

### Instructions

- You are not allowed to use concepts not covered in class or from sections beyond *Control Flow*.
- Make sure your code is clean, well-organized, uses meaningful variable names, includes useful comments, and is efficient.
- Make sure you edit the sections (#1 mandatory, #2 if applicable, and #3 optional) in the given `notes.txt` file as appropriate. In section #1, for each problem, state its goal in your own words and describe your approach to solve the problem along with any issues you encountered and if/how you managed to solve those issues.

**Goal:** Implement simple programs using control-flow (ie, branch and loop) statements.

**Problem 1.** (*Quadratic Equation*) Write a program called `quadratic.py` (a variant of the one we discussed in class) that receives `a` (float), `b` (float), and `c` (float) as command-line inputs, and writes as standard output the roots of the quadratic equation  $ax^2 + bx + c = 0$ . Your program should report the message “Value of `a` must not be 0” if `a` = 0, and the message “Value of discriminant must not be negative” if  $b^2 - 4ac < 0$ .

```
x ~/workspace/controlflow_programs
$ python3 quadratic.py 0 1 -3
Value of a must not be 0
$ python3 quadratic.py 1 1 1
Value of discriminant must not be negative
$ python3 quadratic.py 1 -5 6
3.0 2.0
```

**Problem 2.** (*Wind Chill*) Given the temperature `t` (in Fahrenheit) and the wind speed `v` (in miles per hour), the National Weather Service defines the effective temperature (the wind chill) to be

$$w = 35.74 + 0.6215t + (0.4275t - 35.75)v^{0.16}.$$

Write a program called `wind_chill.py` that receives `t` (float) and `v` (float) as command-line inputs, and writes the wind chill `w` as standard output. Your program should report the message “Value of `t` must be  $\leq 50$  F” if `t` > 50, and the message “Value of `v` must be  $> 3$  mph” if `v`  $\leq$  3.

```
x ~/workspace/controlflow_programs
$ python3 wind_chill.py 51 15
Value of t must be <= 50 F
$ python3 wind_chill.py 32 3
Value of v must be > 3 mph
$ python3 wind_chill.py 32 15
21.588988890532022
```

**Problem 3.** (*Day of the Week*) Write a program called `day_of_week.py` that receives `m` (int), `d` (int), and `y` (int) as command-line inputs, computes the day of the week (0 for Sunday, 1 for Monday, and so on) `dow` using the formulae below, and writes the day as a string (“Sunday”, “Monday”, and so on) as standard output.

$$\begin{aligned} y_0 &= y - (14 - m)/12 \\ x_0 &= y_0 + y_0/4 - y_0/100 + y_0/400 \\ m_0 &= m + 12 \times ((14 - m)/12) - 2 \\ dow &= (d + x_0 + 31 \times m_0/12) \bmod 7 \end{aligned}$$

```
x ~/workspace/controlflow_programs
$ python3 day_of_week.py 3 14 1879
Friday
$ python3 day_of_week.py 4 12 1882
Wednesday
```

**Problem 4.** (*Six-sided Die*) Write a program called `die.py` that simulates the roll of a six-sided die, and writes as standard output the pattern on the top face.

```
x ~/workspace/controlflow_programs
$ python3 die.py
*
*
*
*
$ python3 die.py
*
*
```

**Problem 5.** (*Playing Card*) Write a program called `card.py` that simulates the selection of a random card from a standard deck of 52 playing cards, and writes it as standard output.

```
x ~/workspace/controlflow_programs
$ python3 card.py
3 of Clubs
$ python3 card.py
Ace of Spades
```

**Problem 6.** (*Dragon Curve*) The instructions for drawing a dragon curve are strings of the characters *F*, *L*, and *R*, where *F* means “draw a line while moving 1 unit forward”, *L* means “turn left”, and *R* means “turn right”. The key to solving this problem is to note that a curve of order *n* is a curve of order *n* – 1 followed by an *L* followed by a curve of order *n* – 1 traversed in reverse order, replacing *L* with *R* and *R* with *L*. Write a program called `dragon_curve.py` that receives *n* (int) as command-line input, and writes as standard output the instructions for drawing a dragon curve of order *n*.

```
x ~/workspace/controlflow_programs
$ python3 dragon_curve.py 0
F
$ python3 dragon_curve.py 1
FLF
$ python3 dragon_curve.py 2
FLFLFRF
$ python3 dragon_curve.py 3
FLFLFRFLFLFRFRF
```

**Problem 7.** (*Greatest Common Divisor*) Write a program called `gcd.py` that receives *p* (int) and *q* (int) as command-line inputs, and writes as standard output the greatest common divisor (GCD) of *p* and *q*.

```
x ~/workspace/controlflow_programs
$ python3 gcd.py 408 1440
24
$ python3 gcd.py 21 22
1
```

**Problem 8.** (*Root Finding*) Write a program called `root.py` (a variant of the `sqrt.py` program we discussed in class) that receives  $k$  (int),  $c$  (float), and  $\text{epsilon}$  (float) as command-line inputs, and writes as standard output the  $k$ th root of  $c$ , up to  $\text{epsilon}$  decimal places.

```
x ~/workspace/controlflow_programs
$ python3 root.py 3 2 1e-15
1.2599210498948732
$ python3 root.py 3 27 1e-15
3.0
```

**Problem 9.** (*Sum of Powers*) Write a program called `sum_of_powers.py` that receives  $n$  (int) and  $k$  (int) as command-line inputs, and writes as standard output the sum  $1^k + 2^k + \dots + n^k$ .

```
x ~/workspace/controlflow_programs
$ python3 sum_of_powers.py 15 1
120
$ python3 sum_of_powers.py 10 3
3025
```

**Problem 10.** (*Factorial Function*) Write a program called `factorial.py` that receives  $n$  (int) as command-line input, and writes as standard output the value of  $n!$ , which is defined as  $n! = 1 \times 2 \times \dots \times (n - 1) \times n$ . Note that  $0! = 1$ .

```
x ~/workspace/controlflow_programs
$ python3 factorial.py 0
1
$ python3 factorial.py 5
120
```

**Problem 11.** (*Fibonacci Function*) Write a program called `fibonacci.py` that receives  $n$  (int) as command-line input, and writes as standard output the  $n$ th number from the Fibonacci sequence ( $0, 1, 1, 2, 3, 5, 8, 13, \dots$ ).

```
x ~/workspace/controlflow_programs
$ python3 fibonacci.py 10
55
$ python3 fibonacci.py 15
610
```

**Problem 12.** (*Primality Test*) Write a program called `primality_test.py` that receives  $n$  (int) as command-line input, and writes as standard output if  $n$  is a prime number or not.

```
x ~/workspace/controlflow_programs
$ python3 primality_test.py 31
True
$ python3 primality_test.py 42
False
```

**Problem 13.** (*Counting Primes*) Write a program called `prime_counter.py` that receives `n` (int) as command-line input, and writes as standard output the number of primes less than or equal to `n`.

```
x ~/workspace/controlflow_programs
$ python3 prime_counter.py 10
4
$ python3 prime_counter.py 100
25
$ python3 prime_counter.py 1000
168
```

**Problem 14.** (*Perfect Numbers*) A perfect number is a positive integer whose proper divisors add up to the number. For example, 6 is a perfect number since its proper divisors 1, 2, and 3 add up to 6. Write a program called `perfect_numbers.py` that receives `n` (int) as command-line input, and writes as standard output the perfect numbers that are less than or equal to `n`.

```
x ~/workspace/controlflow_programs
$ python3 perfect_numbers.py 10
6
$ python3 perfect_numbers.py 1000
6
28
496
```

**Problem 15.** (*Ramanujan Numbers*) Srinivasa Ramanujan was an Indian mathematician who became famous for his intuition for numbers. When the English mathematician G. H. Hardy came to visit him one day, Hardy remarked that the number of his taxi was 1729, a rather dull number. Ramanujan replied, “No, Hardy! It is a very interesting number. It is the smallest number expressible as the sum of two cubes in two different ways.” Verify this claim by writing a program `ramanujan_numbers.py` that receives `n` (int) as command-line input, and writes as standard output all integers less than or equal to `n` that can be expressed as the sum of two cubes in two different ways. In other words, find distinct positive integers `a`, `b`, `c`, and `d` such that  $a^3 + b^3 = c^3 + d^3 \leq n$ .

```
x ~/workspace/controlflow_programs
$ python3 ramanujan_numbers.py 10000
1729 = 1^3 + 12^3 = 9^3 + 10^3
4104 = 2^3 + 16^3 = 9^3 + 15^3
$ python3 ramanujan_numbers.py 40000
1729 = 1^3 + 12^3 = 9^3 + 10^3
4104 = 2^3 + 16^3 = 9^3 + 15^3
13832 = 2^3 + 24^3 = 18^3 + 20^3
39312 = 2^3 + 34^3 = 15^3 + 33^3
32832 = 4^3 + 32^3 = 18^3 + 30^3
20683 = 10^3 + 27^3 = 19^3 + 24^3
```

**Files to Submit:**

1. quadratic.py
2. wind\_chill.py
3. day\_of\_week.py
4. die.py
5. card.py
6. dragon\_curve.py
7. gcd.py
8. root.py
9. sum\_of\_powers.py
10. factorial.py
11. fibonacci.py
12. primality\_test.py
13. prime\_counter.py
14. perfect\_numbers.py
15. ramanujan\_numbers.py
16. notes.txt