

X-43 Stabilizer Analysis: Dan Lawson

Perform Stability and Forces analysis for AoA = 4 deg

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%% Constants and Variable Initialization
% Variables
wedge_angle = [2.7, 3.07, 11.5, 0, 13.9];
stab_ang = linspace(5, 40, 20);
x_23 = 1.83;
Y = 0.2225;
x_2 = x_23 - Y / tan(deg2rad(11.5));
x_3 = x_23 - x_2;

x = [3.66, x_2, x_3, 0.762, 1.068];
AoA_sweep = linspace(-2, 16, 19);
M_inf = 7;

% General Constants
gamma = 1.362;
T_inf = 225.5; % K
P_inf = 1397; % Pa
V_inf = 2107; % m/s
altitude = 28974; % m

for j = 7

    for i = 1:length(wedge_angle)

        if i == 1
            % Stage 1
            if AoA_sweep(j) <= wedge_angle(i)
                theta = (wedge_angle(i) - AoA_sweep(j));
                [P_2, T_2, M2, beta] = oblique(theta, M_inf, P_inf, T_inf, gamma);
                M(i) = M2;
                T(i) = T_2;
                P(i) = P_2;
            elseif AoA_sweep(j) > wedge_angle(i)
                theta = (AoA_sweep(j) - wedge_angle(i));
                [P_2, T_2, M2] = PM_sol(theta, M_inf, P_inf, T_inf, gamma);
                M(i) = M2;
                T(i) = T_2;
                P(i) = P_2;
            end

            L(i) = P(i) * cos(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
            D(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
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elseif i == 2
    % Stage 2
    if AoA_sweep(j) < 0 && abs(AoA_sweep(j)) > wedge_angle(i)
        theta = (wedge_angle(i) + AoA_sweep(j));
        [P_2, T_2, M2] = PM_sol(theta, M_inf, P_inf, T_inf, gamma);
        M(i) = M2;
        T(i) = T_2;
        P(i) = P_2;
    else
        theta = (AoA_sweep(j) + wedge_angle(i));
        [P_2, T_2, M2, beta] = oblique(theta, M_inf, P_inf, T_inf, gamma);
        M(i) = M2;
        T(i) = T_2;
        P(i) = P_2;
    end

    L(i) = P(i) * cos(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
    D(i) = P(i) * sin(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
elseif i == 3
    % Stage 3
    theta = (wedge_angle(i) - wedge_angle(i - 1));
    [P_2, T_2, M2, beta] = oblique(theta, M(i - 1), P(i - 1), T(i - 1),
gamma);
    M(i) = M2;
    T(i) = T_2;
    P(i) = P_2;

    L(i) = P(i) * cos(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
    D(i) = P(i) * sin(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
elseif i == 4
    % Stage 4
    theta = (wedge_angle(i - 1));
    [P_2, T_2, M2] = PM_sol(theta, M(i - 1), P(i - 1), T(i - 1), gamma);
    M(i) = M2;
    T(i) = T_2;
    P(i) = P_2;

    L(i) = P(i) * cos(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
    D(i) = P(i) * sin(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
elseif i == 5
    % Stage 5
    theta = (wedge_angle(i - 1) + wedge_angle(i));
    [P_2, T_2, M2] = PM_sol(theta, M(i - 1), P(i - 1), T(i - 1), gamma);
    M(i) = M2;

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        T(i) = T_2;
        P(i) = P_2;

        L(i) = P(i) * cos(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
        D(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) /
cos(deg2rad(wedge_angle(i))));
    end

end

for jj = 1:length(stab_ang)

    [P_2, T_2, M2, beta] = oblique(stab_ang(jj), M_inf, P_inf, T_inf, gamma);
    L_w(jj) = 0.5 * x(5) * P_2 * cos(deg2rad(stab_ang(jj))) - P_inf;
    D_w(jj) = 0.5 * x(5) * P_2 * sin(deg2rad(stab_ang(jj)));

end

Lift(j) = sum(L(2:5)) - L(1) + L_w(19);
Drag(j) = sum(D(2:5)) - D(1) + D_w(19);

for ii = 1:length(wedge_angle)
    if ii < 3
        moment(ii) = L(ii) * 0.5 * (x(ii) / cos(deg2rad(wedge_angle(ii))));
    elseif ii >= 3
        moment(ii) = L(ii) * 0.5 * (x(ii) / cos(deg2rad(wedge_angle(ii))))
+ sum(x(2:ii));
    end
end
Moment(j) = moment(1) - (moment(2) + moment(3) + moment(4) + moment(5)) +
(L_w(19)*(x_23 + x(4) + 0.75*x(5)));

LC(j) = Moment(j) / Lift(j);
CG = 1.83;
SM(j) = (LC(j) - CG) / x(1);

end

fprintf(['To achieve positive Static Margin, a Wedge angle of ' ...
' %g deg is required for the stabilizer at AoA = 4 deg'], stab_ang(19))

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To achieve positive Static Margin, a Wedge angle of 38.1579 deg is required for the stabilizer at AoA = 4 deg

