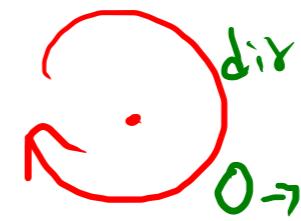


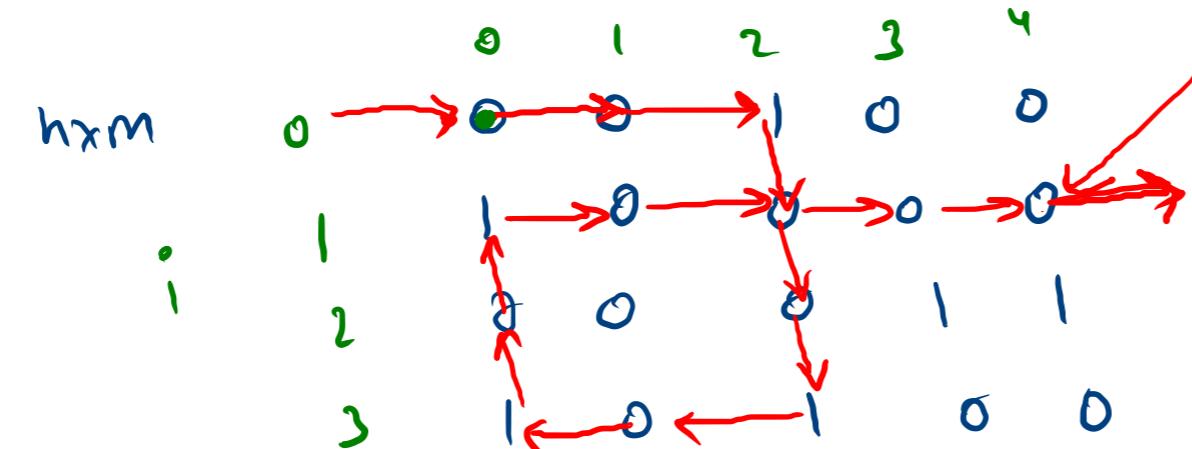
$h = 4$
 $m = 5$

0/1



0 → east

→ j++

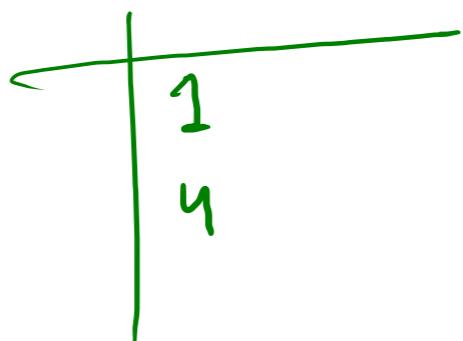


0 → move

1 → turn
move

if (1) turn

move



1 → south

↓
i++

2 → west ← j--

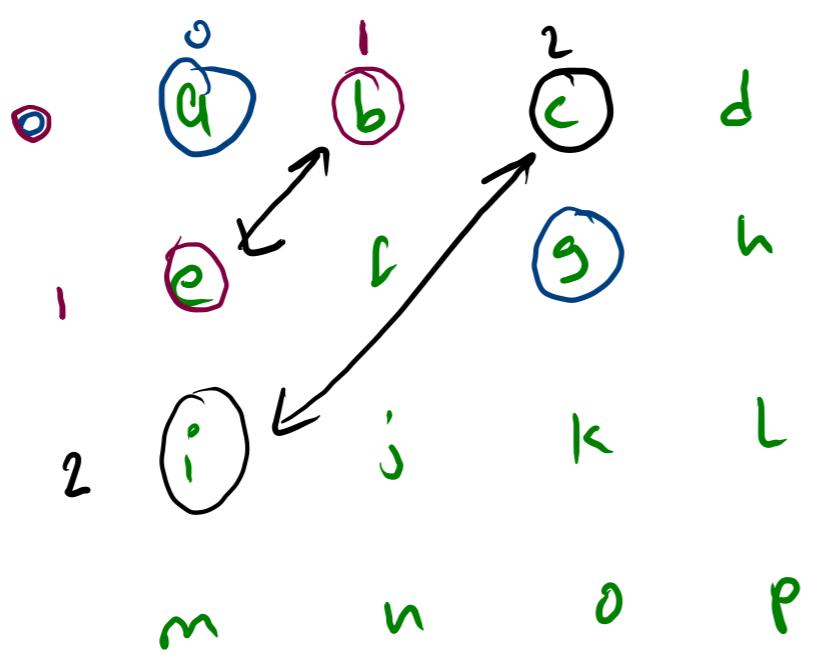
3 → north ↑
↓
0 → east → i--

```

i = 0
j = 0
dir = 0;
while ( ) {
    if ( arr[i][j] == -1 ) {
        change dir by 90° // turn
    }
    // move
    if ( east )
        else if ( west )
            sink
            norm
}

```

$n=4$



$a[i][j]$
$a[j][i]$

↓ transpose

a	e	i	m
b	f	j	n
c	g	k	o
d	h	l	p

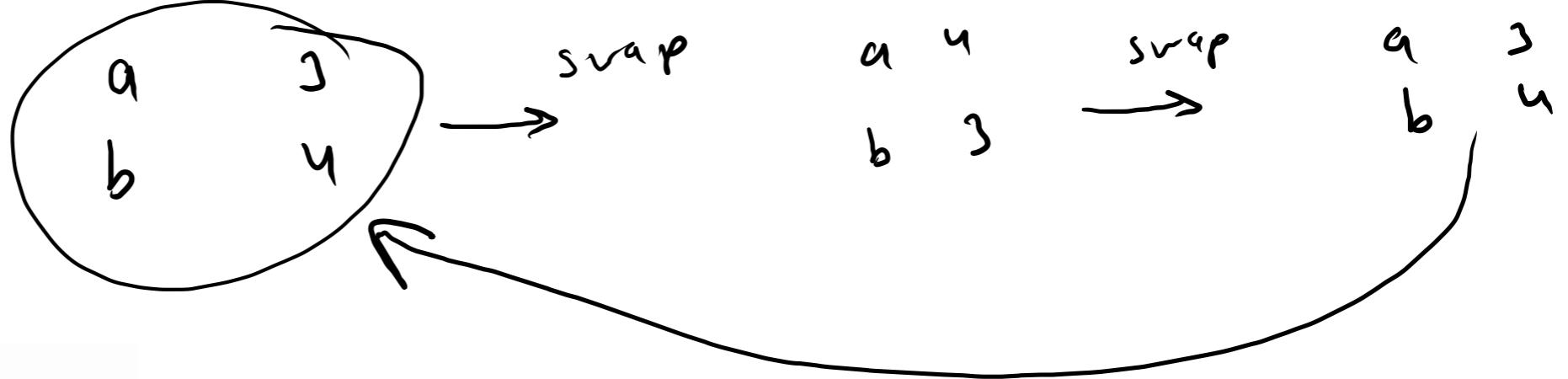
→ reverse
all
rows

m	i	e	a
n	j	f	b
o	k	g	c
p	l	h	d

o	3	$-$	ρ	g
-----	-----	-----	--------	-----

s	c	r	σ
τ	σ	r	c
d	r	s	ρ

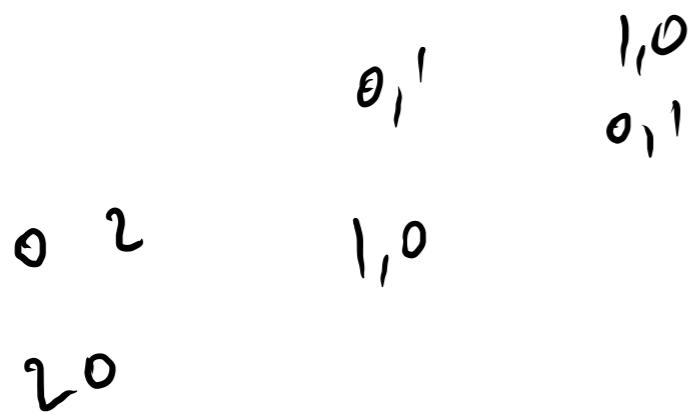
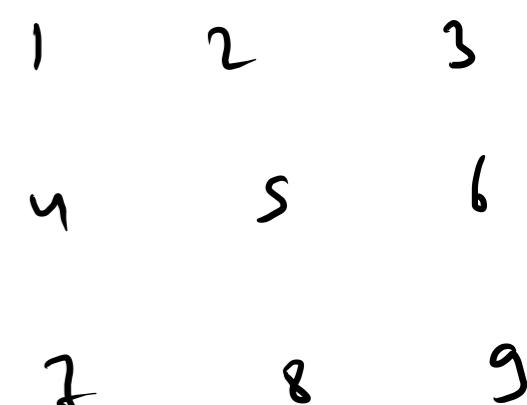
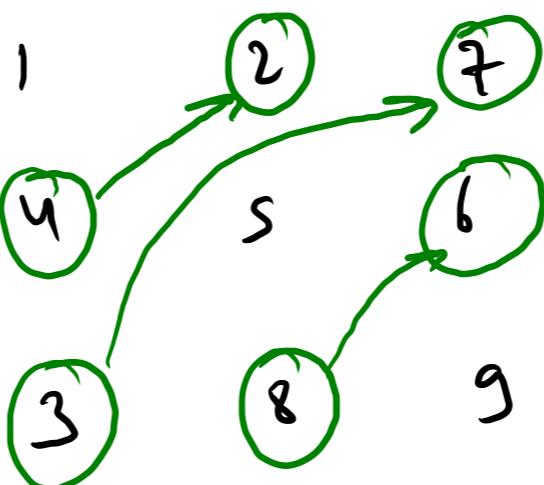
Transpose
// check
reverse
display



```

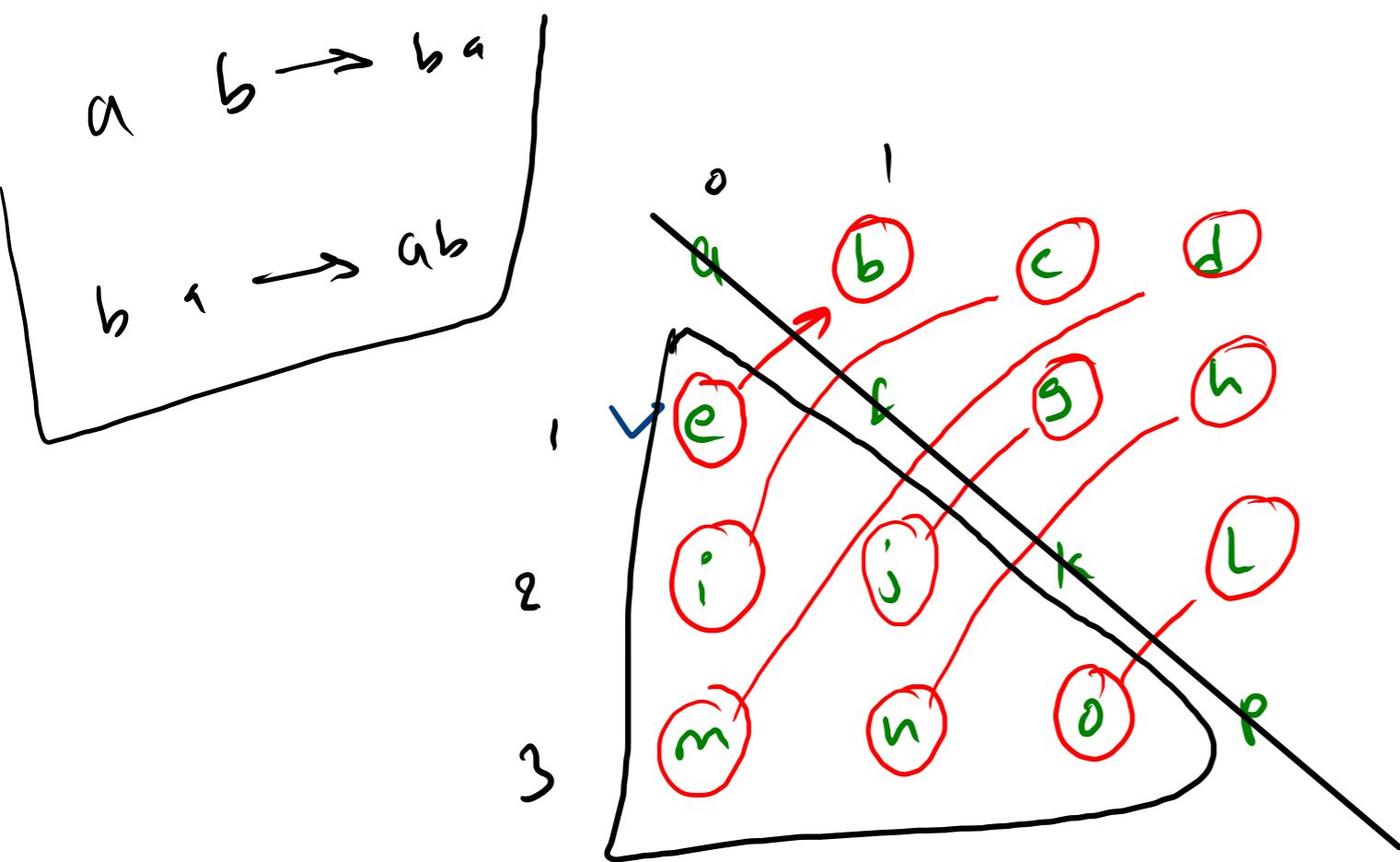
for(int i=0;i<n;i++){
    for(int j=0;j<n;j++){
        // swap [i][j] with [j][i]
        int tmp = arr[i][j];
        arr[i][j] = arr[j][i];
        arr[j][i] = tmp;
    }
}

```



$[i][j] = [j][i]$
 $[0][1]$

$[j][i]$



$i \leftarrow 1 \text{ do } h-1$
 $j \leftarrow 0 \text{ do } i-1$
 $0 \leftarrow 0$
 $0 \leftarrow 1$
 $0 \leftarrow 2$
 $0 \leftarrow i-1$

1 0
 2 0 , 2, 1
 3 0 , 31 , 32
 .
 i

$$h = 4$$

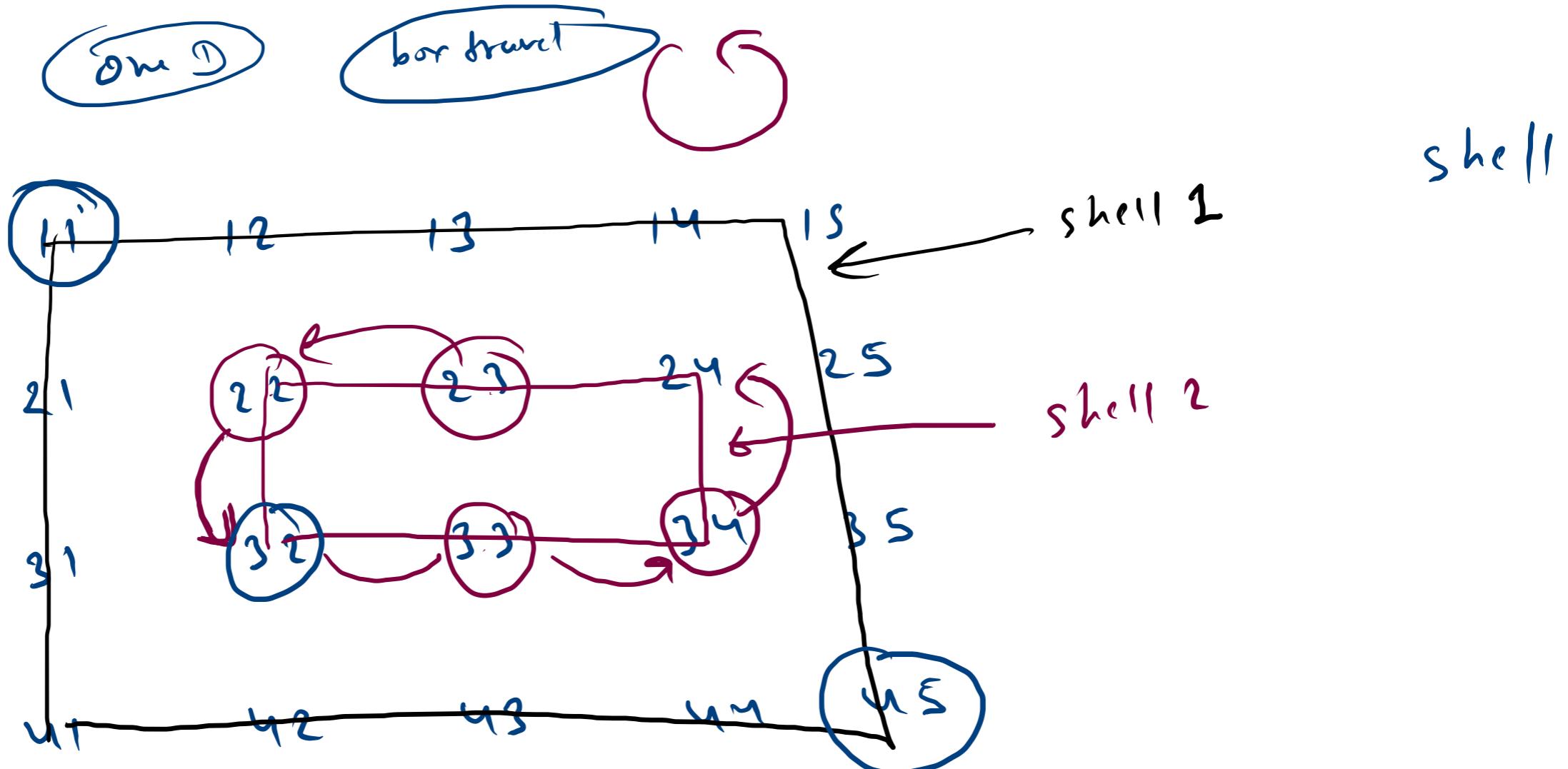
$$m = 5$$

$$s = 2$$

$$\delta = 1$$

$$\delta = 2$$

$$\boxed{\delta = -2}$$



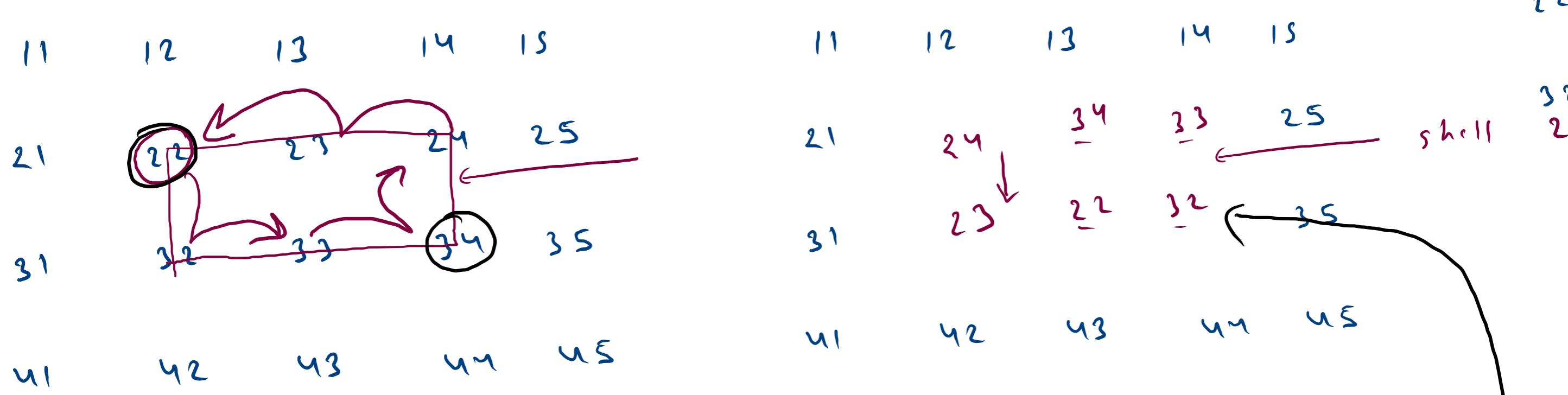
$\times v$

$-v$

\circ

	11	12	13	14	15
21	23	24		25	
31	22	32	33	35	

41	42	43	44	45
----	----	----	----	----



$s = 2$

shell to one D

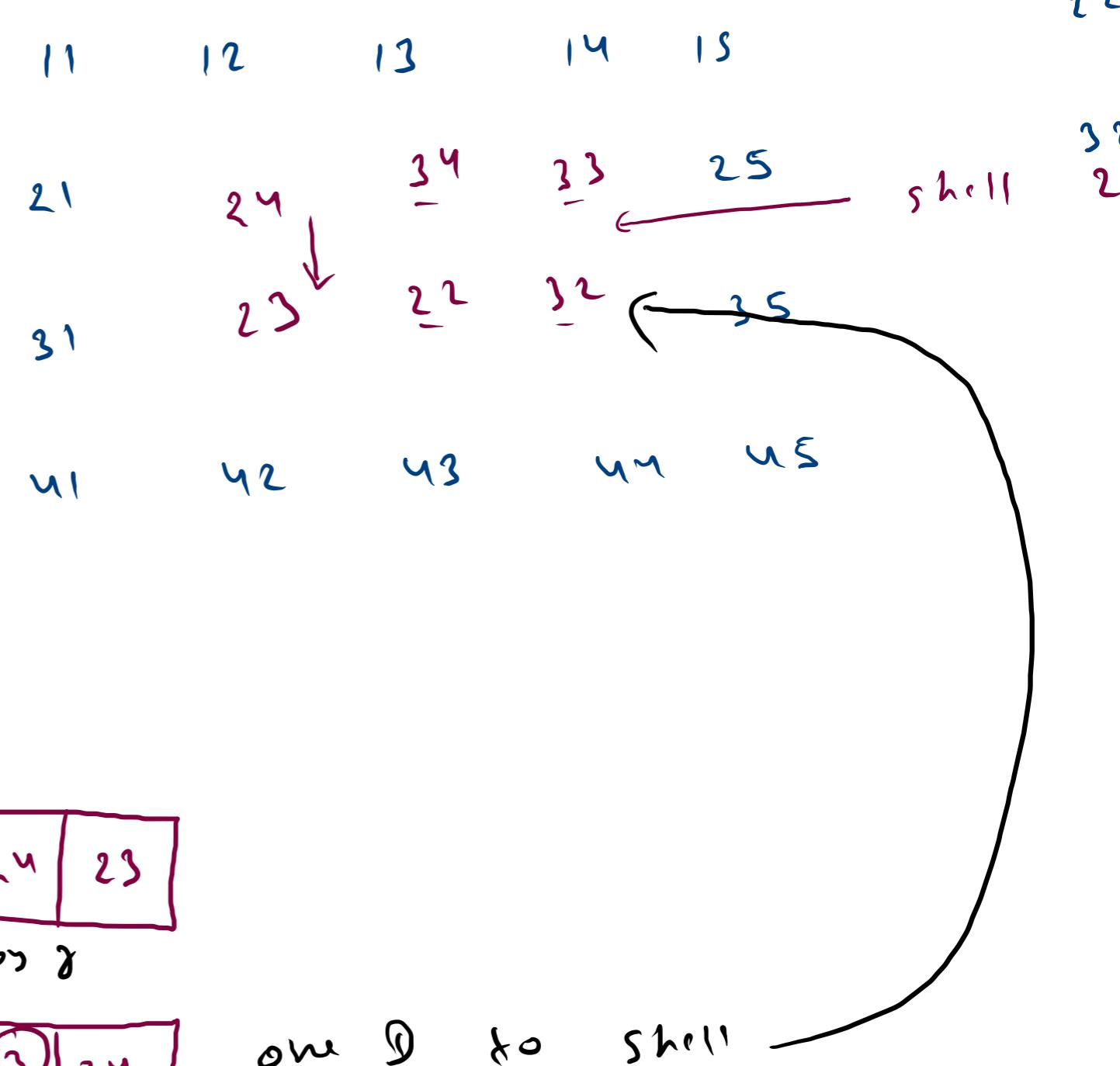
22	31	33	34	24	23
----	----	----	----	----	----

rotate by γ

24	23	22	32	33	34
----	----	----	----	----	----

$\gamma = 2$

$k_i - \infty$ to ∞



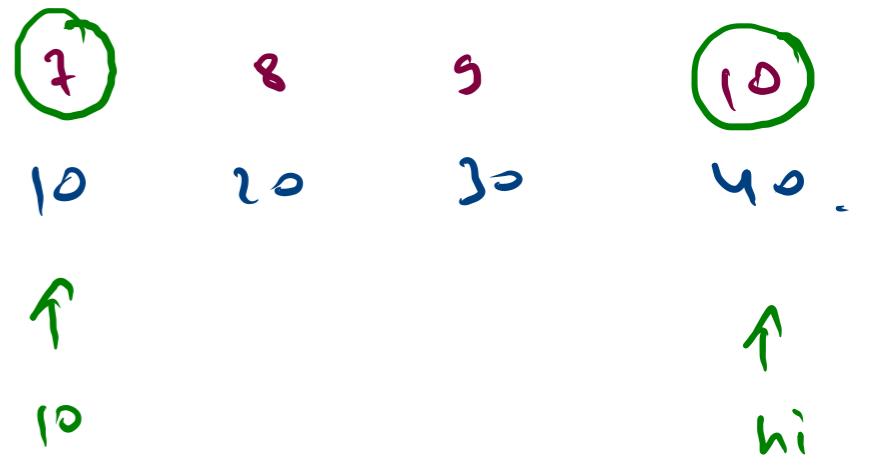
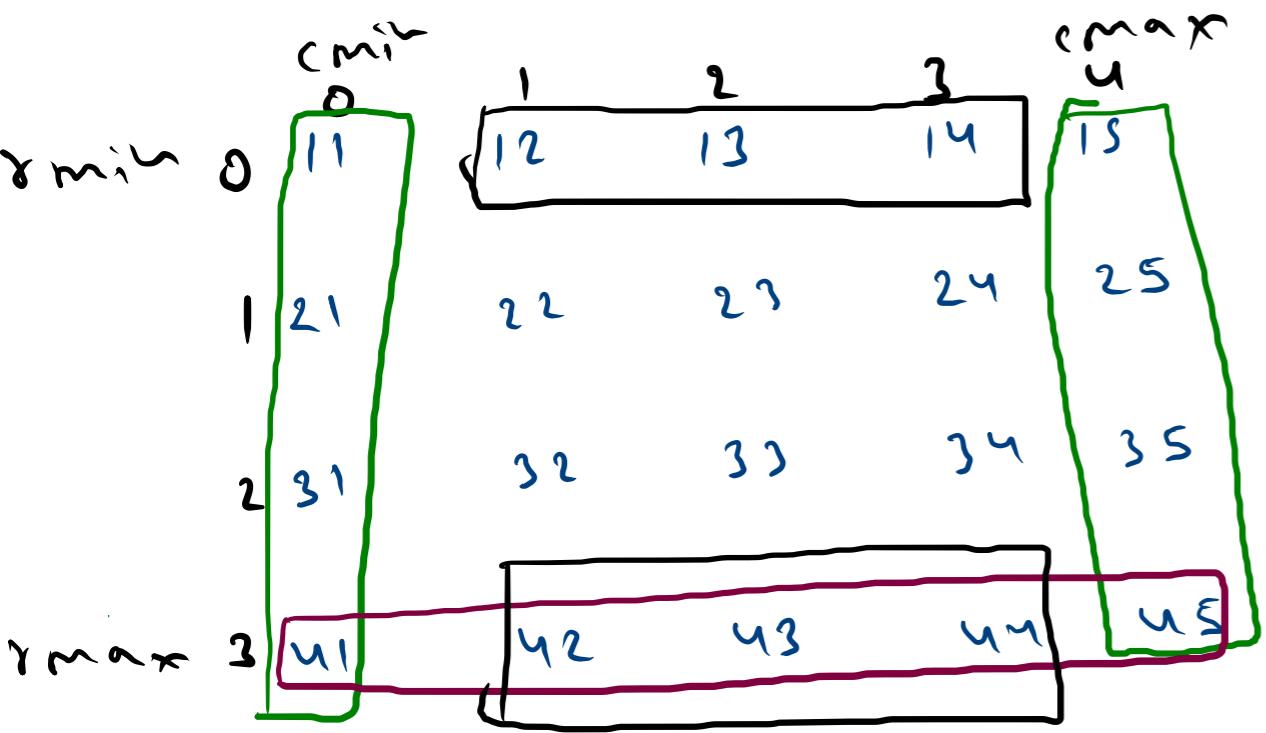
r_{min}	c_{min}	11	12	13	14	c_{max}	$m-2$	$m-1$	15
21		22	23	24	25				
31		32	33	34	35				
r_{max}	$h-1$	41	42	43	44	45			

- identify shell ✓
- size of shell ✓
- shell to one D array ↗
- rotate by γ ✓
- one D to shell

	r_{min}	c_{min}	r_{max}	c_{max}
$s=1$	0	0	$h-1$	$m-1$
$s=2$	1	1	$h-2$	$m-2$
$s=3$	2	2	$h-3$	$m-3$

$[s \quad s-1 \quad s-2 \quad h-s \quad m-s]$

Display



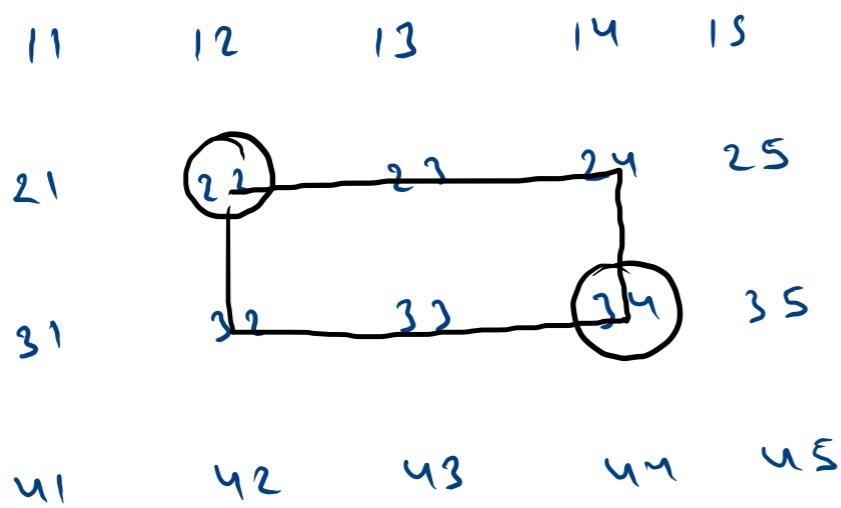
$$hi = 10 + 1$$

$$10 - 2 + 1 = 9$$

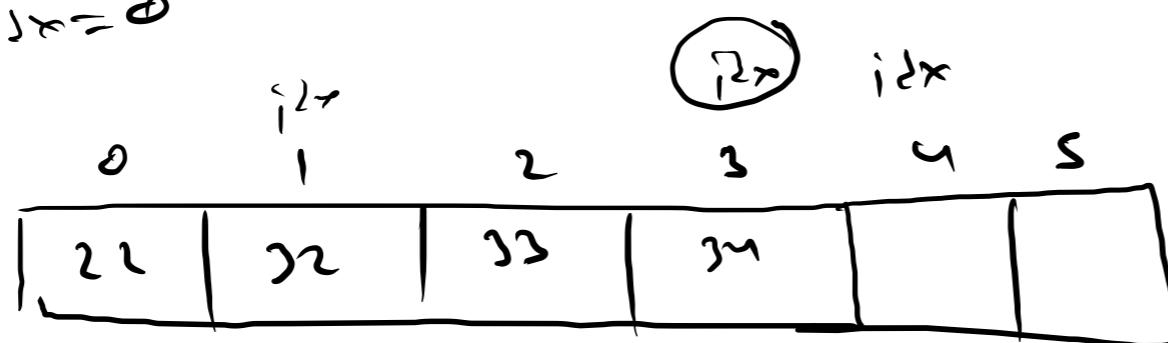
$$2(\gamma_{\max} - \gamma_{\min} + 1) + 2(c_{\max} - c_{\min} + 1 - 2)$$

$$2\gamma_{\max} - 2\gamma_{\min} + 2 + 2c_{\max} - 2c_{\min} + 2 - 4$$

$$2(\gamma_{\max} - \gamma_{\min} + c_{\max} - c_{\min})$$



$idx = 0$



shell to oneD

for ($r < \dots$)

print arr[r][c] \rightarrow oneD[idx] = arr[r][c]

$size = 2(r_{max} - r_{min} + c_{max} - c_{min})$

oneD to shell

arr[r][c]

$\{ arr[r][c] = oneD[idx] \}$

$idx++$

$h = 4$

$h \times h$

$d = 12$

	0	1	2	3	4
0	11	12	13	14	21
1	21	22	23	24	
2	31	32	33	34	
3	41	42	43	44	

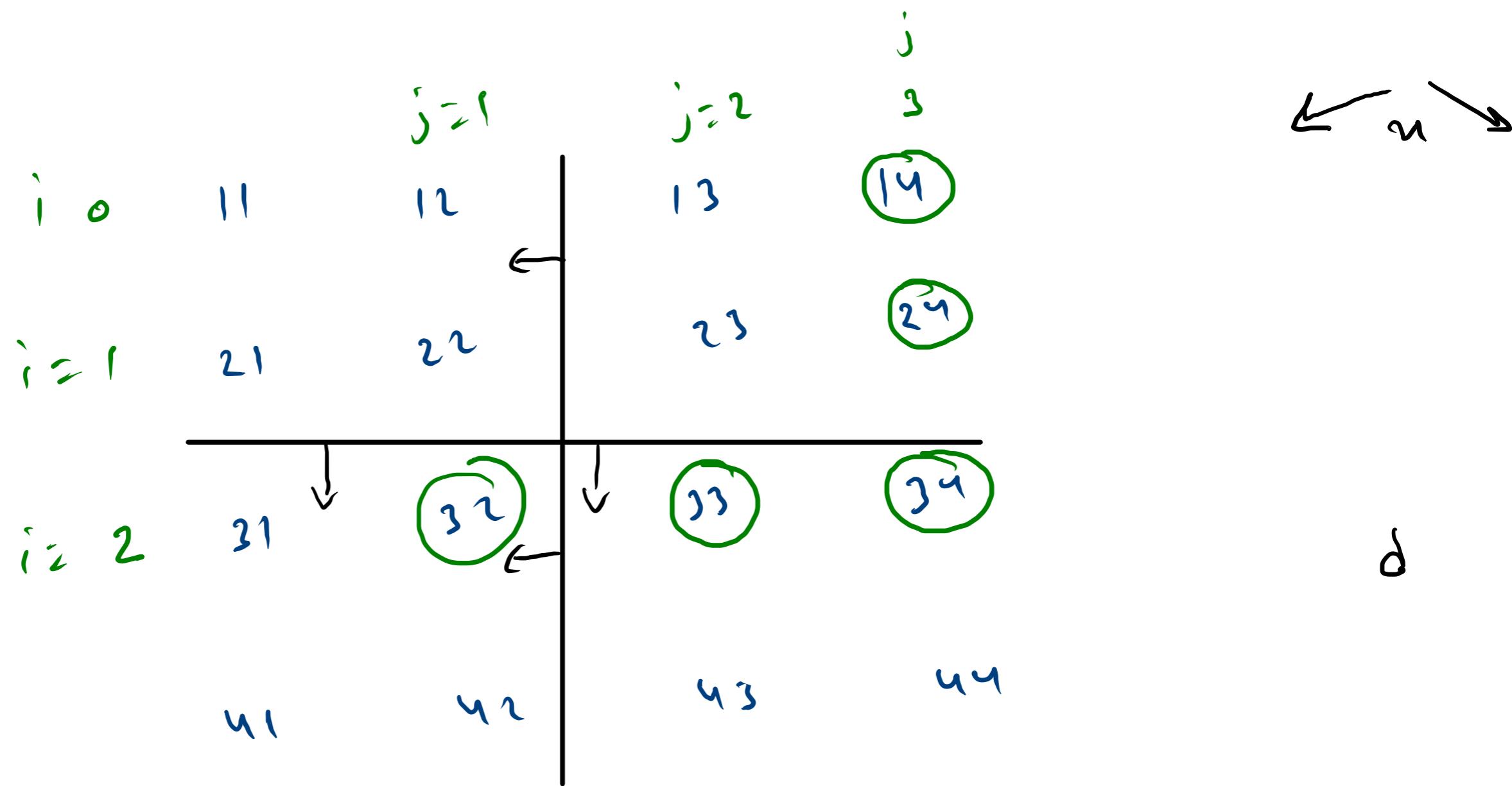
$d = 43$

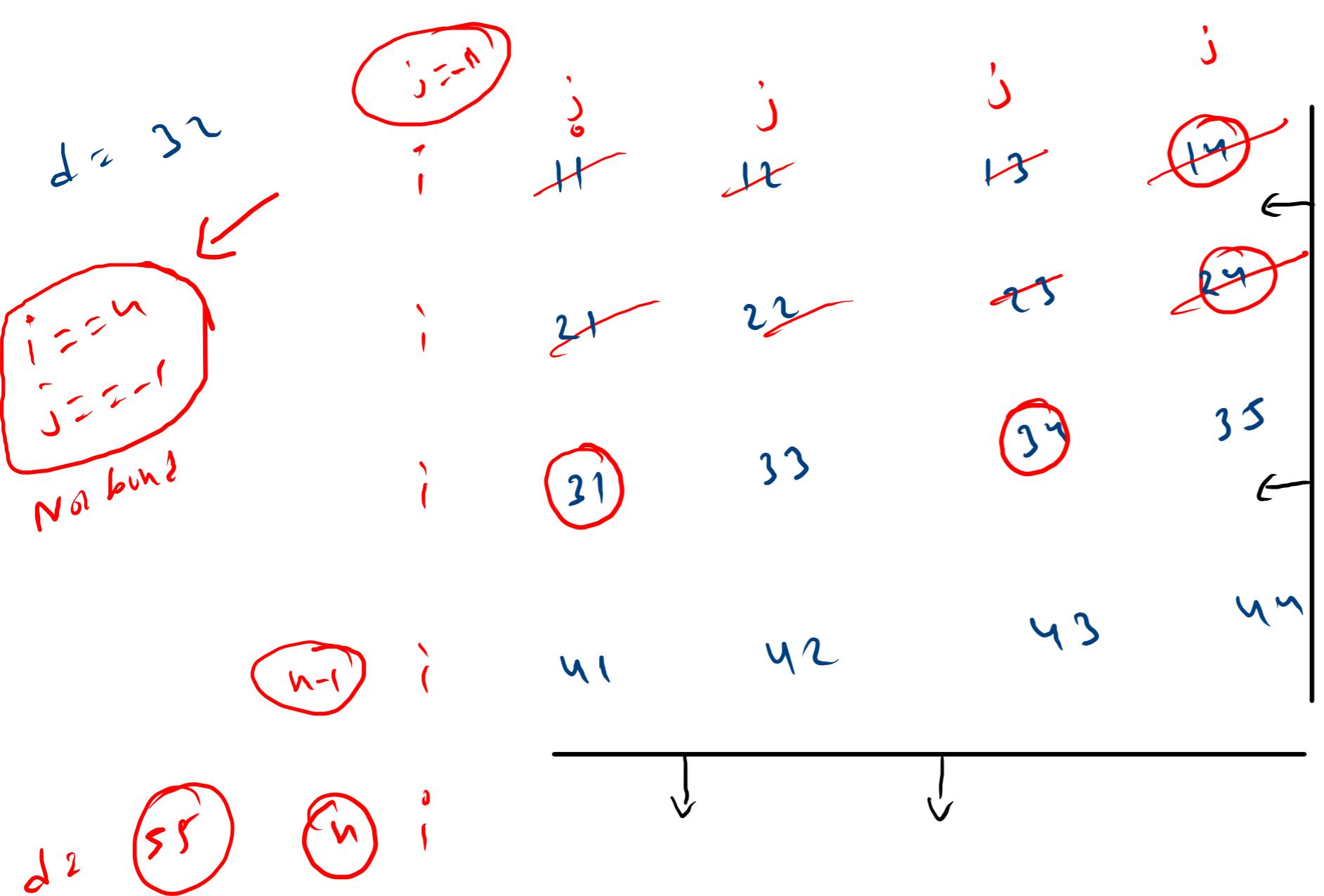
~~3
2~~

$d = 55$

No comb

$$d = 32$$





i = 0
j = n-1

if ($arr[i][j] < d$)
 i++
else if ($arr[i][j] > d$)
 j--

$$\begin{array}{c}
 \text{0} & \text{1} \\
 \boxed{a_{00}} & a_{01} \\
 \text{0} & \text{1} \\
 a_{10} & a_{11} \\
 \end{array}
 \xrightarrow{\quad}
 \begin{array}{c}
 b_{00} \\
 b_{10} \\
 b_{20} \\
 \end{array}
 \begin{array}{c}
 b_{01} \\
 b_{11} \\
 b_{21} \\
 \end{array}
 =
 \begin{array}{c}
 \boxed{ } \\
 \boxed{ } \\
 \boxed{ } \\
 \end{array}$$

2×2

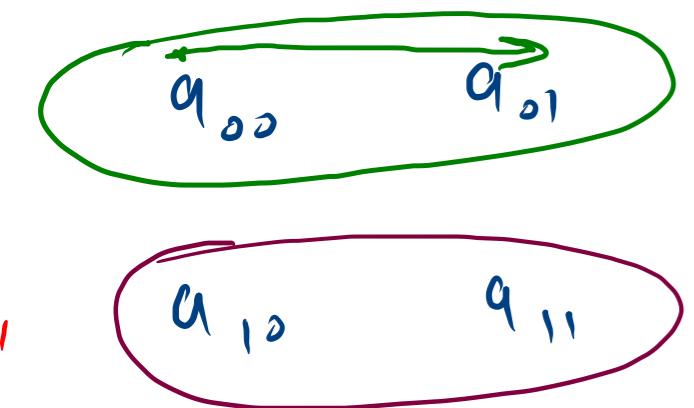
$n_1 \ m_1$

number of column

3×2

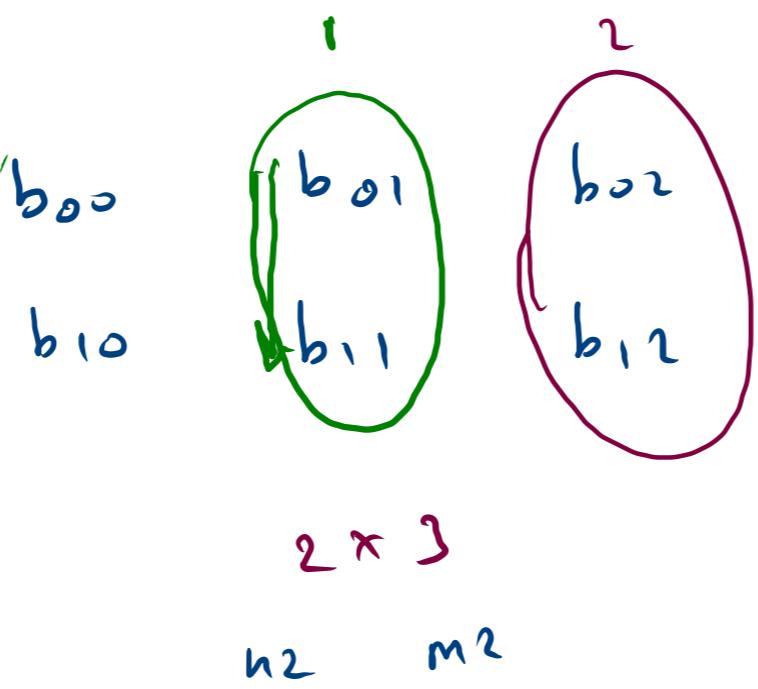
$n_2 \ m_2$

\equiv $n_2 \leq n_1$ row



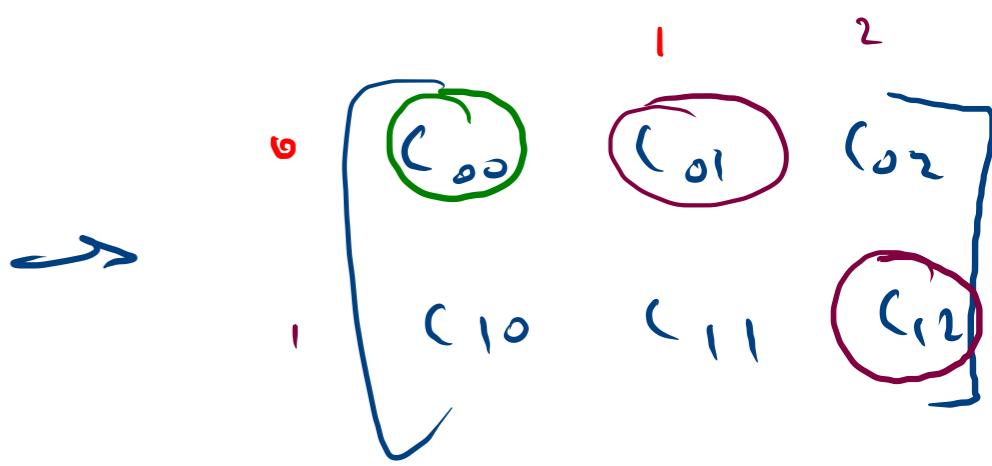
2×2

$n_1 \quad m_1$



2×3

$n_2 \quad m_2$



$n_1 \times m_2$

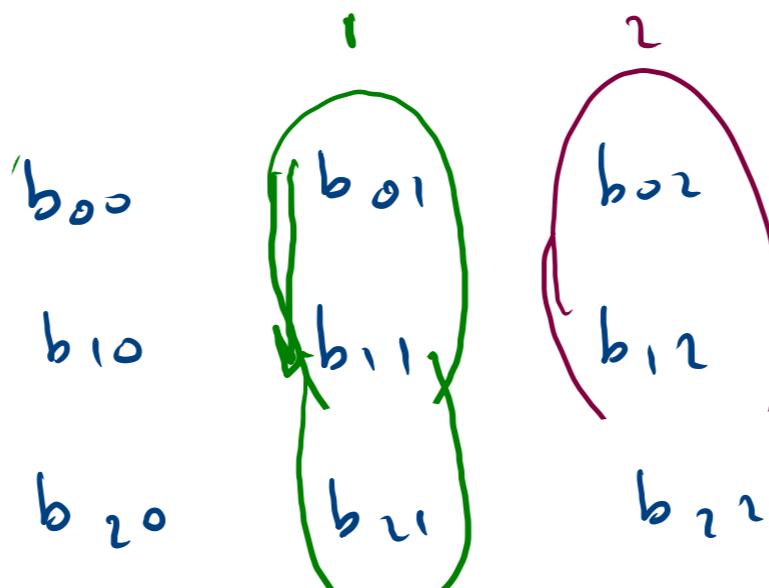
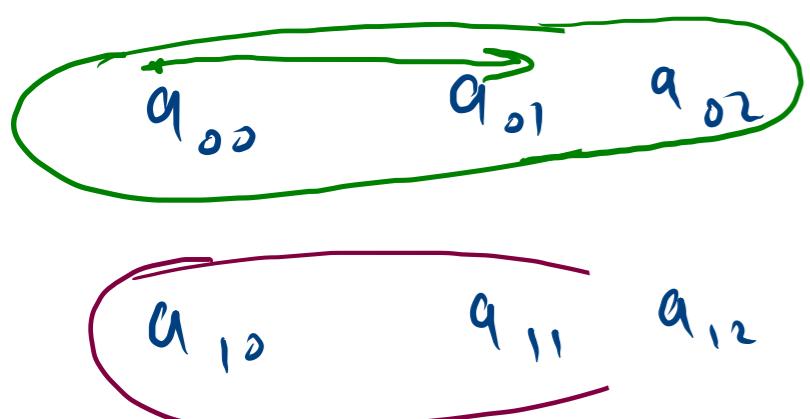
2×3

$i \leftarrow 0 \text{ to } n_1 - 1$
 $j \leftarrow 0 \text{ to } m_2 - 1$

int sum = 0

$\boxed{A[i][k] \times B[k][j]}$
 $k \leftarrow 0 \text{ to } n_2 - 1$
 $ans[i][j] = sum;$

$$C_{ij} = \boxed{a_{00} \times b_{01}} + \boxed{a_{01} \times b_{11}}$$



$n_1 \quad m_1$

$n_2 \times m_2$

vars 0 to $n_2 - 1$

$$c_{ij}^{01} = a_{00}^{01} \times b_{01}^j +$$

Diagram illustrating the calculation of c_{ij}^{01} as the sum of the products of a_{00}^{01} and b_{01}^j .

$$a_{01}^i \times b_{11}^j +$$

Diagram illustrating the calculation of c_{ij}^{01} as the sum of the products of a_{01}^i and b_{11}^j .

$$a_{02}^i \times b_{21}^j$$

Diagram illustrating the calculation of c_{ij}^{01} as the sum of the products of a_{02}^i and b_{21}^j .