

## Module-4

### Brute force approach

It is a fundamental method in problem solving that involves systematically trying every possible solutions to find the correct one.

~~Ex~~ Eg: Pad lock, Password guessing

characteristics of brute force sol<sup>n</sup>:-

- (i) exhaustive search
- (ii) simplicity
- (iii) inefficiency
- (iv) guaranteed sol<sup>n</sup>

### Pad lock

It involves 1000 combinations., 3 digits, 0-9 characters.

Start with 000

Increment sequentially

Stop when lock opens.

def Padlock(Key)

for combination in range(1000)

guess = f" {combination:03}"

Print (f"trying combination {guess}")

If guess == Key

Print (f"padlock open's at {guess}")

break

Padlock (123)

Out: Trying combination 000  
" 001  
" 002 123

Padlock opens at 123

Password guessing

import itertools

import strings

```
def check_password (Password)
    character = string.printable
    for guess in itertools.product(character, repeat=3):
        guess = ''.join(guess)
        Print (f"Trying password: {guess}")
        If guess == Password:
            Print (f"password found: {guess}")
            return
```

Password = "Dog"

check\_password (password)

Out: Trying password: aaa

Trying password: Dog

Password found: Dog

Divide and conquer approach.

Solve problems efficiently.

- (i) divide (division continues recursively until the sub problems are simple enough to solve directly.)
- (ii) conquer
- (iii) Merge

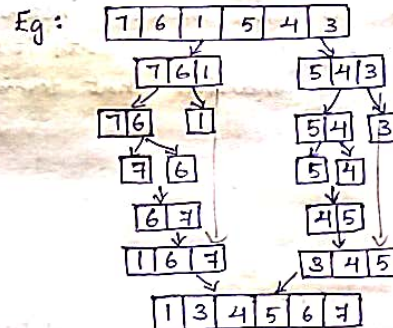
Merge and sort

input: an unsorted array of given

Process

divide array into two halves left and right  
recursively sort left and right.  
Merge left and right into sorted array.

Output: a sorted array





## Dynamic Programming

D.P is a method for solving problems by breaking them down into smaller overlapping sub problems, solving each sub problem just once, and storing their solutions. It is particularly useful for optimisation problems where the problem can be divided into simpler sub-problems that are solved independently and combine to form a solution to the original problem.

### Key Properties/Fundamental Principles of D.P

Optimal Substructure

Overlapping sub problems

Example:- fibonacci series/sequence

To find  $\text{fibonacci}(5)$ , you need the values of  $\text{fibonacci}(4)$  and  $\text{fibonacci}(3)$ . To compute the  $\text{fibonacci}(4)$  of  $n=4$  you need  $\text{fibonacci}(2)$  and  $\text{fibonacci}(3)$ . Here,  $\text{fibonacci}(3)$  is computed multiple times when calculating different fibonacci numbers.

### Without dynamic Programming

To compute  $\text{fibonacci}(5)$ , you should calculate  $\text{fibonacci}(3)$  twice.

This redundancy leads to a lot of repeated work.

### With dynamic Programming

To compute  $\text{fibonacci}(3)$  once and stores its result. Whenever you need  $\text{fibonacci}(3)$  again, you call the stored result instead of recalculating it. This helps to avoid unnecessary calculations and speeds up the process.

Compute and reuse - majorly uses two operations

Steps involved in D.P.

Break down complex problems to sub-problems.  
Find the optimal solutions to the sub-problem.  
Store the result of sub problem.

Reuse the result of sub problems to avoid repeated calculations.

Finally find the result of complex problem.

### Approaches to In D.P

Memoization (top-down approach)

Tabulation (bottom-up approach)

### Greedy Approach

Greedy approach is the most intuitive method in algorithm design. When placed with a problem that requires a series of decisions. A greedy algorithm makes the best choice available at each step, focusing solely on the immediate situation without considering future consequences.

This approach simplifies problem by reducing it into a series of smaller sub-problems each requiring fewer decisions. Greedy algorithm exists in problems with optimal substructure where the problem can be broken into smaller solvable components.

Greedy algorithm approach properties

Greedy solution could be implemented only if the problem statement follows two properties.

- 1) Greedy choice property
- 2) Optimal substructure

Key characteristics of greedy approach.

- 1) Local optimisation (best possible at <sup>each</sup> step)
- 2) Irrevocable decisions (no backtracking or reconsidering)
- 3) Problem specific characteristic
- 4) Optimal solution for specific problems.
- 5) Efficiency

Eg: - Coin exchange.

Motivation for greedy approach

Simplicity and ease of implementation.  
Straight forward logic  
Minimum requirements

2) Efficiency in time and space

- fast execution
- low memory usage

3) \* optimal solutions for specific problems

- Greedy choice property
- Optimal substructure

4) Real world applicability

Practical applications

Quick near optimal solutions.

Advantages and disadvantages of greedy approach.

Advantages - Simplicity, Speed, optimal for certain problems.

Disadvantages - Sub optimal solutions

Global optimum ~~can~~ be reached by making local optimum solutions as assumptions.

Irrevocable decisions

Lack of backtracking

Eg: task completion problem

Q Given an array of positive integers each indicating completion time for a task. Find the maximum number of tasks that can be completed in a limited amount of time that you have.

Eg: completion times = [2, 3, 1, 4, 6]  
available time = 8

Ans) Steps involved

Sort task (arrange task in ascending order.)  
Iterate and track (add task sequentially as long as the total time doesn't exceed the limit and update the task count accordingly.)

Add task with time 1: total time = 1  
task count = 1

Add task with time 2: total time = 3  
task count = 2

3+3  
1+3  
5+1=6

Add task with time 1, 3: total time = 6  
task count = 3

Next task with time 4 will exceed available time, so loop breaks.

Max. no. of tasks that can be completed in 8 units of time is 3.

```
def max_task(completion_times, available_time):
```

```
    completion_times.sort() # to sort array
```

```
    total_time = 0
```

```
    task_count = 0
```

```
    for time in completion_times:
```

```
        if total_time + time <= available_time:
```

```
            total_time += time
```

```
            task_count += 1
```

```
        else:
```

```
            break
```

```
    return task_count
```