

Four

2c)	$Y=0$	$Y=1$	$Y=2$
$X_1=1 \quad X_2=0$	0.08	0.18	0.03
$X_1=1 \quad X_2=1$	0.04	0.03	0.12
$X_1=1 \quad X_2=2$	0.16	0.03	0.09
$X_1=0 \quad X_2=0$	0.08	0.03	0.00
$X_1=0 \quad X_2=1$	0.00	0.03	0.06
$X_1=0 \quad X_2=2$	0.04	0.00	0.00

Bayes error is the probability that the true value is not the most probable

So let  $v_c$  be the vector that matches  $Y$

$$v_c = (X_1, X_2)$$

$$\begin{aligned} P(v_c \neq Y) &= P(v_c \neq Y) \\ &= \sum_{X_1=0}^1 \sum_{X_2=0}^2 P(Y=v_c) \cap (X_1 \neq x_1 \vee X_2 \neq x_2) \end{aligned}$$

$$= (0.08 + 0.03 + 0.04 + 0.03 + 0.03 + 0.09 + 0.03 + 0.03)$$

$$= 0.36$$