X-43 Stabilizer Analysis: Dan Lawson

Perform Stability and Forces analysis for AoA = 4 deg

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%% Constants and Variable Initialization
% Variables
wedge_angle = [2.7, 3.07, 11.5, 0, 13.9];
 stab_ang = linspace(5, 40, 20);
x_23 = 1.83;
Y = 0.2225;
 x_2 = x_{23} - Y / tan(deg2rad(11.5));
 x 3 = x 23 - x 2;
 x = [3.66, x_2, x_3, 0.762, 1.068];
 AoA\_sweep = linspace(-2, 16, 19);
 M inf = 7;
% General Constants
 gamma = 1.362;
 T inf = 225.5; % K
P_inf = 1397; % Pa
V \text{ inf} = 2107; \% \text{ m/s}
 altitude = 28974; % m
for j = 7
                     for i = 1:length(wedge_angle)
                                         if i == 1
                                                            % Stage 1
                                                             if AoA_sweep(j) <= wedge_angle(i)</pre>
                                                                                 theta = (wedge angle(i) - AoA sweep(j));
                                                                                 [P_2, T_2, M2, beta] = oblique(theta, M_inf, P_inf, T_inf, gamma);
                                                                                 M(i) = M2;
                                                                                 T(i) = T_2;
                                                                                 P(i) = P 2;
                                                             elseif AoA_sweep(j) > wedge_angle(i)
                                                                                 theta = (AoA_sweep(j) - wedge_angle(i));
                                                                                 [P_2, T_2, M2] = PM_sol(theta, M_inf, P_inf, T_inf, gamma);
                                                                                 M(i) = M2;
                                                                                 T(i) = T_2;
                                                                                 P(i) = P 2;
                                                             end
                                                             L(i) = P(i) * cos(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) + cos(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) + cos(deg2rad(AoA_s
 cos(deg2rad(wedge angle(i))));
                                                             D(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i)
 cos(deg2rad(wedge_angle(i))));
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elseif i == 2
                                                                                                             % Stage 2
                                                                                                              if AoA sweep(j) < 0 && abs(AoA sweep(j)) > wedge angle(i)
                                                                                                                                                    theta = (wedge angle(i) + AoA sweep(j));
                                                                                                                                                    [P_2, T_2, M2] = PM_sol(theta, M_inf, P_inf, T_inf, gamma);
                                                                                                                                                   M(i) = M2;
                                                                                                                                                   T(i) = T 2;
                                                                                                                                                   P(i) = P_2;
                                                                                                              else
                                                                                                                                                   theta = (AoA sweep(j) + wedge angle(i));
                                                                                                                                                    [P_2, T_2, M2, beta] = oblique(theta, M_inf, P_inf, T_inf, gamma);
                                                                                                                                                   M(i) = M2;
                                                                                                                                                   T(i) = T 2;
                                                                                                                                                   P(i) = P 2;
                                                                                                              end
                                                                                                                 L(i) = P(i) * cos(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i)) * (x(i) / P(i) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i)) * (x(i) / P(i) + wedge_angl
cos(deg2rad(wedge angle(i))));
                                                                                                               D(i) = P(i) * sin(deg2rad(AoA sweep(j) + wedge angle(i))) * (x(i) / P(i) + wedge angle(i)) * (x(i) / P(i) + wedge angle
cos(deg2rad(wedge_angle(i))));
                                                                         elseif i == 3
                                                                                                             % Stage 3
                                                                                                              theta = (wedge_angle(i) - wedge_angle(i - 1));
                                                                                                               [P_2, T_2, M2, beta] = oblique(theta, M(i - 1), P(i - 1), T(i - 1),
gamma);
                                                                                                             M(i) = M2;
                                                                                                             T(i) = T_2;
                                                                                                              P(i) = P_2;
                                                                                                               L(i) = P(i) * cos(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) / equal (AoA_sweep(j) + wedge_angle(i))) * (x(i) / equal (AoA_sweep(i) + wedge_angle(i))) * (x(i) / equal (AoA_sweep
cos(deg2rad(wedge angle(i))));
                                                                                                               D(i) = P(i) * sin(deg2rad(AoA sweep(j) + wedge angle(i))) * (x(i) / P(i) + wedge angle(i)) * (x(i) / P(i) + wedge angle
cos(deg2rad(wedge angle(i))));
                                                                          elseif i == 4
                                                                                                             % Stage 4
                                                                                                             theta = (wedge angle(i - 1));
                                                                                                               [P_2, T_2, M2] = PM_sol(theta, M(i - 1), P(i - 1), T(i - 1), gamma);
                                                                                                             M(i) = M2;
                                                                                                             T(i) = T_2;
                                                                                                              P(i) = P 2;
                                                                                                               L(i) = P(i) * cos(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i)) * (x(i) / P(i) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i)) * (x(i) / P(i) + wedge_angl
cos(deg2rad(wedge angle(i))));
                                                                                                               D(i) = P(i) * sin(deg2rad(AoA_sweep(j) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i)) * (x(i) / P(i) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i)) * (x(i) / P(i) + wedge_angle(i))) * (x(i) / P(i) + wedge_angle(i)) * (x(i) / P(i) + wedge_angle(
cos(deg2rad(wedge angle(i))));
                                                                         elseif i == 5
                                                                                                             % Stage 5
                                                                                                             theta = (wedge_angle(i - 1) + wedge_angle(i));
                                                                                                               [P 2, T 2, M2] = PM sol(theta, M(i - 1), P(i - 1), T(i - 1), gamma);
                                                                                                             M(i) = M2;
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T(i) = T_2;
                                                        P(i) = P_2;
                                                        L(i) = P(i) * cos(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) *
cos(deg2rad(wedge_angle(i))));
                                                        D(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(j) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i) = P(i) * sin(deg2rad(AoA_sweep(i) - wedge_angle(i))) * (x(i) / P(i)
cos(deg2rad(wedge angle(i))));
                                     end
                  end
                  for jj = 1:length(stab ang)
                                      [P_2, T_2, M2, beta] = oblique(stab_ang(jj), M_inf, P_inf, T_inf, gamma);
                                      L_w(jj) = 0.5 * x(5) * P_2 * cos(deg2rad(stab_ang(jj))) - P_inf;
                                    D w(jj) = 0.5 * x(5) * P 2 * sin(deg2rad(stab ang(jj)));
                  end
                                     Lift(j) = sum(L(2:5)) - L(1) + L_w(19);
                                    Drag(j) = sum(D(2:5)) - D(1) + D_w(19);
                                    for ii = 1:length(wedge_angle)
                                                        if ii < 3
                                                                           moment(ii) = L(ii) * 0.5 * (x(ii) / cos(deg2rad(wedge_angle(ii))));
                                                        elseif ii >= 3
                                                                          moment(ii) = L(ii) * 0.5 * (x(ii) / cos(deg2rad(wedge_angle(ii))))
+ sum(x(2:ii));
                                                        end
                                     end
                                    Moment(j) = moment(1) - (moment(2) + moment(3) + moment(4) + moment(5)) +
(L_w(19)*(x_23 + x(4) + 0.75*x(5)));
                                    LC(j) = Moment(j) / Lift(j);
                                    CG = 1.83;
                                     SM(j) = (LC(j) - CG) / x(1);
end
fprintf(['To achieve positive Static Margin, a Wedge angle of about...' ...
                     ' %g deg is required for the stabilizer at AoA = 4 deg'], stab ang(19))
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To achieve positive Static Margin, a Wedge angle of about... 38.1579 deg is required for the stabilizer at AoA = 4