HW3

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```
knitr::opts_chunk$set(echo = TRUE)
library(tidyverse)
## Warning: package 'tidyverse' was built under R version 4.1.3
## -- Attaching packages ----- tidyverse 1.3.1 --
## v ggplot2 3.3.5
                    v purrr
                              0.3.4
## v tibble 3.1.6 v dplyr
                              1.0.7
## v tidyr 1.1.4 v stringr 1.4.0
## v readr 2.1.1 v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(lubridate)
## Attaching package: 'lubridate'
## The following objects are masked from 'package:base':
##
##
      date, intersect, setdiff, union
library(arrow)
## Warning: package 'arrow' was built under R version 4.1.3
##
## Attaching package: 'arrow'
## The following object is masked from 'package:lubridate':
##
      duration
##
## The following object is masked from 'package:utils':
##
##
      timestamp
```

```
library(readr)
library(gender)
## Warning: package 'gender' was built under R version 4.1.3
library(wru)
## Warning: package 'wru' was built under R version 4.1.3
library(lubridate)
library(ggplot2)
library(igraph)
## Warning: package 'igraph' was built under R version 4.1.3
##
## Attaching package: 'igraph'
## The following objects are masked from 'package:lubridate':
##
##
       %--%, union
## The following objects are masked from 'package:dplyr':
##
       as_data_frame, groups, union
##
## The following objects are masked from 'package:purrr':
##
##
       compose, simplify
## The following object is masked from 'package:tidyr':
##
##
       crossing
## The following object is masked from 'package:tibble':
##
##
       as_data_frame
## The following objects are masked from 'package:stats':
##
##
       decompose, spectrum
## The following object is masked from 'package:base':
##
##
       union
library(ggraph)
```

Warning: package 'ggraph' was built under R version 4.1.3

```
library(tidygraph)
## Warning: package 'tidygraph' was built under R version 4.1.3
##
## Attaching package: 'tidygraph'
## The following object is masked from 'package:igraph':
##
##
       groups
## The following object is masked from 'package:stats':
##
##
       filter
Load data
Load the following data: + applications from app_data_sample.parquet + edges from edges_sample.csv
data_path <- "C:/Users/admin/Documents/R projects/2022-ona-assignments/"</pre>
applications <- read_parquet(paste0(data_path, "app_data_sample.parquet"))
edges <- read_csv(paste0(data_path,"edges_sample.csv"))</pre>
## Rows: 32906 Columns: 4
## -- Column specification -----
## Delimiter: ","
## chr (1): application number
## dbl (2): ego_examiner_id, alter_examiner_id
## date (1): advice_date
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
applications
## # A tibble: 2,018,477 x 16
     application_number filing_date examiner_name_last examiner_name_first
##
      <chr>>
                        <date>
                                    <chr>
                                                       <chr>>
## 1 08284457
                        2000-01-26 HOWARD
                                                       JACQUELINE
## 2 08413193
                        2000-10-11 YILDIRIM
                                                       BEKIR
## 3 08531853
                        2000-05-17 HAMILTON
                                                       CYNTHIA
## 4 08637752
                        2001-07-20 MOSHER
                                                       MARY
                                                       MICHAEL
## 5 08682726
                        2000-04-10 BARR
## 6 08687412
                        2000-04-28 GRAY
                                                       LINDA
## 7 08716371
                        2004-01-26 MCMILLIAN
                                                       KARA
## 8 08765941
                        2000-06-23 FORD
                                                       VANESSA
## 9 08776818
                        2000-02-04 STRZELECKA
                                                       TERESA
## 10 08809677
                        2002-02-20 KIM
                                                       SUN
## # ... with 2,018,467 more rows, and 12 more variables:
      examiner_name_middle <chr>, examiner_id <dbl>, examiner_art_unit <dbl>,
## #
      uspc_class <chr>, uspc_subclass <chr>, patent_number <chr>,
      patent_issue_date <date>, abandon_date <date>, disposal_type <chr>,
```

appl_status_code <dbl>, appl_status_date <chr>, tc <dbl>

#

edges

```
## # A tibble: 32,906 x 4
##
      application_number advice_date ego_examiner_id alter_examiner_id
##
      <chr>
                          <date>
                                                 <dbl>
                                                                    <dbl>
   1 09402488
                          2008-11-17
                                                 84356
                                                                    66266
##
    2 09402488
                                                 84356
##
                          2008-11-17
                                                                    63519
##
    3 09402488
                          2008-11-17
                                                 84356
                                                                    98531
##
   4 09445135
                          2008-08-21
                                                92953
                                                                    71313
##
   5 09445135
                          2008-08-21
                                                92953
                                                                    93865
##
   6 09445135
                          2008-08-21
                                                 92953
                                                                    91818
##
   7 09479304
                          2008-12-15
                                                 61767
                                                                    69277
                          2008-12-15
##
   8 09479304
                                                 61767
                                                                    92446
## 9 09479304
                          2008-12-15
                                                 61767
                                                                    66805
## 10 09479304
                          2008-12-15
                                                 61767
                                                                    70919
## # ... with 32,896 more rows
```

Question 1

Get gender for examiners

We'll get gender based on the first name of the examiner, which is recorded in the field examiner_name_first. We'll use library gender for that, relying on a modified version of their own example.

Note that there are over 2 million records in the applications table – that's because there are many records for each examiner, as many as the number of applications that examiner worked on during this time frame. Our first step therefore is to get all *unique* names in a separate list examiner_names. We will then guess gender for each one and will join this table back to the original dataset. So, let's get names without repetition:

```
# install_genderdata_package() # only run this line the first time you use the package, to get data for
# get a list of first names without repetitions
examiner_names <- applications %>%
    distinct(examiner_name_first)
examiner names
```

```
## # A tibble: 2,595 x 1
##
      examiner_name_first
##
      <chr>
   1 JACQUELINE
##
##
   2 BEKIR
##
   3 CYNTHIA
##
   4 MARY
##
  5 MICHAEL
  6 LINDA
##
##
    7 KARA
##
  8 VANESSA
## 9 TERESA
## 10 SUN
## # ... with 2,585 more rows
```

Now let's use function gender() as shown in the example for the package to attach a gender and probability to each name and put the results into the table examiner_names_gender

```
# get a table of names and gender
examiner_names_gender <- examiner_names %>%
   do(results = gender(.$examiner_name_first, method = "ssa")) %>%
   unnest(cols = c(results), keep_empty = TRUE) %>%
   select(
        examiner_name_first = name,
        gender,
        proportion_female
)
```

```
## # A tibble: 1,822 x 3
##
      examiner_name_first gender proportion_female
##
      <chr>
                          <chr>
                                             <dbl>
##
  1 AARON
                                            0.0082
                          male
##
   2 ABDEL
                          male
##
  3 ABDOU
                          male
                                            0
## 4 ABDUL
                          male
                                            0
## 5 ABDULHAKIM
                                            0
                          male
## 6 ABDULLAH
                          male
                                            0
## 7 ABDULLAHI
                          male
                                            0
## 8 ABIGAIL
                          female
                                            0.998
## 9 ABIMBOLA
                          female
                                            0.944
                                            0.0031
## 10 ABRAHAM
                          male
## # ... with 1,812 more rows
```

Vcells 49958911 381.2 93200558 711.1 80274432 612.5

Finally, let's join that table back to our original applications data and discard the temporary tables we have just created to reduce clutter in our environment.

```
# remove extra colums from the gender table
examiner_names_gender <- examiner_names_gender %>%
    select(examiner_name_first, gender)

# joining gender back to the dataset
applications <- applications %>%
    left_join(examiner_names_gender, by = "examiner_name_first")

# cleaning up
rm(examiner_names)
rm(examiner_names_gender)
gc()

## used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 4752052 253.8 8320468 444.4 5177110 276.5
```

Guess the examiner's race

We'll now use package wru to estimate likely race of an examiner. Just like with gender, we'll get a list of unique names first, only now we are using surnames.

```
examiner_surnames <- applications %>%
  select(surname = examiner_name_last) %>%
  distinct()
examiner_surnames
## # A tibble: 3,806 x 1
##
      surname
##
      <chr>
##
   1 HOWARD
##
    2 YILDIRIM
   3 HAMILTON
##
##
   4 MOSHER
##
   5 BARR
    6 GRAY
##
  7 MCMILLIAN
##
  8 FORD
## 9 STRZELECKA
## 10 KIM
## # ... with 3,796 more rows
We'll follow the instructions for the package outlined here https://github.com/kosukeimai/wru.
examiner_race <- predict_race(voter.file = examiner_surnames, surname.only = T) %>%
  as_tibble()
## [1] "Proceeding with surname-only predictions..."
## Warning in merge_surnames(voter.file): Probabilities were imputed for 698
## surnames that could not be matched to Census list.
examiner_race
## # A tibble: 3,806 x 6
##
      surname
                 pred.whi pred.bla pred.his pred.asi pred.oth
##
      <chr>
                    <dbl>
                              <dbl>
                                       <dbl>
                                                 <dbl>
                                                          <dbl>
##
   1 HOWARD
                   0.643
                            0.295
                                     0.0237
                                              0.005
                                                         0.0333
##
   2 YILDIRIM
                   0.861
                            0.0271
                                     0.0609
                                              0.0135
                                                         0.0372
##
    3 HAMILTON
                   0.702
                            0.237
                                     0.0245
                                              0.0054
                                                         0.0309
##
   4 MOSHER
                   0.947
                            0.00410
                                     0.0241
                                              0.00640
                                                         0.0185
##
  5 BARR
                   0.827
                            0.117
                                     0.0226
                                              0.00590
                                                         0.0271
##
   6 GRAY
                   0.687
                            0.251
                                     0.0241
                                              0.0054
                                                         0.0324
##
   7 MCMILLIAN
                   0.359
                            0.574
                                     0.0189
                                              0.00260
                                                         0.0463
##
  8 FORD
                   0.620
                            0.32
                                     0.0237
                                              0.0045
                                                         0.0313
  9 STRZELECKA
                   0.666
                            0.0853
                                     0.137
                                               0.0797
                                                         0.0318
## 10 KIM
                   0.0252
                            0.00390
                                     0.00650
                                              0.945
                                                         0.0198
## # ... with 3,796 more rows
```

As you can see, we get probabilities across five broad US Census categories: white, black, Hispanic, Asian and other. (Some of you may correctly point out that Hispanic is not a race category in the US Census, but these are the limitations of this package.)

Our final step here is to pick the race category that has the highest probability for each last name and then join the table back to the main applications table. See this example for comparing values across columns: https://www.tidyverse.org/blog/2020/04/dplyr-1-0-0-rowwise/. And this one for case_when() function: https://dplyr.tidyverse.org/reference/case_when.html.

```
examiner_race <- examiner_race %>%
  mutate(max_race_p = pmax(pred.asi, pred.bla, pred.his, pred.oth, pred.whi)) %>%
  mutate(race = case_when(
    max_race_p == pred.asi ~ "Asian",
    max_race_p == pred.bla ~ "black",
    max_race_p == pred.his ~ "Hispanic",
    max_race_p == pred.oth ~ "other",
    max_race_p == pred.whi ~ "white",
    TRUE ~ NA_character_
    ))
  examiner_race
```

```
## # A tibble: 3,806 x 8
##
      surname
                 pred.whi pred.bla pred.his pred.asi pred.oth max_race_p race
##
      <chr>
                    <dbl>
                              <dbl>
                                       <dbl>
                                                 <dbl>
                                                          dbl>
                                                                      <dbl> <chr>
##
   1 HOWARD
                   0.643
                            0.295
                                     0.0237
                                              0.005
                                                         0.0333
                                                                      0.643 white
   2 YILDIRIM
                   0.861
                            0.0271
                                     0.0609
                                              0.0135
                                                         0.0372
                                                                     0.861 white
##
##
    3 HAMILTON
                   0.702
                            0.237
                                     0.0245
                                              0.0054
                                                         0.0309
                                                                     0.702 white
  4 MOSHER
##
                   0.947
                            0.00410
                                     0.0241
                                              0.00640
                                                         0.0185
                                                                     0.947 white
## 5 BARR
                   0.827
                            0.117
                                     0.0226
                                              0.00590
                                                         0.0271
                                                                     0.827 white
##
  6 GRAY
                   0.687
                            0.251
                                     0.0241
                                              0.0054
                                                         0.0324
                                                                     0.687 white
   7 MCMILLIAN
                   0.359
                            0.574
                                     0.0189
                                              0.00260
                                                         0.0463
                                                                      0.574 black
## 8 FORD
                   0.620
                                     0.0237
                                              0.0045
                                                         0.0313
                                                                     0.620 white
                            0.32
## 9 STRZELECKA
                   0.666
                            0.0853
                                     0.137
                                              0.0797
                                                         0.0318
                                                                      0.666 white
                   0.0252 0.00390
                                     0.00650 0.945
                                                         0.0198
                                                                     0.945 Asian
## 10 KIM
## # ... with 3,796 more rows
```

Let's join the data back to the applications table.

```
# removing extra columns
examiner_race <- examiner_race %>%
    select(surname,race)

applications <- applications %>%
    left_join(examiner_race, by = c("examiner_name_last" = "surname"))

rm(examiner_race)
rm(examiner_surnames)
gc()
```

Ncells 5091281 272.0 8320468 444.4 6109947 326.4 ## Vcells 53643638 409.3 93200558 711.1 92639527 706.8

used (Mb) gc trigger (Mb) max used

Examiner's tenure

##

To figure out the timespan for which we observe each examiner in the applications data, let's find the first and the last observed date for each examiner. We'll first get examiner IDs and application dates in a

separate table, for ease of manipulation. We'll keep examiner ID (the field examiner_id), and earliest and latest dates for each application (filing_date and appl_status_date respectively). We'll use functions in package lubridate to work with date and time values.

```
examiner_dates <- applications %>%
  select(examiner_id, filing_date, appl_status_date)
examiner_dates
```

```
## # A tibble: 2,018,477 x 3
##
      examiner_id filing_date appl_status_date
##
            <dbl> <date>
                              <chr>>
            96082 2000-01-26 30jan2003 00:00:00
##
   1
##
   2
            87678 2000-10-11 27sep2010 00:00:00
            63213 2000-05-17 30mar2009 00:00:00
##
  3
##
  4
            73788 2001-07-20 07sep2009 00:00:00
            77294 2000-04-10
                              19apr2001 00:00:00
## 5
##
   6
            68606 2000-04-28
                              16jul2001 00:00:00
##
  7
            89557 2004-01-26
                              15may2017 00:00:00
##
   8
            97543 2000-06-23
                              03apr2002 00:00:00
                              27nov2002 00:00:00
##
  9
            98714 2000-02-04
## 10
            65530 2002-02-20
                              23mar2009 00:00:00
## # ... with 2,018,467 more rows
```

The dates look inconsistent in terms of formatting. Let's make them consistent. We'll create new variables start_date and end_date.

```
examiner_dates <- examiner_dates %>%
  mutate(start_date = ymd(filing_date), end_date = as_date(dmy_hms(appl_status_date)))
```

Let's now identify the earliest and the latest date for each examiner and calculate the difference in days, which is their tenure in the organization.

```
examiner_dates <- examiner_dates %>%
  group_by(examiner_id) %>%
  summarise(
    earliest_date = min(start_date, na.rm = TRUE),
    latest_date = max(end_date, na.rm = TRUE),
    tenure_days = interval(earliest_date, latest_date) %/% days(1)
    ) %>%
  filter(year(latest_date)<2018)

examiner_dates</pre>
```

```
## # A tibble: 5,625 x 4
##
      examiner_id earliest_date latest_date tenure_days
                                                   <dbl>
##
            <dbl> <date>
                                 <date>
##
  1
            59012 2004-07-28
                                 2015-07-24
                                                    4013
    2
            59025 2009-10-26
                                2017-05-18
                                                    2761
##
            59030 2005-12-12
##
  3
                                2017-05-22
                                                    4179
            59040 2007-09-11
                                2017-05-23
                                                    3542
##
   4
            59052 2001-08-21
                                                    2017
##
   5
                                2007-02-28
```

```
59054 2000-11-10
                                                    5887
## 6
                                2016-12-23
## 7
            59055 2004-11-02 2007-12-26
                                                    1149
           59056 2000-03-24
                                                   6268
## 8
                                2017-05-22
            59074 2000-01-31
                                2017-03-17
                                                   6255
## 9
## 10
            59081 2011-04-21
                                2017-05-19
                                                    2220
## # ... with 5,615 more rows
Joining back to the applications data.
applications <- applications %>%
 left_join(examiner_dates, by = "examiner_id")
rm(examiner_dates)
gc()
              used (Mb) gc trigger
##
                                     (Mb) max used
                                                        (Mb)
## Ncells 5105019 272.7 15041074 803.3 15041074 803.3
## Vcells 66021822 503.8 134384802 1025.3 134253203 1024.3
Question2
# we pick work group 163 and 172
w164 <- subset(applications, grepl("^164", applications$examiner_art_unit))
w164$gender <- factor(w164$gender)
w164$race <- factor(w164$race)</pre>
w241 <- subset(applications, grepl("^241", applications$examiner_art_unit))
w241$gender <- factor(w241$gender)</pre>
w241$race <- factor(w241$race)</pre>
# summary for group 164
summary(w164$gender)
## female
            male
                   NA's
## 41398 38393 13551
summary(w164$race)
##
      Asian
               black Hispanic
                                 white
##
      21651
                3899
                         1117
                                 66675
summary(w164$tenure_days)
##
      Min. 1st Qu. Median
                                                       NA's
                              Mean 3rd Qu.
                                               Max.
##
       314
              6074
                      6315
                              6128
                                      6338
                                               6350
                                                       1884
```

summry for group 241
summary(w241\$gender)

```
## female male
                   NA's
    2781 13256
                   3554
summary(w241$race)
               black Hispanic
                                  white
##
      Asian
##
      10117
                 848
                          381
                                   8245
summary(w241$tenure_days)
##
      Min. 1st Qu. Median
                               Mean 3rd Qu.
                                               Max.
                                                        NA's
##
       548
              4147
                      5257
                               4688
                                       5911
                                               6335
                                                          75
Race and gender distribution for work group 164 and 241 respectively
```

```
# merge
w164$workgroup <- c('164')
w241$workgroup <- c('241')

merged = union(x = w164,y = w241)</pre>
```

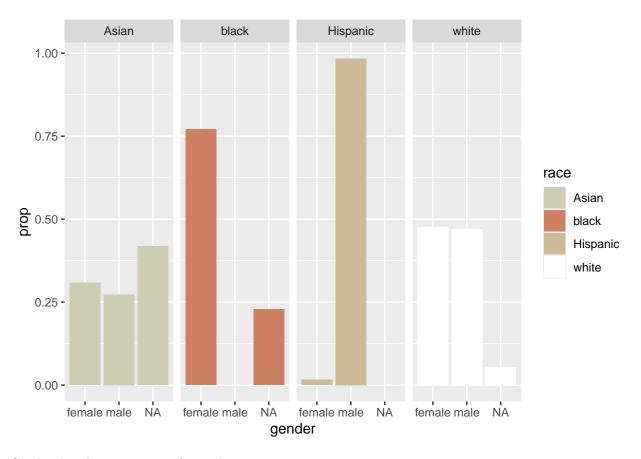
Gender distribution in races for work group 164

'.groups' argument.

```
toPlot<-w164%>%
  group_by(gender, race)%>%
  summarise(n = n())%>%
  group_by(race)%>%
  mutate(prop = n/sum(n))

## 'summarise()' has grouped output by 'gender'. You can override using the
```

```
ggplot(data = toPlot, aes(gender, prop, fill = race)) +
  geom_col() +
  facet_grid(~race)+
  scale_fill_manual(values = c("lightyellow3","lightsalmon3", "wheat3","white"))
```

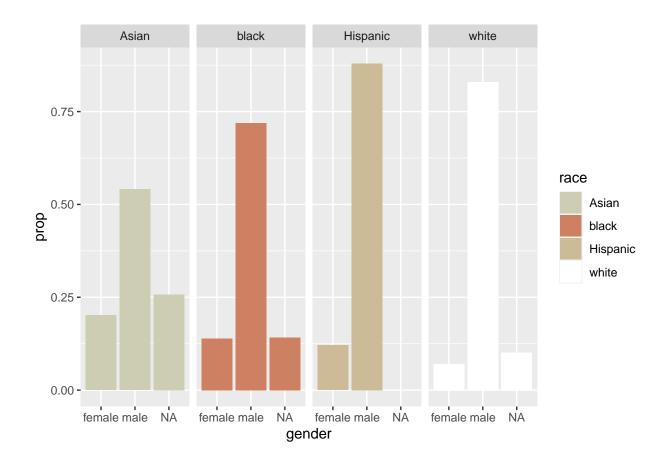


Gender distribution in races for work group 241

```
toPlot<-w241 %>%
  group_by(gender, race)%>%
  summarise(n = n())%>%
  group_by(race)%>%
  mutate(prop = n/sum(n))
```

'summarise()' has grouped output by 'gender'. You can override using the
'.groups' argument.

```
ggplot(data = toPlot, aes(gender, prop, fill = race)) +
  geom_col() +
  facet_grid(~race)+
  scale_fill_manual(values = c("lightyellow3","lightsalmon3", "wheat3","white"))
```

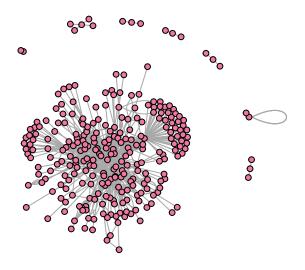


Question 3

Create node lists for each work group

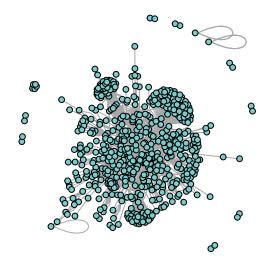
```
# join selected work groups with edges list
edges <- drop_na(edges, ego_examiner_id)</pre>
edges <-drop_na(edges, alter_examiner_id)</pre>
w164_2 <- inner_join(w164, edges, by = "application_number", copy = FALSE)
w241_2 <- inner_join(w241, edges, by = "application_number", copy = FALSE)
# nodes dataframe of work groups and merge them
w164_nodes1 <- w164_2 %>%
  distinct(ego_examiner_id) %>%
  rename(ID = ego_examiner_id)
w164_nodes2 <- w164_2 %>%
  distinct(alter_examiner_id) %>%
  rename(ID = alter_examiner_id)
w241_nodes1 <- w241_2 %>%
  distinct(ego_examiner_id) %>%
  rename(ID = ego_examiner_id)
w241_nodes2 <- w241_2 %>%
  distinct(alter_examiner_id) %>%
```

```
rename(ID = alter_examiner_id)
# merge the two dataframes for each work goup
w164_nodes <- union_all(w164_nodes1, w164_nodes2)</pre>
w241_nodes <- union_all(w241_nodes1, w241_nodes2)</pre>
w164_nodes <- unique(w164_nodes)</pre>
w241_nodes <- unique(w241_nodes)</pre>
head(w164_nodes, 5)
## # A tibble: 5 x 1
##
        ID
##
     <dbl>
## 1 91688
## 2 97910
## 3 75775
## 4 70204
## 5 71120
Create final edge list
w164 edges <- w164 2 %>%
  select(ego_examiner_id, alter_examiner_id)
w241_edges <- w241_2 %>%
  select(ego_examiner_id, alter_examiner_id)
head(w164_edges, 5)
## # A tibble: 5 x 2
    ego_examiner_id alter_examiner_id
##
               <dbl>
                                   <dbl>
## 1
               91688
                                   71059
## 2
                                   67669
               91688
## 3
               97910
                                   59738
## 4
               97910
                                   99004
## 5
               97910
                                   67669
g_w164 <- graph_from_data_frame(w164_edges, directed=FALSE)</pre>
g_w241 <- graph_from_data_frame(w241_edges, directed=FALSE)</pre>
Plot vertex graph for work group 164
plot(g_w164, layout=layout.fruchterman.reingold,
   vertex.size = 5,
    vertex.label = NA,
   vertex.color = "palevioletred2")
```



Plot vertex graph for work group 241

```
plot(g_w241, layout=layout.fruchterman.reingold,
    vertex.size = 5,
    vertex.label = NA,
    vertex.color = "darkslategray3")
```



Calculate centralities

```
# betweenness
bc_w164 <- sort(betweenness(g_w164), decreasing = TRUE)</pre>
bc_w241 <- sort(betweenness(g_w241), decreasing = TRUE)</pre>
# degree
dg_w164 <- sort(degree(g_w164), decreasing = TRUE)</pre>
dg_w241 <- sort(degree(g_w241), decreasing = TRUE)</pre>
# closeness
cc_w164 <- sort(closeness(g_w164), decreasing = TRUE)</pre>
cc_w241 <- sort(closeness(g_w241), decreasing = TRUE)</pre>
print("top 5 of betwenness centrality for work group 164")
## [1] "top 5 of betwenness centrality for work group 164"
print(head(bc_w164,5))
##
       72882
                  87897
                            97910
                                       66266
                                                  73260
## 12338.868 9951.339 6984.072 4250.095 3709.533
print("top 5 of betwenness centrality for work group 241")
```

[1] "top 5 of betwenness centrality for work group 241"

```
print(head(bc_w241,5))
##
      62919
               62038
                        91499
                                 95183
                                           61485
## 67440.85 21071.27 16727.50 15711.58 15142.94
print("top 5 of degree centrality for work group 164")
## [1] "top 5 of degree centrality for work group 164"
print(head(dg_w164,5))
## 97910 72882 87897 59738 99004
           154
     170
                  96
                        83
print("top 5 of degree centrality for work group 241")
## [1] "top 5 of degree centrality for work group 241"
print(head(dg_w241,5))
## 62919 67226 92078 61485 71764
                       101
     178
           175
                 132
print("top 5 of closeness centrality for work group 164")
## [1] "top 5 of closeness centrality for work group 164"
print(head(cc_w164,15))
##
       97706
                 76749
                           75119
                                     67435
                                                84944
                                                          59658
                                                                    80908
                                                                               67013
## 1.0000000 1.0000000 1.0000000 1.0000000 0.5000000 0.5000000 0.5000000
       97072
                 86403
                           68637
                                     97834
                                                95085
## 0.3333333 0.3333333 0.3333333 0.3333333 0.3333333 0.3333333 0.3333333
print("top 5 of closeness centrality for work group 241")
## [1] "top 5 of closeness centrality for work group 241"
print(head(cc_w241,15))
## 91652 93841 66060 97883 63765 72734 70399 61007 66905 96538 64053 97508 75981
##
       1
                         1
                               1
                                     1
                                            1
                                                  1
## 63155 72089
##
       1
```

Pick measures of centrality

I would pick betweenness centrality and degree centrality from the three centralities I calculated above, because in the USPTO case: (1) how many contacts does one examiner have (degree centrality) is a useful information, and (2) the transfer of information among all examiners are important, making the examiner who on the shortest paths between other examiners more important. Additionally, because for work group 241, there are many examiners who are of the highest closeness centrality, the advantage of having the highest closeness centrality is not very strong in my specific case.