

1.

$$a) \sum_n \sum_n \alpha_{dn} (x_{dn} - u_d^T v_n)^2 + \lambda_u \sum_d u_d^T u_d + \lambda_v + \lambda_v \sum_d u_d^T u_d + \lambda_v \sum_n v_n^T v_n$$

$$= \sum_n \sum_n (\alpha_{dn} x_{dn}^2 - \alpha_{dn} 2 x_{dn} u_d^T v_n + \alpha_{dn} (u_d^T v_n)^2) + \lambda_u \sum_d u_d^T u_d + \lambda_v \sum_n v_n^T v_n$$

$$= 0 \circ (X - U^T V)^2 + \lambda_u U^T U + \lambda_v V^T V$$

$$\begin{aligned} \frac{dU}{dt} &= 0 \circ (-2 V (X - V U^T)) + \lambda_u (U + U^T) \\ &= (0 \circ) \circ (-2 V (X - V U^T)) + 0 \circ (2 V^2) + \lambda_u (U + U^T) \\ &= \frac{(0 \circ) \circ (-2 V (X - V U^T))}{\lambda_u} + \frac{0 \circ (2 V^2)}{\lambda_u} + U + U^T \\ &= \frac{0 \circ (2 V^2)}{\lambda_u} + U + U^T \end{aligned}$$

$$\begin{aligned} \frac{dV}{dt} &= 0 \circ (-2 U^T (X - V U^T)) + \lambda_v (V + V^T) \\ &= 0 \circ (2 U^{2T}) + \lambda_v (V + V^T) \\ &= \frac{0 \circ (2 U^{2T})}{\lambda_v} + V + V^T \end{aligned}$$

V^2 and U^2 are not defined so something must be very wrong...