# The LUA-PHYSICAL library

### $Version\ 1.0.4$

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#### Abstract

lua-physical is a pure Lua library, which provides functions and objects for the computation of physical quantities. The package has been written, to simplify the creation physics problem sets. The package provides units of the SI and the imperial system. In order to display the numbers with measurement uncertainties, the package is able to perform gaussian error propagation.

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### 1 Introduction

The author of this package is a physics teacher at the high school Kantonsschule Zug, Switzerland. The main use of this package is to write physics problem sets. It is possible to integrate physical calculations directly into LualATeX. The package has been in use since 2016. Many bugs have been found and fixed. Nevertheless it still is possible, that some were not found yet. Therefore the author recommends not to use this package in industry or science. If one does so, it's the responsability of the user to check results for plausability. If the user finds some bugs, they can be reported at github.com.

### 1.1 Dependencies

This is a standalone library. However, it is compatible with the siunitx package. The results of calculations can be printed to Lual\*TeX by calling the physical.Quantity.tosiunitx() method. It is recommended to use a macro for this purpose. The preamble in the next section, simplifies the printing of quantities by the macros \q{}, \qs{} and \qu{}.

### 2 Loading

By calling require("physical") the lua-physical library is loaded. The following LuaLATEX preamble loads the lua-physical package, does some configuration of the siunitx package and defines the macros \q{}, \qs{} and \qu{} for printing physical quantities.

Listing 1: basic preamble

```
\usepackage{luacode}
\usepackage{siunitx}
% initialize the lua-physical package
\begin{luacode*}
 physical = require("physical")
 N = physical.Number
\end{luacode*}
\% configure the siunitx package
\sisetup{
 output-decimal-marker = {.},
 per-mode = symbol,
 separate-uncertainty = true,
 add-decimal-zero = true.
 exponent-product = \cdot,
 round-mode = off
% declare the unitless unit (siunitx package)
\DeclareSIUnit\number{}
```

```
% print a quantity using the SI\{\}\{\} macro.
 \directlua{
   tex.print(
     physical.Quantity.tosiunitx(
       #1,
       "scientific-notation=fixed, exponent-to-prefix=false"
     )
   )
  }%
 }
 % print a quantity in scientific notation using SI\{\}\{\} macro.
 \directlua{
    tex.print(
     physical.Quantity.tosiunitx(
       #1,
       \verb"scientific-notation=true, exponent-to-prefix=false,
         round-integer-to-decimal=true"
    )
}%
}
 % print the unit of a quantity using the \sitesize{1}{3} macro
 \newcommand{\qu}[1]{\%}
  \directlua{
    tex.print(
     physical.Quantity.tosiunitx(
       #1,
       nil,
       physical.Quantity.SIUNITX_si
   )
}
}%
}
```

#### 2.1 License

This code is freely distributable under the terms of the MIT license.

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### 3 Usage

Given the basic preamble 1, units can be used in lua code directly. By convention, all units have an underscore in front of them, i.e. meter is \_m, second is \_s. For a complete list of all available units, see section 4. The following example illustrates the use of this library.

Listing 2: Velocity of a car.

```
\begin{luacode}
    d = 10 * _m
    t = 2 * _s
    v = d / t
    \end{luacode}

A car travels $\q{d}$ in $\q{t}$. Calculate its velocity.

%
\begin{equation*}
    v=\frac{d}{t} = \frac{\q{d}}{\q{t}} = \underline{\q{v}}
\end{equation*}
```

A car travels 10 m in 2 s. Calculate its velocity.

$$v = \frac{s}{t} = \frac{10 \,\mathrm{m}}{2 \,\mathrm{s}} = \frac{5.0 \,\mathrm{m/s}}{}$$

In the above listing 2, the variable s stands for displacement and has the unit meter  $_m$ , the variable t stands for time and is given in seconds  $_s$ . If physical quantities are divided or multiplied, derived quantities are created. In the example problem above, the velocity v has the unit  $_m/_s$ . By using the macro  $q{}$  all quantities can be printed to the LualATEX code directly.

#### 3.1 Unit conversion

It is often the case, that the result of a calculation has to be converted to other units. Lets assume, that in the problem of listing 2, the velocity should be determined in \_km/\_h. This can be done using the :to() method, which is available on all quantity objects, see 3.

Listing 3: Velocity of a car in kilometers per hour.

```
\begin{luacode}
  d = 10 * _m
  t = 2 * _s
  v = (s / t):to(_km/_h)
\end{luacode}
```

```
A car travels $\q{d}$ in $\q{t}$. Calculate its velocity in $\qu{_km/_h}
}$.
%
\begin{equation*}
v = \frac{d}{t} = \frac{\q{d}}{\q{t}} = \underline{\q{v}}
\end{equation*}
```

A car travels 10 m in 2 s. Calculate its velocity in km/h.

$$v = \frac{d}{t} = \frac{10 \,\mathrm{m}}{2 \,\mathrm{s}} = \underline{18.0 \,\mathrm{km/h}}$$

Another example is given in listing 4. The task is to calculate the volume of a cuboid. The length of the edges are given in different units. The result of the multiplication has the unit cm mm m. If the unit cm<sup>3</sup> is preferred, it has to be converted explicitly. At first this looks a bit cumbersome. The reason of this behaviour is, that the software is not able to guess the unit of the result. In many cases, like in the example problem, it's not clear what unit the volume should have. Is it \_m^3, \_cm^3 or \_L? The user has to give that convertion explicitly.

Listing 4: Volume of a cuboid.

```
\begin{luacode}
    a = 12 * _cm
    b = 150 * _mm
    c = 1.5 * _m

V = ( a * b * c ):to(_dm^3)
\end{luacode}

Find the volume of a rectangular cuboid with lengths $\q{a}$,
    $\q{b}$ and $\q{c}$.

%
\begin{equation*}
    V = a \cdot b \cdot c
    = \q{a} \cdot \q{b} \cdot \q{c}
    = \underline{\q{V}}
\end{equation*}
```

Find the volume of a rectangular cuboid with lengths  $12\,\mathrm{cm},\,150\,\mathrm{mm}$  and  $1.5\,\mathrm{m}.$ 

$$V = a \cdot b \cdot c = 12 \,\mathrm{cm} \cdot 150 \,\mathrm{mm} \cdot 1.5 \,\mathrm{m} = 27.0 \,\mathrm{dm}^3 = 27.0 \,\mathrm{dm}^3$$

The siunitx package has definitions or all SI units plus some non-SI units. If a quantity has a unit, which is not defined by the siunitx package, it has to be declared using the \DeclareSIUnit macro.

Listing 5: Non-SI units.

```
% add this declaration to the preamble
\DeclareSIUnit\inch{in}

% document
\begin{luacode}
  l = 12 * _in
\end{luacode}

Convert $\q{l}$ to the unit $\qu{_cm}$.

%
\begin{equation*}
  l = \q{l} \cdot \frac{\q{_in:to(_cm)}}{\qu{_in}} = \q{l:to(_cm)}
\end{equation*}
```

Convert 12 in (inches) to the unit cm.

$$l = 12 \operatorname{in} \cdot \frac{2.54 \operatorname{cm}}{\operatorname{in}} = \underline{30.48 \operatorname{cm}}$$

#### 3.1.1 Temperature Conversion

Most physical units transform linearly. Exceptions are temperature units lie degree Celsius <code>\_degC</code> and degree Fahrenheit <code>\_degF</code>. These units are ambigous and can be interpreted as temperature differences or as an absolute temperatures. In the latter case, the conversion to base units is not a linear, but an affine transformation. This is because degree Celsius and degree Fahrenheit scales have their zero points at different temperatures compared to the unit Kelvin.

By default  $_{\text{degC}}$  and  $_{\text{degF}}$  units are temperature differences. If one wants to have it converted absolutely, it has to be done adding / subtracting  $_{\text{degC}_0} = 273.15*_{\text{K}}$  or  $_{\text{degF}_0} = (273.15 - 32*(5/9)) * _K$ , the zero point temperatures of the scales.

In the following problem, listing 6, the task is to convert temperatures given in the unit degree Celsius and degree Fahrenheit to Kelvin.

Listing 6: Temperature conversion.

```
\begin{luacode}
  theta_1 = 110 * _degC
  T_1 = ( theta_1 + _degC_0 ):to(_K)

T_2 = 100 * _K
  theta_2 = ( T_2 - _degC_0 ):to(_degC)

theta_3 = 212 * _degF
  T_3 = ( theta_3 + _degF_0 ):to(_K)
```

```
T_4 = 100 * _K
theta_4 = ( T_4 - _degF_0 ):to(_degF)

theta_5 = 100 * _degC
    theta_6 = ( ( theta_5 + _degC_0 ):to(_K) - _degF_0):to(_degF)

\end{\luacode}

\begin{align*}
    \q{theta_1} &\mathrel{\widehat{=}} \q{T_1} \\
    \%
    \q{theta_2} &\mathrel{\widehat{=}} \q{T_2} \\
    \%
    \q{theta_3} &\mathrel{\widehat{=}} \q{T_3} \\
    \%
    \q{theta_4} &\mathrel{\widehat{=}} \q{T_4} \\
    \%
    \q{theta_5} &\mathrel{\widehat{=}} \q{T_4} \\
    \%
    \q{theta_5} &\mathrel{\widehat{=}} \q{theta_6} \\
    \end{align*}
```

```
110 \,^{\circ}\text{C} \stackrel{?}{=} 383.15 \,\text{K}
-173.15 \,^{\circ}\text{C} \stackrel{?}{=} 100 \,\text{K}
212 \,^{\circ}\text{F} \stackrel{?}{=} 373.15 \,\text{K}
-279.67 \,^{\circ}\text{F} \stackrel{?}{=} 100 \,\text{K}
100 \,^{\circ}\text{C} \stackrel{?}{=} 212.0 \,^{\circ}\text{F}
```

#### 3.2 Uncertainty Propagation

The lua-physical library supports uncertainty propagation. To create a number with an uncertainty, an instance of physical.Number has to be created. It has to be remembered, that N is a alias for physical.Number. The first argument of the constructor N(mean, uncertainty) is the mean value and the second one the uncertainty of the measurement.

For the uncertainty propagation the gaussian formula

$$\Delta f = \sqrt{\left(\frac{\partial f}{x_1} \cdot \Delta x_1\right)^2 + \dots + \left(\frac{\partial f}{x_n} \cdot \Delta x_2\right)^2}$$

is used. This formula is a good estimation for the uncertainty  $\Delta f$ , if the quantities  $x_1, \ldots, x_n$  the function f depends on, have no correlation. Further, the function f has to change linearly, if quantities  $x_i$  are changed in the range of their uncertainties.

The example in listing 7 shows the usage of N(). At the defintion of the distance and the speed of light, the constants are given with full precision, i.e. The distance \_au is 149 597 870.7 km and \_c is 299 792.458 km/s. By multipling these quantities with N(1,0.0001) the precision is reduced. The uncertainty propagation takes

care of rounding the resulting time t to the correct precision. For printing, the macro \qs{} for scientific notation is used.

Listing 7: Time of flight.

Calculate the time, a lightray travels from the surface of the sun to the earth. The mean distance from the sun to the eart is  $1.496 \cdot 10^8$  km. The speed of light is  $2.998 \cdot 10^5$  km/s.

$$t = \frac{d}{v} = \frac{1.496 \cdot 10^8 \text{ km}}{2.998 \cdot 10^5 \text{ km/s}} = \underline{8.32 \text{ min}}$$

Another example is given in listing 8, the task is to find the volume of an ideal gas. Given are pressure p in \_bar, amount of substance n in \_mol and absolute temperature T in degree celsius \_degC.

Listing 8: Volume of an ideal gas.

```
\begin{luacode}
N.omitUncertainty = true

p = N(1.013,0.0001) * _bar
n = N(1,0.01) * _mol
T = N(30,0.1) * _degC

V = ( n * _R * (T + _degC_0):to(_K) / p ):to(_L)
\end{luacode}

An ideal gas ($\q{n}$) has a pressure of $\q{p}$ and a temperature of $\q{T}$. Calculate the volume of the gas.

\[
\begin{equation*}
V = \frac{ \q{n} \cdot \q{_R} \cdot \q{(T + _degC_0):to(_K)} }{ \q{p}} \]
= \q{V}
```

```
= \underline{\q{V}}
\end{equation*}
```

An ideal gas  $(1.0\,\mathrm{mol})$  has a pressure of  $1.013\,\mathrm{bar}$  and a temperature of  $30\,^{\circ}\mathrm{C}$ . Calculate the volume of the gas.

$$V = \frac{1.0\, \mathrm{mol} \cdot 8.31\, \mathrm{J/(mol\,K)} \cdot 303\, \mathrm{K}}{1.013\, \mathrm{bar}} = \underline{25\, \mathrm{L}}$$

This example shows, that the result has only two digits. If more digits are needed, the uncertainties of the given quantities should be made smaller.

#### 3.2.1 Print the Uncertainty explicitly

It is possible to print the uncertainty explicitly. By default the parameter N.omitUncertainty is set to true. In listing 9 it is set to false and the uncertainty is printed.

Listing 9: Uncertainty in area calculation.

```
\begin{luacode}
   N.omitUncertainty = false

a = N(2,0.1) * _m
b = N(3,0.1) * _m

A = ( a * b ):to(_m^2)
\end{luacode}

Calculate the area of a rectangle with lengths $\q{a}$ and $\q{b}$.

%
\begin{equation*}
   A = a \cdot b
   = \q{a} \cdot \q{b}
   = \underline{\q{A}}
\end{equation*}
```

Calculate the area of a rectangle with lengths  $(2.00\pm0.10)\,\mathrm{m}$  and  $(3.00\pm0.10)\,\mathrm{m}.$ 

$$A = a \cdot b = (2.00 \pm 0.10) \,\mathrm{m} \cdot (3.00 \pm 0.10) \,\mathrm{m} = (6.0 \pm 0.4) \,\mathrm{m}^2$$

### 3.3 Mathematical operations

Two physical quantities with identical dimensions can be added or subtracted. The library checks the validity of those operations and throws an error if two addends haven't the same dimensions.

Listing 10: Addition and subtraction

New physical quantities can be created by division and multiplication. As long as no division by zero is made, no errors should occur.

Listing 11: Multiplication and Division

```
l_1 = 1 * _m
l_2 = 2 * _cm
(l_1 * l_2):to(_m^2)
0.02 * _m^2
(l_1 / l_2):to(_1)
50.0 * _1
```

Physical quantities can be exponentiated. The library doesn't check, if the result has units with non integer exponents.

Listing 12: Exponentiation

```
1 = 5 * _m
A = 1^2

A:to(_m^2)
25.0 * _m^2

A:sqrt()
5.0 * _m

A^0.5
5.0 * _m
```

Exponential functions an the logarithms should have dimensionless arguments. The library throws an error if that's not the case.

Listing 13: Exponential function and logarithm

```
N_0 = 1000 * _1
lambda = Q.log(2)/(2*_h)
t = 50 * _min

N_0 * Q.exp(-lambda * t)
749.15353843834 * _1
```

### 4 Supported Units

All supported units are listed in this section. Subsection 4.2 lists the seven base units of the International System of Units (SI). In subsection 4.3 mathematical and physical constants are defined. The subsection 4.4 contains all coherent derived units from the SI system and 4.5 those which are accepted to use with the SI. The subsection 4.6 lists nominal astronomical units, which are proposed by [4]. Subsection 4.7 lists units, which are common but outside of the SI system. The subsections 4.8 and 4.9 are dedicated to imperial and U.S. customary units. The last subsection 4.10 containts international currencies.

### 4.1 Prefixes

All SI units have prefixed versions, i.e. \_us microsecond, \_cm centimeter, \_mN millinewton, see table 1. Some units of data processing, like \_bit have prefixes which are powers of 2. They are called binary or IEC prefixes, see table 2 [2, 121].

Prefix	Symbol	Definition	Prefix	Symbol	Definition
yotta	Y	1e24	deci	d	1e-1
zetta	Z	1e21	centi	С	1e-2
exa	E	1e18	milli	m	1e-3
peta	P	1e15	micro	u	1e-6
tera	T	1e12	nano	n	1e-9
giga	G	1e9	pico	p	1e-12
mega	M	1e6	femto	f	1e-15
kilo	k	1e3	atto	a	1e-18
hecto	h	1e2	zepto	z	1e-21
deca	da	1e1	yocto	У	1e-23

Table 1: SI prefixes [2, 121]

Prefix	Symbol	Definition
kibi	Ki	1024
mebi	Mi	1048576
gibi	Gi	1073741824
tebi	Ti	1099511627776
pebi	Pi	1125899906842624
exbi	Ei	1152921504606846976
zebi	Zi	1180591620717411303424
yobi	Yi	1208925819614629174706176

Table 2: IEC prefixes [2, 121]

### 4.2 Base Units

The lua-physical library has nine base quantities. These are the seven basis units or basis quantities of the SI system [3] and in addition the base quantity of information \_bit and of currency \_EUR. All other quantities are derived from these base units.

Quantity	$\operatorname{Unit}$	Symbol	Dim.	Definition	
number <sup>1</sup>	_	_1	1	The dimensionless number one.	
time	second _s T		Τ	The SI unit of time. It is defined by taking the fixed numerical value of the caesium frequency $\Delta\nu_{Cs}$ , the unperturbed ground-state hyperfine transition frequency of the caesium 133 atom, to be 9192631770 when expressed in the unit 1/s.	
length	meter	_m	L	The SI unit of length. It is defined by taking the fixed numercial value of the speed of light in vacuum $c$ to be 299 792 458 when expressed in the unit of m/s.	

 $<sup>^{1}\</sup>mathrm{The}$  number one is a unit with dimension zero. Stricly speaking it is not a base unit.

Quantity	Unit	Symbol	Dim.	Definition
mass	kilogram	_kg	M	The SI unit of mass. It is defined by taking the fixed numerical value of the Planck constant $h$ to be $6.62607015\cdot10^{-34}$ when expressed in m <sup>2</sup> kg/s.
electric current	ampere	_A	I	The SI unit of electric current. It is defined by taking the fixed numerical value of the elementary charge $e$ to be $1.602176634\cdot10^{-19}$ when expressed in As.
thermody- namic temperature	kelvin	_K	K <sup>1</sup>	The SI unit of the thermodynamic temperature. It is defineed by taking the fixed numerical value of the Boltzmann constant $k_B$ to be $1.380649\cdot10^{-23}$ when expressed in kg m <sup>2</sup> /(s <sup>2</sup> K)
amount of substance	mole	_mol	N	The SI unit of amount of substance. One mole contains exactly $6.02214076\cdot10^{23}$ elementary entities. This number is the fixed numerical value of the Avogadro constant $N_A$ when expressed in 1/mol.
luminous intensity	candela	_cd	J	The SI unit of luminous intensity in a given direction. It is defined by taking the fixed numerical value of the luminous efficacy of monochromatic radiation of frequency $5.4 \cdot 10^{14} \mathrm{Hz}$ , $K_{cd}$ , to be 683 when expressed in the unit $\mathrm{cd}  \mathrm{sr}  \mathrm{s}^3 / (\mathrm{kg}  \mathrm{m}^2)$ .
informa- tion	bit	_bit	В	The smallest amount of information.
currency	euro	_EUR	С	The value of the currency Euro.

Table 3: Base units

 $<sup>^1</sup>$ The SI symbol for the dimension of temperature is  $\Theta$ , but all symbols of this library consist of roman letters, numbers and underscores only. Therefore the symbol for the dimension of the thermodynamic temperature is the letter K.

## 4.3 Constants

All physical constants are taken from the NIST webpage [1].

Name	Symbol	Definition
pi	_Pi	3.1415926535897932384626433832795028841971 * _1
eulersnumber	_E	2.7182818284590452353602874713526624977572 * _1
speedoflight	_c	299792458 * _m/_s
gravitationalconstant	_Gc	N(6.67408e-11,3.1e-15) * _m^3/(_kg*_s^2)
planckconstant	_h_P	6.62607015e-34 * _J*_s
${\it reduced planck constant}$	_h_Pbar	_h_P/(2*_Pi)
elementarycharge	_e	1.602176634e-19 * _C
vacuumpermeability	_u_0	4e-7*Pi * _N/_A^2
vacuumpermitivity	_e_0	1/(_u_0*_c^2)
atomicmassunit	_u	N(1.66053904e-27, 2e-35) * _kg
electronmass	_m_e	N(9.10938356e-31, 1.1e-38) * _kg
protonmass	_m_p	N(1.672621898e-27, 2.1e-35) * _kg
neutronmass	_m_n	N(1.674927471e-27, 2.1e-35) * _kg
bohrmagneton	_u_B	_e*_h_Pbar/(2*_m_e)
nuclearmagneton	_u_N	_e*_h_Pbar/(2*_m_p)
electronmagneticmoment	_u_e	N(-928.4764620e-26,5.7e-32) * _J/_T
protonmagneticmoment	_u_p	N(1.4106067873e-26,9.7e-35) * _J/_T
neutronmagneticmoment	_u_n	N(-0.96623650e-26,2.3e-26) * _J/_T
fine structure constant	_alpha	_u_0*_e^2*_c/(2*_h_P)
rydbergconstant	_Ry	_alpha^2*_m_e*_c/(2*_h_P)
avogadronumber	_N_A	6.02214076e23/_mol
boltzmannconstant	_k_B	1.380649e-23 * _J/_K
molargasconstant	_R	N(8.3144598, 4.8e-6) * _J/(_K*_mol)
${\it stefanboltz} mann constant$	_sigma	_Pi^2*_k_B^4/(60*_h_Pbar^3*_c^2)
standardgravity	_g_0	9.80665 * _m/_s^2

Table 4: Physical and mathematical constants

### 4.4 Coherent derived units in the SI

All units in this section are coherent derived units from the SI base units with special names, [2, 118].

Quantity	Unit	Symbol	Definition
Plane Angle <sup>1</sup>	radian	_rad	_1
Solid Angle <sup>2</sup>	steradian	_sr	_rad^2
Frequency	hertz	_Hz	1/_s
Force	newton	_N	_kg*_m/_s^2
Pressure	pascal	_Pa	_N/_m^2
Energy	joule	_J	_N*_m
Power	watt	_W_	_J/_s
Electric Charge	$\operatorname{coulomb}$	_C	_A*_s
Electric Potential	volt	_V	_J/_C
Electric Capacitance	farad	_F	_C/_V
Electric Resistance	ohm	_Ohm	_V/_A
Electric Conductance $^3$	siemens	_S	_A/_V
Magnetic Flux	weber	_Wb	_V*_s
Magnetic Flux Density	tesla	_T	_Wb/_m^2
Inductance	henry	_H	_Wb/_A
$Temperature^4$	celsius	_degC	_K
Luminous Flux	lumen	_lm	_cd*_sr
Illuminance	lux	_lx	_lm/_m^2
Activity	becquerel	_Bq	1/_s
Absorbed Dose	gray	_Gy	_J/_kg
Dose Equivalent	sievert	_Sv	_J/_kg
Catalytic Activity	katal	_kat	_mol/_s

<sup>&</sup>lt;sup>1</sup>In the SI system, the quantity Plane Angle has the dimension of a number.

 $<sup>^2\</sup>mathrm{In}$  the SI system, the quantity Solid Angle has the dimension of a number.

<sup>&</sup>lt;sup>3</sup>The unit \_PS stands for peta siemens and is in conflict with the metric version of the unit horsepower (german Pferdestärke). Since the latter is more common than peta siemens, \_PS is defined to be the metric version of horsepower.

 $<sup>^4{\</sup>rm The~unit~\_degC}$  is by default interpreted as a temperature difference.

### 4.5 Non-SI units accepted for use with the SI

There are a few units with dimension 1. [2, 124].

Quantity	Unit	Symbol	Definition
Time	minute	_min	60 * _s
	hour	_h	60 * _min
	day	_d	24 * _h
Plane Angle	degree	_deg	(_Pi/180) * _rad
	arcminute	_arcmin	_deg/60
	arcsecond	_arcsec	_arcmin/60
Area	hectare	_hectare	1e4 * _m^2
Volume	liter	_L	1e-3 * _m^3
Mass	tonne	_t	1e3 * _kg

## 4.6 Nominal Astronomical Units

The nominal values of solar, terrestrial and jovial quantities are taken from IAU Resolution B3 [4].

Quantity	Unit	Symbol	Definition
Length	nomsolradius	_R_S_nom	6.957e8 * _m
Irradiance	${\bf nom solir radiance}$	_S_S_nom	1361 * _W/_m^2
Radiant Flux	nom solluminosity	_L_S_nom	3.828e26 * _W
Temperature	nom so leff temperature	_T_S_nom	5772 * _K
Mass Parameter	nom sol mass parameter	_GM_S_nom	1.3271244e20 * _m^3*_s^-2
Length	nomterreqradius	_Re_E_nom	6.3781e6 * _m
Length	nomterrpolradius	_Rp_E_nom	6.3568e6 * _m
Mass Parameter	nom terr mass parameter	_GM_E_nom	3.986004e14 * _m^3*_s^-2
Length	nomjoveqradius	_Re_J_nom	7.1492e7 * _m
Length	nomjovpolradius	_Rp_J_nom	6.6854e7 * _m
Mass Parameter	${\bf nomjov mass parameter}$	_GM_J_nom	1.2668653e17 * _m^3*_s^-2

## 4.7 Other Non-SI units

The unit Bel is only available with prefix decibel, because \_B is the unit byte.

Quantity	Unit	Symbol	Definition
Length	angstrom	_angstrom	1e-10 * _m
	fermi	_fermi	1e-15 * _m
Time	svedberg	_svedberg	1e-13 * _s
	week	_wk	7 * _d
	year	_a	365.25 * _d
	astronomicalunit	_au	149597870700 * _m
	lightsecond	_ls	_c*_s
	lightyear	_ly	_c*_a
	parsec	_pc	(648000/_Pi) * _au
Area	barn	_barn	1e-28 * _m^2
	are	_are	1e2 * _m^2
Volume	metricteaspoon	_tsp	5e-3 * _L
	metrictablespoon	_Tbsp	3 * _tsp
Plane Angle	gradian	_gon	(Pi/200) * _rad
	turn	_tr	2*Pi * _rad
Solid Angle	spat	_sp	4*Pi * _sr
Force	kilopond	_kp	_kg*_g_0
Pressure	bar	_bar	1e5 * _Pa
	standardatmosphere	_atm	101325 * _Pa
	technical atmosphere	_at	_kp/_cm^2
	millimeterofmercury	_mmHg	133.322387415 * _Pa
	torr	_Torr	(101325/760) * _Pa
Energy	thermochemical calorie	_cal	4.184 * _J
	internationalcalorie	_cal_IT	4.1868 * _J
	gramoftnt	_g_TNT	1e3 * _cal
	tonoftnt	_t_TNT	1e9 * _cal

Quantity	Unit	Symbol	Definition
	electronvolt	_eV	_e*_V
	wattsecond	_Ws	_W*_s
	watthour	_Wh	_W*_h
Power	voltampere	_VA	_V*_A
Electric Charge	amperesecond	_As	_A*_s
	amperehour	_Ah	_A*_h
Information	nibble	_nibble	4 * _bit
	byte	_B	8 * _bit
Information Transfer Rate	bitpersecond	_bps	_bit/_s
Number	percent	_percent	1e-2 * _1
	permille	_permille	1e-3 * _1
	partspermillion	_ppm	1e-6 * _1
	partsperbillion	_ppb	1e-9 * _1
	partspertrillion	_ppt	1e-12 * _1
	partsperquadrillion	_ppq	1e-15 * _1
	decibel	_dB	_1
Power	metrichorsepower	_PS	75 * _g_0*_kg*_m/_s
Activity	curie	_Ci	3.7e10 * _Bq
Absorbed Dose	rad	_Rad	1e-2 * _Gy
Dose Equivalent	rem	_rem	1e-2 * _Sv
Viscosity	poiseuille	_P1	_Pa*_s

## 4.8 Imperial Units

Quantity	$\operatorname{Unit}$	Symbol	Definition
Length	inch	_in	2.54e-2 * _m
	thou	_th	1e-3 * _in
$DTP Point^1$	point	_pt	_in/72
	pica	_pica	12 * _pt
	hand	_hh	4 * _in
	foot	_ft	12 * _in
	yard	_yd	3 * _ft
	$\operatorname{rod}$	_rd	5.5 * _yd
	chain	_ch	4 * _rd
	furlong	_fur	10 * _ch
	mile	_mi	8 * _fur
	league	_lea	3*_mi
	nautical mile	_nmi	1852 * _m
	${\it nautical league}$	_nlea	3 * _nmi
	cable	_cbl	0.1 * _nmi
	fathom	_ftm	6 * _ft
Velocity	knot	_kn	_nmi/_h
Area	acre	_ac	10 * _ch^2
Volume	gallon	_gal	4.54609*_L
	quart	_qt	_gal/4
	pint	_pint	_qt/2
	cup	_cup	_pint/2
	gill	_gi	_pint/4
	fluidounce	_fl_oz	_gi/5
	fluiddram	_fl_dr	_fl_oz/8

 $<sup>^{1}</sup>$ The desktop publishing point or PostScript point is 1/72 of an international inch.

Quantity	Unit	Symbol	Definition
Mass	grain	_gr	64.79891*_mg
	pound	_1b	7000*_gr
	ounce	_oz	_lb/16
	dram	_dr	_1b/256
	stone	_st	14*_lb
	quarter	_qtr	2*_st
	hundredweight	_cwt	4*_qtr
	longton	_ton	20*_cwt
	troypound	_lb_t	5760*_gr
	troyounce	_oz_t	_lb_t/12
	pennyweight	_dwt	24*_gr
	firkin	_fir	56*_1b
Time	sennight	_sen	7*_d
	fortnight	_ftn	14*_d
${\bf Temperature^1}$	fahrenheit	_degF	(5/9)*_K
Force	poundforce	_lbf	_lb*_g_0
	poundal	_pdl	_lb*_ft/_s^2
Mass	slug	_slug	_lbf*_s^2/_ft
Pressure	poundforcepersquareinch	_psi	_lbf/_in^2
Energy, Torque	the hembritish thermal unit	_BTU	(1897.83047608/1.8)*_J
Energy, Torque	int british thermal unit	_BTU_it	1055.05585262 * _J
Power	horsepower	_hp	33000*_ft*_lbf/_min

 $<sup>^1\</sup>mathrm{The~unit~\_degF}$  is by default interpreted as a temperature difference.

## 4.9 U.S. customary units

In the U.S., the length units are bound to the meter differently than in the imperial system. The followin definitions are taken from https://en.wikipedia.org/wiki/United\_States\_customary\_units.

Quantity	Unit	Symbol	Definition
Length	ussurveyinch	_in_US	_m/39.37
	ussurveyhand	_hh_US	4 * _in_US
	ussurveyfoot	_ft_US	3 * _hh_US
	ussurveylink	_li_US	0.66 * _ft_US
	ussurveyyard	_yd_US	3 * _ft_US
	ussurveyrod	_rd_US	5.5 * _yd_US
	ussurveychain	_ch_US	4 * _rd_US
	us survey furlong	_fur_US	10 * _ch_US
	ussurveymile	_mi_US	8 * _fur_US
	us survey league	_lea_US	3 * _mi_US
	us survey fathom	_ftm_US	72 * _in_US
	ussurveycable	_cbl_US	120 * _ftm_US
Area	ussurveyacre	_ac_US	_ch_US * _fur_US
Volume	usgallon	_gal_US	231 * _in^3
	usquart	_qt_US	_gal_US/4
	uspint	_pint_US	_qt_US/2
	uscup	_cup_US	_pint_US/2
	usgill	_gi_US	_pint_US/4
	usfluidounce	_fl_oz_US	_gi_US/4
	ustablespoon	_Tbsp_US	_fl_oz_US/2
	usteaspoon	_tsp_US	_Tbsp_US/3
	usfluiddram	_fl_dr_US	_fl_oz_US/8
Mass	usquarter	_qtr_US	25 * _lb
	ushundred weight	_cwt_US	4 * _qtr_US
	uston	_ton_US	20 * _cwt_US

## 4.10 International Currencies

International currency units based on exchange rates from 7.3.2019, 21:00 UTC.

Name	Symbol	Definition
AfghanAfghani	_AFN	0.012 * _EUR
AfghanPul	_cAFN	0.01 * _AFN
AlbanianLek	_ALL	0.008 * _EUR
ArmenianDram	_AMD	0.0018 * _EUR
ArmenianLuma	_cAMD	0.01 * _AMD
AngolanKwanza	_AOA	0.0028 * _EUR
AngolanCentimo	_cAOA	0.01 * _AOA
ArgentinePeso	_ARS	0.021 * _EUR
ArgentineCentavo	_cARS	0.01 * _ARS
AustralianDollar	_AUD	0.63 * _EUR
AustralianCent	_cAUD	0.01 * _AUD
AzerbaijaniManat	_AZN	0.63 * _EUR
AzerbaijaniQepik	_cAZN	0.01 * _AZN
BosnianMark	_BAM	0.51 * _EUR
BosnianFenings	_cBAM	0.01 * _BAM
BangladeshiTaka	_BDT	0.011 * _EUR
BangladeshiPoisha	_cBDT	0.01 * _BDT
BurundianFranc	_BIF	0.00049 * _EUR
BurundianCentime	_cBIF	0.01 * _BIF
BolivianBoliviano	_BOB	0.13 * _EUR
BolivianCentavo	_cBOB	0.01 * _BOB
BrazilianReal	_BRL	0.23 * _EUR
BrazilianCentavo	_cBRL	0.01 * _BRL
BotswanaPula	_BWP	0.083 * _EUR
BotswanaThebe	_cBWP	0.01 * _BWP
BelarusianRuble	_BYN	0.42 * _EUR
BelarusianKapiejka	_cBYN	0.01 * _BYN

Name	Symbol	Definition
CanadianDollar	_CAD	0.66 * _EUR
CanadianCent	_cCAD	0.01 * _CAD
CongoleseFranc	_CDF	0.00055 * _EUR
CongoleseCentime	_cCDF	0.01 * _CDF
SwissFranc	_CHF	0.88 * _EUR
SwissRappen	_cCHF	0.01 * _CHF
ChileanPeso	_CLP	0.0013 * _EUR
ChileanCentavo	_cCLP	0.01 * _CLP
ChineseRenminbiYuan	_CNY	0.13 * _EUR
ChineseRenminbiFen	_cCNY	0.01 * _CNY
ColombianPeso	_COP	0.00028 * _EUR
ColombianCentavo	_cCOP	0.01 * _COP
CostaRicanColon	_CRC	0.0015 * _EUR
CostaRicanCentimos	_cCRC	0.01 * _CRC
CzechKoruna	_CZK	0.039 * _EUR
CzechHaler	_cCZK	0.01 * _CZK
DanishKrone	_DKK	0.13 * _EUR
DanishOre	_cDKK	0.01 * _DKK
DominicanPeso	_DOP	0.018 * _EUR
DominicanCentavo	_cDOP	0.01 * _DOP
AlgerianDinar	_DZD	0.0074 * _EUR
AlgerianSanteem	_cDZD	0.01 * _DZD
EgyptianPound	_EGP	0.051 * _EUR
EgyptianPiastre	_cEGP	0.01 * _EGP
EthiopianBirr	_ETB	0.031 * _EUR
EthiopianSantim	_cETB	0.01 * _ETB
FijianDollar	_FJD	0.42 * _EUR
FijianCent	_cFJD	0.01 * _FJD

Name	Symbol	Definition
PoundSterling	_GBP	1.16 * _EUR
PennySterling	_cGBP	0.01 * _GBP
GeorgianLari	_GEL	0.33 * _EUR
GeorgianTetri	_cGEL	0.01 * _GEL
GhanaianCedi	_GHS	0.16 * _EUR
GhanaianPesewa	_cGHS	0.01 * _GHS
GambianDalasi	_GMD	0.018 * _EUR
GambianButut	_cGMD	0.01 * _GMD
GuineanFranc	_GNF	9.6e-05 * _EUR
GuineanCentime	_cGNF	0.01 * _GNF
${\bf Guatemalan Quetzal}$	_GTQ	0.12 * _EUR
GuatemalanCentavo	_cGTQ	0.01 * _GTQ
GuyaneseDollar	_GYD	0.0043 * _EUR
GuyaneseCent	_cGYD	0.01 * _GYD
${\bf Hong Kong Dollar}$	_HKD	0.11 * _EUR
HongKongCent	_cHKD	0.01 * _HKD
HonduranLempira	_HNL	0.036 * _EUR
HonduranCentavo	_cHNL	0.01 * _HNL
CroatianKuna	_HRK	0.13 * _EUR
CroatianLipa	_cHRK	0.01 * _HRK
HaitianGourde	_HTG	0.011 * _EUR
HaitianCentime	_cHTG	0.01 * _HTG
HungarianForint	_HUF	0.0032 * _EUR
HungarianFiller	_cHUF	0.01 * _HUF
IndonesianRupiah	_IDR	6.2e-05 * _EUR
IndonesianSen	_cIDR	0.01 * _IDR
IsraeliNewShekel	_ILS	0.25 * _EUR
IsraeliNewAgora	_cILS	0.01 * _ILS

Name	Symbol	Definition
IndianRupee	_INR	0.013 * _EUR
IndianPaisa	_cINR	0.01 * _INR
IraqiDinar	_IQD	0.00074 * _EUR
IraqiFils	_cIQD	0.001 * _IQD
IranianRial	_IRR	2.7e-05 * _EUR
IranianToman	_cIRR	10.0 * _IRR
IcelandicKrona	_ISK	0.0073 * _EUR
JamaicanDollar	_JMD	0.007 * _EUR
JamaicanCent	_cJMD	0.01 * _JMD
JapaneseYen	_JPY	0.008 * _EUR
KenyanShilling	_KES	0.0089 * _EUR
KenyanCent	_cKES	0.01 * _KES
KyrgyzstaniSom	_KGS	0.013 * _EUR
KyrgyzstaniTyiyn	_cKGS	0.01 * _KGS
CambodianRiel	_KHR	0.00022 * _EUR
NorthKoreanWon	_KPW	0.00099 * _EUR
NorthKoreanChon	_cKPW	0.01 * _KPW
SouthKoreanWon	_KRW	0.00078 * _EUR
SouthKoreanJeon	_cKRW	0.01 * _KRW
KuwaitiDinar	_KWD	2.93 * _EUR
KuwaitiFils	_cKWD	0.001 * _KWD
KazakhstaniTenge	_KZT	0.0023 * _EUR
KazakhstaniTiyn	_cKZT	0.01 * _KZT
LaoKip	_LAK	0.0001 * _EUR
LaoAtt	_cLAK	0.01 * _LAK
SriLankanRupee	_LKR	0.005 * _EUR
SriLankanCent	_cLKR	0.01 * _LKR
LiberianDollar	_LRD	0.0055 * _EUR
LiberianCent	_cLRD	0.01 * _LRD

Name	Symbol	Definition
LibyanDinar	_LYD	0.64 * _EUR
LibyanDirham	_cLYD	0.001 * _LYD
MoroccanDirham	_MAD	0.092 * _EUR
MoroccanSantim	_cMAD	0.01 * _MAD
MoldovanLeu	_MDL	0.052 * _EUR
MoldovanBan	_cMDL	0.01 * _MDL
MalagasyAriary	_MGA	0.00025 * _EUR
MalagasyIraimbilanja	_cMGA	0.2 * _MGA
MacedonianDenar	_MKD	0.016 * _EUR
MacedonianDeni	_cMKD	0.01 * _MKD
BurmeseKyat	_MMK	0.00059 * _EUR
BurmesePya	_cMMK	0.01 * _MMK
MongolianTogrog	_MNT	0.00034 * _EUR
MongolianMongo	_cMNT	0.01 * _MNT
MauritanianOuguiya	_MRU	0.025 * _EUR
MauritanianKhoums	_cMRU	0.2 * _MRU
MauritianRupee	_MUR	0.025 * _EUR
MauritianCent	_cMUR	0.01 * _MUR
MaldivianRufiyaa	_MVR	0.058 * _EUR
MaldivianLaari	_cMVR	0.01 * _MVR
MalawianKwacha	_MWK	0.0012 * _EUR
MalawianTambala	_cMWK	0.01 * _MWK
MexicanPeso	_MXN	0.046 * _EUR
MexicanCentavo	_cMXN	0.01 * _MXN
MalaysianRinggit	_MYR	0.22 * _EUR
MalaysianSen	_cMYR	0.01 * _MYR
MozambicanMetical	_MZN	0.014 * _EUR
MozambicanCentavo	_cMZN	0.01 * _MZN

Name	Symbol	Definition
NigerianNaira	_NGN	0.0025 * _EUR
NigerianKobo	_cNGN	0.01 * _NGN
NicaraguanCordoba	_NIO	0.027 * _EUR
NicaraguanCentavo	_cNIO	0.01 * _NIO
NorwegianKrone	_NOK	0.1 * _EUR
NorwegianOre	_cNOK	0.01 * _NOK
New Zeal and Dollar	_NZD	0.61 * _EUR
NewZealandCent	_cNZD	0.01 * _NZD
PeruvianSol	_PEN	0.27 * _EUR
PeruvianCentimo	_cPEN	0.01 * _PEN
PapuaNewGuineanKina	_PGK	0.26 * _EUR
PapuaNewGuineanToea	_cPGK	0.01 * _PGK
PhilippinePeso	_PHP	0.017 * _EUR
PhilippineSentimo	_cPHP	0.01 * _PHP
PakistaniRupee	_PKR	0.0064 * _EUR
PakistaniPaisa	_cPKR	0.01 * _PKR
PolishZloty	_PLN	0.23 * _EUR
PolishGrosz	_cPLN	0.01 * _PLN
ParaguayanGuarani	_PYG	0.00015 * _EUR
ParaguayanCentimo	_cPYG	0.01 * _PYG
QatariRiyal	_QAR	0.24 * _EUR
QatariDirham	_cQAR	0.01 * _QAR
RomanianLeu	_RON	0.21 * _EUR
RomanianBan	_cRON	0.01 * _RON
SerbianDinar	_RSD	0.0085 * _EUR
SerbianPara	_cRSD	0.01 * _RSD
RussianRuble	_RUB	0.013 * _EUR
RussianKopeyka	_cRUB	0.01 * _RUB

Name	Symbol	Definition
RwandanFranc	_RWF	0.00098 * _EUR
RwandanCentime	_cRWF	0.01 * _RWF
${\bf Solomon Islands Dollar}$	_SBD	0.11 * _EUR
SolomonIslandsCent	_cSBD	0.01 * _SBD
SeychelloisRupee	_SCR	0.065 * _EUR
SeychelloisCent	_cSCR	0.01 * _SCR
SudanesePound	_SDG	0.019 * _EUR
SudaneseQirsh	_cSDG	0.01 * _SDG
SwedishKrona	_SEK	0.094 * _EUR
SwedishOre	_cSEK	0.01 * _SEK
SingaporeDollar	_SGD	0.65 * _EUR
SingaporeCent	_cSGD	0.01 * _SGD
SierraLeoneanLeone	_SLL	0.0001 * _EUR
SierraLeoneanCent	_cSLL	0.01 * _SLL
SomalilandShilling	_SQS	0.00013 * _EUR
SomalilandCent	_cSQS	0.01 * _SQS
SomaliShilling	_SOS	0.0015 * _EUR
SomaliSenti	_cSOS	0.01 * _SOS
SurinameseDollar	_SRD	0.12 * _EUR
SurinameseCent	_cSRD	0.01 * _SRD
SyrianPound	_SYP	0.0017 * _EUR
SyrianPiastre	_cSYP	0.01 * _SYP
ThaiBaht	_THB	0.028 * _EUR
ThaiSatang	_cTHB	0.01 * _THB
TajikistaniSamani	_TJS	0.094 * _EUR
TajikistaniDiram	_cTJS	0.01 * _TJS
Tonganpaanga	_TOP	0.397 * _EUR
TonganSeniti	_cTOP	0.01 * _TOP

Name	Symbol	Definition
TurkishLira	_TRY	0.16 * _EUR
TurkishKurus	_cTRY	0.01 * _TRY
${\bf Trinidad And Tobago Dollar}$	_TTD	0.13 * _EUR
${\bf Trinidad And Tobago Cent}$	_cTTD	0.01 * _TTD
NewTaiwanDollar	_TWD	0.029 * _EUR
NewTaiwanCent	_cTWD	0.01 * _TWD
TanzanianShilling	_TZS	0.00038 * _EUR
TanzanianSenti	_cTZS	0.01 * _TZS
UkrainianHryvnia	_UAH	0.00038 * _EUR
UkrainianKopiyka	_cUAH	0.01 * _UAH
UgandanShilling	_UGX	0.00024 * _EUR
UgandanCent	_cUGX	0.01 * _UGX
USDollar	_USD	0.89 * _EUR
USCent	_cUSD	0.01 * _USD
UruguayanPeso	_UYU	0.027 * _EUR
UruguayanCentesimo	_cUYU	0.01 * _UYU
UzbekistaniSom	_UZS	0.00011 * _EUR
UzbekistaniTiyin	_cUZS	0.01 * _UZS
${\bf Venezuel an Bolivar Soberano}$	_VES	0.0003 * _EUR
Venezuelan Centimo Soberano	_cVES	0.01 * _VES
VietnameseDong	_VND	3.8e-05 * _EUR
VietnameseXu	_cVND	0.01 * _VND
SamoanTala	_WST	0.34 * _EUR
SamoanSene	_cWST	0.01 * _WST
YemeniRial	_YER	0.0036 * _EUR
YemeniDinar	_cYER	0.01 * _YER
SouthAfricanRand	_ZAR	0.062 * _EUR
SouthAfricanCent	_cZAR	0.01 * _ZAR
ZambianKwacha	_ZMW	0.074 * _EUR
ZambianNgwee	_cZMW	0.01 * _ZMW

### 4.10.1 Pegged International Currencies

International currency which are pegged to other currencies.

Name	Symbol	Definition
UnitedArabEmiratesDirham	_AED	(1/3.6725) * _USD
${\bf United Arab Emirates Fils}$	_cAED	0.01 * _AED
Netherlands Antillean Guilder	_ANG	(1/1.79) * _USD
${\bf Netherlands Antillean Cent}$	_cANG	0.01 * _ANG
ArubanFlorin	_AWG	(1/1.79) * _USD
ArubanCent	_cAWG	0.01 * _AWG
BarbadianDollar	_BBD	0.5 * _USD
BarbadianCent	_cBBD	0.01 * _BBD
BulgarianLev	_BGN	0.51129 * _EUR
BulgarianStotinka	_cBGN	0.01 * _BGN
BahrainiDinar	_BHD	(1/0.376) * _USD
BahrainiFils	_cBHD	0.001 * _BHD
BermudianDollar	_BMD	1 * _USD
BermudianCent	_cBMD	0.01 * _BMD
BruneiDollar	_BND	1 * _SGD
BruneiSen	_cBND	0.01 * _BND
BahamianDollar	_BSD	1 * _USD
BahamianCent	_cBSD	0.01 * _BSD
Bhutanese Ngultrum	_BTN	1 * _INR
Bhutanese Chhertum	_cBTN	0.01 * _BTN
BelizeDollar	_BZD	0.5 * _USD
BelizeCent	_cBZD	0.01 * _BZD
${\bf Cubano Convertible Peso}$	_CUC	1 * _USD
${\bf Cubano Convertible Centavo}$	_cCUC	0.01 * _CUC
CubanPeso	_CUP	(1/24) * _CUC
CubanCentavo	_cCUP	0.01 * _CUP

Name	Symbol	Definition
CapeVerdeanEscudo	_CVE	(1/110.265) * _EUR
CapeVerdeanCentavo	_cCVE	0.01 * _CVE
DjiboutianFranc	_DJF	(1/177.721) * _USD
DjiboutianCentime	_cDJF	0.01 * _DJF
EritreanNakfa	_ERN	(1/15) * _USD
EritreanCent	_cERN	0.01 * _ERN
Falkland Islands Pound	_FKP	1 * _GBP
FalklandIslandsPenny	_cFKP	0.01 * _FKP
GuernseyPound	_GGP	1 * _GBP
GuernseyPenny	_cGGP	0.01 * _GGP
GibraltarPound	_GIP	1 * _GBP
GibraltarPenny	_cGIP	0.01 * _GIP
ManxPound	_IMP	1 * _GBP
ManxPenny	_cIMP	0.01 * _IMP
JerseyPound	_JEP	1 * _GBP
JerseyPenny	_cJEP	0.01 * _JEP
JordanianDinar	_JOD	(1/0.708) * _USD
JordanianFils	_cJOD	0.001 * _JOD
KiribatiDollar	_KID	1 * _AUD
KiribatiCent	_cKID	0.01 * _KID
Comorianfranc	_KMF	(1/491.96775) * _EUR
ComorianCentime	_cKMF	0.01 * _KMF
CaymanIslandsDollar	_KYD	1.2 * _USD
CaymanIslandsCent	_cKYD	0.01 * _KYD
LebanesePound	_LBP	(1/1507.5) * _USD
LebaneseQeresh	_cLBP	0.01 * _LBP
MacanesePataca	_MOP	(1/1.03) * _HKD
MacaneseAvo	_cMOP	0.01 * _MOP

Name	Symbol	Definition
NamibianDollar	_NAD	1 * _ZAR
NamibianCent	_cNAD	0.01 * _NAD
NepaleseRupee	_NPR	(1/1.6) * _INR
NepalesePaisa	_cNPR	0.01 * _NPR
OmaniRial	_OMR	(1/2.6008) * _USD
OmaniBaisa	_cOMR	0.001 * _OMR
PanamanianBalboa	_PAB	1 * _USD
PanamanianCentesimo	_cPAB	0.01 * _PAB
TransnistrianRuble	_PRB	(1/16.1) * _USD
TransnistrianKopeck	_cPRB	0.01 * _PRB
SaudiRiyal	_SAR	(1/3.75) * _USD
SaudiHalalah	_cSAR	0.01 * _SAR
SaintHelenaPound	_SHP	1 * _GBP
SaintHelenaPenny	_cSHP	0.01 * _SHP
SouthSudanesePound	_SSP	1 * _SDG
South Sudanese Piaster	_cSSP	0.01 * _SSP
${\bf Sao Tome And Principe Dobra}$	_STN	(1/24.5) * _EUR
${\bf Sao Tome And Principe Centimo}$	_cSTN	0.01 * _STN
SwaziLilangeni	_SZL	1 * _ZAR
SwaziCent	_cSZL	0.01 * _SZL
TurkmenistanManat	_TMT	(1/3.5) * _USD
TurkmenistanTenge	_cTMT	0.01 * _TMT
TuvaluanDollar	_TVD	1 * _AUD
TuvaluanCent	_cTVD	0.01 * _TVD
${\bf Central African CFAFranc}$	_XAF	(1/655.957) * _EUR
${\bf Central African CFA Centime}$	_cXAF	0.01 * _XAF
EasternCaribbeanDollar	_XCD	(1/2.7) * _USD
EasternCaribbeanCent	_cXCD	0.01 * _XCD

Name	Symbol	Definition
WestAfricanCFAFranc	_XOF	(1/655.957) * _USD
${\bf West A frican CFA Centime}$	_cXOF	0.01 * _XOF
CFPFranc	_XPF	(1000/8.38) * _EUR
CFPCentime	_cXPF	0.01 * _XPF
ZimbabweanBonds	_ZWL	1 * _USD
ZimbabweanCent	_cZWL	0.01 * _ZWL

# 5 Lua Documentation

In this section, the following shortcuts will be used.

```
local D = physical.Dimension
local U = physical.Unit
local N = physical.Number
local Q = physical.Quantity
```

The term number refers to a lua integer or a lua float number. By string a lua string is meant and by bool a lua boolean.

### 5.1 physical.Quantity

The quantity class is the main part of the library. Each physical Quantity and all units are represented by an instance of this class.

#### Q.new(q=nil)

Copy Constuctor

```
q: Q, number, object, nil returns: Q
```

As an argument it takes Q, number, object or nil. If an instance of Q is given, a copy is made and returned. If a number or an instance object of another class is given, the function creates a dimensionless quantity with the number or the instance as a value. In the case nil is given, a dimensionless quantity with value 1 is returned.

```
print( Q() )
1

print( Q(42) )
42

print( Q(73*_m) )
73 * _m
```

## Q.defineBase(symbol,name,dimension)

This function is used to declare base quantities from which all other quantities are derived from.

```
symbol : string
The symbol of the base quantity.
```

name: string

The name of the base quantity.

dimension: D

An instance of the D class, which represents the dimension of the quantity.

returns: Q

The created Q instance.

The function creates a global variable of the created base quantity. The name consist of an underscore concatenated with the  ${\tt symbol}$  argument, i.e. the symbol  ${\tt m}$  becomes the global variable  ${\tt \_m}$ .

The name is used for example in the siunitx conversion function, e.g meter will be converted to \meter.

Each quantity has a dimension associated with it. The argument dimension allows any dimension to be associated to base quantities.

```
Q.defineBase("m", "meter", L)
Q.defineBase("kg", "kilogram", M)
```

#### Q.define(symbol, name, q)

Creates a new derived quantity from an expression of other quantities. Affine quantities like the absolute temperature in celsius are not supported.

symbol: string

Symbol of the base quantity

 ${\tt name: string, nil}$ 

The Name of the derived quantity.

q: physical.Quantity

The definition of the derived quantity.

returns: Q

The created quantity.

The function creates a global variable of the created base quantity. The name consist of an underscore concatenated with the symbol argument, i.e. the symbol N becomes the global variable \_N.

The name is used for example in the siunitx conversion function, e.g newton will be converted to \newton.

```
Q.define("L", "liter", _dm^3)
Q.define("Pa", "pascal", _N/_m^2)
Q.define("C", "coulomb", _A*_s)
Q.define("degC", "celsius", _K)
```

#### Q.definePrefix(symbol,name,factor)

Defines a new prefix.

symbol : string

Symbol of the base quantity

name: string

Name of the base quantity

factor: number

The factor which corresponds to the prefix

```
Q.definePrefix("c", "centi", 1e-2)
Q.definePrefix("a", "atto", 1e-18)
```

#### Q.addPrefix(prefixes, units)

Create several units with prefixes from a given unit.

prefixes: string

A list of unit symbols.

units: Q

A list of quantities.

$$\label{eq:QaddPrefix} \verb"Q.addPrefix({"n","u","m","k","M","G"},{_m,\_s,\_A})$$

#### Q.isclose(self,q,r)

Checks if this quantity is close to another one. The argument  ${\tt r}$  is the maximum relative deviation. The function returns  ${\tt true}$  if the following condition is fullfilled

$$\frac{abs(\texttt{self}-\texttt{q})}{min(\texttt{self},\texttt{q})} \leq \texttt{r} \quad .$$

 $\mathtt{self}:\,\mathtt{Q},\,\mathtt{N},\,\mathtt{number}$ 

q: Q, N, number

r: number

maximum relative deviation of self and q

 $\operatorname{returns}: \mathtt{bool}$ 

true if q is close to self, otherwise false

```
s_1 = 1.9 * _m
s_2 = 2.0 * _m
print( s_1:isclose(s_2,0.1) )
true
print( s_1:isclose(s_2,0.01) )
false
```

# Q.to(self,q=nil)

Converts the quantity self to the unit of the quantity q. If no q is given, the quantity self is converted to base units.

```
self: Q
q: Q, nil

s = 1.9 * _km
  print( s:to(_m) )
  1900.0 * _m

T = 10 * _degC
  print( T:to(_K) )
  10.0 * _K

  print( T:to() )
  10 * _K
```

#### Q.tosiunitx(self,param,mode=Q.siunitx\_SI)

Converts the quantity into a siunitx string.

```
self : Q
param : string
mode : number
```

If mode is equal Q.SIUNITX\_SI, which is the default, the quantity is converted to an  $SI\{\}\{\}$  macro. If mode is Q.SIUNITX\_num, the quantity is converted to  $\sum_{s=1}^{n} Q.SIUNITX_si$  the macro  $\sum_{s=1}^{n} Q.SIUNITX_si$ 

```
s = 1.9 * _km

print( s:tosiunitx() )
\SI{1.9}{\kilo\meter}

print( s:tosiunitx(nil,Q.SIUNITX_num) )
\num{1.9}

print( s:tosiunitx(nil,Q.SIUNITX_si) )
\si{\kilo\meter}
```

# Q.min(q1, q2, ...)

q1: Q, N, number

Returns the smallest quantity of the given ones. The function returns q1 if the Quantities are equal.

```
\begin{array}{l} q2:\, Q,\, N,\, number\\ \dots\\ qN:\, Q,\, N,\, number\\ \\ \\ returns:\, Q\\ \\ \\ the\,\, smallest\,\, quantity\,\, of\,\, q1,\, \dots\,,\,\, qN \end{array}
```

```
s_1 = 15 * _m
s_2 = 5 * _m
print(s_1:min(s_2))
5 * _m
```

# Q.max(q1, q2, ...)

Returns the biggest quantity of several given ones. The function returns q1 if the Quantities are equal.

```
q1: Q, N, number
q2: Q, N, number
...
qN: Q, N, number
returns: Q
    the biggest quantity of q1, ... , qN
```

```
s_1 = 15 * _m
s_2 = 5 * _m
print(s_1:max(s_2))
15 * _m
```

# Q.abs(q)

Returns the absolute value of the given quantity q.

```
\mathbf{q} : \mathbf{Q}, \mathbf{N}, number  \mathrm{returns} : \mathbf{Q}  the absolute value of \mathbf{q}
```

```
U = -5 * _V
print(U)
-5 * _V
print(U:abs())
5 * _V
```

## Q.sqrt(q)

Returns the square root of the given quantity.

 $\begin{array}{l} \textbf{q}: \ \textbf{Q}, \ \textbf{N}, \ \textbf{number} \\ & \text{dimensionless argument} \\ \\ \text{returns}: \ \textbf{Q} \\ & \text{the square root of } \textbf{q} \end{array}$ 

```
A = 25 * _m^2
s = A:sqrt()
print(s)
5.0 * _m
```

# Q.log(q, base=nil)

Returns the logarithm of a given quantity to the given base. If no base is given, the natural logarithm is returned.

q: Q, N, number dimensionless argument base: Q, N, number, nil dimensionless argument

returns: Q

logarithm of q to the base

```
I = 1 * _W/_m^2
I_0 = 1e-12 * _W/_m^2
print(10 * (I/I_0):log(10) * _dB)
120.0 * _dB
```

# Q.exp(q)

Returns the value of the natural exponential function of the given quantitiy.

q: Q, N, number dimensionless argument

 $\begin{array}{c} \text{returns}: \ Q \\ \text{natural exponential of } \ q \end{array}$ 

```
x = 2 * _1
print( x:exp() )
7.3890560989307
```

## Q.sin(q)

Returns the value of the sinus function of the given quantitiy.

```
q: Q, N, number
   dimensionless argument

returns: Q
   sine of q

alpha = 30 * _deg
   print( alpha:sin() )
   0.5
```

# Q.cos(q)

Returns the value of the cosinus function of the given quantity. The quantity has to be dimensionless.

```
q: Q, N, number
   dimensionless argument

returns: Q
   cosine of q

alpha = 60 * _deg
   print( alpha:cos() )
   0.5
```

# Q.tan(q)

Returns the value of the tangent function of the given quantity. The quantity has to be dimensionless.

```
q: Q, N, number dimensionless argument returns: Q tangent of q
```

```
alpha = 45 * _deg
print( alpha:tan() )
1.0
```

### Q.asin(q)

Returns the value of the arcus sinus function of the given quantity. The quantity has to be dimensionless.

 $\begin{array}{l} q:\, Q,\, N,\, number\\ & \text{dimensionless argument} \\ \\ \text{returns}:\, Q\\ & \text{inverse sine of } q \end{array}$ 

```
x = 0.5 * _1
print( x:asin():to(_deg) )
30.0 * _deg
```

# Q.acos(q)

Returns the value of the arcus cosinus function of the given quantity. The quantity has to be dimensionless.

q: Q, N, number dimensionless argument returns: Q inverse cosine of q

```
x = 0.5 * _1
print( x:acos():to(_deg) )
60.0 * _deg
```

# Q.atan(q)

Returns the value of the arcus tangent function of the given quantity. The quantity has to be dimensionless.

 $\begin{array}{l} q: \ Q, \ N, \ number \\ & \ dimensionless \ argument \\ returns: \ Q \\ & \ inverse \ tangent \ of \ q \end{array}$ 

```
x = 1 * _1
print( x:atan():to(_deg) )
45.0 * _deg
```

#### Q.sinh(q)

Returns the value of the hyperbolic sine function of the given quantity. The quantity has to be dimensionless. Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\sinh(x) = 0.5 \cdot e^x - 0.5/e^x \quad .$$

q: Q, N, number

dimensionless argument

returns: Q

hyperbolic sine of q

```
x = 1 * _1
print( x:sinh() )
1.1752011936438
```

### Q.cosh(q)

Returns the value of the hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\cosh(x) = 0.5 \cdot e^x + 0.5/e^x \quad .$$

q: Q, N, number

dimensionless argument

returns: Q

hyperbolic cosine of q

```
x = 1 * _1
print( x:cosh() )
1.5430806348152
```

### Q.tanh(q)

Returns the value of the hyperbolic tangent function of the given quantity. The quantity has to be dimensionless. Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} \quad .$$

q: Q, N, number

dimensionless argument

 $\operatorname{returns}: Q$ 

hyperbolic tangent of  ${\tt q}$ 

```
x = 1 * _1
print( x:tanh() )
0.76159415595576
```

#### Q.asinh(q)

Returns the value of the inverse hyperbolic sine function of the given quantity. The quantity has to be dimensionless. Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$asinh(x) = \ln\left(x + \sqrt{x^2 + 1}\right)$$
.

q: Q, N, number

dimensionless argument

returns: Q

inverse hyperbolic sine of q

```
x = 1 * _1
print( x:asinh() )
0.88137358701954
```

#### Q.acosh(q)

Returns the value of the inverse hyperbolic cosine function of the given quantity. The quantity has to be dimensionless. Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$a\cosh(x) = \ln\left(x + \sqrt{x^2 - 1}\right) \quad , x > 1 \quad .$$

q: Q, N, number

dimensionless argument bigger or equal to one

returns : Q

inverse hyperbolic cosine of q

```
x = 2 * _1
print( x:acosh() )
1.3169578969248
```

# Q.atanh(q)

Returns the value of the inverse hyperbolic tangent function of the given quantity. The quantity has to be dimensionless. Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\operatorname{atanh}(x) = \ln\left(\frac{1+x}{1-x}\right) \quad , -1 < x < 1 \quad .$$

## q: Q, N, number

dimensionless argument with magnitude smaller than one

### returns : Q

inverse hyperbolic tangent of  ${\tt q}$ 

x = 0.5 \* \_1
print( x:atanh() )
0.54930614433405

#### 5.2 physical.Dimension

All physical quantities do have a physical dimension. For example the quantity Area has the dimension  $L^2$  (length to the power of two). In the SI-System there are seven base dimensions, from which all other dimensions are derived. Each dimension is represented by an n-tuple, where n is the number of base dimensions. Each physical quantity has an associated dimension object. It is used to check equality and if addition or substraction is allowed.

#### D.new(d)

Constructor of the Dimension class.

d: Dimension or string, nil

The name or symbol of the dimension.

returns : D

The created D instance

If d is a string, a copy of the perviously defined dimension is made. If d is a dimension, a copy of it is made. If no argument ist given, a dimension *zero* is created.

#### Example

```
V_1 = D("Velocity")
L = D("L")
V_2 = D(L/T)
```

#### D.defineBase(symbol, name)

Defines a base dimension.

symbol: string

name: string

returns: D

The created D instance

#### Example

```
V_1 = D("Velocity")
L = D("L")
V_2 = D(L/T)
```

### 5.3 physical.Unit

The task of this class is keeping track of the unit term. The unit term is a fraction of units. The units in the enumerator and denominator can have an exponent.

#### Unit.new(u=nil)

Copy Constructor. It copies a given unit object. If nothing is given, an empty unit is created.

u: Unit

The unit object which will be copied.

returns: Unit

The created Unit object

#### Unit.new(symbol, name, prefixsymbol=nil, prefixname=nil)

Constructor. A new Unit object with symbol is created. The prefixsymbol and prefixname are optional.

symbol : String

The symbol of the unit.

name: String

The name of the unit.

prefixsymbol : String

The optional symbol of the prefix.

prefixname : String

The optional name of the prefix.

returns: Unit

The created Unit object

#### Unit.tosiunitx(self)

The unit term will be compiled into a string, which the LaTeX package siunitx can understand.

returns: String

The siunitx representation of the unit term.

#### 5.4 physical.Number

This class enhances the Lua number with an uncertainty and gaussian error propagation. A number instance has a mean value called x and an uncertainty value called dx.

### N.omitUncertainty=true

This variable controls, wether the uncertainty dx is printed or not. The default value is true, i.e. the uncertainty is omitted.

```
n = N(45,0.012)

N.omitUncertainty = false
print(n)
(45.000 +/- 0.012)

N.omitUncertainty = true
print(n)
45.0
```

#### N.seperateUncertainty=true

This variable controls, how the uncertainty is printed. If set to false, the parenthesis notation is used. If set to true the plus minus notation is used. The default value is true.

```
n = N(56,0.025)

N.seperateUncertainty = false
print(n)
56.00(3)

N.seperateUncertainty = true
print(n)
(56.00 +/- 0.03)
```

#### N.format=N.SCIENTIFIC

This variable controls, how the number is printed. If set to N.SCIENTIFIC, scientific notation is used. If set to N.DECIMAL the decimal notation is used. The default value is N.SCIENTIFIC.

```
n = N(12000000,0.1)

N.format = N.SCIENTIFIC
print(n)
1.2000000e7
```

```
N.format = N.DECIMAL
print(n)
12000000
```

#### N.new(n=nil)

This is the copy Constructor for the Number class. It copies a given number object. If n is nil, an instance representing number zero with uncertainty zero is created.

#### n: Number

The number object to be copied.

returns: Number

The created Number instance.

```
n = N(56,0.012)

m = N(n)

print(m)

56.0
```

## N.new(x, dx=nil)

This constructor, creates a new instance of N with mean value x and uncertainty dx. If dx is not given, the uncertainty is zero.

```
x : number
    mean value

dx : number, nil
    uncertainty value

returns : N
```

The created N instance.

```
n = N(56,0.012)
print(n)
56.0
```

#### N.new(str)

This constructor creates a new instance of N from a string. It can parse strings of the form "3.4", "3.4e-3", "5.4e-3 +/- 2.4e-6" and "5.45(7)e-23".

```
str: string
```

returns: N

```
n_1 = N("12.3e-3")
print(n_1)
0.0123

n_2 = N("12 +/- 0.1")
print(n_2)
12

n_3 = N("12.0(1)")
print(n_3)
12

n_4 = N("15.0(12)")
print(n_4)
15.0
```

### N.mean(n)

Returns the mean value of n.

### Parameters / Return

 ${\rm returns}: {\tt number}$ 

```
n = N(1.25,0.0023)
print( n:mean() )
1.25
```

# N.uncertainty(n)

Returns the uncertainty value of n.

```
n:N
```

returns: number

```
n = N(1.25,0.0023)
print( n:uncertainty() )
0.0023
```

### N.abs(n)

Returns the absolute value of n.

```
n:N
returns:N
```

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \Delta x$$
 .

```
n = N(-10,1)
print( n:abs() )
10.0
```

# N.sqrt(n)

Returns the square root of n.

n: N returns: N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{2\sqrt{x}} \cdot \Delta x \quad .$$

```
n = N(25,1)
print( n:sqrt() )
5
```

## N.log(n,base=nil)

Returns the logarithm of a given number n to the given base base. If no base is given, the natural logarithm of n is returned.

n:N

base : number, nil

returns: N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\mid x \cdot \log(b) \mid} \cdot \Delta x \quad .$$

```
n = N(25,1)
print( n:log() )
3.2
```

# N.exp(n)

Returns the value of the natural exponential function of the given number.

q:N returns:N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = e^x \cdot \Delta x \quad .$$

```
n = N(25,1)
print( n:sqrt() )
5
```

# N.sin(n)

Returns the value of the sine function of the given number.

n:N returns:N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = |\cos(x)| \cdot \Delta x$$
.

```
n = N(3,0.1)
print( n:sin() )
0.1
```

### N.cos(n)

Returns the value of the cosine function of the given number.

n:N returns:N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = |\sin(x)| \cdot \Delta x$$
.

```
n = N(0.5,0.01)
print( n:cos() )
0.88
```

#### N.tan(n)

Returns the value of the tangent function of the given number.

n: N

returns: N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \mid \frac{1}{\cos^2(x)} \mid \cdot \Delta x \quad .$$

```
n = N(1.5,0.001)
print( n:tan() )
14
```

#### N.asin(n)

Returns the value of the inverse sine function of the given number.

n:N

returns: N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\sqrt{1 - x^2}} \cdot \Delta x \quad .$$

```
n = N(0.99,0.001)
print( n:asin() )
1.43
```

#### N.acos(n)

Returns the value of the inverse cosine function of the given number.

n: N

returns: N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\sqrt{1 - x^2}} \cdot \Delta x \quad .$$

```
n = N(0.99,0.001)
print( n:acos() )
0.14
```

### N.atan(n)

Returns the value of the inverse tangent function of the given number.

n:N

returns: N

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\sqrt{1+x^2}} \cdot \Delta x \quad .$$

```
n = N(1,0.001)
print( n:atan() )
0.785
```

### N.sinh(q)

Returns the value of the hyperbolic sine function of the given number.

n: N

returns: N

Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\sinh(x) = 0.5 \cdot e^x - 0.5/e^x \quad .$$

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = (0.5 \cdot e^x + 0.5/e^x) \cdot \Delta x \quad .$$

```
n = N(1,0.001)
print( n:sinh() )
1.18
```

# N.cosh(q)

Returns the value of the hyperbolic cosine function of the given number.

n:N

returns: N

Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\cosh(x) = 0.5 \cdot e^x + 0.5/e^x \quad .$$

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = (0.5 \cdot e^x - 0.5/e^x) \cdot \Delta x \quad .$$

```
n = N(1,0.001)
print( n:cosh() )
1.54
```

### N.tanh(q)

Returns the value of the hyperbolic tangent function of the given number.

n: N returns: N

Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}} \quad .$$

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\left(0.5 \cdot e^x + 0.5/e^x\right)^2} \cdot \Delta x \quad .$$

```
n = N(1,0.001)
print( n:tanh() )
0.762
```

### Q.asinh(q)

Returns the value of the inverse hyperbolic sine function of the given number.

n: N returns: N

Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$asinh(x) = ln\left(x + \sqrt{x^2 + 1}\right)$$
.

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\sqrt{x^2 + 1}} \cdot \Delta x \quad .$$

```
n = N(1,0.001)
print( n:asinh() )
0.881
```

# Q.acosh(q)

Returns the value of the inverse hyperbolic cosine function of the given number.

n: N returns: N

Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$a\cosh(x) = \ln\left(x + \sqrt{x^2 - 1}\right) \quad , x > 1 \quad .$$

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\sqrt{x^2 - 1}} \cdot \Delta x \quad .$$

```
n = N(2,0.001)
print( n:acosh() )
1.317
```

#### Q.atanh(q)

Returns the value of the inverse hyperbolic tangent function of the given number.

n: N returns: N Since Lua doesn't implement the hyperbolic functions, the following formula is used

$$\operatorname{atanh}(x) = \ln \left( \frac{1+x}{1-x} \right) \quad , -1 < x < 1 \quad .$$

The uncertainty  $\Delta y$  is calculated by the following expression

$$\Delta y = \frac{1}{\mid x^2 - 1 \mid} \cdot \Delta x \quad .$$

n = N(-0.5,0.0001)
print( n:atanh() )
-0.549

# 6 Change History

#### $V1.0.4 \quad (2020/09/15)$ Minor release

 $Changed\ default\ value\ of\ {\tt Number.omitUncertainty}\ and\ {\tt Number.seperateUncertainty}\ to\ {\tt true}.\ Documentation\ added.$ 

#### V1.0.3 (2020/09/09) Minor release

Changed foldername physical to src. Changed Classvariables  $Q.siunitx\_SI$ ,  $Q.siunitx\_num$  and  $Q.siunitx\_si$  to uppercase  $Q.SIUNITX\_SI$ ,  $Q.SIUNITX\_num$  and  $Q.SIUNITX\_si$ .

### $V1.0.2 \quad (2020/09/07)$ Minor release

Path issues resolved. Documentation added.

V1.0.1 (2020/09/05) Minor release

Files renamed.

V1.0.1 (2020/09/03) First official release.

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