

x = branch constraints

x = node constraints

$$\begin{aligned}
 & \exists \mathbf{A}_2 . \exists_{\mathbf{f} \in \mathbf{F}} open_{\mathbf{f},2} . \forall b_2 . \exists \mathbf{A}_1 . \exists_{\mathbf{f} \in \mathbf{F}} open_{\mathbf{f},1} . \forall b_1 . \exists \mathbf{A}_0 . \exists_{\mathbf{f} \in \mathbf{F}} open_{\mathbf{f},0} . \\
 & \bigwedge_{i \in [0..\text{depth}]} \bigwedge_{\mathbf{A} \in \mathbf{O}} \left( \mathbf{A}_i \Rightarrow \bigwedge_{\mathbf{f} \in \text{Cond}_{\mathbf{A}}} open_{\mathbf{f},i} \right) \quad \textcolor{blue}{1} \\
 & \wedge \left( \bigwedge_{i \in [1..\text{depth}]} b_i \Rightarrow \bigwedge_{\mathbf{f} \in \mathbf{G}} \left( open_{\mathbf{f},0} \vee \bigvee_{\substack{\mathbf{A} \in \mathbf{O} \\ \mathbf{f} \in \text{Add}_{\mathbf{A}}}} \mathbf{A}_0 \right) \right) \quad \textcolor{red}{2} \\
 & \wedge \left( \bigwedge_{i \in [1..\text{depth}]} \neg b_i \Rightarrow \bigwedge_{\mathbf{f} \in \mathbf{F} \setminus \mathbf{I}} \neg open_{\mathbf{f},0} \right) \quad \textcolor{red}{3} \\
 & \wedge \bigwedge_{i \in [1..\text{depth}]} \bigwedge_{\mathbf{f} \in \mathbf{F}} \left( \left( open_{\mathbf{f},i} \wedge \neg b_i \wedge \bigwedge_{j \in [1..i-1]} b_j \right) \Rightarrow \left( open_{\mathbf{f},0} \vee \bigvee_{\substack{\mathbf{A} \in \mathbf{O} \\ \mathbf{f} \in \text{Add}_{\mathbf{A}}}} \mathbf{A}_0 \right) \right) \quad \textcolor{red}{4} \\
 & \wedge \bigwedge_{i \in [1..\text{depth}]} \bigwedge_{\mathbf{f} \in \mathbf{F}} \left( \left( open_{\mathbf{f},0} \wedge b_i \wedge \bigwedge_{j \in [1..i-1]} \neg b_j \right) \Rightarrow \left( open_{\mathbf{f},i} \vee \bigvee_{\substack{\mathbf{A} \in \mathbf{O} \\ \mathbf{f} \in \text{Add}_{\mathbf{A}}}} \mathbf{A}_i \right) \right) \quad \textcolor{red}{5} \\
 & \wedge \bigwedge_{i \in [1..\text{depth}]} \bigwedge_{\mathbf{f} \in \mathbf{F}} \left( \left( open_{\mathbf{f},i} \wedge \neg b_i \wedge \bigwedge_{j \in [1..i-1]} b_j \right) \Rightarrow \bigwedge_{\substack{\mathbf{A} \in \mathbf{O} \\ \mathbf{f} \in \text{Del}_{\mathbf{A}}}} \neg \mathbf{A}_0 \right) \quad \textcolor{red}{6} \\
 & \wedge \bigwedge_{i \in [1..\text{depth}]} \bigwedge_{\mathbf{f} \in \mathbf{F}} \left( \left( open_{\mathbf{f},0} \wedge b_i \wedge \bigwedge_{j \in [1..i-1]} \neg b_j \right) \Rightarrow \bigwedge_{\substack{\mathbf{A} \in \mathbf{O} \\ \mathbf{f} \in \text{Del}_{\mathbf{A}}}} \neg \mathbf{A}_i \right) \quad \textcolor{red}{7} \\
 & \wedge \bigwedge_{i \in [0..\text{depth}]} \bigwedge_{\mathbf{A} \in \mathbf{O}} \bigwedge_{\mathbf{f} \in (\text{Add}_{\mathbf{A}} \cup \text{Cond}_{\mathbf{A}})} \bigwedge_{\substack{\mathbf{B} \in \mathbf{O} \\ \mathbf{A} \neq \mathbf{B} \wedge \mathbf{f} \in \text{Del}_{\mathbf{B}}}} (\neg \mathbf{A}_i \vee \neg \mathbf{B}_i) \quad \textcolor{blue}{8}
 \end{aligned}$$