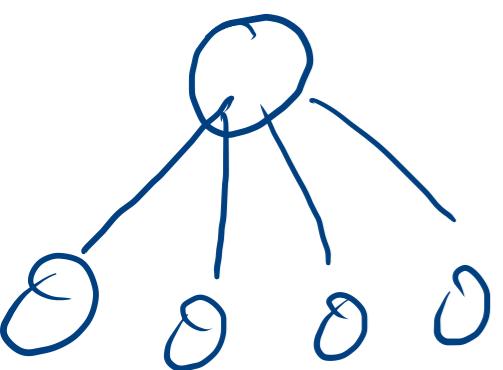
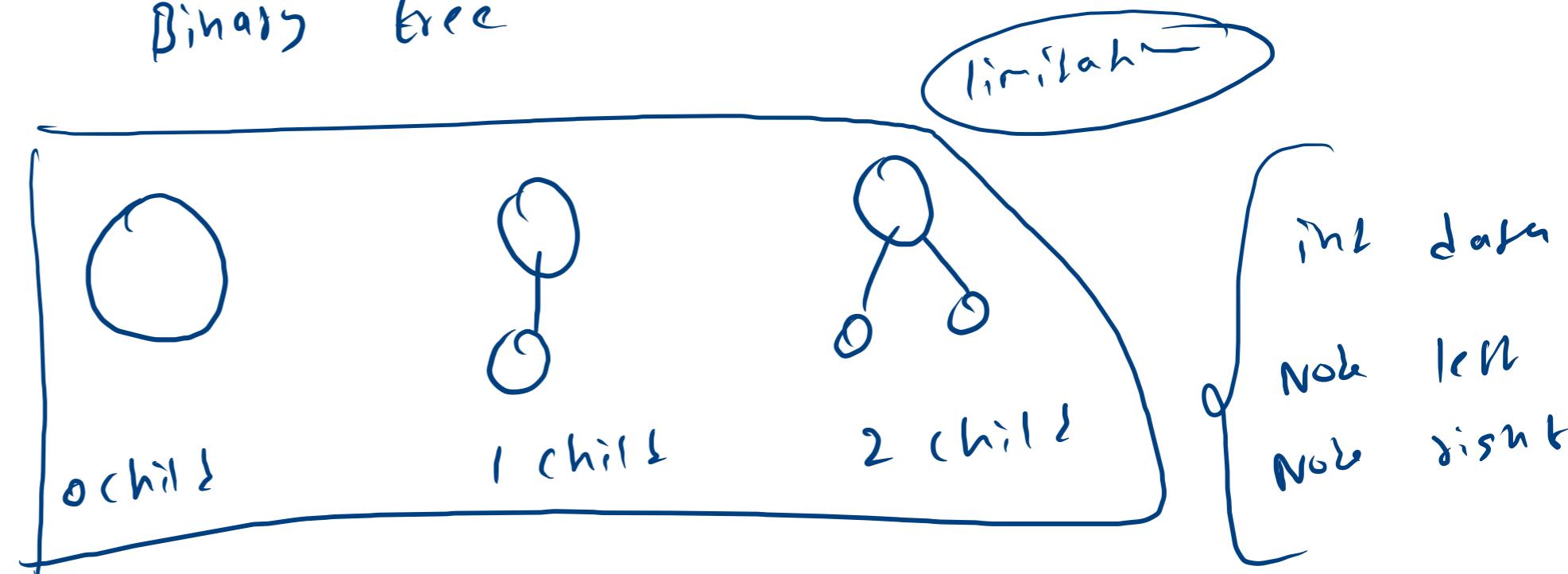


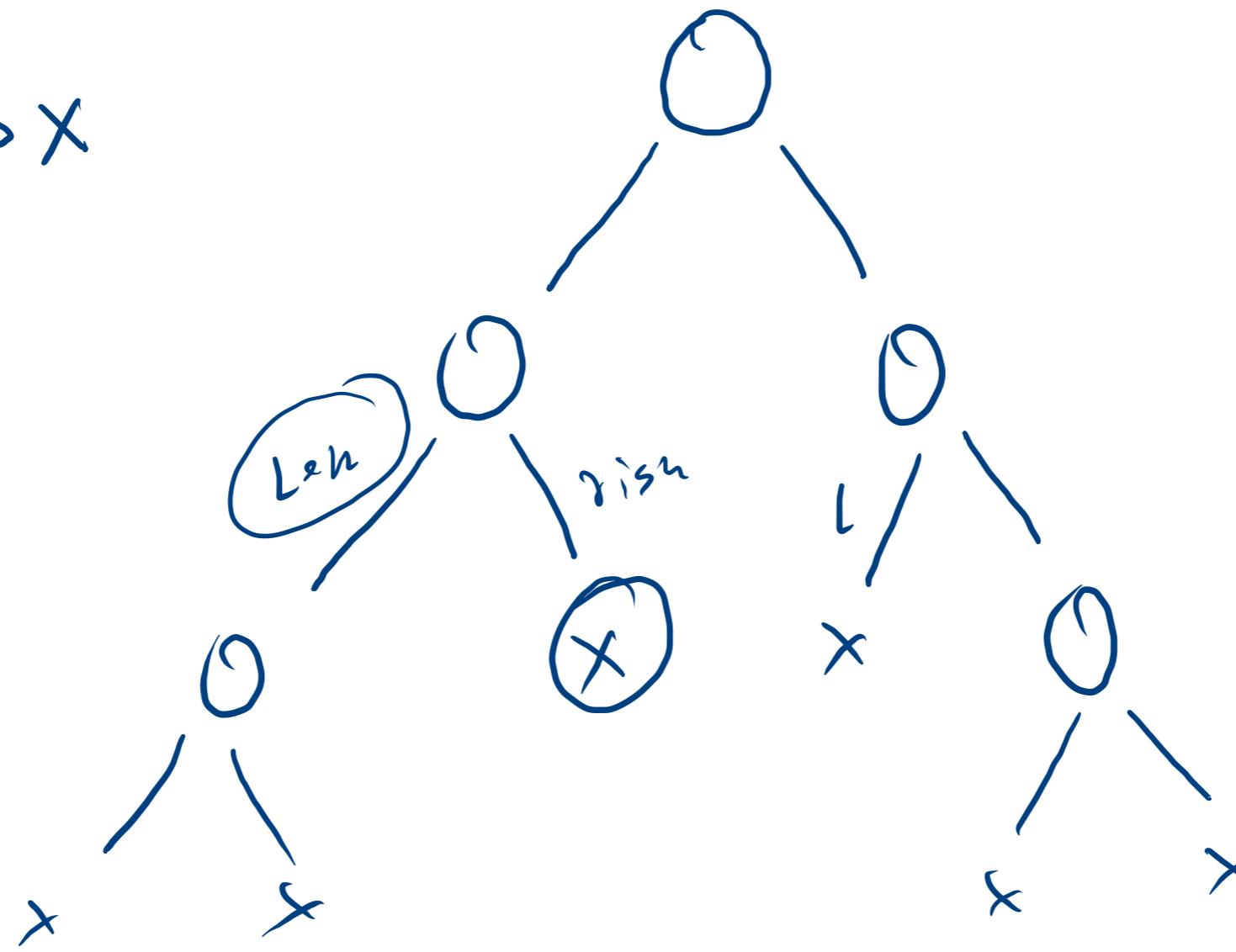
Binary tree

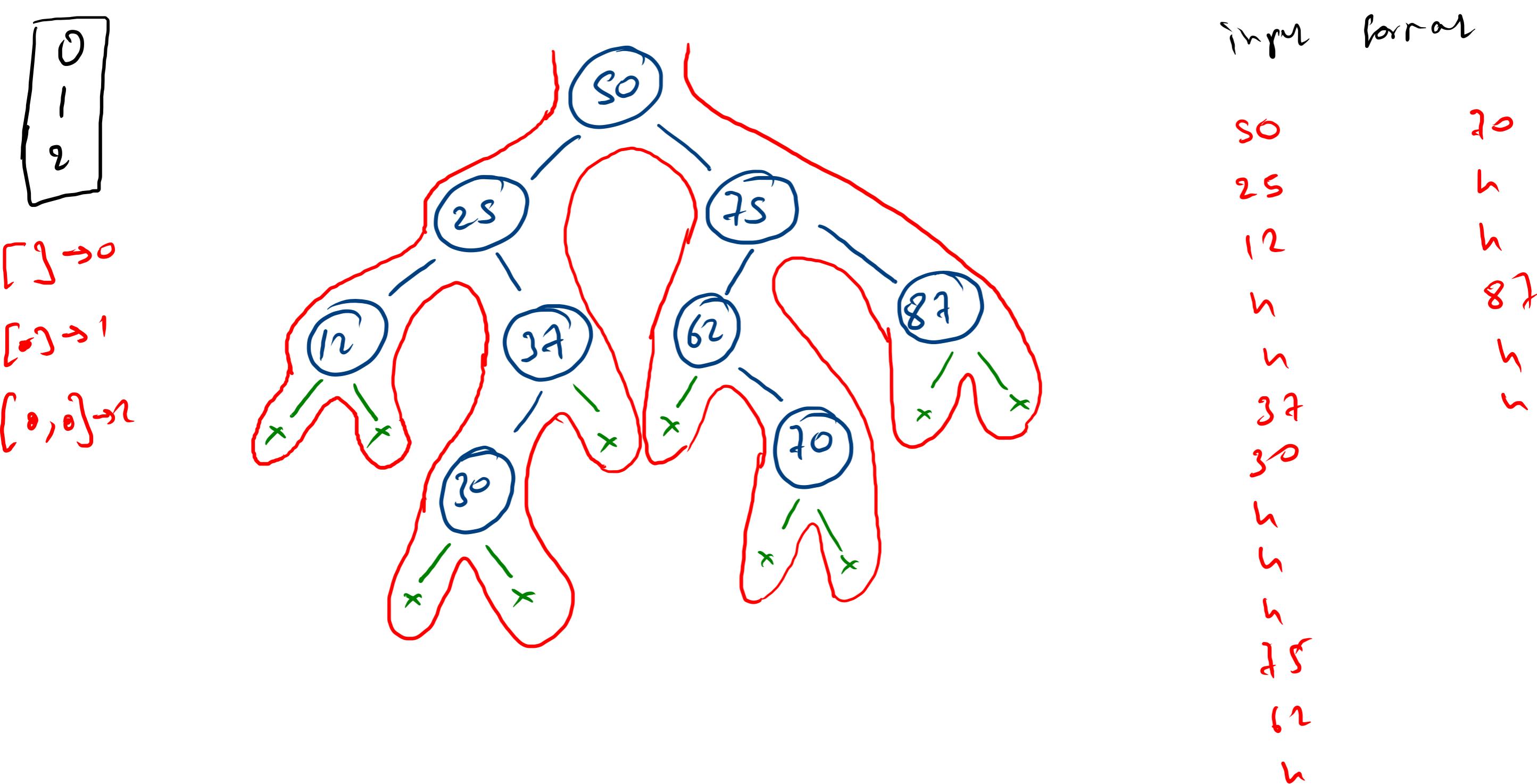
data
AL child



Node next

$\emptyset \rightarrow \emptyset \rightarrow \emptyset \rightarrow X$





$0 \rightarrow \text{left}$
 $1 \rightarrow \text{right}$

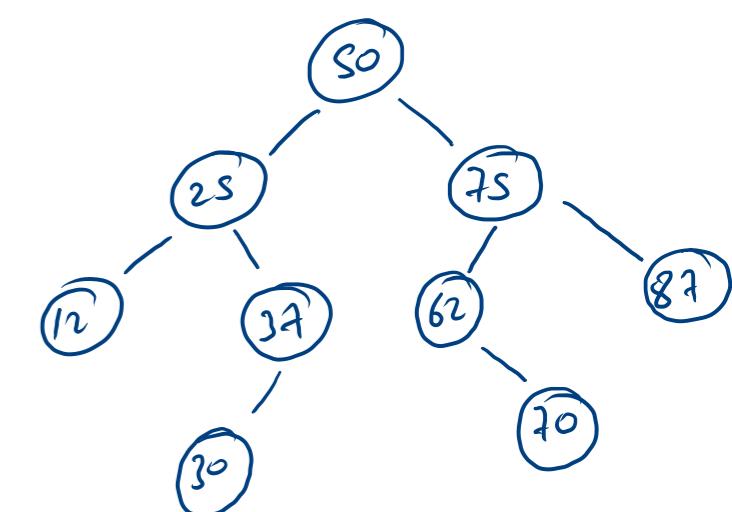
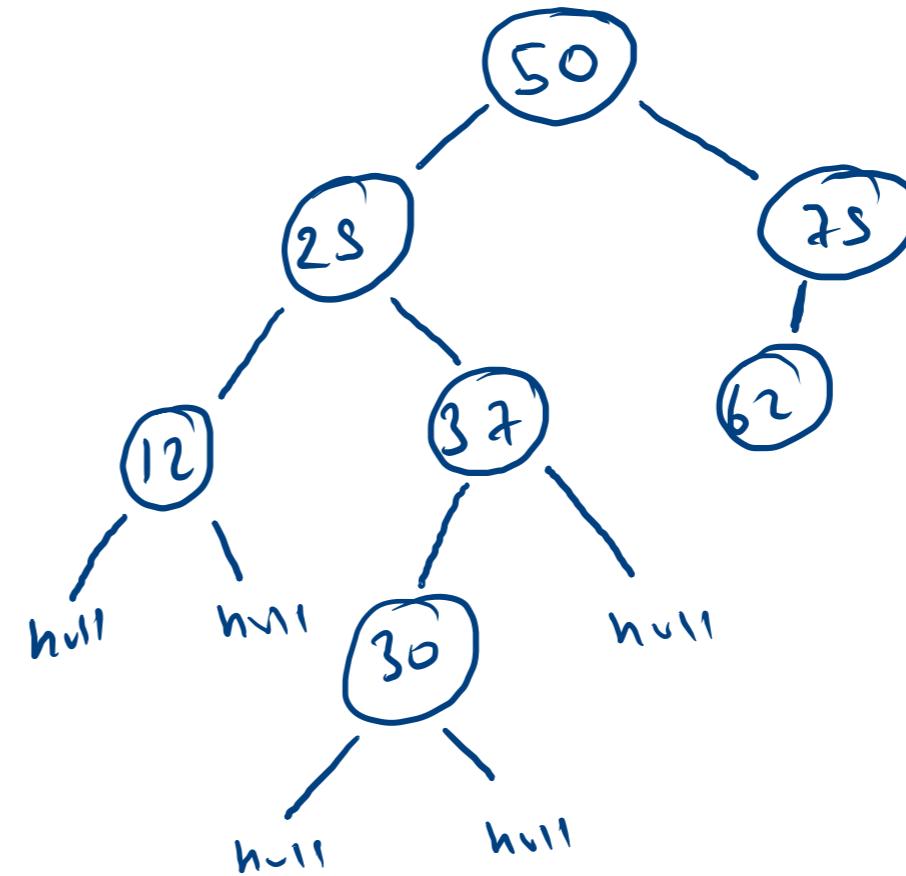
50 ←
 25 ←
 12 ←
 h ←
 h ← 87
 h ←
 37 ←
 30 ←
 h ←
 h ←
 h ← 25
 62 ←
 h ←

node = new Node

make node child or parent

if node != null push

62	0
25	0
37	1
25	1
50	1



```
• Stack<Pair> st = new Stack<>();  
• root = new Node(arr[0], null, null);  
int idx=1;  
• Pair p = new Pair(root, 0);  
• st.push(p);
```

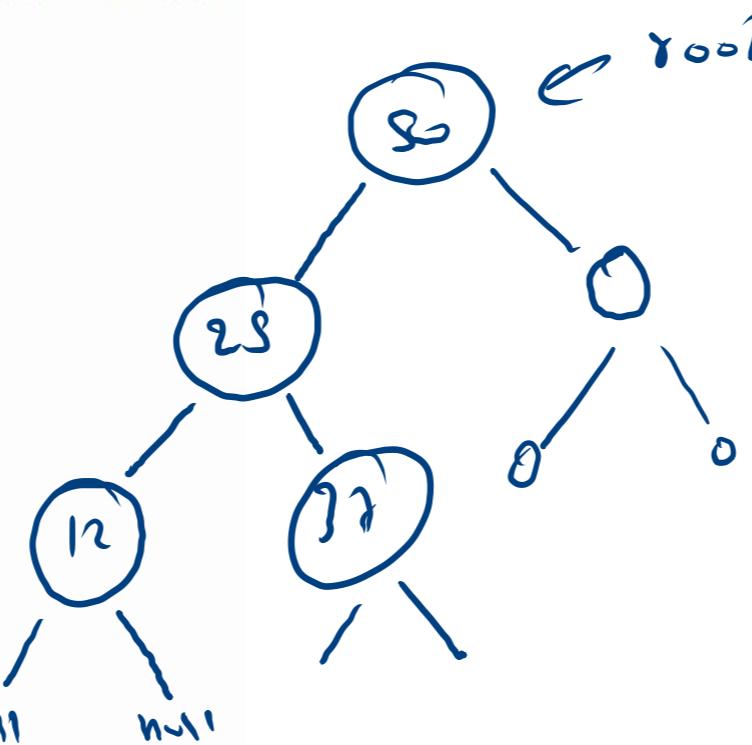
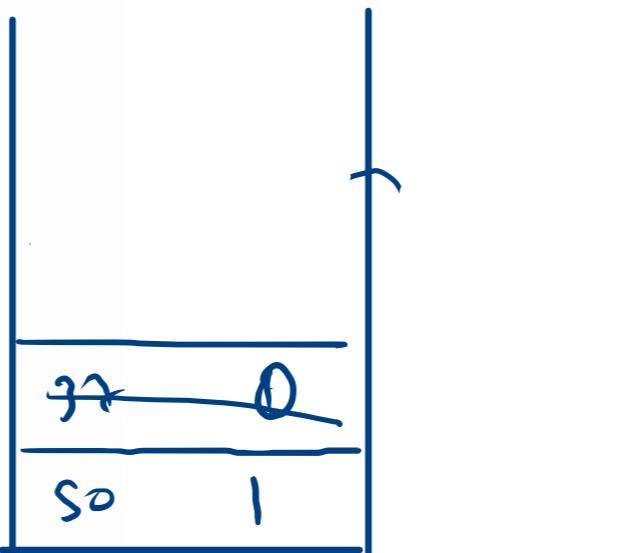
```

while(st.size() > 0){
    Node node;
    if(arr[idx] == null){
        node = null;
    }else{
        node = new Node(arr[idx], null, null);
    }
    idx++;

    Pair top = st.peek();
    if(top.status == 0){
        top.node.left = node;
        top.status = 1;
    }else{
        top.node.right = node;
        st.pop();
    }

    if(node != null){
        st.push(new Pair(node, 0)); null null
    }
}

```



```

public static void display(Node node){    lcv="25"    rcv="25"
    String left="";
    if(node.left == null){
        left = ".";
    }else{
        left = ""+node.left.data;
    }

    String right="";
    if(node.right == null){
        right = ".";
    }else{
        right = ""+node.right.data;
    }

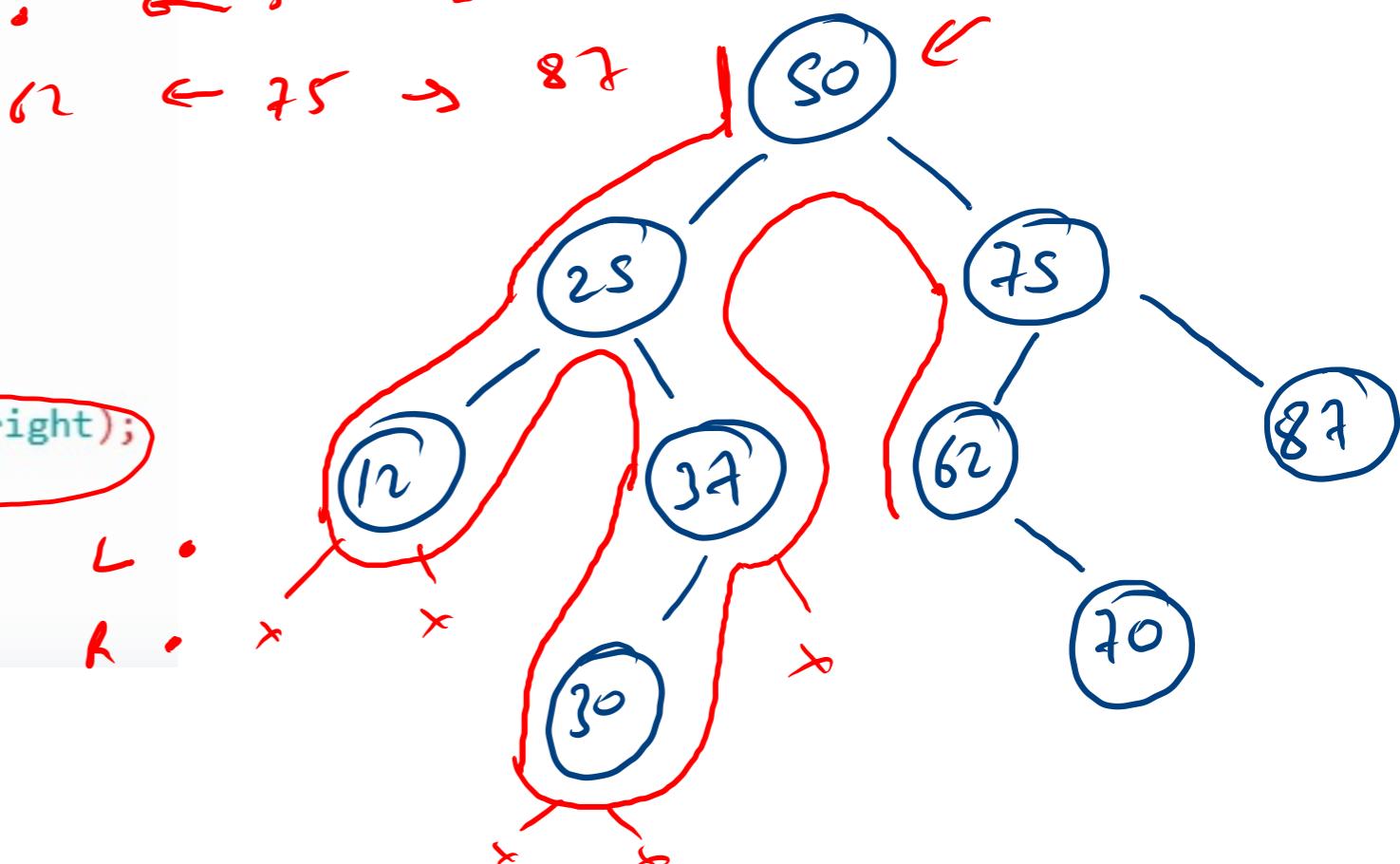
    System.out.println(left+" <- "+node.data+" -> "+ right);
    if(node.left != null)display(node.left);
    if(node.right != null)display(node.right);
}

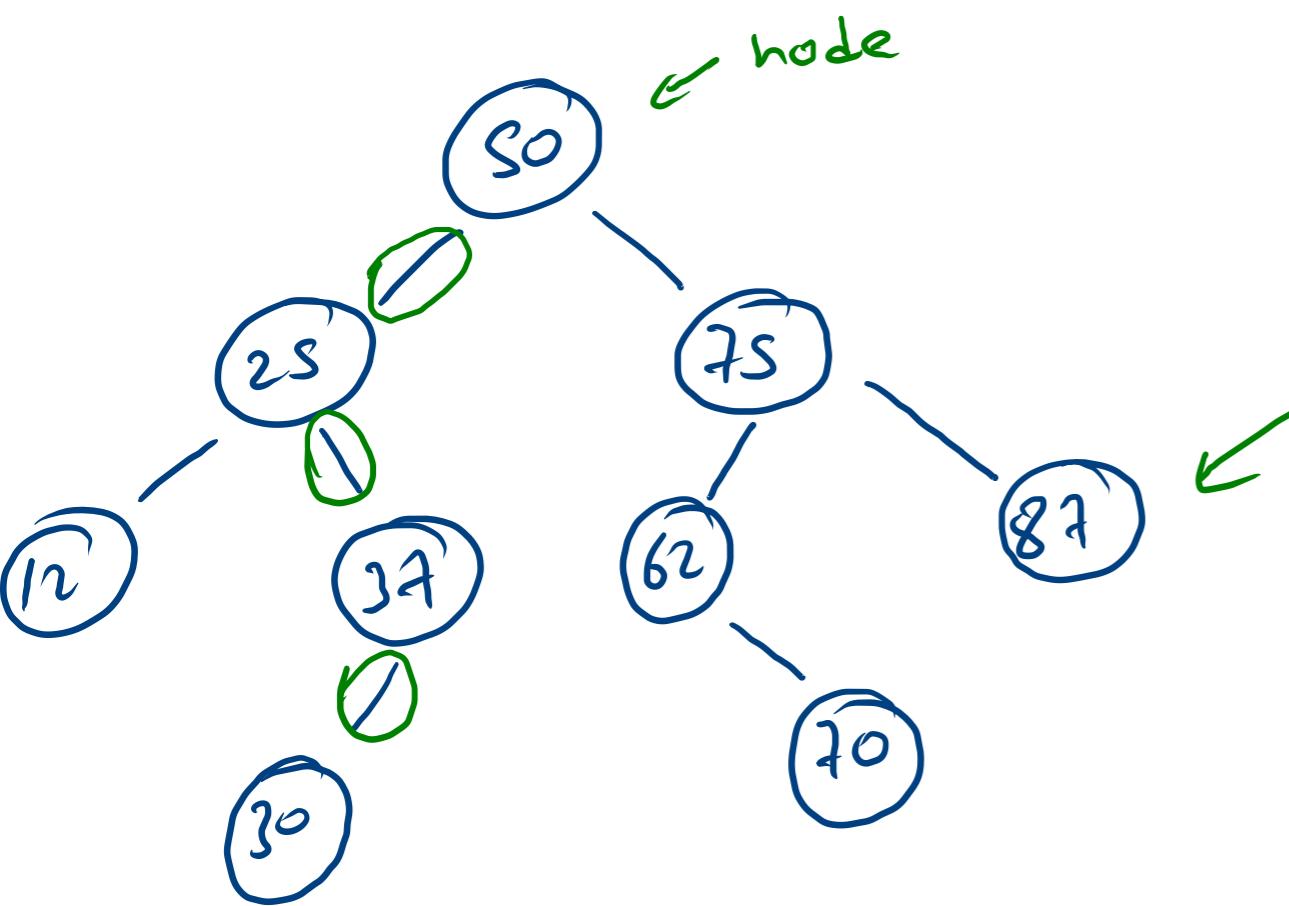
```

lcv="25"

rcv="25"

$25 \leftarrow s_0 \rightarrow 75$
 $12 \leftarrow 25 \rightarrow 37$
 $\cdot \leftarrow 12 \rightarrow \cdot$
 $30 \leftarrow 37 \rightarrow \cdot$
 $\cdot \leftarrow 30 \rightarrow \cdot$
 $62 \leftarrow 75 \rightarrow 87$





Size → 5
 sum → $12 + 25 + 70 + 10 + 62 + 87 = 270$
 max → 87
 height → 3

call(node.height)

Left
 right
 call(left)
 call(right)

$$l+1=2$$

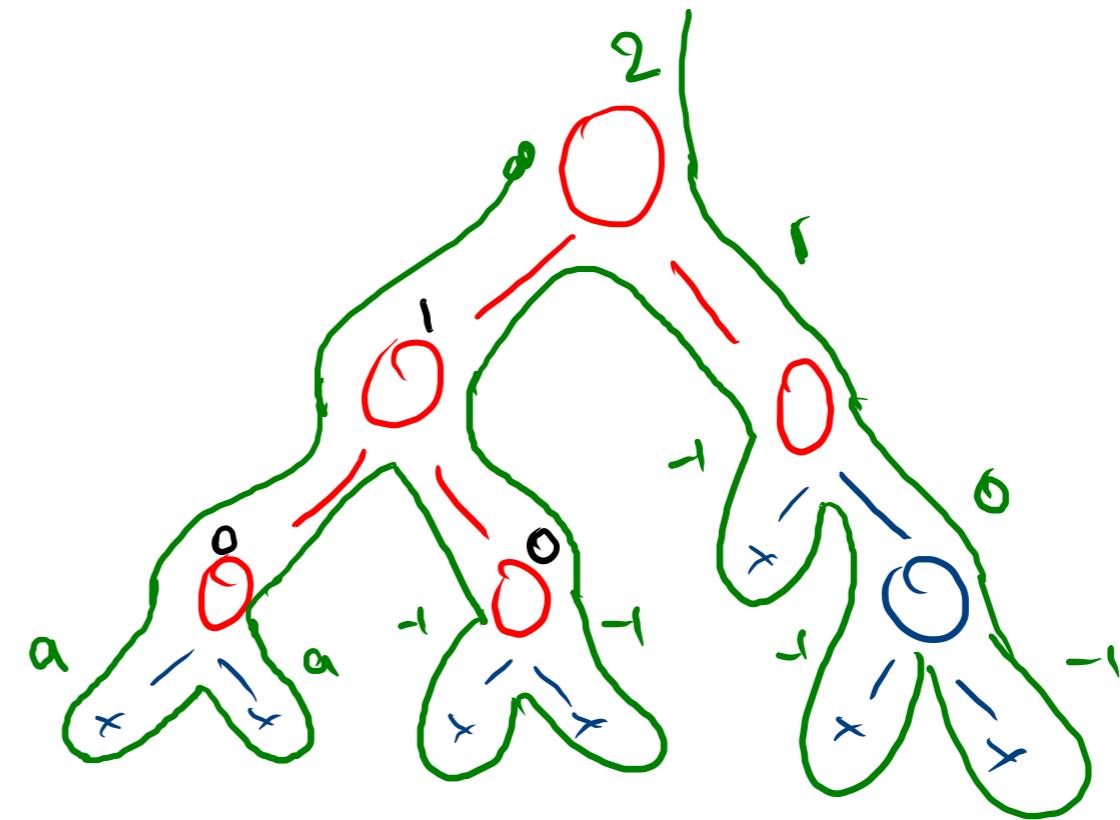
$$0+l=1$$

$$-1+l=0$$

0+1

```
public static int height(Node node) {  
    if(node == null){  
        return ???; a, -1  
    }  
    int lh = height(node.left);  
    int rh = height(node.right);  
    return Math.max(0, 0)+1;  
}
```

-1+1

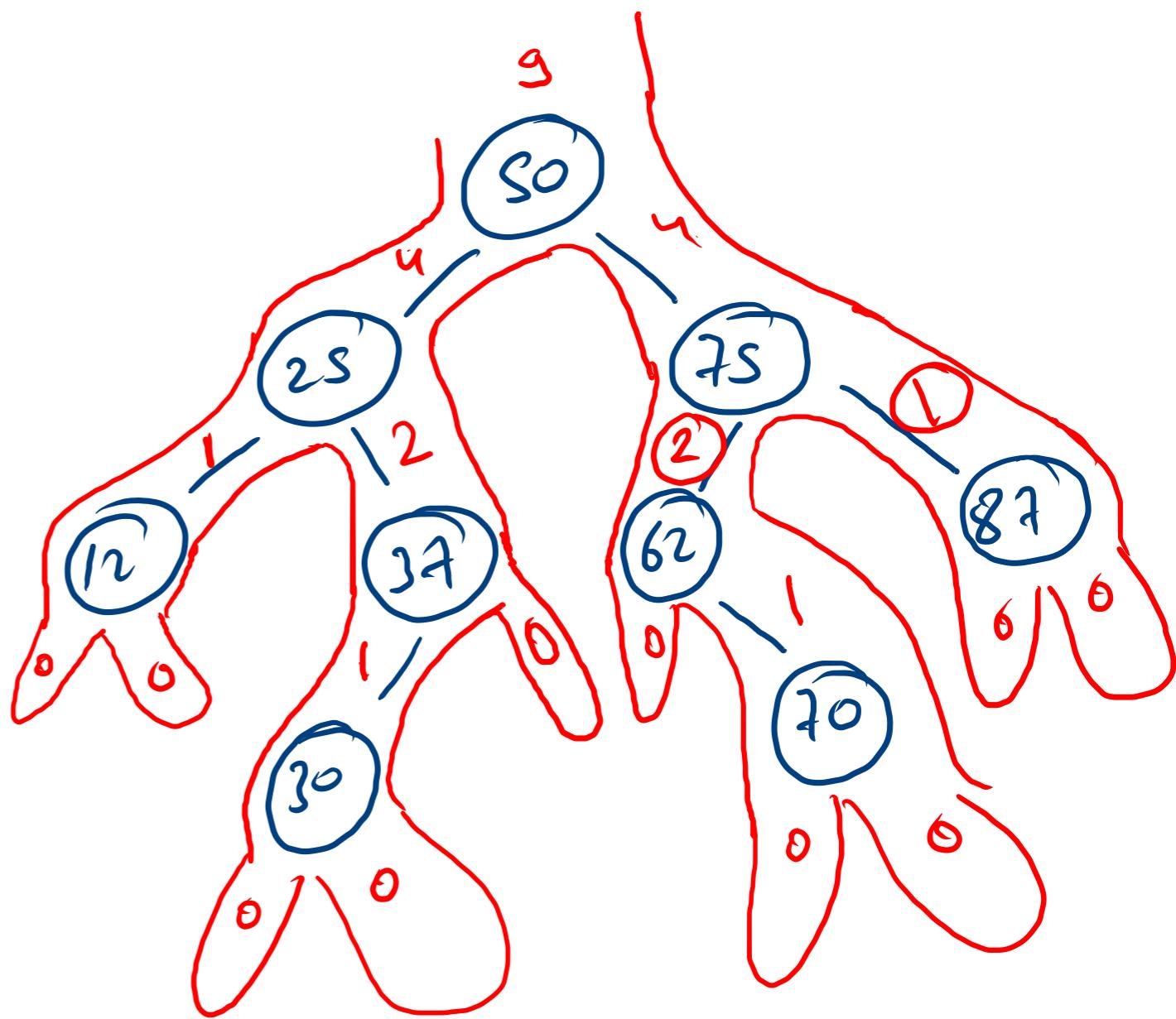


$$0 = \max(a, a)+1$$

$$0-1 = \max(a, a)$$

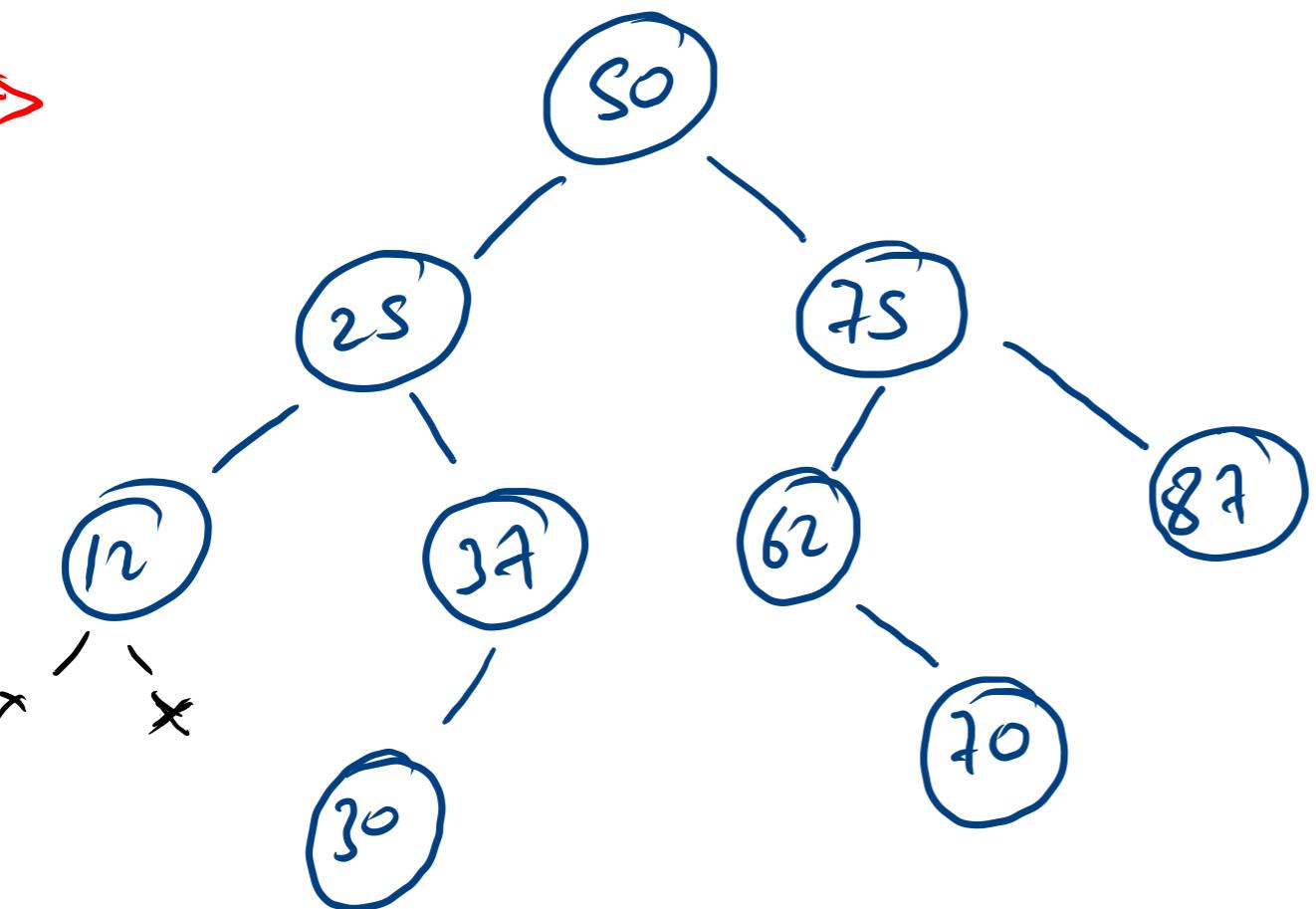
$$[-1 \sim a]$$

```
public static int size(Node node) {  
    if(node == null) return 0;  
  
    int left = size(node.left);  
    int right = size(node.right);  
  
    return left+right+1;  
}
```

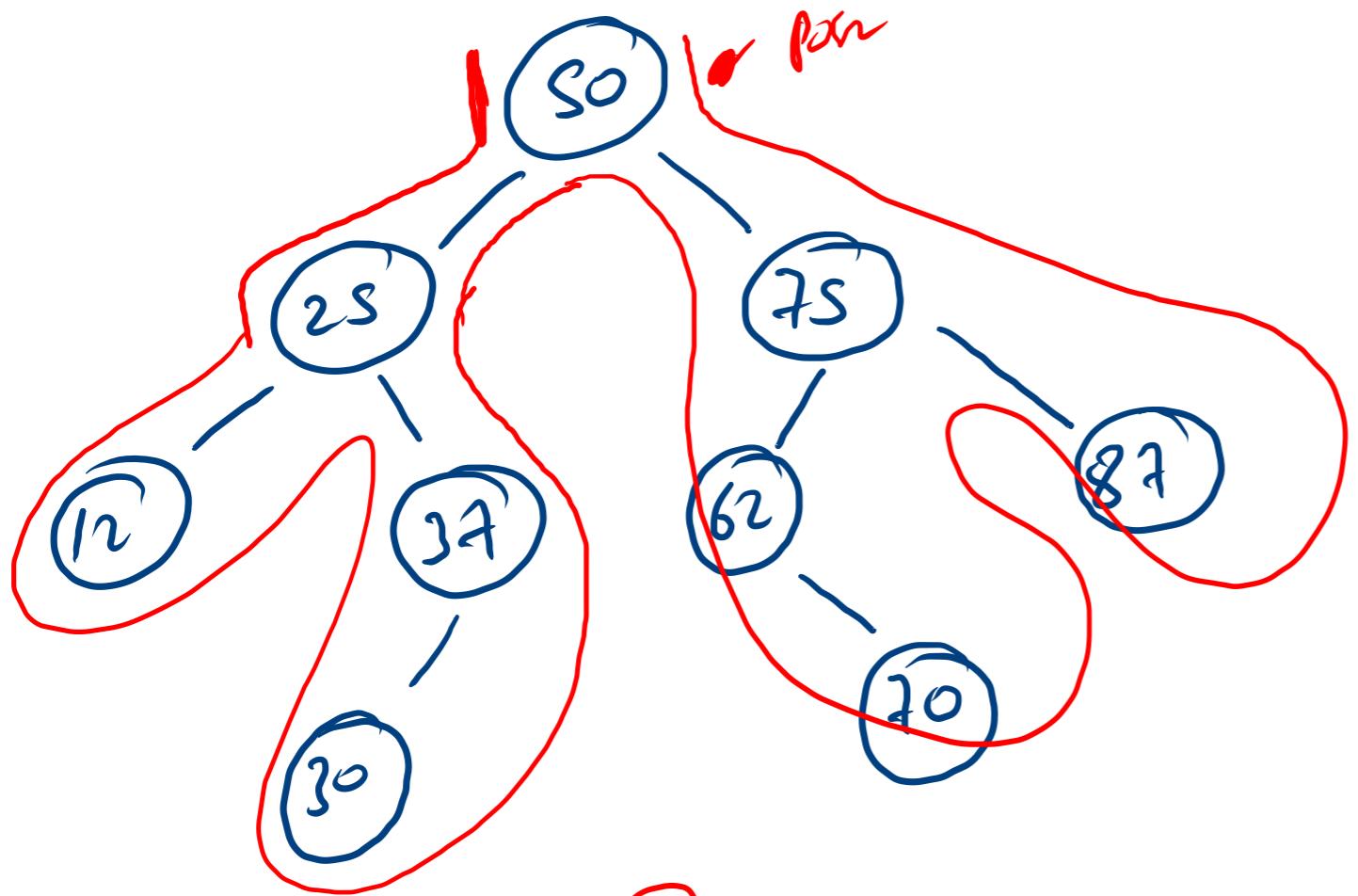


H.W.

Levelorder Traversal Of Binary Tree

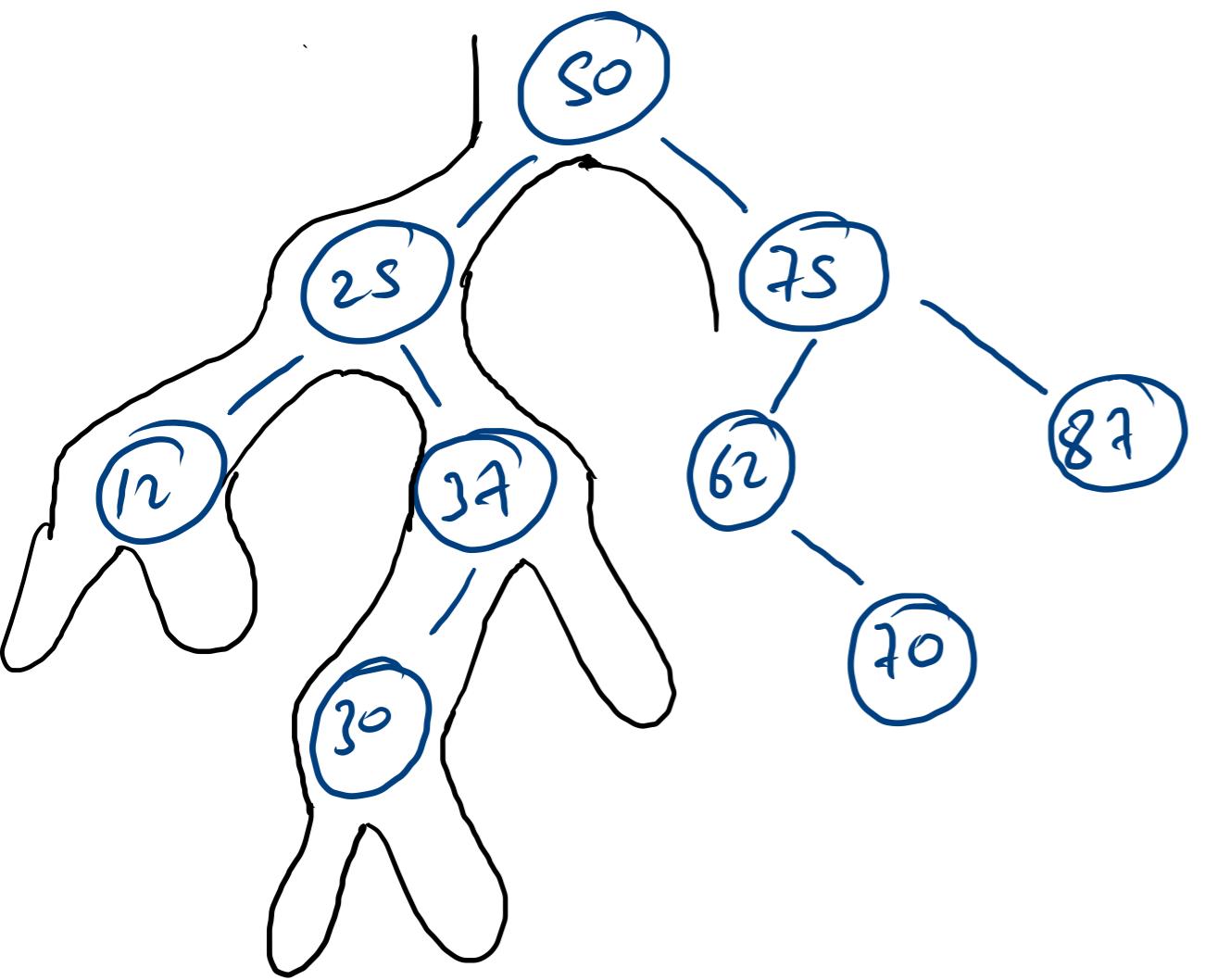


50
25 75
12 37 62 87
30 70



Pre	Post	Inhib
SO	SO	SO

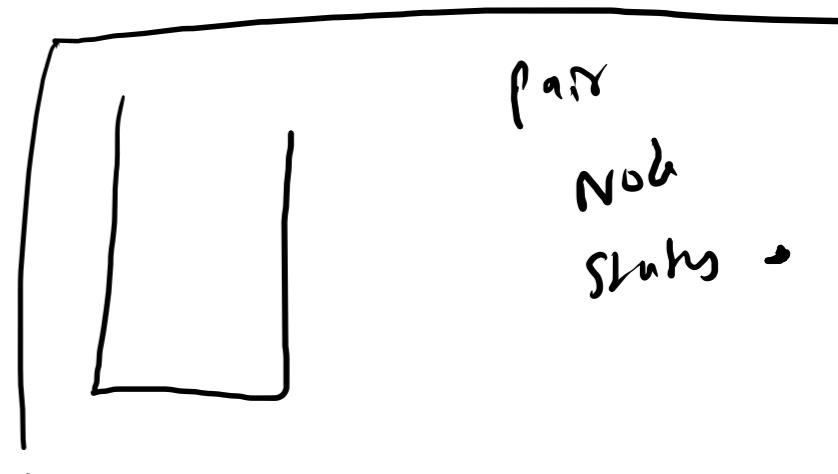


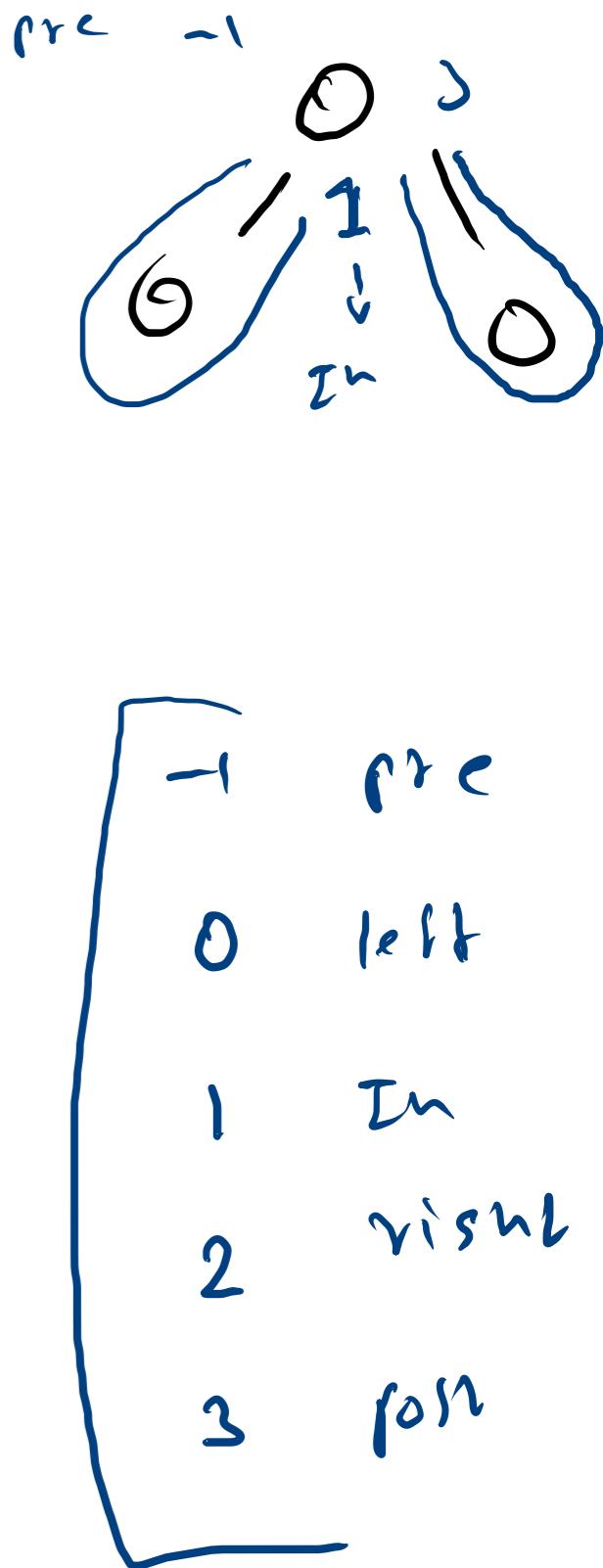
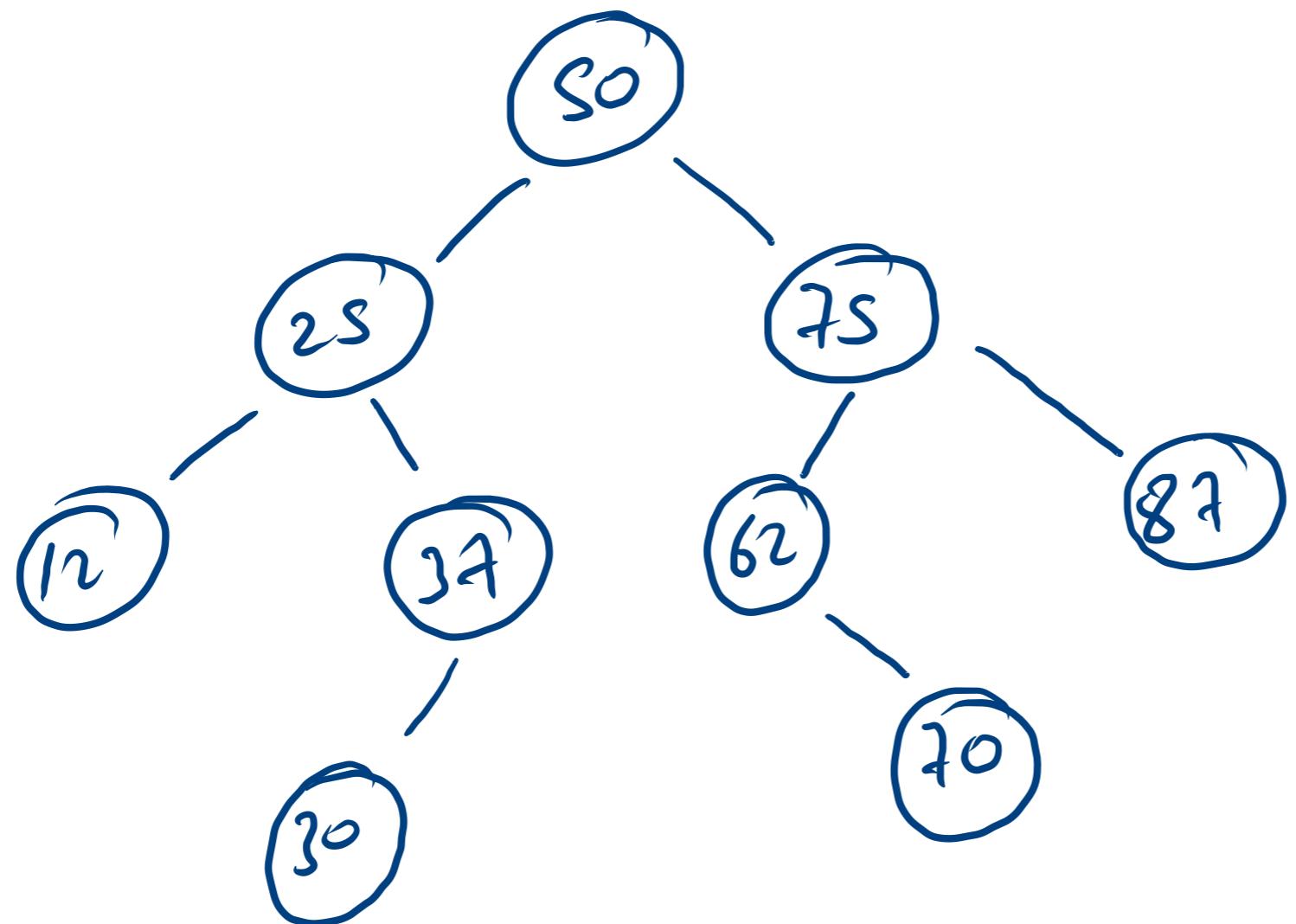


Pre
50
25
12
37
30
25

Post
12
30
37
25

In
12
25
30
37
50



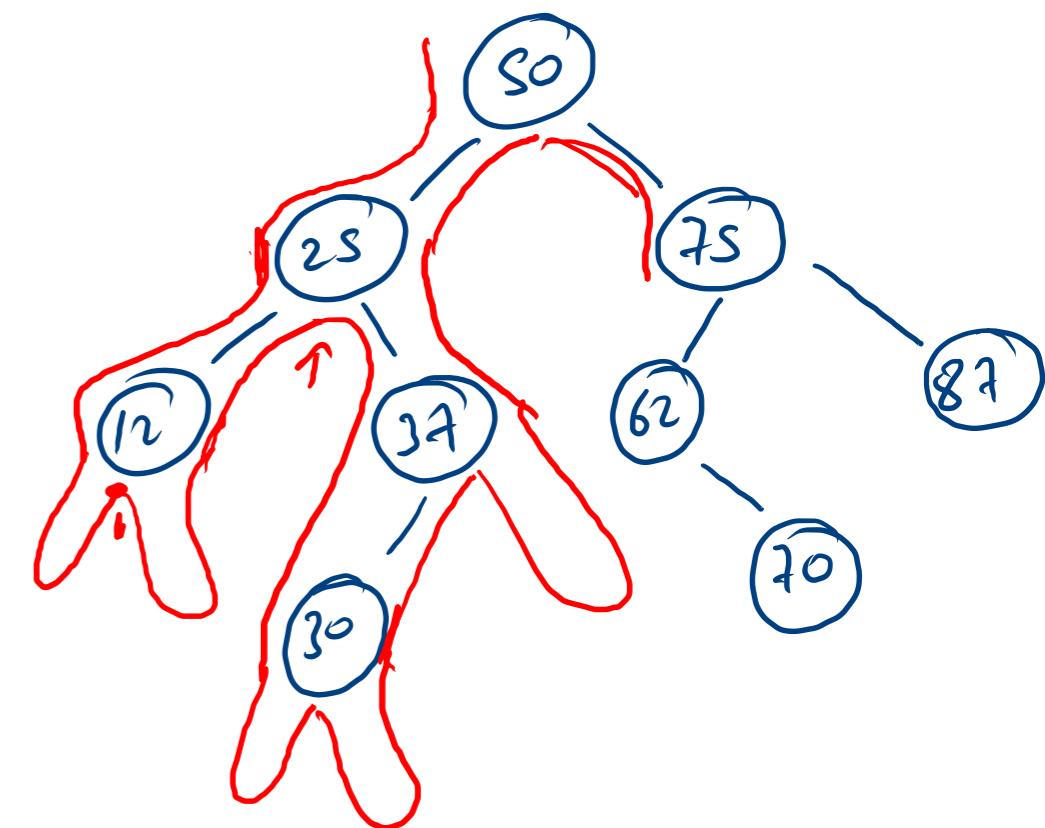
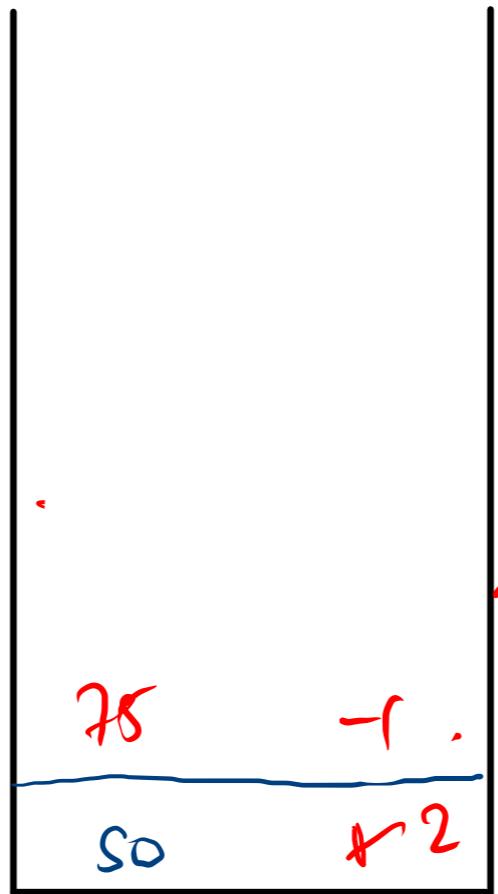


```

while(st.size() > 0){
    Pair2 p = st.peek(); ←

    if(p.status == -1){
        //pre
        pre.append(p.node.data+" ");
        p.status++;
    }else if(p.status == 0){
        // left
        if(p.node.left != null){
            st.push(new Pair2(p.node.left, -1));
        }
        p.status++;
    }else if(p.status == 1){
        // inorder
        in.append(p.node.data+" ");
        p.status++;
    }else if(p.status == 2){
        // right
        if(p.node.right != null){
            st.push(new Pair2(p.node.right, -1));
        }
        p.status++;
    }else{
        // post
        post.append(p.node.data+" ");
        st.pop();
    }
}

```



pre	50	25	12	37	82
in	12	25	30	37	50
post	12	82	37	25	

N.W.

Find And NodeToRootpath In Binary Tree

data → 30

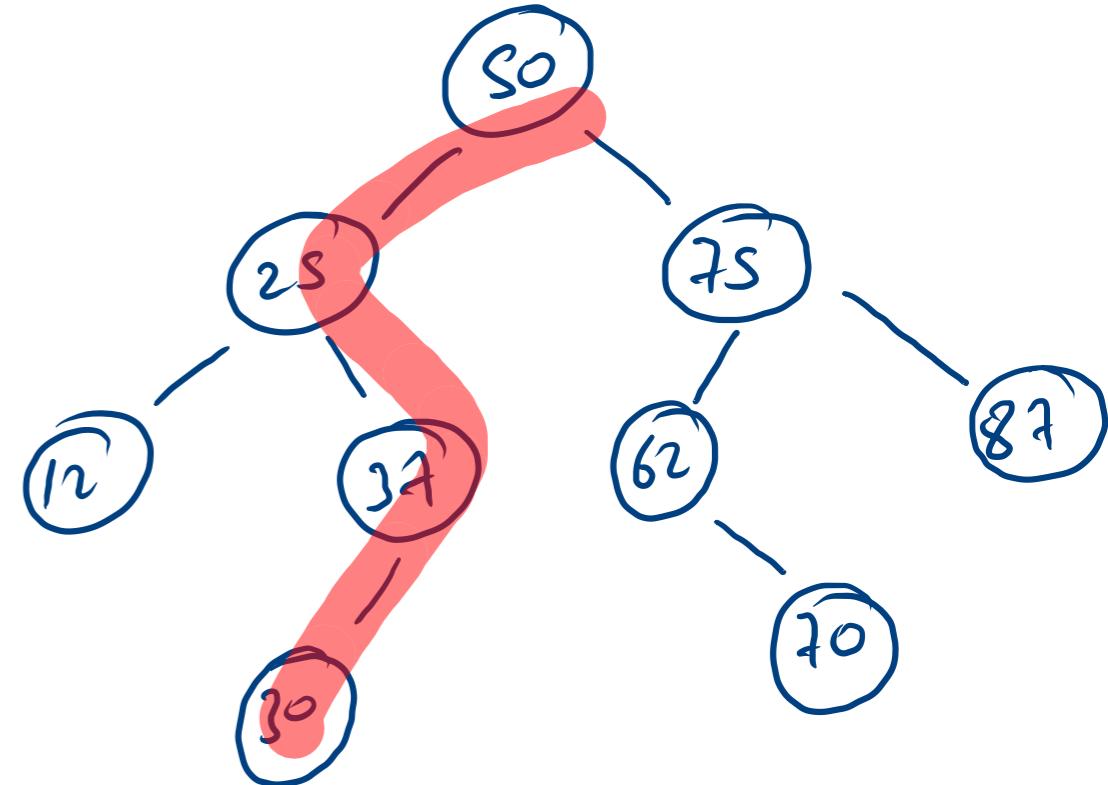
find → true

hboral → [30 , 32, 25, 50]

data → 31

find → false

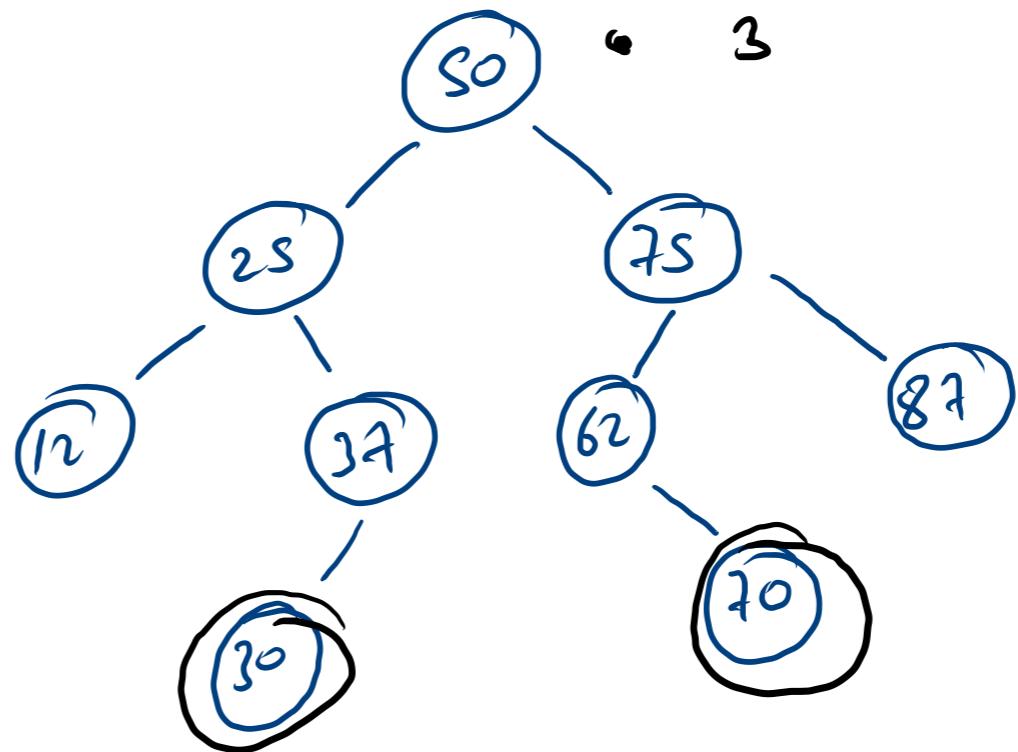
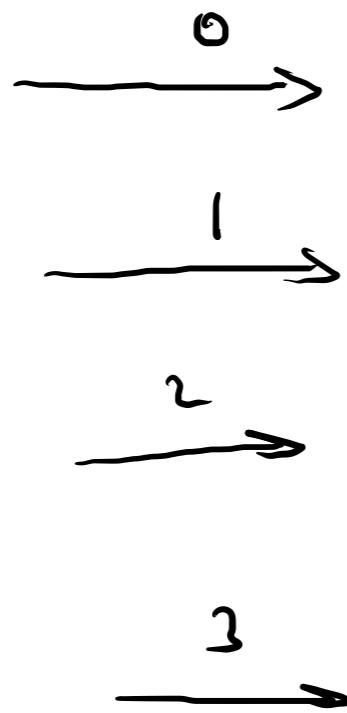
hboral → []



level \rightarrow 3

level = 2

30
70

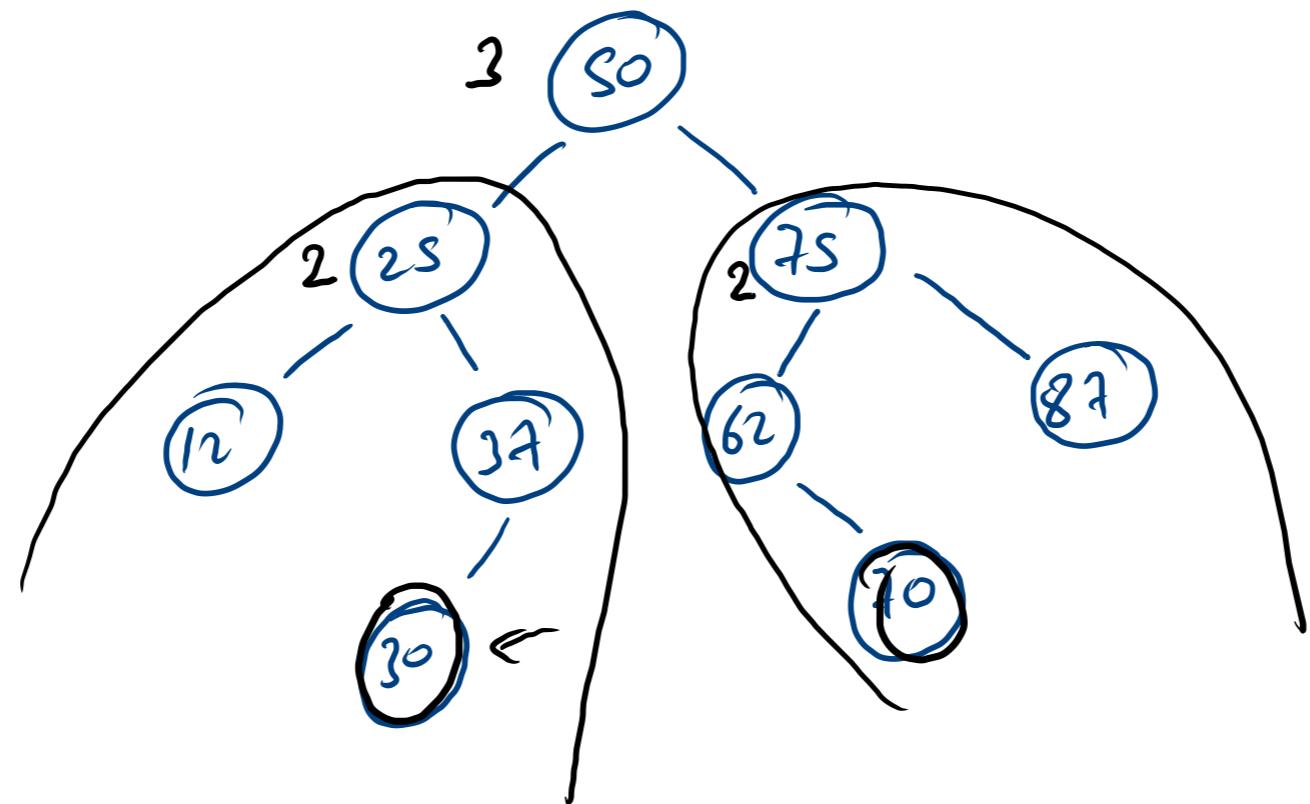


12
37
62
87

$[-\infty \leq \text{level} \leq +\infty]$

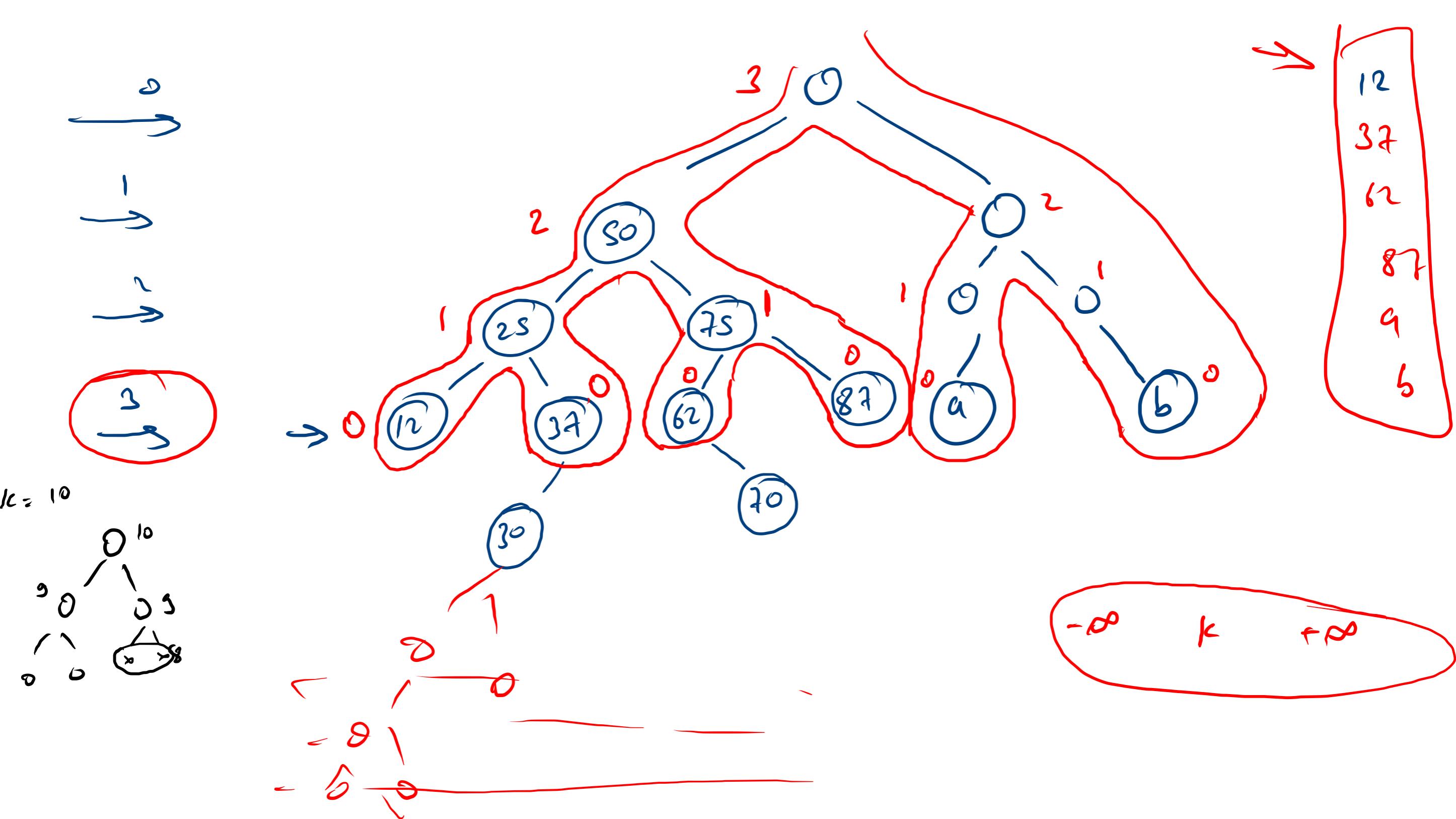
K

level → 3



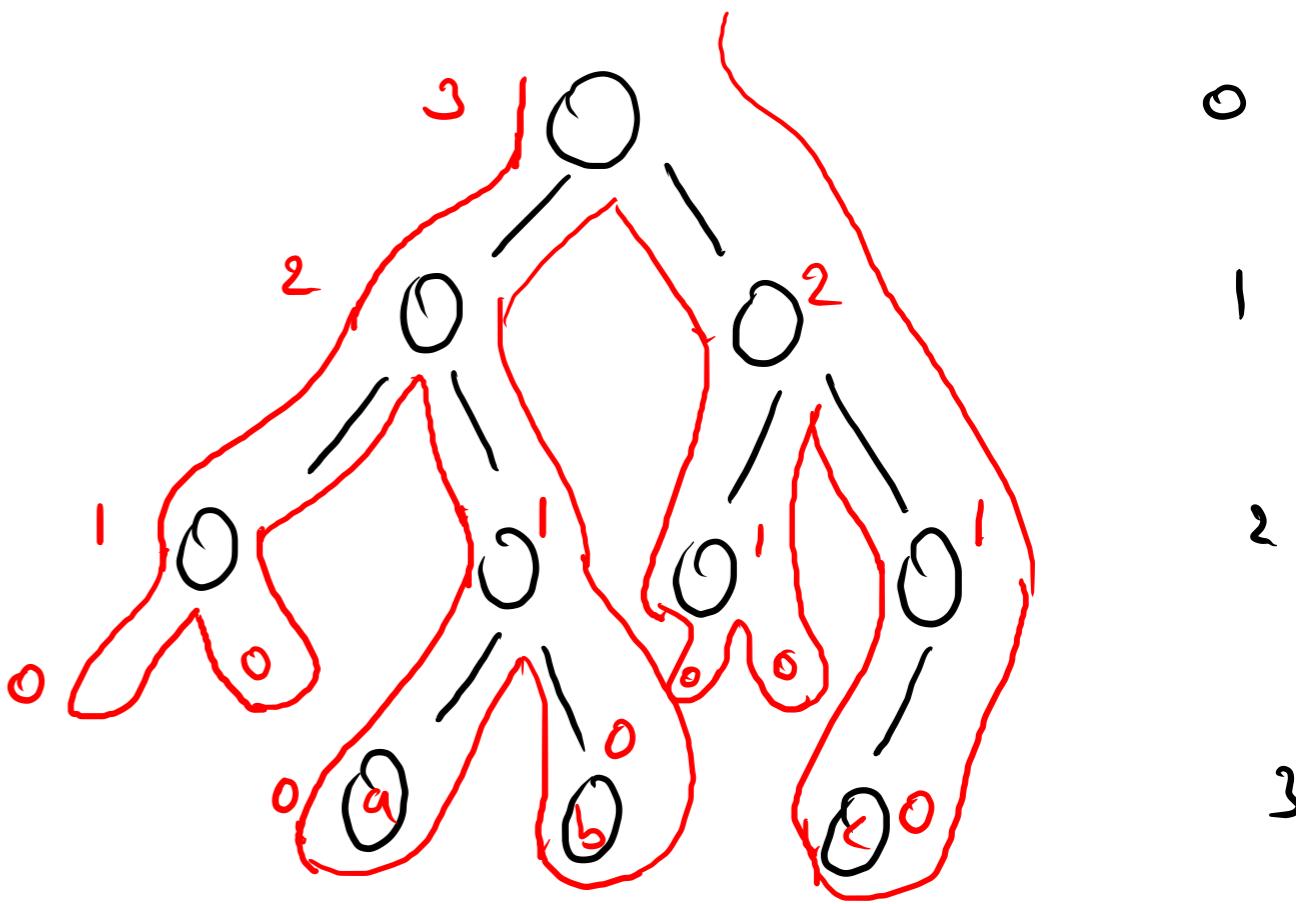
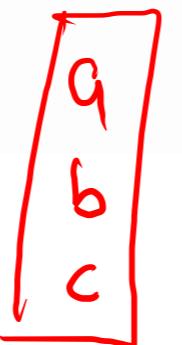
prim (left, k-1)

prim (right, k-1)



level = 3

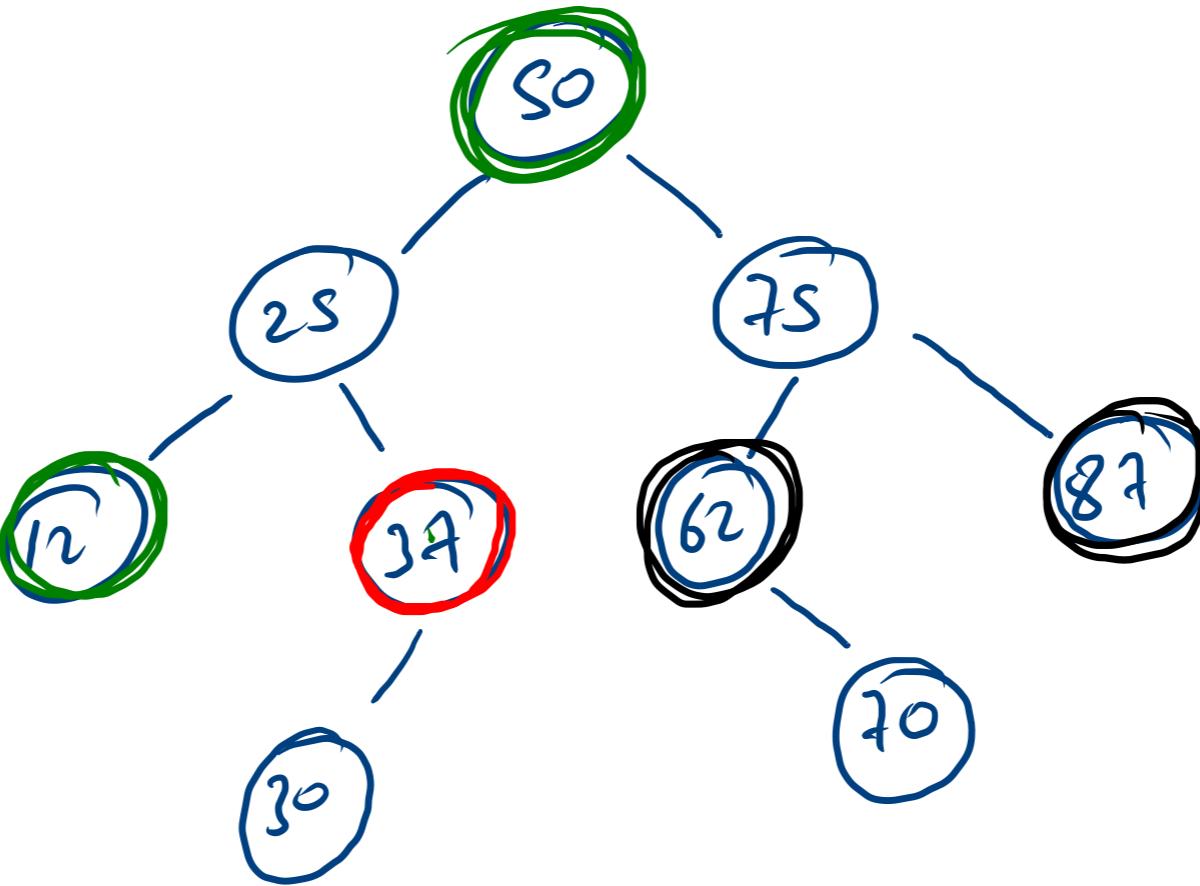
```
public static void printKLevelsDown(Node node, int k){  
    if(k<0 || node == null){  
        return;  
    }  
  
    if(k==0){  
        System.out.println(node.data);  
        return;  
    }  
  
    printKLevelsDown(node.left, k-1);  
    printKLevelsDown(node.right, k-1);  
}
```



data \rightarrow 37
 $k \rightarrow 2$

k distance

12
50

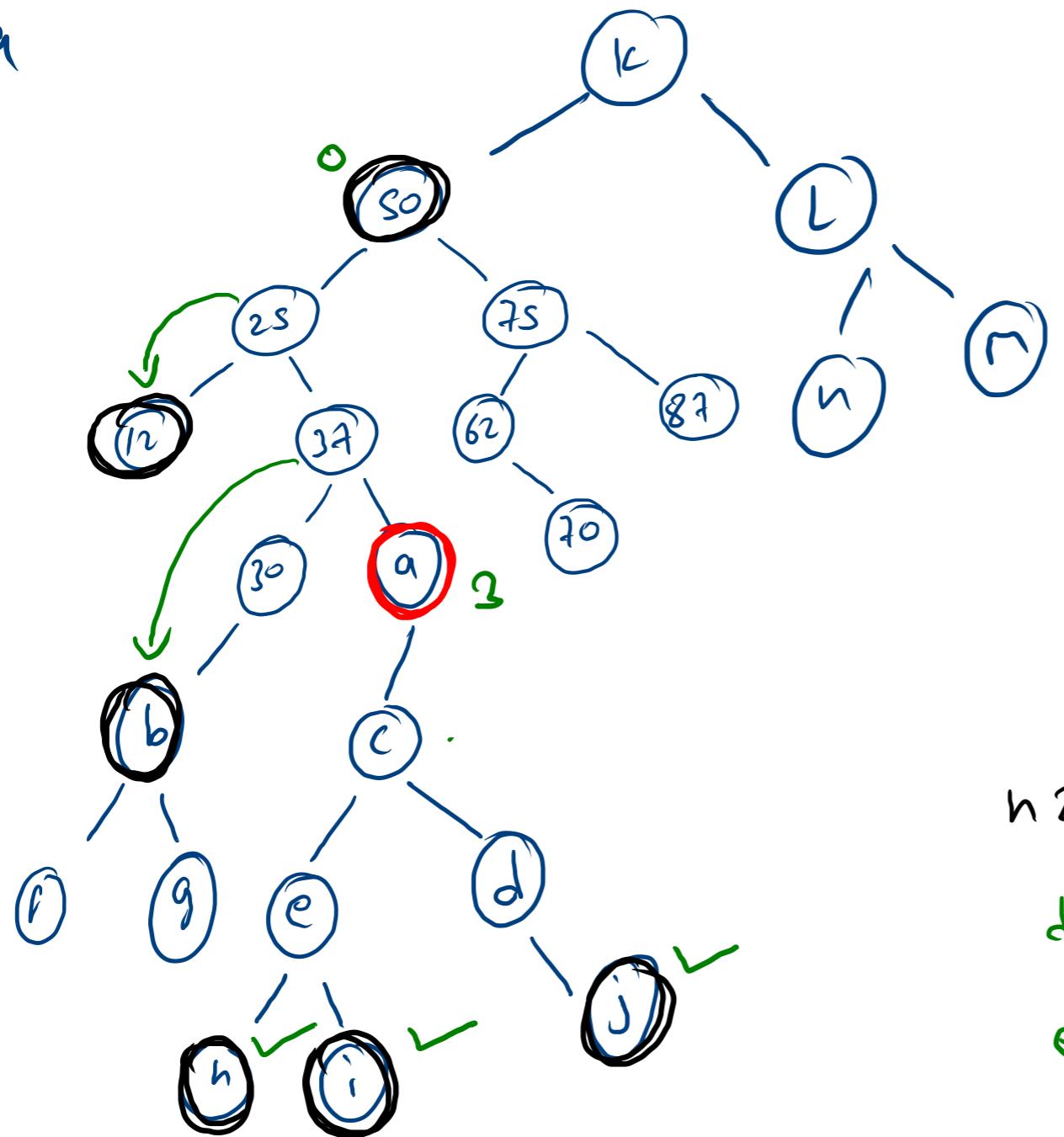


$k = 2$

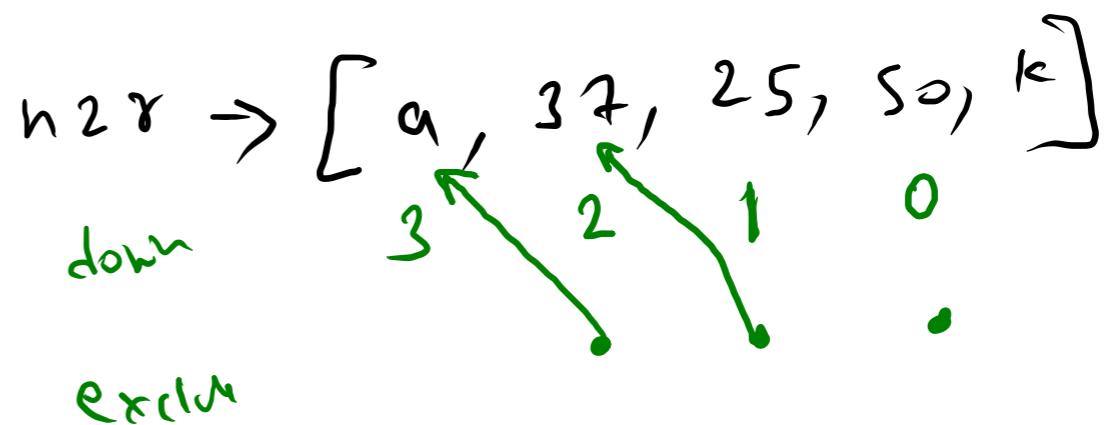
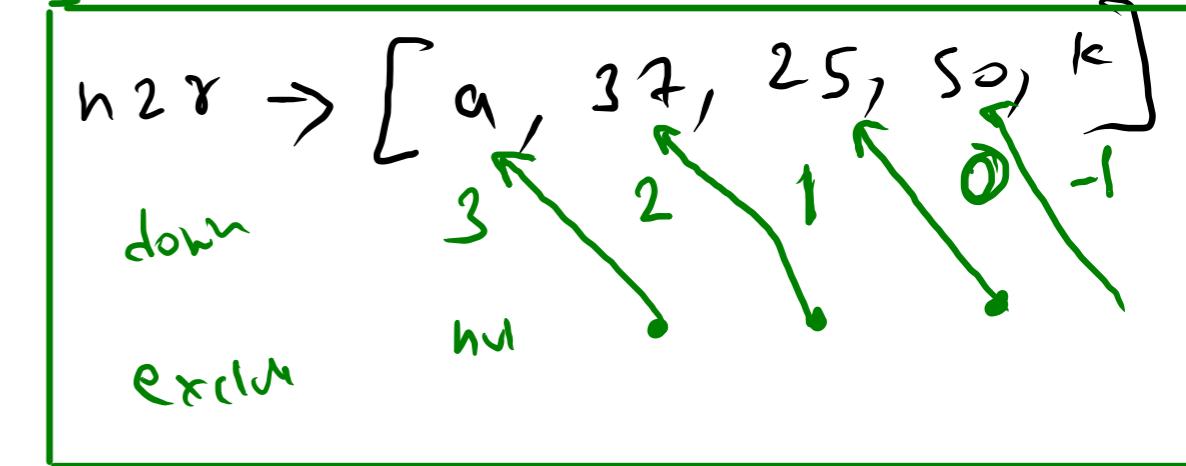
62
87

$\text{data} \rightarrow q$

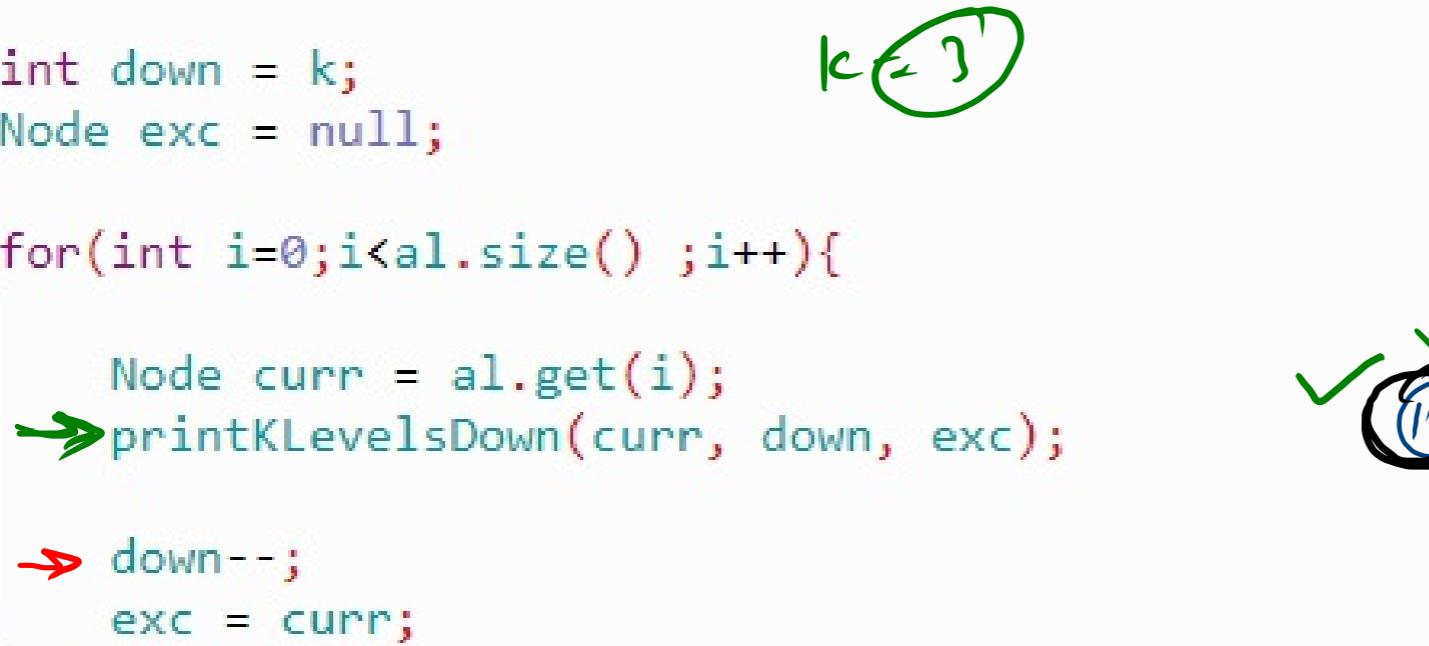
$k = 3$



$\rightarrow v$



```
public static void printKNodesFar(Node node, int data, int k) {  
    ArrayList<Integer> al = nodeToRootPath(node, data);  
  
    int down = k;  
    Node exc = null;  
  
    for(int i=0;i<al.size() ;i++){  
        Node curr = al.get(i);  
        → printKLevelsDown(curr, down, exc);  
  
        → down--;  
        exc = curr;  
    }  
}
```



$$a \in [0, 1, 2, 3, 4]$$

bw	3	2	1	0	-1
exc	411	9	37	25	50

