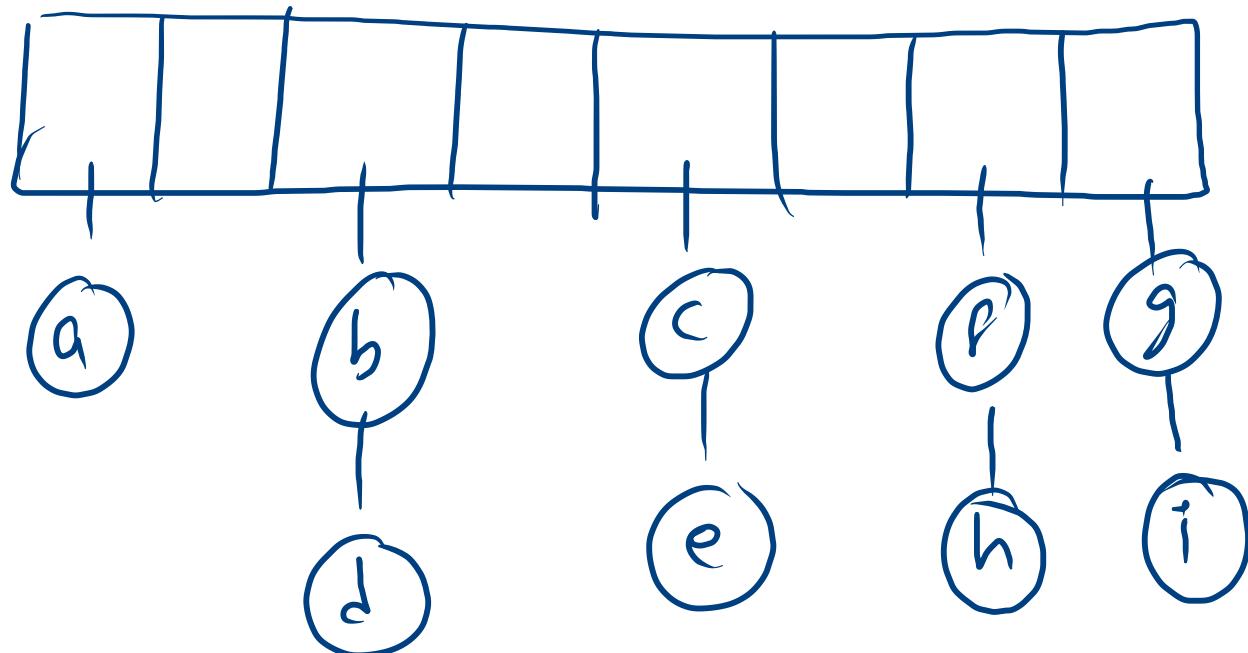


$$h = 9$$

$$N = 4$$

$$\frac{h}{N} = \frac{9}{4} = 2.25$$

$$\boxed{2.25 \leq 2}$$



$$h = 9$$

$$N = 8$$

$$\lambda = \frac{9}{8} = 1.125 \leq \frac{k}{2}$$

```
int hs = key.hash();
```

$$[-\infty, \infty]$$

```
hs = Math.abs(hs); // -2 → 2  
-3 → 3
```

$$[0, \infty]$$

```
hs = hs % buckets.length;
```

$$[0, \dots, (N-1)]$$

```
return hs;
```

$$\frac{95}{3} = 32$$

$$0 \dots 2$$

$$\frac{n}{N} \leq k$$

$$\frac{n}{N} > k \rightarrow \text{rehashing}$$

$$n > N \cdot k \rightarrow \text{size} > \text{buckets.length} / 2$$

